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LIB

Rare and baryonic decays of charm hadrons at Belle and Belle II

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Belle and Belle II Experiments



BELLE @ KEKB



Selected Topics

- Rare FCNC $c \rightarrow u l^+ l^-$ decays
 - $D^0 \to h^- h^{(')+} e^+ e^- (h = K, \pi)$

•
$$\Xi_c^0 \to \Xi^0 l^+ l^-$$

• Baryon number violation • $D^0 \rightarrow pl$ Branching fraction of Ξ⁰_c and Λ⁺_c decays
Ξ⁰_c → Ξ⁰h⁰(h⁰ = π⁰, η, η')
Λ⁺_c → pK⁰_Sπ⁰
Λ⁺_c → pK⁰_Sη, Λ⁺_c → pK⁰_SK⁰_S
Λ⁺_c → Σ⁺η^(')
Λ⁺_c → ΛK⁺, Λ⁺_c → Σ⁰K⁺



Search for $D^0 \rightarrow hh'e^+e^-$, $(h = K, \pi)$

- FCNC processes with $c \rightarrow ull$ are suppressed in SM, good probe for NP
- **SM long-distance** contributions dominate, especially near resonances.
- BSM contributions may be visible far from resonances.



BABAR: PRL **122**, 081802 (2019) BESIII: PRD **97**, 072015 (2019) LHCb: PRL **119**, 181805 (2017) PLB **517**, 558(2016)

Measured BFs or ULs at 90% CL [$\times 10^{-7}$]

	KKee	ππее	Клее
PAPAP	_	_	$40.0 \pm 5.0 \pm 2.3$
DADAN			< 31 (non-res
BESIII	< 110	< 70	< 410
	ΚΚμμ	ππμμ	Κπμμ
LHCb	$1.54 \pm 0.27 \pm 0.19$	$9.64 \pm 0.48 \pm 1.10$	$4.17 \pm 0.12 \pm 0.4$

Search for signal candidates in $q^2 = m^2(e^+e^-)$ regions

 \rightarrow Near resonances \rightarrow BR measurement

 \rightarrow Far from resonances (non-resonant) \rightarrow Sensitive to NP











First Search for $\Xi_c^0 \rightarrow \Xi^0 l^+ l^-$

- No FCNC neutrino-less decays in charm baryons
- \rightarrow Only upper limits of $\Lambda_c^+ \rightarrow p l^+ l^-$ [1,2] decays were set for charmed baryons
 - Both W-exchange and FCNC processes contribute.
- \rightarrow Theoretically more complicated than $c \rightarrow ull$ in meson decays. Sensitive to Hamiltonian helicity structure through W-exchange diagrams.

 \rightarrow If observed, the signal channels would allow to test LFU with $l = e, \mu$ [1] PRD **84**, 072006 (2011) [2] PRD **97**, 091101 (2018)



Belle 980/fb, PRD 109, 052003 (2024)

- **Belle Result**: No significant signal was observed but consistent with SM
- First set upper limits set at 90% CL:

	Measured	SM pred
$\mathscr{B}(\Xi_c^0\to\Xi^0e^+e^-)$	< 9.9 x 10 ⁻⁵	< 2.35 x
$\mathcal{B}(\Xi_c^0\to\Xi^0\mu^+\mu^-)$	< 6.5 x 10 ⁻⁵	< 2.25 x

SM prediction: PRD **103**, 013007 (2021)











pl

- **Baryon Number Violation (BNV)** is a required condition to explain the observed matter-antimatter asymmetry in the universe
- → Several BSM models^[1-5] allow nucleon BNV with $\Delta(B L) = 0$
 - $\rightarrow B$: baryon number, L: lepton number



- **Belle Result**:
- Search for 8 channels: $D^0/\overline{D}^0 \rightarrow pl^-, \bar{p}l^+$ with $l = e, \mu$
- $\rightarrow D^*$ tag for D^0/\overline{D}^0 determination
- $\rightarrow D^0 \rightarrow K\pi$ as a reference mode
- No significant signal was observed
- Set upper limits at $(5 8) \times 10^{-7}$ (90% CL)
- → Most stringent upper limit for the electron channels to date
- → First measurement for the muon channels

[1] PRD, **8**, 1240 (1973) [2] PRL. **32**, 438 (1974) [3] PRD **20**, 776 (1979) [4] PLB. **91B**, 222 (1980) [5] PLB **314**, 336 (1993).

