

# **Hadron Spectroscopy at Belle & Belle II**

**MENU 2023**

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**Seongbae Yang (Korea University)**

**on behalf of Belle & Belle II Collaborations**

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## 3. Hyperon: New peak structures near the mass thresholds

- $\Lambda\eta$  threshold cusp in  $pK^-$  system

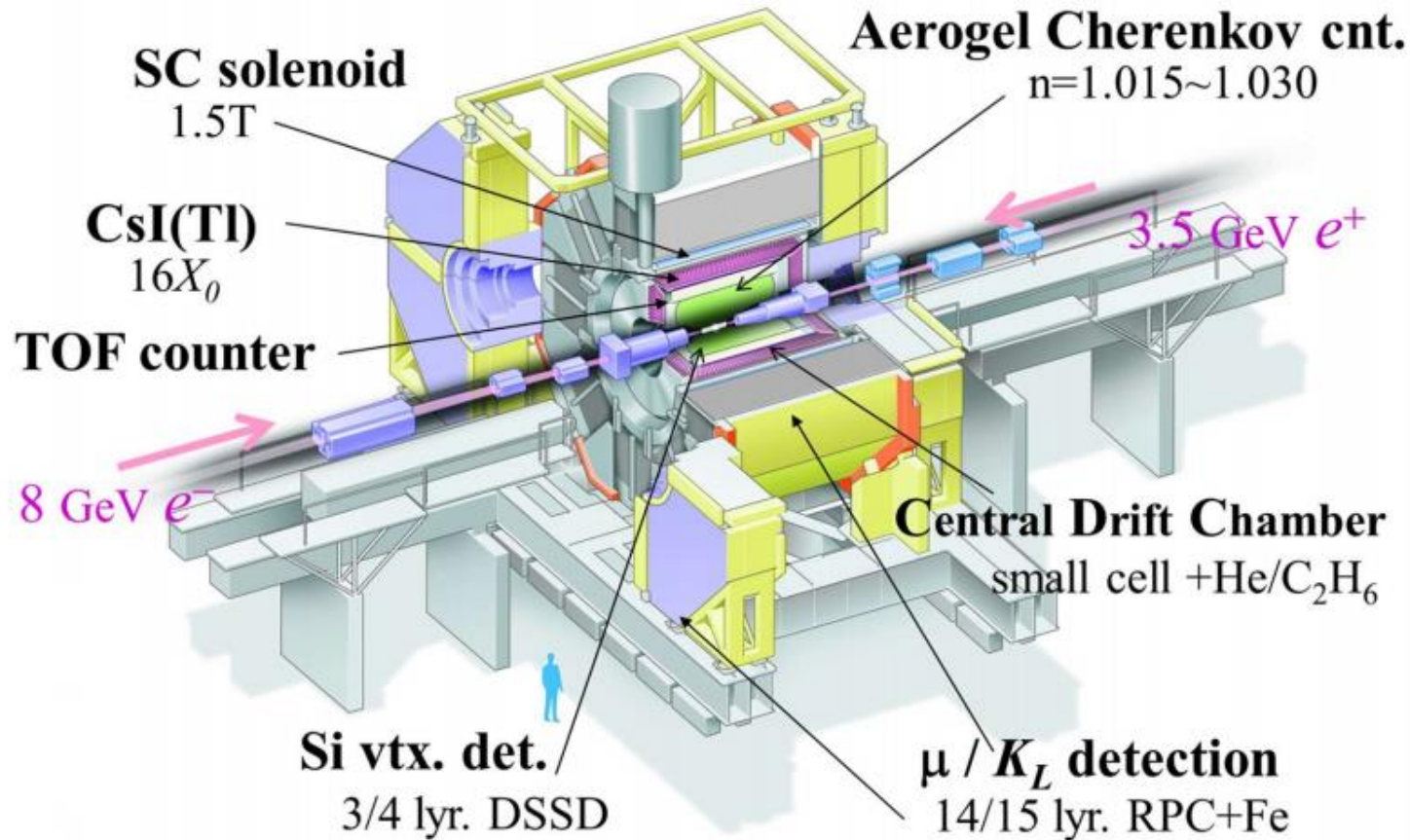
- New peaking structures near the  $\bar{K}N$  threshold in  $\Lambda\pi$  system

