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3 Charm physics at the Belle and Belle II experiments\*

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10 We present recent results on charm physics at the Belle and Belle II experiments, cover-  
 11 ing measurements of charm lifetimes, branching fractions of the decays of charmed  
 12 mesons and baryons and the decay asymmetry parameters of two-body decays of charmed  
 13 baryons, searches for rare and forbidden decays, and measurements of  $CP$  violating pa-  
 14 rameters in the four-body decays of charmed mesons and two-body decays of charmed  
 15 baryons.

16 Keywords: Charm physics;  $CP$  violation; Belle; Belle II.

17 1. Charm production at Belle and Belle II

18 The Belle II experiment, operating in the energy-asymmetric  $e^+e^-$  collider Su-  
 19 perKEKB, has been designed to conduct precise measurements of weak interac-  
 20 tion parameters, explore exotic hadrons, and probe for novel phenomena beyond  
 21 the Standard Model of particle physics. From 2019 to 2022, it accumulated an in-  
 22 tegrated luminosity  $427 \text{ fb}^{-1}$ , thereby, a total  $1.4 \text{ ab}^{-1}$  from Belle and Belle II  
 23 experiments provides large samples of beauty and charm hadrons, as well as tau  
 24 leptons. There exist two primary avenues of charm production at Belle and Belle II:  
 25 (1) via the continuum process  $e^+e^- \rightarrow c\bar{c}$ , having a cross section of  $\sigma = 1.3 \text{ nb}$ ; (2)  
 26 from decays of  $B$  mesons, where charmed hadrons are involved in the final state.  
 27 In Table 1, a comparison of available charm samples at BESIII, Belle, Belle II, and  
 28 LHCb, along with their own typical characters, is presented. Importantly, these  
 29 experiments will continue to collect data with increased luminosity in the future,  
 30 heralding a promising outlook for further research in charm physics.





31 2. Charm lifetime measurements

32 Hadron lifetimes are difficult to calculate theoretically, as they depend on nonper-  
 33 turbative effects arising from quantum chromodynamics (QCD). Comparing cal-

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Table 1. Comparison of available charm samples at BESIII, Belle and Belle II, and LHCb experiments. The typical characters of these three kinds of experiment are also listed.

Experiment	Machine	$E_{C.M.}$	Luminosity	$N_{\text{prod}}$	Efficiency	Characters
	BEPc-II ( $e^+e^-$ )	3.77 GeV 4.18-4.23 GeV 4.6-4.7 GeV	2.9 (8 → 20) $\text{fb}^{-1}$ 7.3 $\text{fb}^{-1}$ 4.5 $\text{fb}^{-1}$	$D^{0,+}$ : $10^7$ (→ $10^8$ ) $D_s^+$ : $5 \times 10^6$ $\Lambda_c^+$ : $0.8 \times 10^6$ ★☆☆	~ 10-30% ★★★	<ul style="list-style-type: none"> <li>⊙ extremely clean environment</li> <li>⊙ quantum coherence</li> <li>⊙ no boost, no time-dept analysis</li> </ul>
	SuperKEKB ( $e^+e^-$ )	10.58 GeV	0.4 (→ 50) $\text{ab}^{-1}$	$D^0$ : $6 \times 10^8$ (→ $10^{11}$ ) $D_{(s)}^+$ : $10^8$ (→ $10^{10}$ ) $\Lambda_c^+$ : $10^7$ (→ $10^9$ )	$\mathcal{O}(1-10\%)$	<ul style="list-style-type: none"> <li>⊙ high-efficiency detection of neutrals</li> <li>⊙ good trigger efficiency</li> <li>⊙ time-dependent analysis</li> <li>⊙ smaller cross-section than LHCb</li> </ul>
	KEKB ( $e^+e^-$ )	10.58 GeV	1 $\text{ab}^{-1}$	$D^{0,+}$ , $D_s^+$ : $10^9$ $\Lambda_c^+$ : $10^8$ ★★★	★★	
	LHC ( $pp$ )	7+8 TeV 13 TeV	1+2 $\text{fb}^{-1}$ 6 $\text{fb}^{-1}$ (→ 23 → 50) $\text{fb}^{-1}$	$5 \times 10^{12}$ $10^{13}$ ★★★★	$\mathcal{O}(0.1\%)$ ★	<ul style="list-style-type: none"> <li>⊙ very large production cross-section</li> <li>⊙ large boost, excellent time resolution</li> <li>⊙ dedicated trigger required</li> </ul>

Here uses  $\sigma(D^0\bar{D}^0@3.77\text{ GeV})=3.61$  nb,  $\sigma(D^+D^-@3.77\text{ GeV})=2.88$  nb,  $\sigma(D_s^*D_s@4.17\text{ GeV})=0.967$  nb;  $\sigma(c\bar{c}@10.58\text{ GeV})=1.3$  nb where each  $c\bar{c}$  event averagely has 1.1/0.6/0.3  $D^0/D^+/D_s^+$  yields;  $\sigma(D^0@CDF)=13.3$   $\mu\text{b}$ , and  $\sigma(D^0@LHCb)=1661$   $\mu\text{b}$ , mainly from Int. J. Mod. Phys. A 29(2014)24,14300518.

culated and measured values improves our understanding of QCD. At Belle II, the decay-time resolution is about twice better than that at Belle and BABAR. Utilizing the early Belle II dataset, three world-leading charm lifetimes have been measured:  $\tau(D^0) = 410.5 \pm 1.1 \pm 0.8$  fs,  $\tau(D^+) = 1030.4 \pm 4.7 \pm 3.1$  fs, and  $\tau(\Lambda_c^+) = 203.20 \pm 0.89 \pm 0.77$  fs;<sup>1,2</sup> and also a measurement<sup>3</sup> of  $\tau(\Omega_c^0) = 410.5 \pm 1.1 \pm 0.8$  fs agrees with the measurement by LHCb<sup>4</sup> and confirm that the  $\Omega_c^0$  is not the shortest-lived weakly decaying charmed baryon.

