

# Amplitude Analysis of

# $B^0 \longrightarrow K^+ \pi^- \pi^0$ Decays

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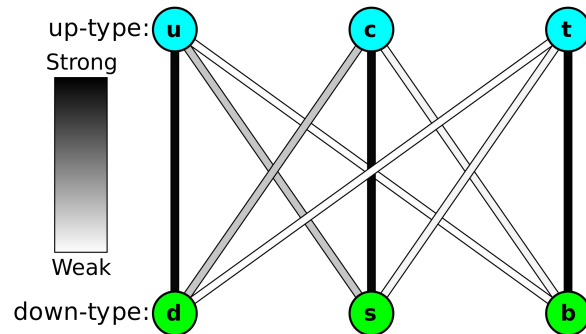
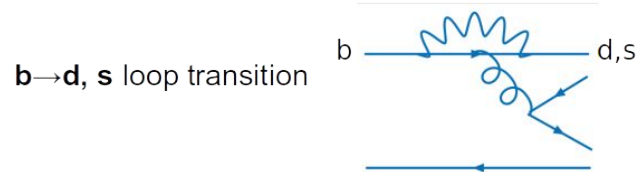
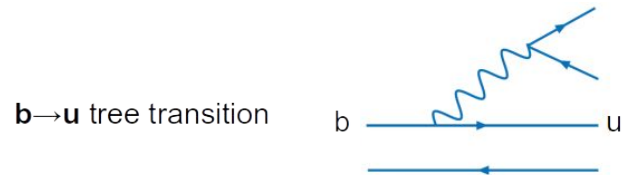
# Introduction



- ❖ Our goal: to extract branching ratios of the virtual particles and CP asymmetry
- ❖ Our method: Dalitz Plot analysis
- ❖ Why charmless B-decays:
  - CKM suppressed on tree level
  - loop transitions are the dominating contributions
  - New Physics particles could appear as virtual particles in loops
  - small effects visible, because SM physics suppressed
- ❖ We study simulation generated data from Belle II

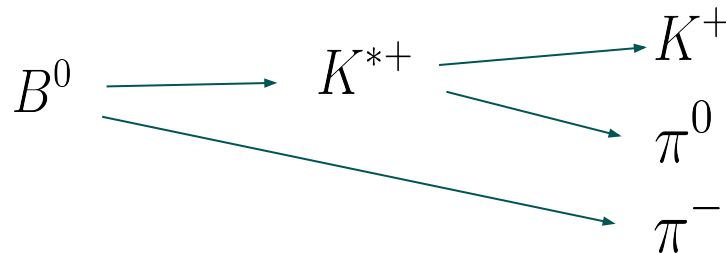
$$B^0 \longrightarrow K^+ \pi^- \pi^0$$

- need to transform:  $b \rightarrow u, d, s$



# The Decay and the Resonances

- We use the isobar model to describe the 3 body decay
  - Isobar Model: within the Isobar Model one assumes that the B decay proceeds via an intermediate two-body resonance
  - i.e. we treat the system as two subsequent two-body decays
- Resonance: pull in the decay amplitude, describes particles with very short lifetimes or virtual particles



Resonances
$K^*(892)^0$ and $K^*(892)^+$
$\rho(770)^-$ , $\rho(1450)^-$ and $\rho(1700)^-$
$(K\pi)_0^{*0}$ and $(K\pi)_0^{*+}$
non-resonant