## 4. Summary

\* In Hadron Spectroscopy section (Oct. 17, 12:10PM),

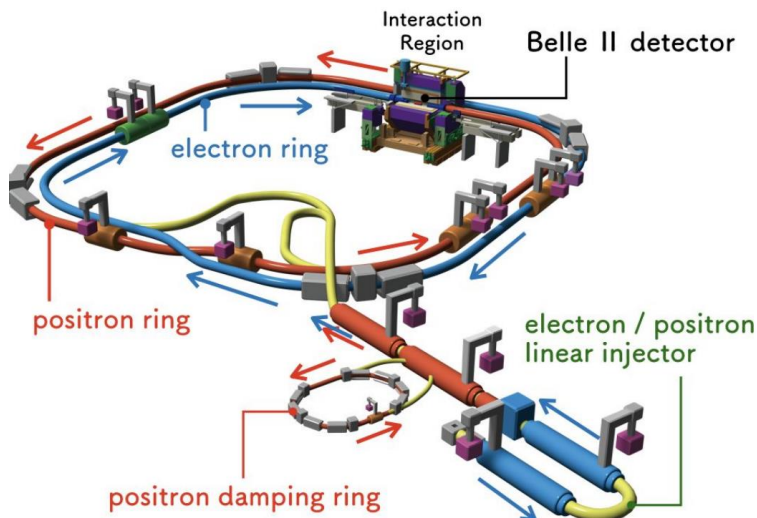
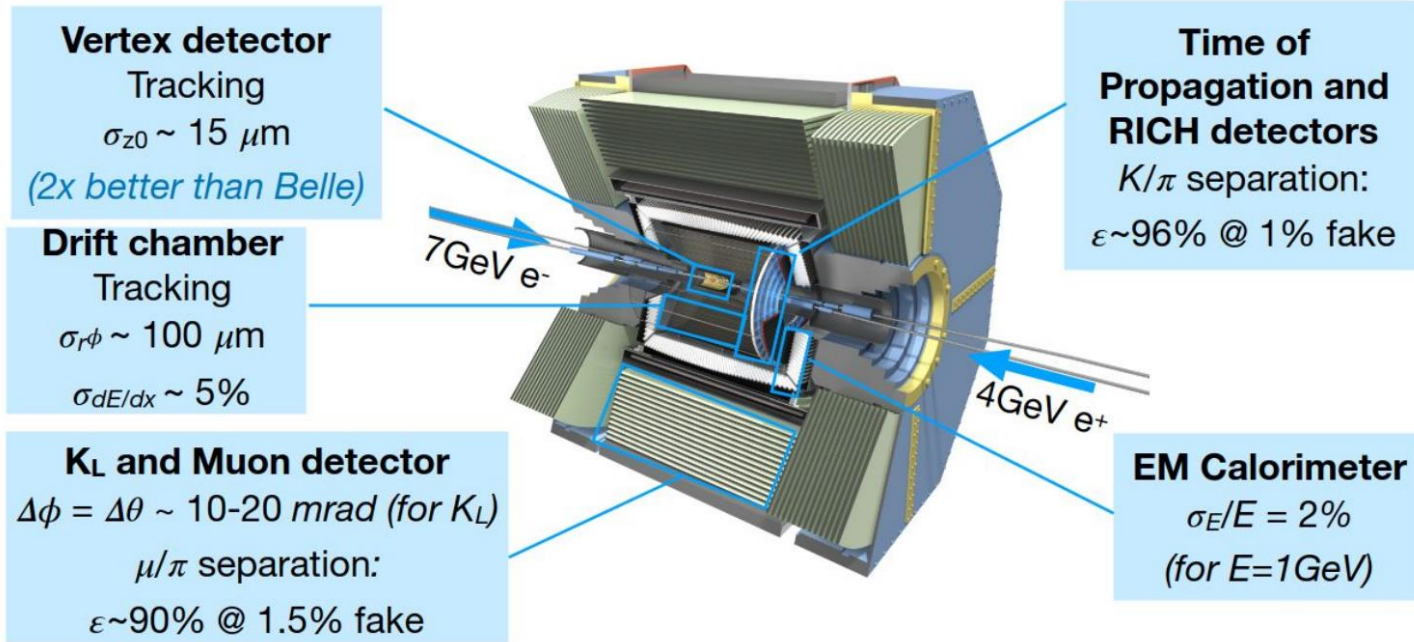
‘Recent results on charmed baryon’ by Suxian Li

# Belle Experiment



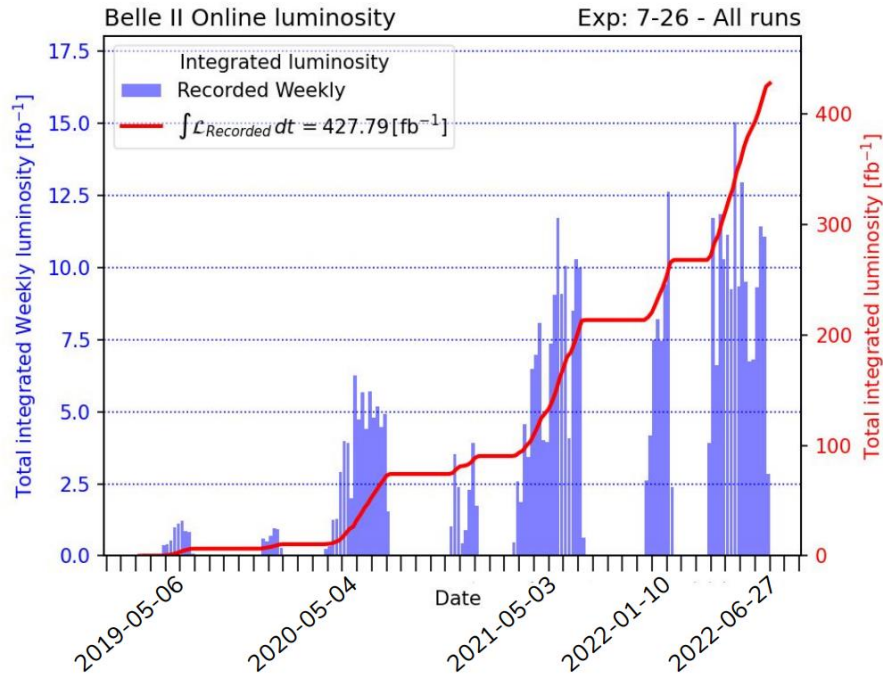
- Physics beamtime: 1999~2010
- $\sqrt{s} = \sim 10.6$  GeV
- **Huge statistics**,  $\sim 10^9 B\bar{B}$  pairs,  $\sim 1 \text{ ab}^{-1}$  integrated luminosity

# Belle → Belle II Experiment

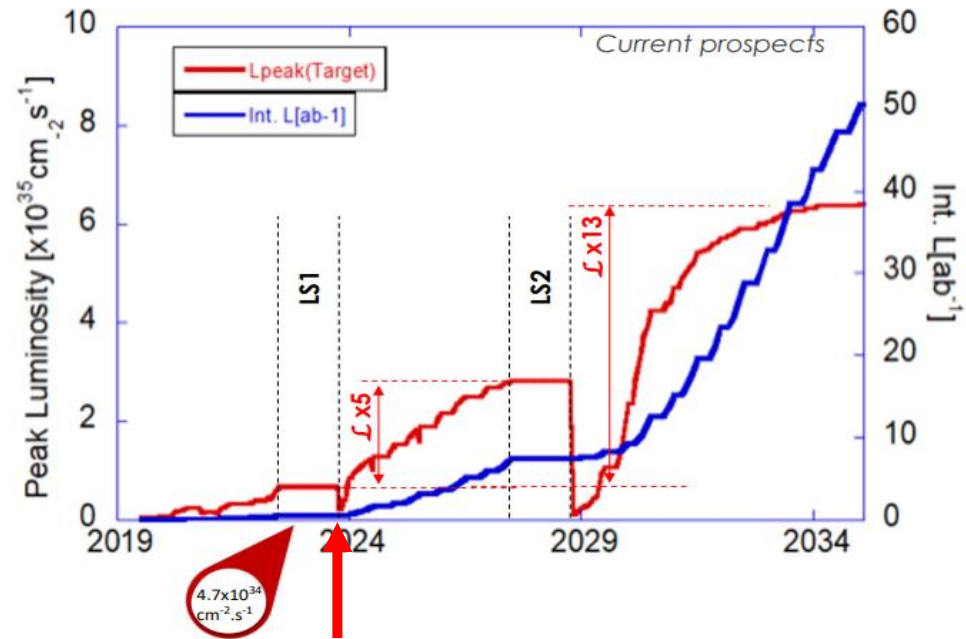


- SuperKEKB and Belle II upgrades
  - Higher beam current ( $\times 2$ )
  - and smaller beam focus ( $\times \frac{1}{20}$ ) at IR
  - Upgrades in all parts of the detector (vertex, resolution, trigger, and DAQ, ...)