Based on a clean sample of 116k  $D_s^+ \rightarrow \phi\pi^+$  reconstructed in 207  $\text{fb}^{-1}$  of data at Belle II, the  $D_s^+$  lifetime is extracted via an unbinned maximum likelihood fit to the lifetime ( $t$ ) and its uncertainty ( $\sigma_t$ ).<sup>5</sup> The likelihood function for  $i$ th event is calculated by:

$$\mathcal{L}(\tau|t^i, \sigma_t^i) = f_{\text{sig}}P_{\text{sig}}(t^i|\tau, \sigma_t^i)P_{\text{sig}}(\sigma_t^i) + (1 - f_{\text{sig}})P_{\text{bkg}}(t^i|\tau, \sigma_t^i)P_{\text{bkg}}(\sigma_t^i)$$

where  $P_{\text{sig}}(\sigma_t^i)$  and  $P_{\text{bkg}}(\sigma_t^i)$  exist to avoid the Punzi bias. The fitted results are shown in Figure 1, and we obtain  $\tau_{D_s^+} = (499.5 \pm 1.7 \pm 0.9)$  fs, the world most precise measurement to date. Thus, Belle II has made the world's most precise measurements of the  $D^{0,+}$ ,  $D_s^+$ ,  $\Lambda_c^+$  lifetimes; their small systematic uncertainty demonstrates the excellent performance and understanding of the Belle II detector.

### 3. Measurement of branching fraction and decay asymmetry parameter

#### 3.1. Branching fraction of Cabibbo-suppressed decays of charmed mesons

Cabibbo-suppressed (CS) hadronic decays of charm mesons offer a potent avenue for exploring new physics. Precise measurements of their branching fractions are of paramount importance. Singly Cabibbo-suppressed (SCS) charm decays serve as essential probes to search for charm  $CP$  violation (CPV) and probe physics beyond the SM. The abundant charm sample available from Belle and Belle II provides

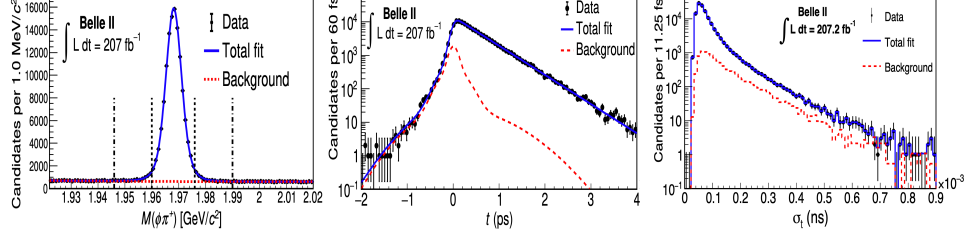


Figure 1. Invariant mass of reconstructed  $D_s^+ \rightarrow \phi\pi^+$  candidates; the projections of lifetime extraction with a fitting on  $(t, \sigma_t)$  at Belle II.<sup>5</sup>

57 an excellent opportunity to accurately measure their branching fractions. Recently,  
 58 Belle reported several first or most precise branching fractions of charmed meson  
 59 decays, based on the full dataset. The invariant mass distributions of reconstructed  
 60 decays are shown in Figure 2. Using the corresponding well-measured reference  
 61 modes, we obtain branching fractions ( $\mathcal{B}$ ) of three SCS decays:<sup>6,7</sup>

$$\mathcal{B}(D^+ \rightarrow K^+ K^- \pi^+ \pi^0) = (7.08 \pm 0.08 \pm 0.16 \pm 0.20) \times 10^{-3}, \quad (1)$$

$$\mathcal{B}(D_s^+ \rightarrow K^+ \pi^- \pi^+ \pi^0) = (9.44 \pm 0.34 \pm 0.28 \pm 0.32) \times 10^{-3}, \quad (2)$$

$$\mathcal{B}(D_s^+ \rightarrow K^+ K^- K_s^0 \pi^+) = (1.29 \pm 0.14 \pm 0.04 \pm 0.11) \times 10^{-4}; \quad (3)$$

62 and one DCS decays:<sup>6</sup>

$$\mathcal{B}(D^+ \rightarrow K^+ \pi^- \pi^+ \pi^0) = (1.05 \pm 0.07 \pm 0.02 \pm 0.03) \times 10^{-3}, \quad (4)$$

63 where the last one confirms the BESIII finding<sup>8,9</sup> of a significantly larger  $\mathcal{B}$  than  
 64 other known DCS decays.

### 65 3.1.1. Branching fraction of charmed baryon decays

66 The weak decays of charmed baryons provide an excellent platform for understand-  
 67 ing QCD with transitions involving the charm quark. The decay amplitudes consist  
 68 of factorizable and non-factorizable contributions. Experimentally, the study of  
 69 charmed baryons is more challenging than that of charmed meson due to smaller ex-  
 70 perimental samples. Some CF decays are still poorly or not yet measured. Recently,  
 71 Belle and Belle II reported many branching fractions of charmed baryons.<sup>10–12,14</sup>  
 72 The distributions of invariant mass of reconstructed  $\Lambda_c^+$  in six decay channels, and  
 73 their corresponding fit results, are shown in Figure 3.