Belle 921/fb, PRD 109, L031101 (2024)



X : non-SM gauge bosons



Intermediate states in $\Lambda_c^+ \to p K_{\varsigma}^0 \pi^0$

With a large statistics, first investigation of Dalitz plots/Intermediate states



→ No distinct peaking structure of Σ^{*+} in $M(pK_{\varsigma}^{0})$ \rightarrow At 1.5 GeV/ c^2 , a clear structure is seen in $M(p\pi^0)$ (continued in next page)

Preliminary Belle 980/fb





Possible $N(1535)^+$ enhanced by $p\eta$ threshold



- to deal with **non-factorizable processes**



- First Belle + Belle II combined charm measurement
- First measurements of branching fractions
- Rules out several theoretical models
- \rightarrow The results prefer a $SU(3)_F$ breaking model^(*)

Model	$\mathcal{B}(\Xi_c^0 o \Xi^0 \pi^0)$	$\mathcal{B}(\Xi_c^0 o \Xi^0 \eta)$	$\mathcal{B}(\Xi_c^0 o \Xi^0 \eta')$	(*)
${ m SU}(3)_{ m F} ext{-breaking}$	$7.74\substack{+2.52\\-2.32}$	$2.43\substack{+2.79\\-2.90}$	$1.63\substack{+5.09 \\ -5.14}$	

Branching fraction of Λ_c^+ decays

- First or most precise BF measurements with uncertainties in $(\pm stat. \pm syst. \pm norm.)$
- ➡ CF decays
- $B(\Lambda_c^+ \to \Sigma^+ \eta) = (3.14 \pm 0.35 \pm 0.17 \pm 0.25) \times 10^{-3}$
- $B(\Lambda_c^+ \to \Sigma^+ \eta') = (4.16 \pm 0.75 \pm 0.17 \pm 0.25) \times 10^{-3}$ •
- $B(\Lambda_c^+ \to pK_S^0\eta) = (4.35 \pm 0.10 \pm 0.20 \pm 0.22) \times 10^{-3}$ •
- $B(\Lambda_c^+ \to pK_S^0 \pi^0) = (2.11 \pm 0.01 \pm 0.05 \pm 0.10) \times 10^{-2}$ (new) •

➡ SCS decays

- $B(\Lambda_c^+ \to pK_S^0 K_S^0) = (2.35 \pm 0.12 \pm 0.07 \pm 0.04) \times 10^{-4}$
- $B(\Lambda_c^+ \to \Lambda K^+) = (6.57 \pm 0.17 \pm 0.11 \pm 0.35) \times 10^{-4}$
- $B(\Lambda_c^+ \to \Sigma^0 K^+) = (3.58 \pm 0.19 \pm 0.06 \pm 0.19) \times 10^{-4}$



Belle 980/fb, PRD 107, 032003 (2023)



Belle 980/fb,



Preliminary Belle 980/fb







Summary

- Belle is still producing important measurements although its data-taking finished nearly 15 years ago
 - → A large amount of data samples allows significant improvement in our understanding of SM and baryon decays.
 - \rightarrow Rare FCNC $c \rightarrow u l^+ l^-$

$$\rightarrow D^0 \rightarrow h^- h^{(')+} e^+ e^- (h = K, \pi)$$

- $\Rightarrow \Xi_c^0 \rightarrow \Xi^0 l^+ l^-$
- \rightarrow Baryon number violating $D^0 \rightarrow pl$
- Branching fraction measurements
- $\Lambda_c^+ \rightarrow p K_s^0 \pi^0$ (and Intermediate structures)
- $\Lambda_c^+ \to p K_S^0 \eta, \ \Lambda_c^+ \to p K_S^0 K_S^0$
- $\Lambda_c^+ \to \Sigma^+ \eta^{(\prime)}$