## Belle II Luminosity



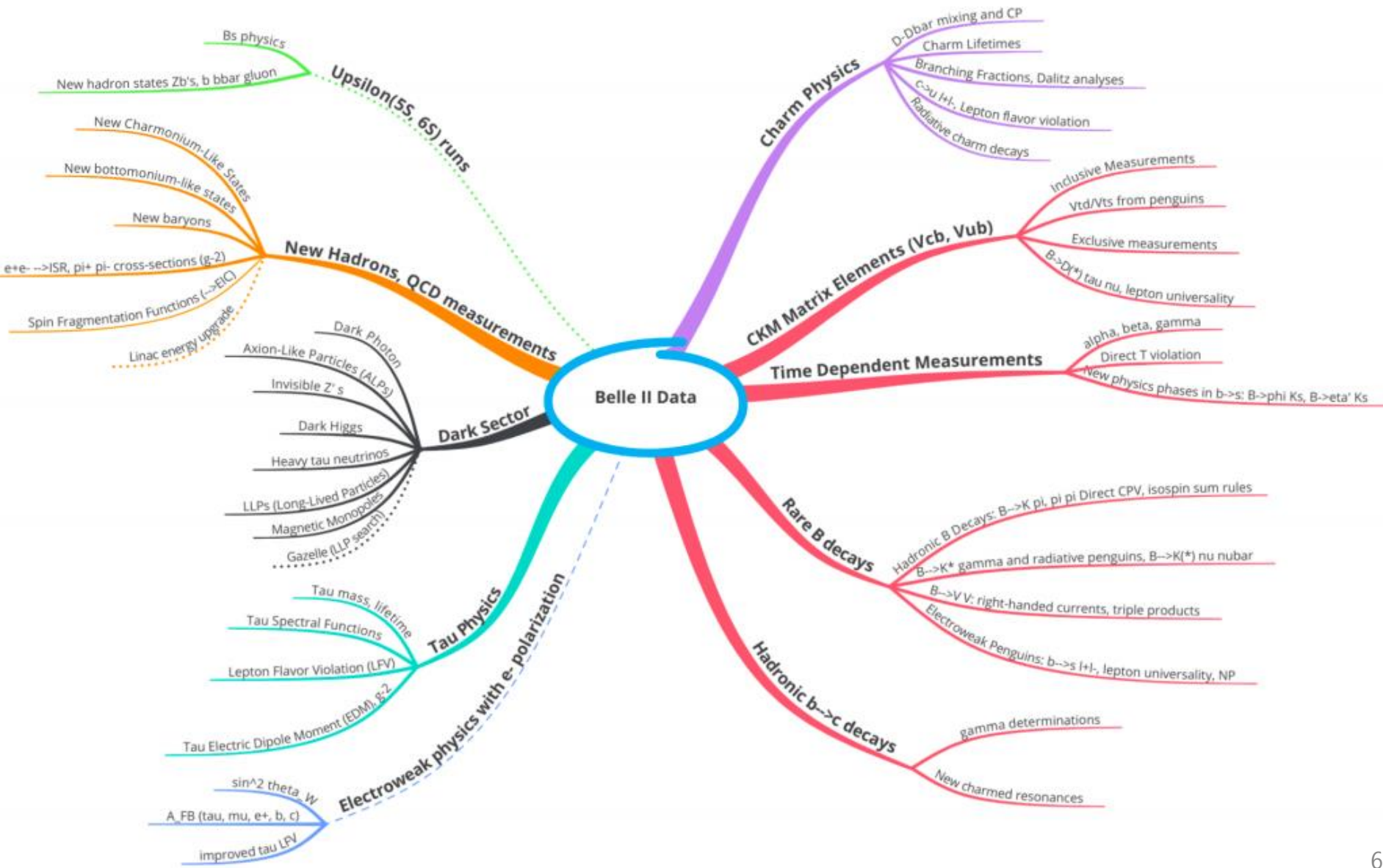
## Long term plan



**We are here!!**

- Instantaneous luminosity record of  $4.7 \times 10^{34} \text{cm}^{-2} \text{s}^{-1}$  (world record)
- Total integrated luminosity of  $424 \text{fb}^{-1}$  until now.
- We plan to take 50 times more data than Belle in the future

# Physics Program of Belle & Belle II



# Hadron Spectroscopy at Belle & Belle II

- Huge statistics, Belle + Belle II:  $\sim 1.5 \text{ ab}^{-1}$  until now
  - Excellent detector performance with  $4\pi$  solid angle
  - EM calorimeter for gamma detection ( $\sigma_E/E = 2\%$  at 1 GeV)
  - Various channels for hadron spectroscopy
- $e^+e^- \rightarrow q\bar{q}$ ,  $B$  decays,  $\Upsilon(1S)$  decays, and charmed baryon decays (for hyperons)

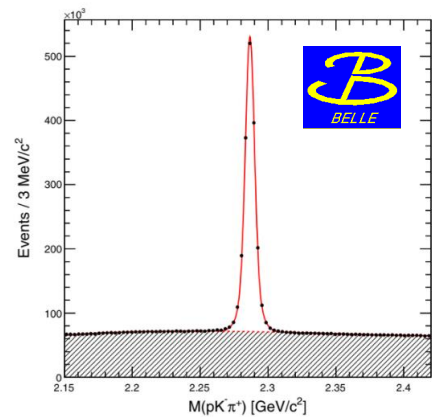
$$\Lambda_c^+ \rightarrow pK^-\pi^+$$

$$\Lambda_c^+ \rightarrow \eta\Lambda\pi^+;$$

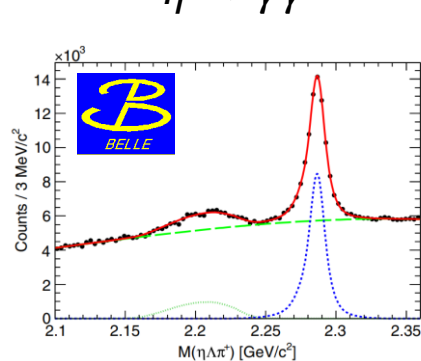
$$\eta \rightarrow \gamma\gamma$$

$X(3872)$  in  $B$  decays

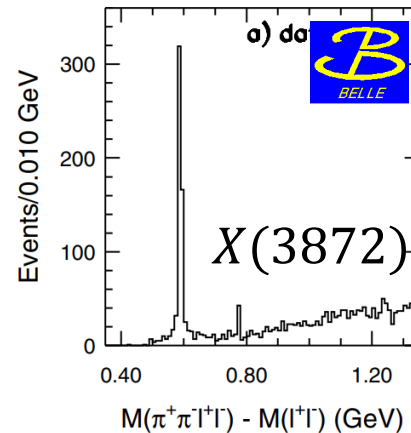
$\Omega(2012)^-$  in  $\Upsilon(1S)$  decays