# The Dalitz Plot and How to Model It



The Amplitude for one resonance is given by:

$$A_i = L_i(J, x) \cdot T_i(J, x, y) \cdot B_i(J, x)$$

Line shape

Angular  
dependence

Angular momentum  
Barrier factor

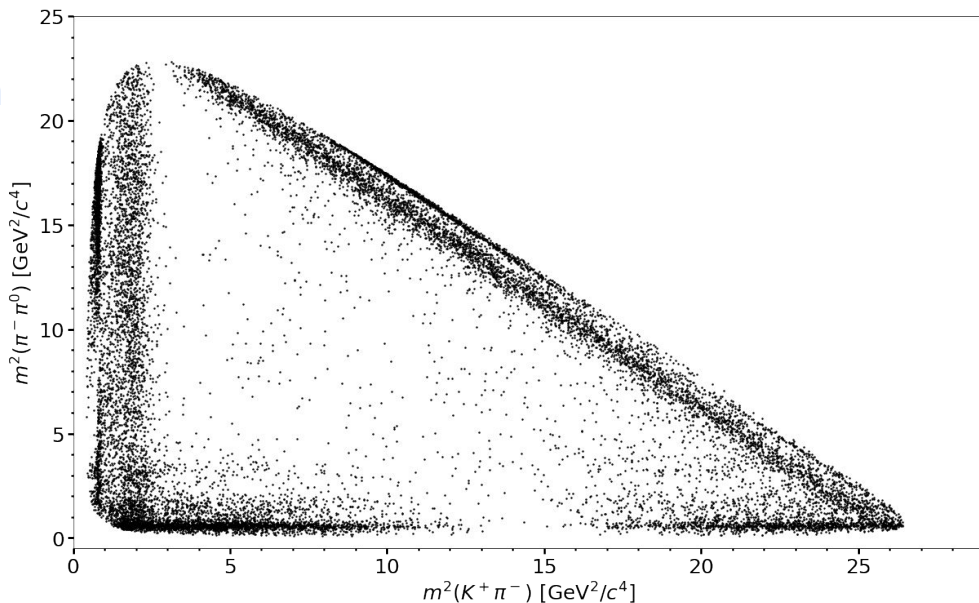
J: Angular momentum    x, y: invariant masses of  
the two body systems

The full Amplitude is then given by :

$$A = \sum_i c_i \cdot A_i$$

complex coefficient (amplitude and phase)  
(This is what we want to determine!)  
from the fit