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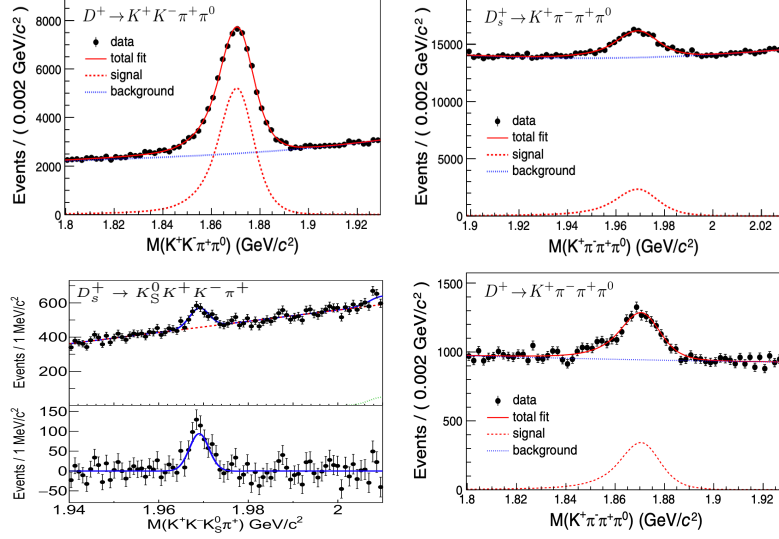


Figure 2. Invariant mass of reconstructed  $D$  candidates for the SCS decays  $D^+ \rightarrow K^+ K^- \pi^+ \pi^0$ ,  $D_s^+ \rightarrow K^+ \pi^- \pi^+ \pi^0$ ,  $D_s^+ \rightarrow K^+ K^- K_S^0 \pi^+$ , and the DCS decay  $D^+ \rightarrow K^+ \pi^- \pi^+ \pi^0$  at Belle.<sup>6,7</sup>

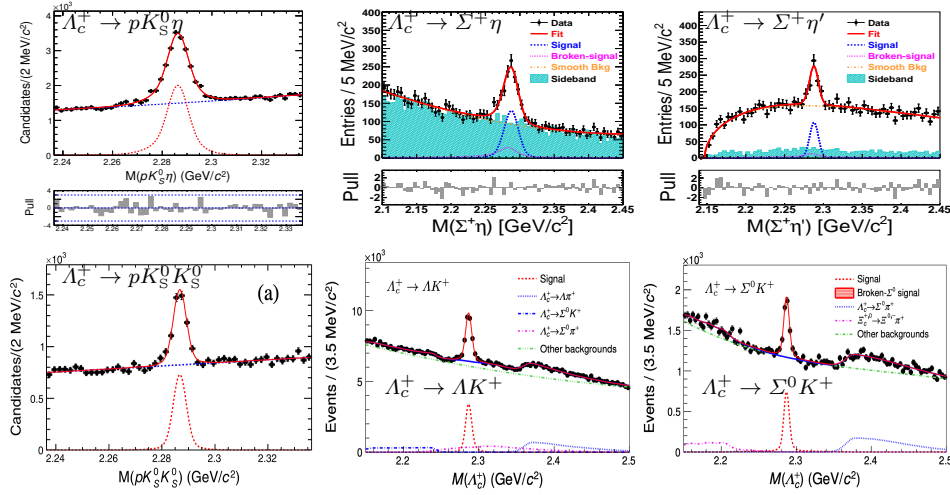


Figure 3. Invariant mass distributions of reconstructed  $\Lambda_c^+$  candidates and their corresponding fit results for six decay modes at Belle.<sup>10–12,14</sup>

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We report the branching fractions of three CF and three SCS decays:

$$\mathcal{B}(\Lambda_c^+ \rightarrow p K_S^0 \eta) = (4.35 \pm 0.10 \pm 0.20 \pm 0.22) \times 10^{-3}, \quad (5)$$

$$\mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^+ \eta) = (3.14 \pm 0.35 \pm 0.17 \pm 0.25) \times 10^{-3}, \quad (6)$$

$$\mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^+ \eta') = (4.16 \pm 0.75 \pm 0.25 \pm 0.33) \times 10^{-3}, \quad (7)$$

$$\mathcal{B}(\Lambda_c^+ \rightarrow p K_S^0 K_S^0) = (2.35 \pm 0.12 \pm 0.07 \pm 0.12) \times 10^{-4}, \quad (8)$$

$$\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda K^+) = (6.57 \pm 0.17 \pm 0.11 \pm 0.35) \times 10^{-4}, \quad (9)$$

$$\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda K^+) = (3.58 \pm 0.19 \pm 0.06 \pm 0.19) \times 10^{-4}, \quad (10)$$

75 and five results for the  $\Xi_c^0$  and  $\Omega_c^0$  decays:

$$\mathcal{B}(\Xi_c^0 \rightarrow \Xi^0 \pi^0) = (6.9 \pm 0.3 \pm 0.5 \pm 1.5) \times 10^{-3}, \quad (11)$$

$$\mathcal{B}(\Xi_c^0 \rightarrow \Xi^0 \eta) = (1.6 \pm 0.2 \pm 0.2 \pm 0.4) \times 10^{-3}, \quad (12)$$

$$\mathcal{B}(\Xi_c^0 \rightarrow \Xi^0 \eta') = (1.2 \pm 0.3 \pm 0.1 \pm 0.3) \times 10^{-3}, \quad (13)$$

$$\frac{\mathcal{B}(\Omega_c^0 \rightarrow \Xi^- \pi^+)}{\mathcal{B}(\Omega_c^0 \rightarrow \Omega^- \pi^+)} = 0.253 \pm 0.052 \pm 0.030, \quad (14)$$

$$\frac{\mathcal{B}(\Omega_c^0 \rightarrow \Xi^- K^+)}{\mathcal{B}(\Omega_c^0 \rightarrow \Omega^- \pi^+)} < 0.070. \quad (15)$$