•
$$\Lambda_c^+ \to \Lambda K^+, \Lambda_c^+ \to \Sigma^0 K^+$$

• First Belle + Belle II combined data analysis in charm physics

→
$$\Xi_c^0 \rightarrow \Xi^0 h^0 (h^0 = \pi^0, \eta, \eta')$$
: Branching fraction

 \rightarrow Rules out several theoretical approaches. Preferring one of theoretical models based on $SU(3)_F$ -breaking



Backup



Results for $m(e^+e^-)$ regions $(D^0 \rightarrow hh^{(')}l^+l^-)$

TABLE I. $D^0 \rightarrow h^- h^{(')+} e^+ e^-$ modes yields, significance, branching fractions, branching fraction upper limits, and the efficiencies of each m_{ee} region [×10⁻⁷]. A fitted yield and a branching fraction are not reported for $K^-K^+e^+e^-$ mode with m_{ee} in the m_{η} region since only one event is observed, and the significance is determined from the CL_s distribution.

m_{ee} region	$[\text{MeV}/c^2]$	Yield	Significance	\mathcal{B}	UL @ 90% CL	Efficiency	BABAR	BE:
$K^-K^+e^+e^-$								
η	520 - 560	-	$< 0.1\sigma$	_	< 2.3	3.53 ± 0.04		
$ ho^0/\omega$	> 675	2.6 ± 1.8	2.0σ	$1.2\pm0.9\pm0.1$	< 3.0	6.00 ± 0.06		<
non-resonant	$> 200^{a}$	3.5 ± 3.3	1.5σ	$3.1 \pm 3.0 \pm 0.4$	< 7.7	3.19 ± 0.04		
$\pi^-\pi^+e^+e^-$								
η	520 - 560	0.6 ± 2.3	0.3σ	$0.4\pm1.4\pm0.2$	< 3.2	5.31 ± 0.05		
$ ho^0/\omega$	675 - 875	3.7 ± 4.1	0.9σ	$2.0\pm2.2\pm0.8$	< 6.1	5.69 ± 0.05		< 7
ϕ	995 - 1035	3.6 ± 3.2	1.1σ	$1.1\pm1.1\pm0.2$	< 3.1	9.41 ± 0.06		
non-resonant	> 200	-0.2 ± 4.1	$< 0.1\sigma$	$-0.2\pm3.4\pm0.9$	< 7.2	3.69 ± 0.04		
$K^-\pi^+e^+e^-$								
η	520 - 560	4.0 ± 2.7	1.6σ	$2.2 \pm 1.5 \pm 0.5$	< 5.6	5.09 ± 0.04		
$ ho^0/\omega$	675 - 875	110 ± 13	11.8σ	$39.6 \pm 4.5 \pm 2.9$		8.01 ± 0.06		< -
ϕ	990 - 1034	4.6 ± 2.4	2.5σ	$1.4 \pm 0.8 \pm 0.3$	< 2.9	9.19 ± 0.06		
non-resonant	> 560	2.2 ± 4.2	0.4σ	$1.3\pm2.4\pm0.6$	< 6.5	4.89 ± 0.09	< 31*	

^a Excluding resonance regions, which is same for all three modes.

*non-resonant region excluding [100,200], [491,560], [675, 875], [902,964], [1005,1035] MeV/c²



(90% CL)





Results of $D^0 \rightarrow pl$

TABLE I. Reconstruction efficiency (ϵ), signal yield (N_S), signal significance (S), upper limit on the signal yield $(N_{p\ell}^{UL})$, and branching fraction (\mathcal{B}) at 90% confidence level for each decay mode.

Decay mode	ϵ (%)	N_S	$\mathcal{S}\left(\sigma ight)$	N_{pl}^{UL}	$\mathcal{B} imes 10^{-7}$
$\overline{D^0 \to pe^-}$	10.2	-6.4 ± 8.5		17.5	< 5.5
$D^0 \rightarrow pe^-$ $D^0 \rightarrow \bar{p}e^+$	10.2	-18.4 ± 23.0 -4.7 ± 23.0		22.0 22.0	< 6.9 < 7.2
$\bar{D} \rightarrow \bar{p}e^+$ $\bar{D}^0 \rightarrow \bar{p}e^+$	09.6	-4.7 ± 23.0 7.1 ± 9.0	0.6	22.0	< 7.6
$D^0 \rightarrow p\mu^-$	10.7	11.0 ± 23.0	0.9	17.1	< 5.1
$\bar{D}^0 \rightarrow p \mu^-$	10.7	-10.8 ± 27.0		21.8	< 6.5
$D^0 o \bar{p}\mu^+$	10.5	-4.5 ± 14.0		21.1	< 6.3
$ar{D}^0 o ar{p} \mu^+$	10.4	16.7 ± 8.8	1.6	21.4	< 6.5