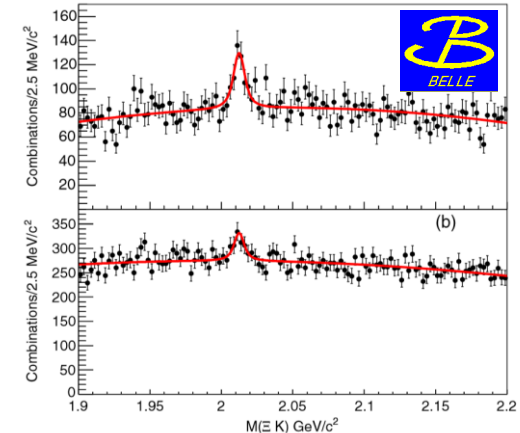
\*PRL 117, 011801 (2016)



\*PRD 103, 052005 (2021)

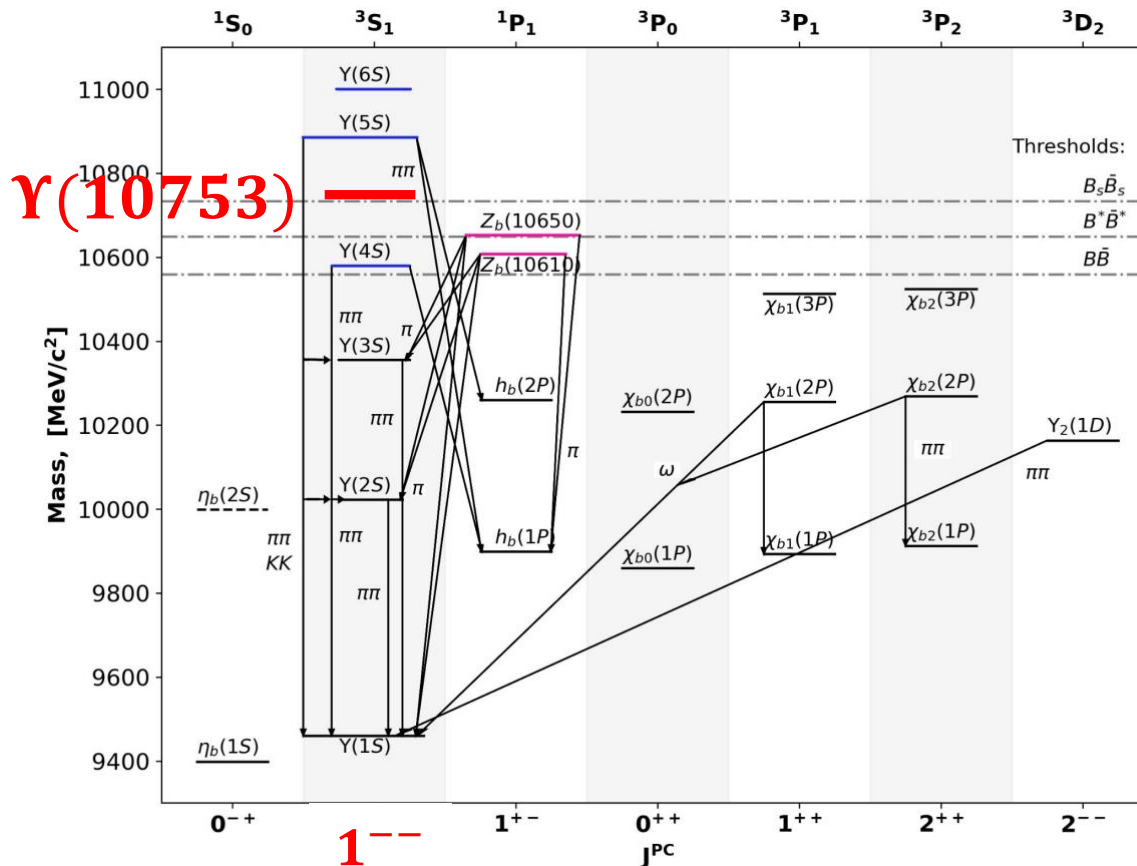


\*PRL 91, 262001 (2003)



\*PRL 121, 052003 (2018)

## Bottomonium Scheme



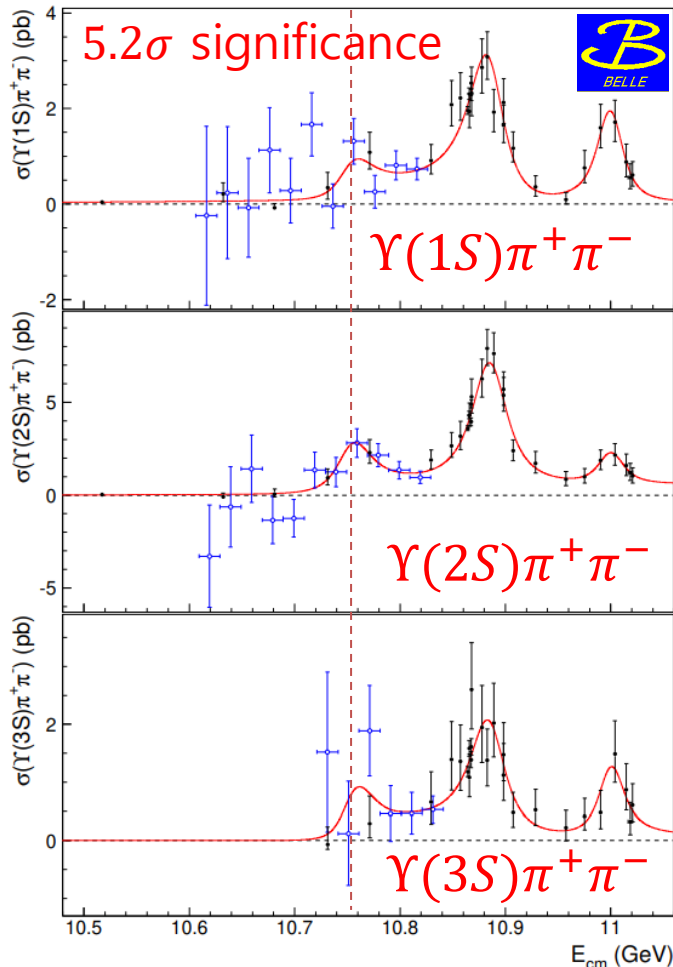
- Below  $B\bar{B}$  threshold: States are well described by potential models
- Above  $B\bar{B}$  threshold: Unexpected properties are seen.
  - Two charged  $Z_b^+$  states ( $B^{(*)}\bar{B}^*$  molecular states?)
  - Hadronic transitions are strongly enhanced
  - $\eta$  transitions are not suppressed compared to  $\pi^+\pi^-$  transitions