We fit the model to the data distributions

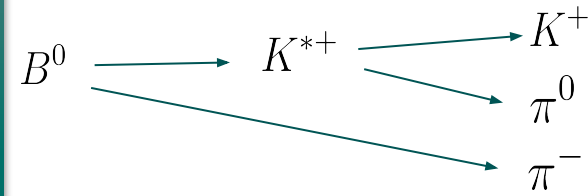


Example Dalitz plot with data from Belle II  
simulation

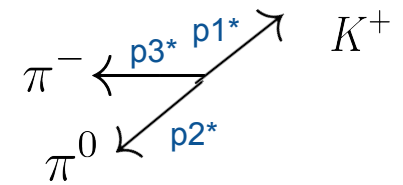
# Model Parameters



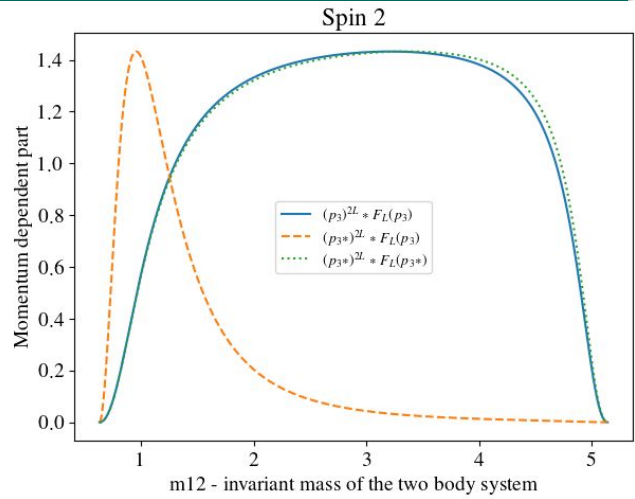
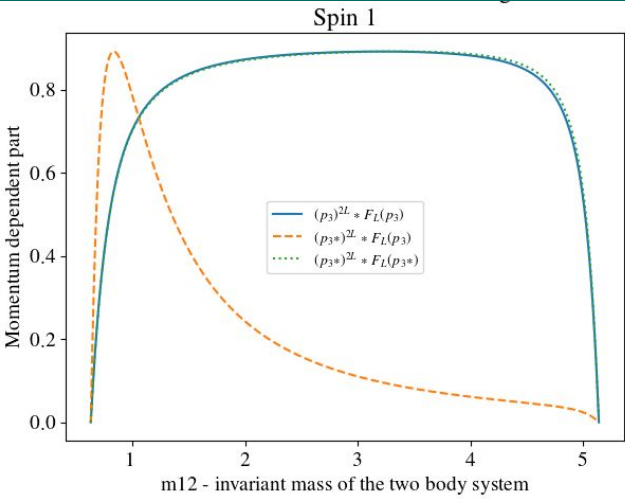
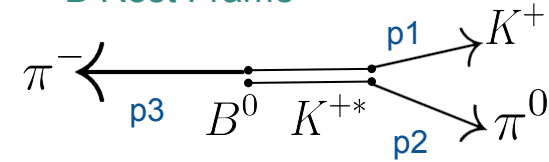
- Angular Momentum Barrier Factor:
  - $B_{iR} = |p_1^*|^L \sqrt{F_L(p_1^*)}$     $B_{iB} = |p_3|^L \sqrt{F_L(p_3)}$  or  $|p_3^*|^L \sqrt{F_L(p_3^*)}$
- $F_L(p)$ : Blatt-Weisskopf compensation factors
  - compensate the high-energy behavior of the  $|p^L|$  term
- Different formalisms suggest different momenta
- How to continue with the compensation factors?
  - $B_R^2 = |p_1^*|^{2L} F_L(p_1^*)$
  - $B_B^2 = |p_3|^{2L} F_L(p_3)$     $|p_3^*|^{2L} F_L(p_3)$    or    $|p_3^*|^{2L} F_L(p_3^*)$
  - $B = B_R B_B$