76 All of these results are the first or most precise measurements to date.

### 77 3.1.2. Decay asymmetry parameters of two-body decays of charmed baryons

78 The decay asymmetry parameter  $\alpha$  was introduced by Lee and Yang to study  
 79 the parity-violating and parity-conserving amplitudes in weak hyperon decays. In  
 80  $1/2^+ \rightarrow 1/2^+ + 0^-$ ,  $\alpha \equiv 2 \cdot \text{Re}(S^*P)/(|S|^2 + |P|^2)$ , where  $S$  and  $P$  denote the parity-  
 81 violating  $S$ -wave and parity-conserving  $P$ -wave amplitudes, respectively. Taking  
 82  $\Lambda_c^+ \rightarrow \Lambda h^+$ ,  $\Sigma^+ h^0$  decays for example, the differential decay rate has a dependence  
 83 on  $\alpha$ :

$$\frac{dN(\Lambda_c^+ \rightarrow \Lambda h^+)}{d \cos \theta_A} \propto 1 + \alpha_{\Lambda_c^+} \alpha_- \cos \theta_A, \quad (16)$$

84 where  $\alpha_-$  is hyperon decay asymmetry parameter. For  $\Lambda_c^+ \rightarrow \Sigma^0 h^+$  decays, consid-  
 85 ering  $\alpha(\Sigma^0 \rightarrow \gamma \Lambda)$  is zero due to parity conservation for an electromagnetic decay,  
 86 the differential decay rate is

$$\frac{dN(\Lambda_c^+ \rightarrow \Sigma^0 h^+)}{d \cos \theta_{\Sigma^0} d \cos \theta_A} \propto 1 - \alpha_{\Lambda_c^+} \alpha_- \cos \theta_{\Sigma^0} \cos \theta_A \quad (17)$$

87 By studying the hyperon helicity angle, we can extract  $\alpha$  from charmed baryon  
 88 decays. The results are listed in Tab. 2.

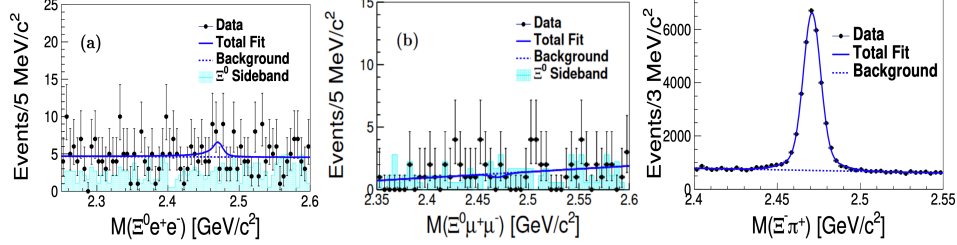
## 89 4. Search for rare or forbidden decays in charm sector

90 In the Standard Model (SM), the weak-current interaction has an identical coupling  
 91 to all lepton generations (Lepton Flavor Universality (LFU)). LFU can be tested  
 92 in semi-leptonic decays, such as  $\Xi_c^0 \rightarrow \Xi^0 \ell^+ \ell^-$  where a comparison of  $\ell = e$  and  $\mu$   
 93 decay rates would comprise such a test. Recently Belle reported a search for  $\Xi_c^0 \rightarrow$   
 94  $\Xi^0 \ell^+ \ell^-$  based on the Belle full data set.<sup>21</sup> The fits of invariant mass of reconstructed  
 95  $\Xi_c^0$  candidates for signal modes and reference mode are shown in Figure 4. The upper  
 96 limits on branching fractions relative to reference mode  $\Xi_c^0 \rightarrow \Xi^- \pi^+$  are measured  
 97 to be  $\frac{\mathcal{B}(\Xi_c^0 \rightarrow \Xi^- e^+ e^-)}{\mathcal{B}(\Xi_c^0 \rightarrow \Xi^- \pi^+)} < 6.7 \times 10^{-3}$  and  $\frac{\mathcal{B}(\Xi_c^0 \rightarrow \Xi^- \mu^+ \mu^-)}{\mathcal{B}(\Xi_c^0 \rightarrow \Xi^- \pi^+)} < 4.3 \times 10^{-3}$ . A more precise  
 98 analysis based on larger data samples collected by Belle II is expected in the future.  
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 Table 2. Recent measurements of  $\alpha$  at Belle,<sup>11–15</sup> with BE-SIII,<sup>16,18,19</sup> CLEO<sup>20</sup> and world average (W.A.)<sup>17</sup> values.