# Observation of $\Upsilon(10753)$

- Measurement of  $e^+e^- \rightarrow \Upsilon(nS)\pi^+\pi^-$  cross sections
- Belle energy scan data in the energy range from 10.63 GeV to 11.02 GeV

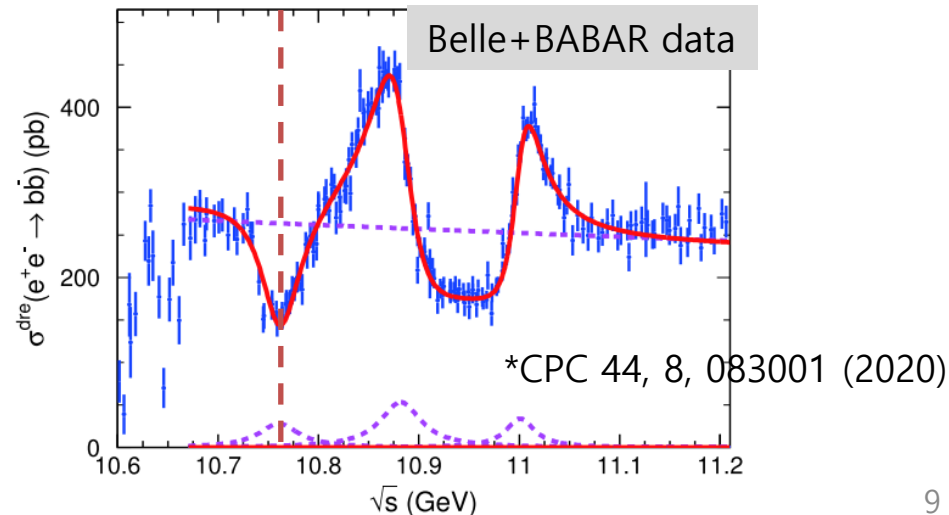
$\Upsilon(10753)$



\*Belle, JHEP 10 (2019) 220

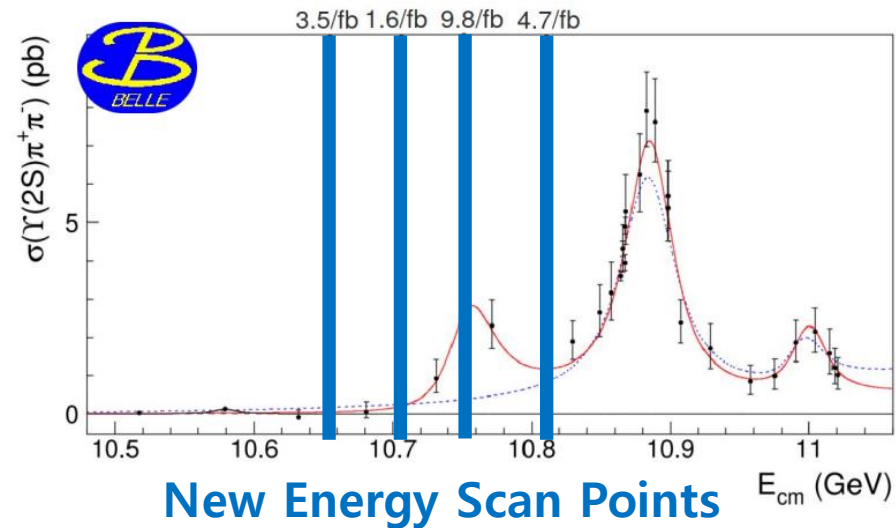
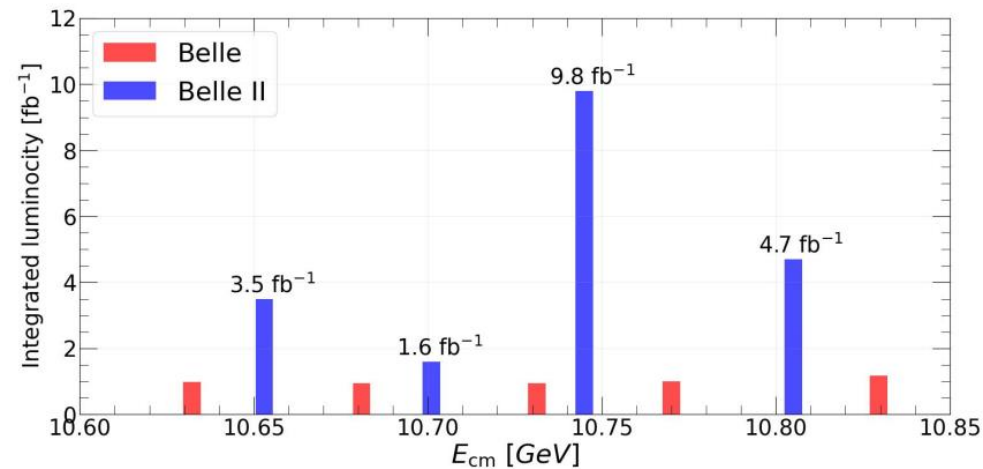
	$\Upsilon(10860)$	$\Upsilon(11020)$	New structure
M (MeV/c <sup>2</sup> )	$10885.3 \pm 1.5^{+2.2}_{-0.9}$	$11000.0^{+4.0}_{-4.5} {}^{+1.0}_{-1.3}$	$10752.7 \pm 5.9^{+0.7}_{-1.1}$
$\Gamma$ (MeV)	$36.6^{+4.5}_{-3.9} {}^{+0.5}_{-1.1}$	$23.8^{+8.0}_{-6.8} {}^{+0.7}_{-1.8}$	$35.5^{+17.6}_{-11.3} {}^{+3.9}_{-3.3}$