Isobar(e.g.  $K^{*+}$ ) Rest Frame



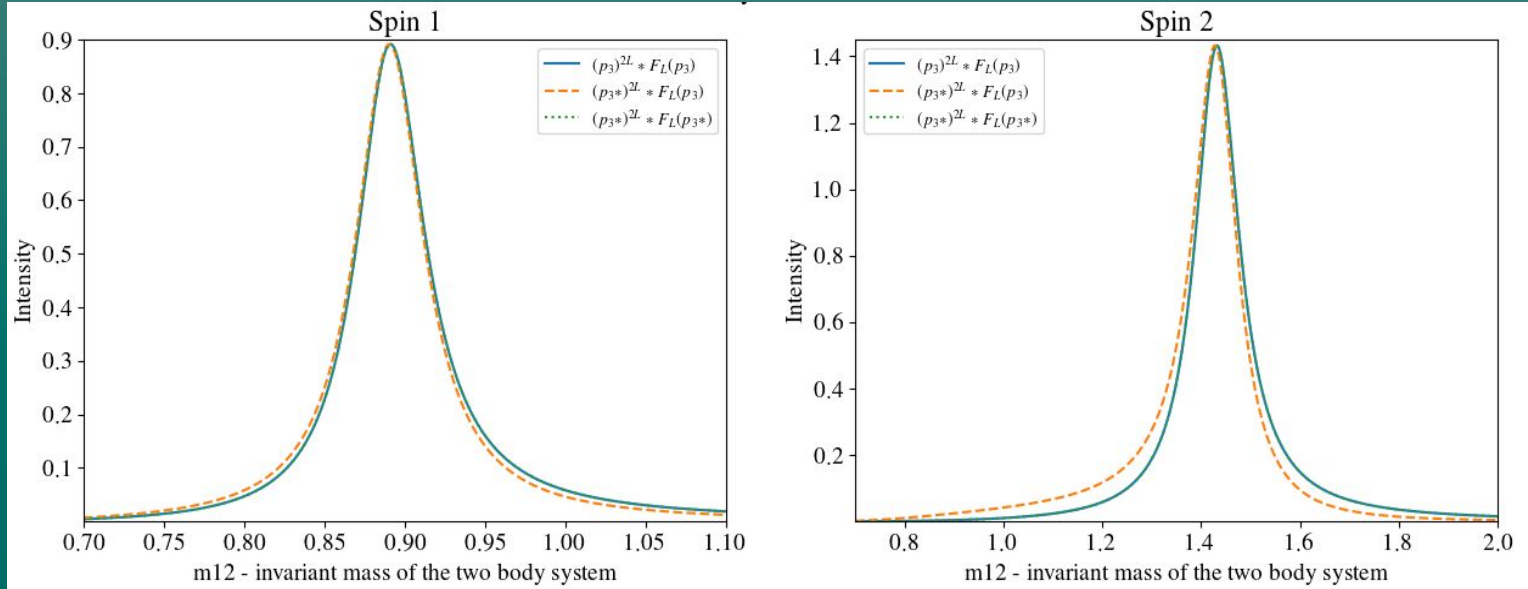
B Rest Frame



# Intensity



- Does this difference in modelling affect the full amplitude?
- What we can measure are the intensities  $\rightarrow I = |A|^2 = B^2 |L_i|^2 (p_1 p_3)$  Line Shape: here Breit Wigner as an example



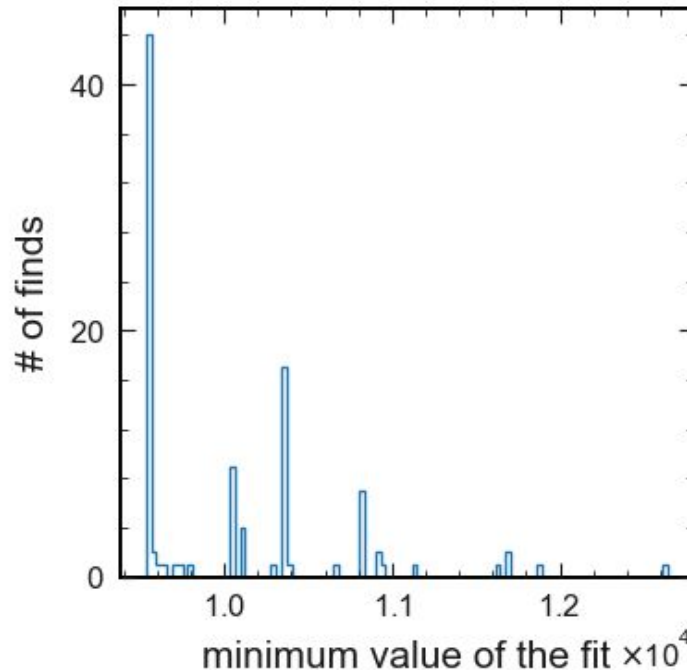
- ▶ Using the same momentum for both factors gives similar shape
- ▶ Slight shift when using different momentums
- ▶ We need to be careful when writing the compensation factors
- ▶ If the resonance was broader, we could observe a larger effect.

# The Fit

- We fit the  $C_i$  to the data using an unbinned maximum-likelihood fit.
- We fit to signal-MC only (no background)
- Given how fitting works, we need to define the set of start parameters
- To study the dependence on the choice of start parameters, we perform multiple fits with random start parameters.