Decay	Belle	Other experiments
$\Lambda_c^+ \rightarrow pK_S^0$	–	$0.18 \pm 0.45$ <sup>16</sup>
$\Lambda_c^+ \rightarrow \Lambda K^+$	$-0.585 \pm 0.052$ <sup>11</sup>	–
$\Lambda_c^+ \rightarrow \Sigma^0 K^+$	$-0.54 \pm 0.20$ <sup>11</sup>	–
$\Lambda_c^+ \rightarrow \Lambda \pi^+$	$-0.755 \pm 0.006$ <sup>11</sup>	$-0.84 \pm 0.09$ <sup>17</sup>
$\Lambda_c^+ \rightarrow \Sigma^0 \pi^+$	$-0.463 \pm 0.018$ <sup>11</sup>	$-0.73 \pm 0.18$ <sup>16</sup>
$\Lambda_c^+ \rightarrow \Sigma^+ \pi^0$	$-0.480 \pm 0.028$ <sup>12</sup>	$-0.55 \pm 0.11$ <sup>17</sup>
$\Lambda_c^+ \rightarrow \Sigma^+ \eta$	$-0.990 \pm 0.058$ <sup>12</sup>	–
$\Lambda_c^+ \rightarrow \Sigma^+ \eta'$	$-0.460 \pm 0.067$ <sup>12</sup>	–
$\Lambda_c^+ \rightarrow \Xi^0 K^+$	–	$+0.01 \pm 0.16$ <sup>18</sup>
$\Lambda_c^+ \rightarrow \Lambda \rho^+$	–	$-0.76 \pm 0.07$ <sup>19</sup>
$\Lambda_c^+ \rightarrow \Sigma'^+ \pi^0$	–	$-0.92 \pm 0.09$ <sup>19</sup>
$\Lambda_c^+ \rightarrow \Sigma'^0 \pi^+$	–	$-0.79 \pm 0.11$ <sup>19</sup>
<hr/>		
$\Xi_c^0 \rightarrow \Xi^- \pi^+$	$-0.63 \pm 0.03$ <sup>13</sup>	$-0.56 \pm 0.40$ <sup>20</sup>
$\Xi_c^0 \rightarrow \Xi^0 \pi^0$	$-0.90 \pm 0.27$ <sup>14</sup>	–
$\Xi_c^0 \rightarrow \Lambda \bar{K}^{*0}$	$+0.15 \pm 0.22$ <sup>15</sup>	–
$\Xi_c^0 \rightarrow \Sigma^+ K^{*-}$	$-0.52 \pm 0.30$ <sup>15</sup>	–


 Figure 4. The invariant mass of reconstructed  $\Xi_c^0$  candidates for signal modes  $\Xi_c^0 \rightarrow \Xi^0 \ell^+ \ell^-$  and reference mode  $\Xi_c^0 \rightarrow \Xi^- \pi^+$  at Belle.<sup>21</sup>

100 Baryon number violation (BNV) is one of the crucial conditions to create matter-  
 101 antimatter asymmetry as observed in the universe. Several grand unified theories,  
 102 supersymmetry and other SM extensions propose BNV processes of nucleons. The  
 103  $D \rightarrow p\ell$  decays violate baryon (B) and lepton (L) numbers but their difference is  
 104 conserved ( $\Delta(B-L) = 0$ ). The previous stringent limit is  $\mathcal{B}(D^0 \rightarrow \bar{p}e^+) < 1.2 \times 10^{-6}$   
 105 at a 90% C.L. and recent BESIII result is  $\mathcal{B}(D^0 \rightarrow pe^-) < 2.2 \times 10^{-6}$ . Recently,  
 106 Belle reported a stricter upper limits:  $(5-8) \times 10^{-7}$  dependent on the decay modes,  
 107 as shown in Table 3.

## 108 5. Charm $CP$ violation searches

109 The violation of  $CP$ -symmetry, the combination of charge conjugation symmetry  
 110 and parity asymmetry, is essential for elucidating the matter-antimatter asymmetry  
 111 in the universe. In the Standard Model (SM) of particle physics, the sole source of

Table 3. Reconstruction efficiency ( $\varepsilon$ ), signal yield ( $N_S$ ), signal significance ( $S$ ), upper limit on the signal yield ( $N_{p\ell}^{\text{UL}}$ ), and branching fraction ( $\mathcal{B}$ ) at 90% confidence level for baryon number violating decay modes.

Decay mode	$\varepsilon(\%)$	$N_S$	$S(\sigma)$	$N_{p\ell}^{\text{UL}}$	$\mathcal{B} (10^{-7})$
$D^0 \rightarrow pe^-$	10.2	$-6.4 \pm 8.5$	–	17.5	$< 5.5$
$\bar{D}^0 \rightarrow pe^-$	10.2	$-18.4 \pm 23.0$	–	22.0	$< 6.9$
$D^0 \rightarrow \bar{p}e^+$	9.7	$-4.7 \pm 23.0$	–	22.0	$< 7.2$
$\bar{D}^0 \rightarrow \bar{p}e^+$	9.6	$7.1 \pm 9.0$	0.6	23.0	$< 7.6$
$D^0 \rightarrow p\mu^-$	10.7	$11.0 \pm 23.0$	0.9	17.1	$< 5.1$
$\bar{D}^0 \rightarrow p\mu^-$	10.7	$-10.8 \pm 27.0$	–	21.8	$< 6.5$
$D^0 \rightarrow \bar{p}\mu^+$	10.5	$-4.5 \pm 14.0$	–	21.1	$< 6.3$
$\bar{D}^0 \rightarrow \bar{p}\mu^+$	10.4	$16.7 \pm 8.8$	1.6	21.4	$< 6.5$

112  $CP$  violation (CPV) arises from a single complex phase in the Cabibbo-Kobayashi-  
 113 Maskawa matrix. However, this source is insufficient to account for the observed  
 114 matter-antimatter asymmetry. Therefore, we need new CPV sources beyond the  
 115 SM. Charm CPV in the SM is very small, at level of  $\mathcal{O}(10^{-3})$  or smaller, but new  
 116 physics (NP) may enhance it. Therefore, a study of charm CPV may help to test  
 117 the SM and act as a sensitive probe for NP. Experimentally, we have only one CPV  
 118 observation in charm sector:  $\Delta A_{CP}(D^0 \rightarrow K^+K^-, \pi^+\pi^-) = (-15.4 \pm 2.9) \times 10^{-4}$   
 119 ( $5.3\sigma$ ) from LHCb. To understand such CPV, we need to work on more channels  
 120 and improve the precision of measured  $CP$  asymmetries. On the other hand, CPV  
 121 has been observed in the open-flavored meson sector, but not yet in the baryon  
 122 sector. Baryogenesis, the process by which the baryon-antibaryon asymmetry of  
 123 the universe developed, is directly related to baryon CPV. Discovering the CPV  
 124 in charmed baryon decays is correctly one of the main targets of charm physics.  
 125 Recently we have reported CPV searches in four-body decays of charmed mesons,  
 126 and  $\alpha$ -induced CPV and direct CPV in  $\Lambda_c^+$  two-body decays.