- $e^+e^- \rightarrow B\bar{B}$  cross sections
- A dip near 10.75 GeV



## New Energy Scan for $\Upsilon(10753)$

- In November 2021, Belle II collected unique energy scan data around 10.75 GeV
- The main goal was to confirm and study  $\Upsilon(10753)$
- Total integrated luminosity:  $19 \text{ fb}^{-1}$
- Fill in the gaps between the Belle points



# Observation of $\Upsilon(10753) \rightarrow \omega \chi_{bJ}$

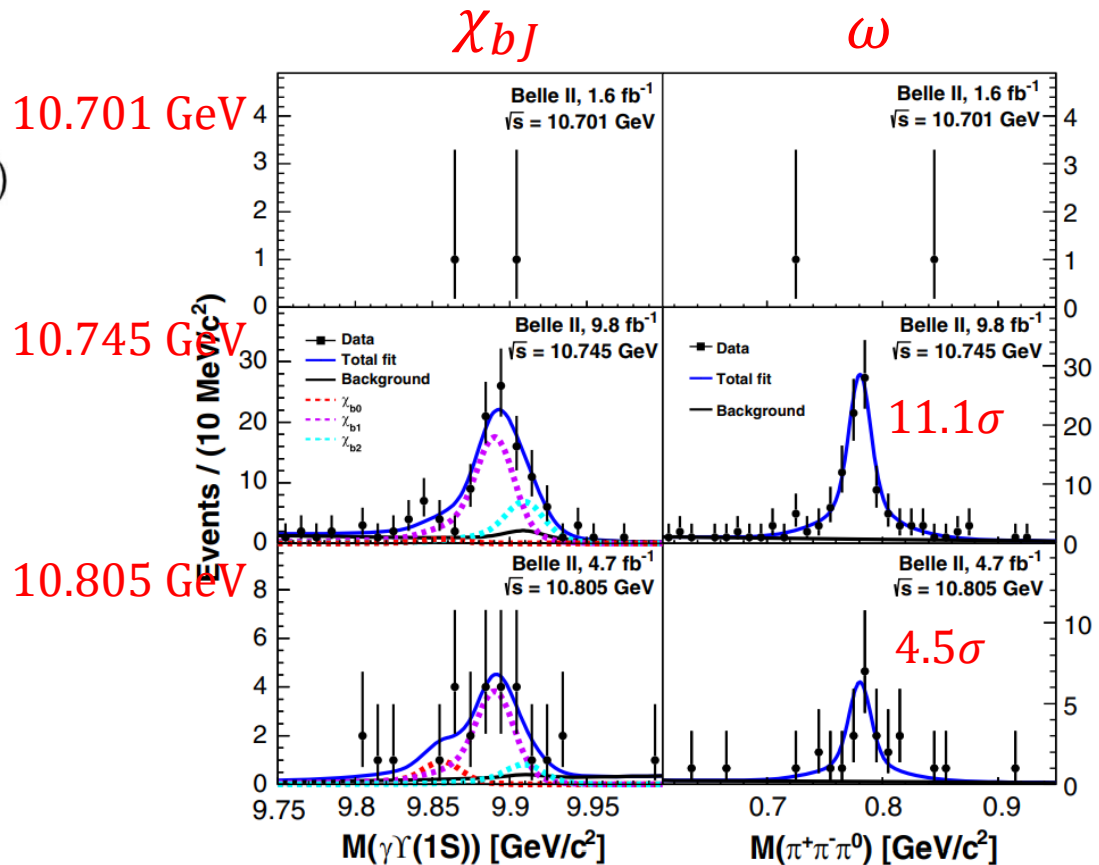
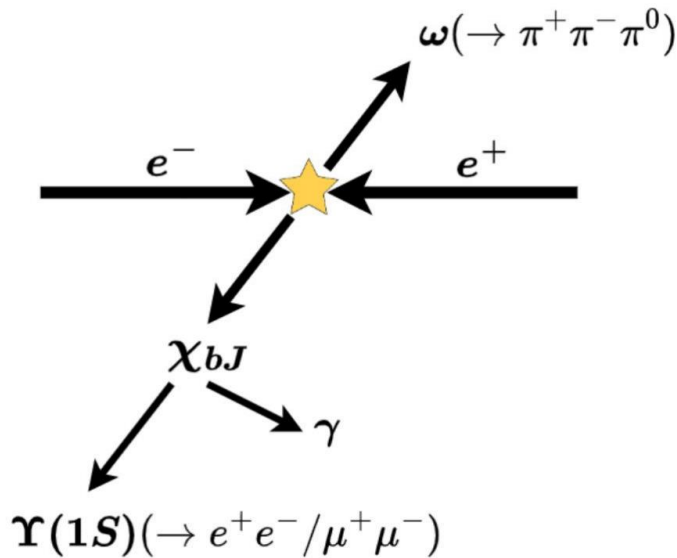
- $\Upsilon(10753) \rightarrow \omega \chi_{bJ}$  and  $\gamma X_b$

-  $Y(4220) \rightarrow \omega \chi_{c0}$  and  $\gamma X(3872)$  are observed  $\rightarrow$