$\rightarrow \Xi^0 h^0$ theoretical predictions

Table 1. Theoretical predictions for the branching fractions and decay asymmetry parameters for $\Xi_c^0 \to \Xi^0 h^0$ decays. Branching fractions are given in units of 10^{-3} .

=	Reference	Model	$\mathcal{B}(\Xi_c^0 o \Xi^0 \pi^0)$	$\mathcal{B}(\Xi_c^0 o \Xi^0 \eta)$	${\cal B}(\Xi^0_c o\Xi^0\eta')$	$\alpha(\Xi_c^0\to\Xi^0\pi^0)$
_	Körner, Krämer [5]	Quark	0.5	3.2	11.6	0.92
	Ivanov et al. [6]	$\mathbf{Q}\mathbf{u}\mathbf{a}\mathbf{r}\mathbf{k}$	0.5	3.7	4.1	0.94
	Xu, Kamal [7]	Pole	7.7	-	-	0.92
	Cheng, Tseng [8]	Pole	3.8	-	-	-0.78
	Żenczykowski [9]	Pole	6.9	1.0	9.0	0.21
	Zou <i>et al.</i> [10]	Pole	18.2	26.7	-	-0.77
	Sharma, Verma [11]	\mathbf{CA}	-	-	-	-0.8
	Cheng, Tseng [8]	\mathbf{CA}	17.1	-	-	0.54
	Geng et al. $[12]$	${ m SU}(3)_{ m F}$	4.3 ± 0.9	$1.7^{+1.0}_{-1.7}$	$8.6^{+11.0}_{-6.3}$	-
	Geng <i>et al.</i> [13]	${ m SU}(3)_{ m F}$	7.6 ± 1.0	10.3 ± 2.0	9.1 ± 4.1	$-1.00\substack{+0.07\\-0.00}$
	Zhao <i>et al.</i> [14]	${ m SU}(3)_{ m F}$	4.7 ± 0.9	8.3 ± 2.3	7.2 ± 1.9	-
	Huang $et al. [15]$	${ m SU}(3)_{ m F}$	2.56 ± 0.93	-	-	-0.23 ± 0.60
	Hsiao $et al. [16]$	${ m SU}(3)_{ m F}$	6.0 ± 1.2	$4.2^{+1.6}_{-1.3}$	-	-
	Hsiao $et al. [16]$	${ m SU}(3)_{ m F} ext{-breaking}$	3.6 ± 1.2	7.3 ± 3.2	-	-
	Zhong et al. $[17]$	${ m SU}(3)_{ m F}$	$1.13\substack{+0.59\\-0.49}$	1.56 ± 1.92	$0.683\substack{+3.272\\-3.268}$	$0.50\substack{+0.37 \\ -0.35}$
Best fit →	Zhong et al. $[17]$	${ m SU}(3)_{ m F} ext{-breaking}$	$7.74\substack{+2.52\\-2.32}$	$2.43\substack{+2.79 \\ -2.90}$	$1.63\substack{+5.09 \\ -5.14}$	$-0.29\substack{+0.20\\-0.17}$
	Xing <i>et al.</i> [18]	${ m SU}(3)_{ m F}$	1.30 ± 0.51	-	-	-0.28 ± 0.18
	Geng <i>et al.</i> [19]	${ m SU}(3)_{ m F}$	7.10 ± 0.41	2.94 ± 0.97	5.66 ± 0.93	-0.49 ± 0.09
	Zhong et al. $[20]$	${ m Diagrammatic-SU(3)_F}$	7.45 ± 0.64	2.87 ± 0.66	5.31 ± 1.33	-0.51 ± 0.08
	Zhong et al. $[20]$	$\operatorname{Irreducible-SU(3)_{F}}$	7.72 ± 0.65	2.28 ± 0.53	5.66 ± 1.62	-0.51 ± 0.09