### 127 5.1. CPV in four-body decays of charmed mesons

128 Sensitivity to CPV varies with the decay channel, motivating CPV searches in di-  
 129 verse charm decays. The  $D$  four-body decays, with large branching fractions and  
 130 involving various intermediate processes, provide a good platform for CPV searches.  
 131 CPV in  $D$  four-body decay was probed with triple-product asymmetries by the  
 132 FOCUS, BABAR, LHCb and Belle experiments. The triple-product (TP) is de-  
 133 fined in the  $D$  rest frame using the momenta of three particles in the final state,  
 134  $C_{\text{TP}} = \vec{p}_i \cdot (\vec{p}_j \times \vec{p}_k)$  for  $D \rightarrow P_i P_j P_k P_l$  decays, and satisfies  $CP(C_{\text{TP}}) = -\bar{C}_{\text{TP}}$ .  
 135 The sign of  $C_{\text{TP}}$  denotes whether the  $\vec{p}_i$  points “upward” or “downward” in the  
 136 plane defined by  $\vec{p}_j$  and  $\vec{p}_k$ , therefore, its asymmetry is called an up-down asymme-

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 137 try. The TP asymmetries in  $D^+$  and  $D^-$  decays are defined as

$$A_T(D^+) = \frac{N_+(C_T > 0) - N_+(C_T < 0)}{N_+(C_T > 0) + N_+(C_T < 0)}, \quad (18)$$

$$\bar{A}_T(D^-) = \frac{N_-(-\bar{C}_T > 0) - N_-(-\bar{C}_T < 0)}{N_-(-\bar{C}_T > 0) + N_-(-\bar{C}_T < 0)}. \quad (19)$$

138 And their difference is assigned as a  $CP$ -violating parameter, i.e.  $a_{CP}^{T\text{-odd}} =$   
 139  $\frac{1}{2} \cdot (A_T(D^+) - \bar{A}_T(D^-))$ . This parameter  $a_{CP}^{T\text{-odd}} \propto \sin \phi \cos \delta$ , where  $\phi$  and  $\delta$  are  
 140 the weak and strong phase differences, respectively, between at least two amplitudes  
 141 contributing to the decay. The  $a_{CP}^{T\text{-odd}}$  has its largest value when  $\delta = 0$ , while a  
 142 non-zero direct  $CP$  asymmetry requires  $\delta \neq 0$ , therefore  $a_{CP}^{T\text{-odd}}$  is an observable  
 143 complementary to direct  $CP$  asymmetry.

144 Recently Belle searched for CPV with TP asymmetries in the decays of  $D^0 \rightarrow$   
 145  $K_S^0 K_S^0 \pi^+ \pi^-$ ,<sup>22</sup>  $D_{(s)}^+ \rightarrow K_S^0 h^+ \pi^+ \pi^-$ ,<sup>7</sup> and  $D_{(s)}^+ \rightarrow K h \pi^+ \pi^0$ .<sup>23</sup> They are listed in  
 146 Figure 5. Most of these  $a_{CP}^{T\text{-odd}}$  results from Belle are first or most precise measurements.

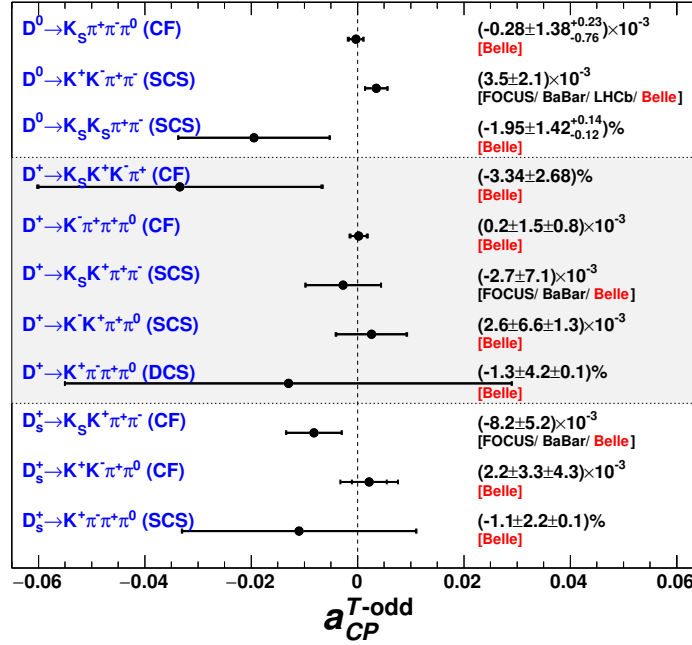


Figure 5. Belle results for  $a_{CP}^{T\text{-odd}}$  along with other measurements for  $D^0$  and  $D_{(s)}^+$  decays. For decays in which more than one measurement has been made, the world average value is plotted.