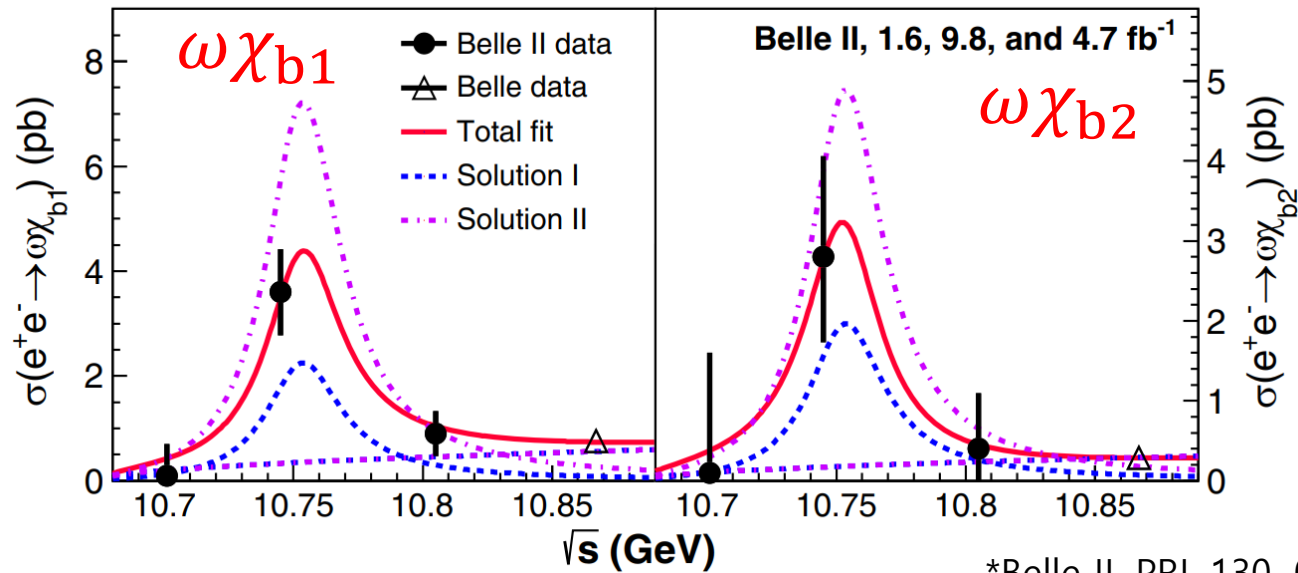
\*BESIII, PRL 122, 232002 (2019) and PRD 99, 091103 (2019)

Similar nature with  $Y(4220)$  in charmonium section

- 2D unbinned maximum likelihood fits to  $M(\gamma\Upsilon(1S))$  and  $M(\pi^+\pi^-\pi^0)$  distributions



- Cross sections of  $e^+e^- \rightarrow \omega\chi_{b1}$  and  $\omega\chi_{b2}$



\*Belle II, PRL 130, 091902 (2023)

- $\frac{\sigma(e^+e^- \rightarrow \omega\chi_{b1})}{\sigma(e^+e^- \rightarrow \Upsilon(nS)\pi^+\pi^-)} = \sim 1.5$  at  $\sqrt{s} = 10.745$  GeV

- The ratio is significantly different with the ratio of  $\Upsilon(5S)$  ( $\sim 0.15$ )

- Different internal structure with  $\Upsilon(5S)$ ?

\*Belle, PRL 113, 142001 (2014)

- $\frac{\sigma(e^+e^- \rightarrow \omega\chi_{b1}(1P))}{\sigma(e^+e^- \rightarrow \omega\chi_{b2}(1P))} = 1.3 \pm 0.6$  at  $\sqrt{s} = 10.745$  GeV

- Prediction for  $D$ -wave bottomonium state: 15 \*Phys. Lett. B 738, 172 (2014)

- Prediction for  $S$ - $D$  mixed state: 0.2 \*Phys. Rev. D 104, 034036 (2021)

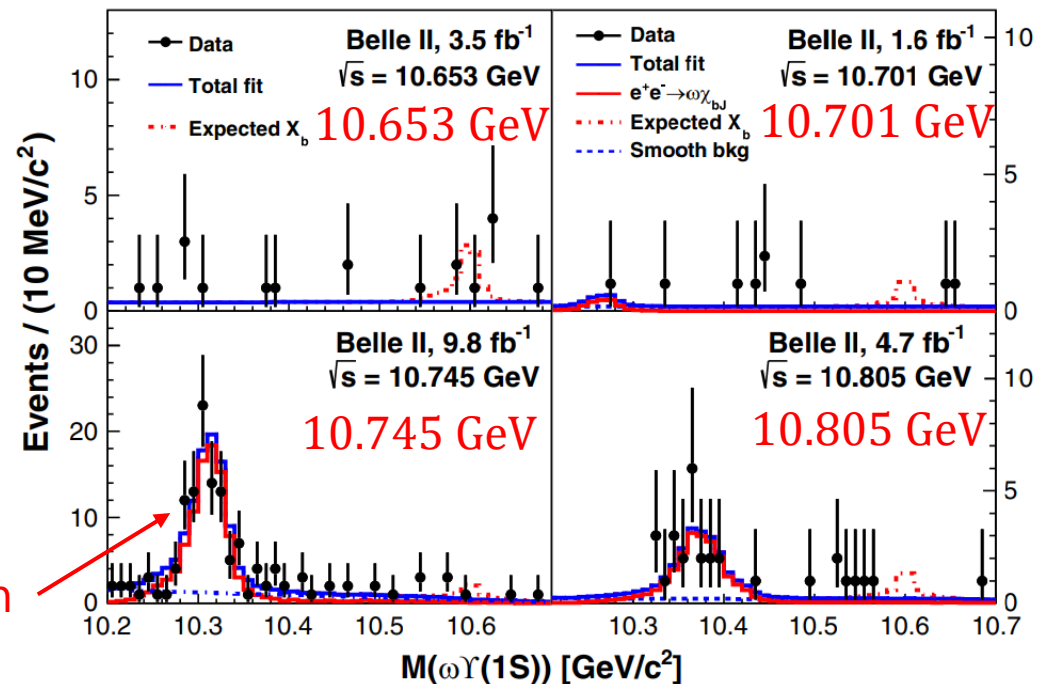
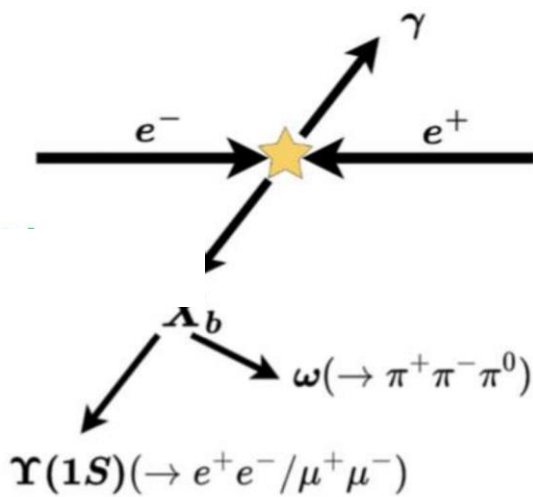
- Close to  $S$ - $D$  mixed state?

- Search for  $\Upsilon(10753) \rightarrow \gamma X_b$ 
  - Search for  $X_b$  in  $M(\omega\Upsilon(1S))$  distributions
    - Reflections from  $\Upsilon(10753) \rightarrow \omega\chi_{b1}$  and  $\omega\chi_{b2}$  are seen.
    - No significant signal of  $X_b$  is observed.