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 $\rightarrow \Xi^0 \pi^0$ asymmetry parameter Ξ^+



• $\Xi_c^+ \to \Xi^0 \pi^0$ asymmetry parameter: $\Rightarrow \alpha(\Xi_c^+ \to \Xi^0 \pi^0) = -0.90 \pm 0.15 (\text{stat.}) \pm 0.23 (\text{syst.})$ $\rightarrow \frac{dN}{d\cos\theta_{\Xi^0}} \propto 1 + \alpha(\Xi_c^0 \to \Xi^0 \pi^0) \alpha(\Xi^0 \to \Lambda \pi^0) \cos\theta_{\Xi^0}$





 $\Lambda_c^+ \to \Lambda K^+ \text{ and } \Lambda_c^+ \to \Sigma K^+$

• Direct CPV via raw asymmetry measurements in SCS decays:

$$A_{raw}(\Lambda_c^+ \to \Lambda K^+) = \frac{N(\Lambda_c^+ \to \Lambda K^+) - N(\bar{\Lambda}_c^- \to \bar{\Lambda} K^-)}{N(\Lambda_c^+ \to \Lambda K^+) + N(\bar{\Lambda}_c^- \to \bar{\Lambda} K^-)}$$

→ The raw asymmetry of $\Lambda_c^+ \to \Lambda K^+$ includes several asymmetry sources: $A_{raw}(\Lambda_c^+ \to \Lambda K^+) = A_{CP}^{dir}(\Lambda_c^+ \to \Lambda K^+) + A_{CP}^{dir}(\Lambda \to p\pi^-) + A_{\epsilon}^{\Lambda} + A_{\epsilon}^{K^+} + A_{FR}^{\Lambda_c^+}$ Detection efficiency correction, between K^+ , K^-

 \rightarrow Using CF mode $\Lambda_c^+ \rightarrow \Lambda \pi^+$ as a reference mode, common asymmetry sources are canceled out.

$$\Delta A_{raw} = A_{raw}^{corr}(\Lambda_c^+ \to \Lambda K^+) - A_{raw}^{corr}(\Lambda_c^+ \to \Lambda \pi^+)$$

$$= A_{raw}^{dir}(\Lambda_c^+ \to \Lambda K^+) - A_{raw}^{dir}(\Lambda_c^+ \to \Lambda \pi^+) = A_{raw}^{dir}(\Lambda_c^+ \to \Lambda K^+)$$

- → Similarly, $\Lambda_c^+ \to \Sigma^0 \pi^+$ mode was used as a reference mode for $\Lambda_c^+ \to \Sigma^0 K^+$.
- First A_{CP}^{dir} for SCS two-body decays of charmed baryons.

•
$$A_{CP}^{dir}(\Lambda_c^+ \to \Lambda K^+) = (2.1 \pm 2.6 \pm 0.1) \times 10^{-2}$$

- $A_{CP}^{dir}(\Lambda_c^+ \to \Sigma^0 K^+) = (2.5 \pm 5.4 \pm 0.4) \times 10^{-2}$
- No significant direct CP violation was observed.



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Belle 980/fb, Science Bulletin 68 (2023) 583



- Branching fractions were measured as well
- $B(\Lambda_c^+ \to \Lambda K^+) = (6.57 \pm 0.17 \pm 0.11 \pm 0.35) \times 10^{-4}$
- $B(\Lambda_c^+ \to \Sigma^0 K^+) = (3.58 \pm 0.19 \pm 0.06 \pm 0.19) \times 10^{-4}$





Flatté model



$$f_{\rm el} = -\frac{1}{2q} \frac{\Gamma_P}{E - E_{\rm BW} + i\frac{\Gamma_P}{2} + i\bar{g}_K\frac{k}{2}}$$

where, $k = \sqrt{m_K}(\sqrt{s} - 2m_k)$ *k is imaginary when $m < 2m_K$