148 5.2. CPV in  $\Lambda_c^+ \rightarrow \Lambda K^+, \Sigma^0 K^+$ 

 149 Recently, a search for direct CPV and  $\alpha$ -induced CPV in  $\Lambda_c^+ \rightarrow \Lambda K^+, \Sigma^0 K^+$  was  
 150 reported based on the Belle full data set.<sup>11</sup>

 151 For SCS decay, for example  $\Lambda_c^+ \rightarrow \Lambda K^+$ , the raw asymmetry includes several  
 152 sources:

$$A_{\text{raw}} = A_{CP}^{\Lambda_c^+ \rightarrow \Lambda K^+} + A_{CP}^{\Lambda \rightarrow p \pi^-} + A_\varepsilon^\Lambda + A_\varepsilon^{K^+} + A_{\text{FB}}^{\Lambda_c^+} \quad (20)$$

 153 where  $A_{CP}^{\Lambda_c^+ \rightarrow \Lambda K^+}$  ( $A_{CP}^{\Lambda \rightarrow p \pi^-}$ ) is the  $CP$  asymmetry associated with  $\Lambda_c^+$  ( $\Lambda$ ) decay;  
 154  $A_\varepsilon^\Lambda$  is an asymmetry arising from detection efficiencies of  $\Lambda$  and  $\bar{\Lambda}$ ;  $A_\varepsilon^{K^+}$  is the  
 155  $K^+$  reconstruction and identification asymmetry and can be removed by weighting  
 156  $w_{\Lambda_c^+, \bar{\Lambda}_c^-} = 1 \mp A_\varepsilon^{K^+} [\cos \theta, p_T]$ ;  $A_{\text{FB}}^{\Lambda_c^+}$  arises from the forward-backward asymmetry of  
 157  $\Lambda_c^+$  production due to  $\gamma$ - $Z^0$  interference and higher-order QED effects in  $e^+e^- \rightarrow c\bar{c}$   
 158 collisions. We use the corresponding CF modes,  $\Lambda_c^+ \rightarrow \Lambda \pi^+$  and  $\Lambda_c^+ \rightarrow \Sigma^0 \pi^+$ , as  
 159 reference modes to remove the common asymmetry sources:  $A_{CP}^{\Lambda \rightarrow p \pi^-}$ ,  $A_\varepsilon^\Lambda$  and  $A_{\text{FB}}^{\Lambda_c^+}$ .  
 160 Under the current precision, the CPV in charm CF mode is consistent with zero,  
 161 i.e.  $A_{CP}^{\Lambda_c^+ \rightarrow \Lambda \pi^+} = 0$ . Finally, we have first results of a search for direct  $CP$  asymmetry  
 162 in two-body SCS decays of charmed baryons:

$$A_{CP}^{\text{dir}}(\Lambda_c^+ \rightarrow \Lambda K^+) = (+2.1 \pm 2.6 \pm 0.1)\%, \quad (21)$$

$$A_{CP}^{\text{dir}}(\Lambda_c^+ \rightarrow \Sigma^0 K^+) = (+2.5 \pm 5.4 \pm 0.4)\%. \quad (22)$$

 163 For  $\Lambda_c^+ \rightarrow \Lambda h^+$  decays, the differential decay rate depends on  $\alpha$  parameters and  
 164 one helicity angle:

$$\frac{dN}{d \cos \theta_\Lambda} \propto 1 + \alpha_{\Lambda_c^+} \alpha_- \cos \theta_\Lambda, \quad (23)$$

 165 where  $\alpha_{\Lambda_c^+}$  is the decay asymmetry parameter of  $\Lambda_c^+ \rightarrow \Lambda h^+$ , and  $\theta_\Lambda$  is the angle  
 166 between the proton momentum and the direction opposite the  $\Lambda_c^+$  momentum in  
 167 the  $\Lambda$  rest frame.

 168 For  $\Lambda_c^+ \rightarrow \Sigma^0 h^+$  decays, considering  $\alpha(\Sigma^0 \rightarrow \gamma \Lambda)$  is zero due to parity conser-  
 169 vation for an electromagnetic decay, the differential decay rate is given by

$$\frac{dN}{d \cos \theta_{\Sigma^0} d \cos \theta_\Lambda} \propto 1 - \alpha_{\Lambda_c^+} \alpha_- \cos \theta_{\Sigma^0} \cos \theta_\Lambda, \quad (24)$$

 170 where  $\theta_\Lambda$  ( $\theta_{\Sigma^0}$ ) is the angle between the proton ( $\Lambda$ ) momentum and the direction  
 171 opposite the  $\Sigma^0$  ( $\Lambda_c^+$ ) momentum in the  $\Lambda$  ( $\Sigma^0$ ) rest frame. Since  $\alpha$  is a CP-odd  
 172 observable, the corresponding  $CP$ -violating parameter is defined as

$$A_{CP}^\alpha = \frac{\alpha_{\Lambda_c^+} + \alpha_{\bar{\Lambda}_c^-}}{\alpha_{\Lambda_c^+} - \alpha_{\bar{\Lambda}_c^-}}. \quad (25)$$

 173 Under  $CP$  conservation, we have  $\alpha_{\Lambda_c^+} = -\alpha_{\bar{\Lambda}_c^-}$ . We measured the  $\alpha$ -parameters  
 174 for the separate  $\Lambda_c^+$  and  $\bar{\Lambda}_c^-$  samples, as shown in Figure 6 for  $\Lambda_c^+ \rightarrow \Lambda K^+$ , and

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175 calculate the  $\alpha$ -induced CPV parameter  $A_{CP}^\alpha$ . We have

$$A_{CP}^\alpha(\Lambda_c^+ \rightarrow \Lambda K^+) = -0.023 \pm 0.086 \pm 0.071, \quad (26)$$

$$A_{CP}^\alpha(\Lambda_c^+ \rightarrow \Sigma^0 K^+) = +0.08 \pm 0.35 \pm 0.14. \quad (27)$$