- The fitter seems to find the same minimum ~45% of the time

Histogram of the minimum value of the fit

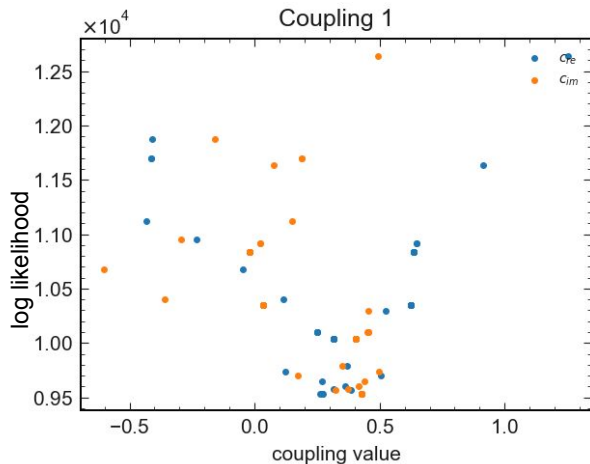
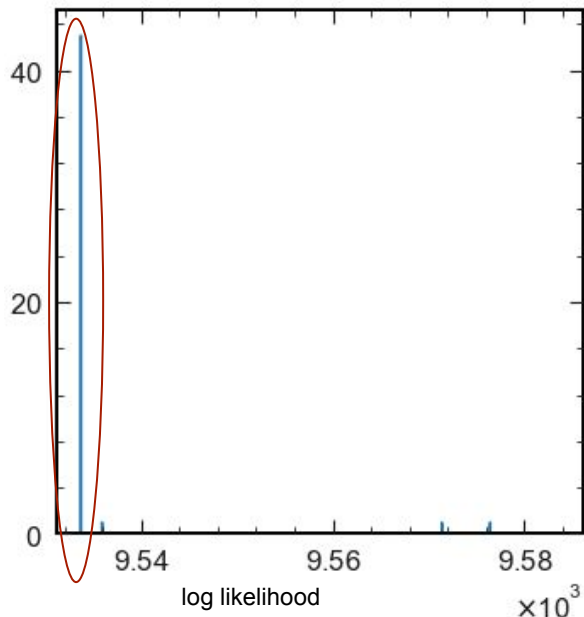


showing 100 fit attempts

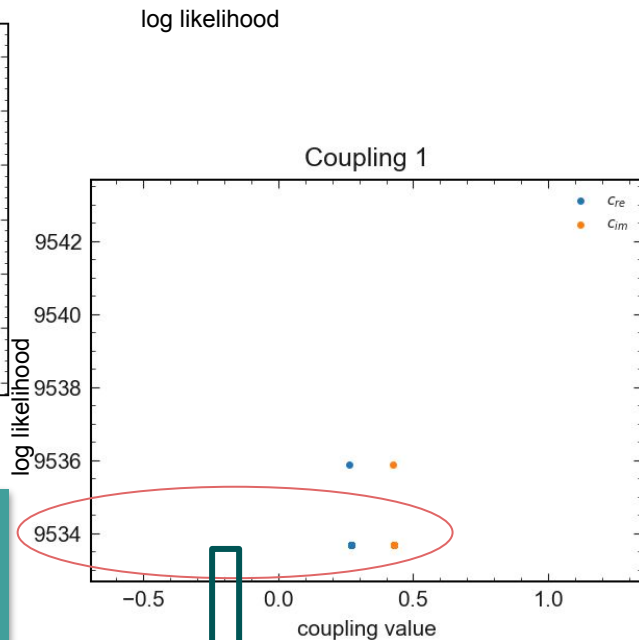
# Dependence on start values



- We also investigate if the value of the couplings fitted are consistent



While the values seem to be scattered for the general fit, we see that they are indeed consistent for the lowest minima!



There are around 40 couplings at this value



# Summary



- ❖ Studied barrier factors in different reference frames
- ❖ Investigated which reference frames to choose for the parameters of the Blatt-Weisskopf factors
- ❖ Studied dependence on start values:
  - the fit yields the same minimum in a reasonable amount of fit attempts
  - the couplings the fit gives are the same for the lowest minima

# Outlook

- Testing parametrization for different partial wave models
- Inclusion of background
- Fitting model to real data
- Calculating branching ratios and CP asymmetry

*Thanks for listening!*