176 No evidence of CPV is found in these two decays.

177 We also probe the  $\Lambda$ -hyperon CPV in CF decays  $\Lambda_c^+ \rightarrow \Lambda \pi^+$  and  $\Lambda_c^+ \rightarrow \Sigma^0 \pi^+$ ,  
 178 inspired by a theoretical paper.<sup>24</sup> The  $\Lambda$ -hyperon CP asymmetry  $A_{CP}^\alpha(\Lambda \rightarrow p \pi^-)$   
 179 can be extracted from the total  $\alpha$ -induced CP asymmetry of  $\Lambda_c^+$  decay chain:

$$A_{CP}^\alpha(\text{total}) \equiv \frac{\alpha_{\Lambda_c^+} \alpha_- - \alpha_{\bar{\Lambda}_c^-} \alpha_+}{\alpha_{\Lambda_c^+} \alpha_- + \alpha_{\bar{\Lambda}_c^-} \alpha_+} = A_{CP}^\alpha(\Lambda \rightarrow p \pi^-). \quad (28)$$

180 for Cabibbo-favored (CF) decays  $\Lambda_c^+ \rightarrow (\Lambda, \Sigma^0) \pi^+$ ,  $\alpha_{\Lambda_c^+} = -\alpha_{\bar{\Lambda}_c^-}$  since no CP  
 181 asymmetry is expected in the SM. CPV in hyperon decays is predicted to be at the  
 182 level of  $\mathcal{O}(10^{-4})$  or smaller in the SM<sup>25-28</sup> and can be enhanced to reach the level  
 183 of  $10^{-3}$  in some new physics models.<sup>28-32</sup> The average value of  $A_{CP}^\alpha(\Lambda \rightarrow p \pi^-)$  in  
 184 two such CF modes is calculated to be

$$A_{CP}^\alpha(\Lambda \rightarrow p \pi^-) = +0.013 \pm 0.007 \pm 0.011. \quad (29)$$

185 This is the first measurement of hyperon CPV searches in CF charm decays. No  
 186 evidence of  $\Lambda$ -hyperon CPV is found.

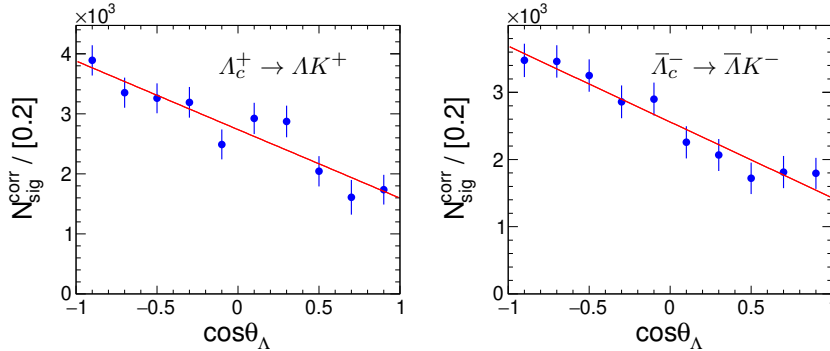


Figure 6. The  $\cos\theta_\Lambda$  distribution of  $\Lambda_c^+ \rightarrow \Lambda K^+$  after efficiency-correction. We fit with a linear function of  $1 + \alpha_{\Lambda_c^\pm} \alpha_\mp \cos\theta_\Lambda$  with goodness-of-fit  $\chi^2/9 = 1.04, 0.57$ , respectively, at Belle.<sup>11</sup>

## 187 6. Summary

188 Belle continues to produce the fruitful charm results, even though its data taking  
 189 finished 13 years ago. Belle II has joined the game since 2019. Now a dataset with  
 190  $427 \text{ fb}^{-1}$  is available. We reported some recent results on measurements of  $\mathcal{B}$  and  
 191  $\alpha$ , CPV searches in the charmed meson and baryon decays, and several searches  
 192 for rare or forbidden decays. By utilizing the early dataset at Belle II, we obtain

193 the world's best  $\tau(D^{0,+})$ ,  $\tau(D_s^+)$ , and  $\tau(\Lambda_c^+)$ , and confirmation of the LHCb  $\tau(\Omega_c^0)$   
 194 result. More charm results based on a combined dataset of  $1.4 \text{ ab}^{-1}$  at Belle and  
 195 Belle II will be forthcoming. The scheduled luminosity accumulations, as shown in  
 Figure 7, promise the fruitful charm results at Belle II in the future.

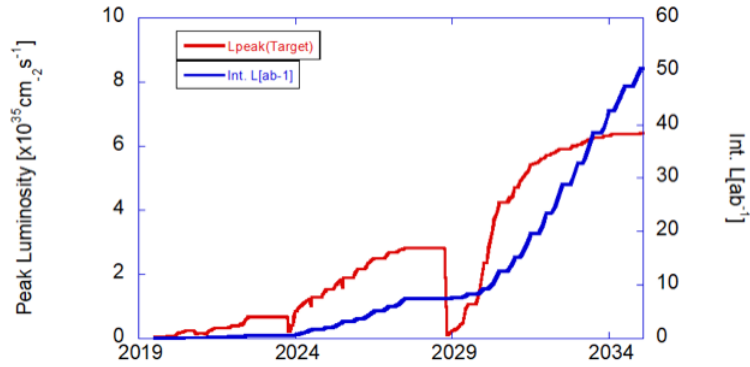


Figure 7. Luminosity projection with plans up to spring 2034 at SuperKEKB.

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