$\sqrt{s}$ (GeV)	10.653	10.701	10.745	10.805
Upper limits on $\sigma_B(e^+e^- \rightarrow \gamma X_b) \cdot B(X_b\omega\Upsilon(1S))$ (pb)	(10.14, 0.55)	(0.25, 0.84)	(0.06, 0.14)	(0.08, 0.37)

\*with varying  $M(X_b)$  from 10.45 to 10.65  $\text{GeV}/c^2$

### $X_b \rightarrow \omega\Upsilon(1S)$



Reflection

## Search for $\Upsilon(10753) \rightarrow \omega\eta_b(1S)$ and $\omega\chi_{b0}$

- Tetraquark interpretation predicts a strong transition of  $\omega\eta_b(1S)$  compared to  $\Upsilon\pi^+\pi^-$  transition.

$$\frac{\Gamma(\omega\eta_b)}{\Gamma(\Upsilon\pi^+\pi^-)} \sim 30 \quad \text{*Chin. Phys. C 43, 123102 (2019)}$$

There is no convenient way to reconstruct  $\eta_b$ .

- In charmonium section,  $Y(4220) \rightarrow \omega\chi_{c0}$  transition is enhanced compared to  $\omega\chi_{c1}$  and  $\omega\chi_{c2}$ . \*PRL 130, 091902 (2023) But  $e^+e^- \rightarrow \omega\chi_{b0}$  was not observed in the full reconstruction due to  $B(\chi_{b0} \rightarrow \gamma\Upsilon(1S)) = (1.94 \pm 0.27)\%$ .

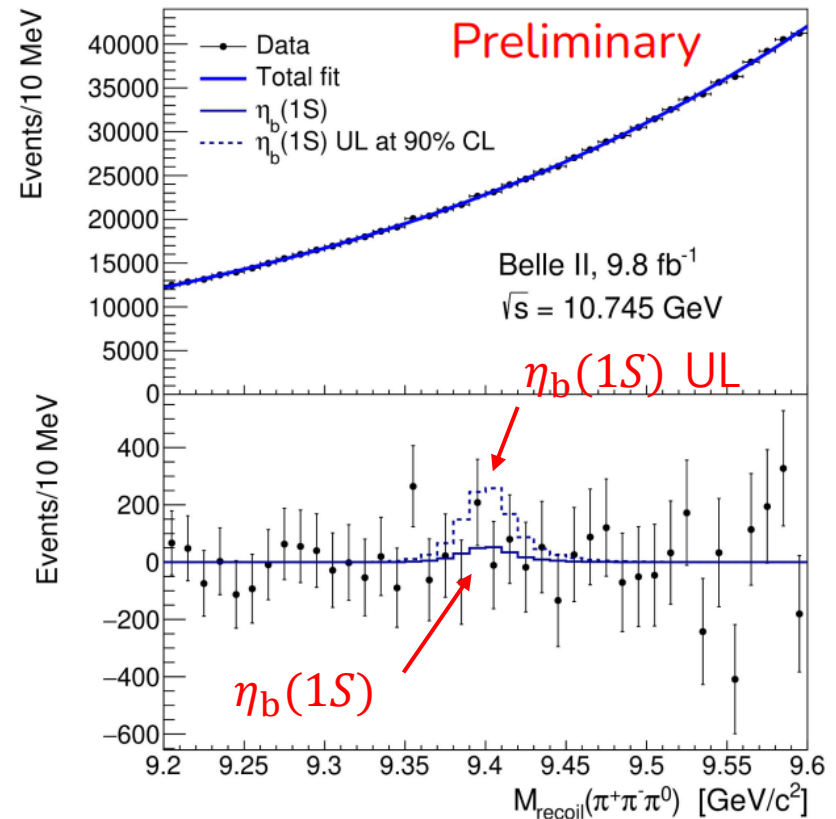
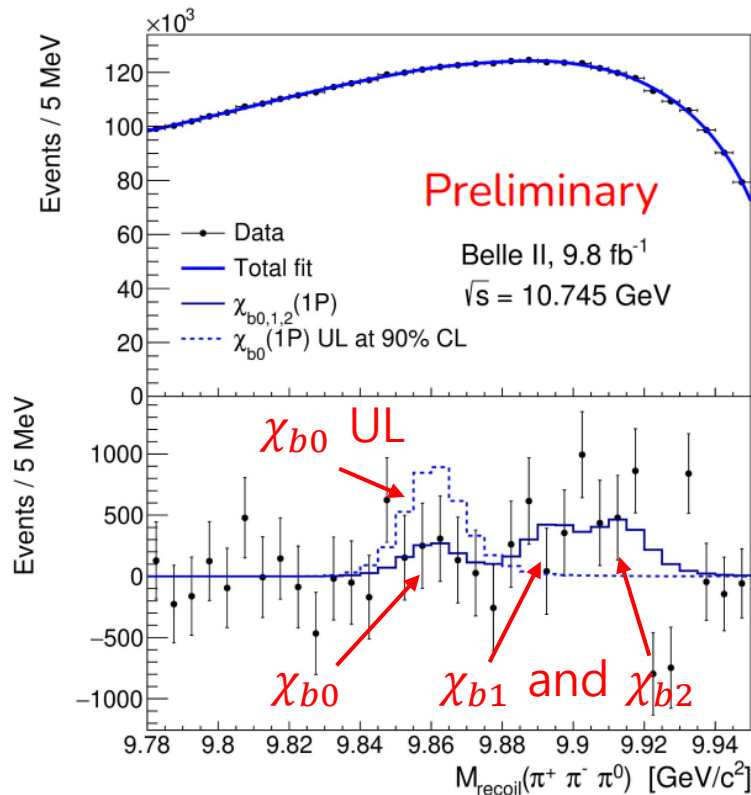
- Search for these above transitions by the recoil mass of  $\omega \rightarrow \pi^+\pi^-\pi^0$

$$M_{\text{recoil}}(\pi^+\pi^-\pi^0) = \sqrt{\left(\frac{E_{c.m.} - E^*}{c^2}\right)^2 - \left(\frac{p^*}{c}\right)^2},$$

where  $E_{c.m.}$ : total  $e^+e^-$  energy

$E^*$  and  $p^*$ : energy and momentum of  $\omega \rightarrow \pi^+\pi^-\pi^0$   
in the center of mass frame.

- $\omega \rightarrow \pi^+ \pi^- \pi^0$  recoil mass distributions



→ No significant  $\chi_{b0}$  and  $\eta_b(1s)$  signals are observed.

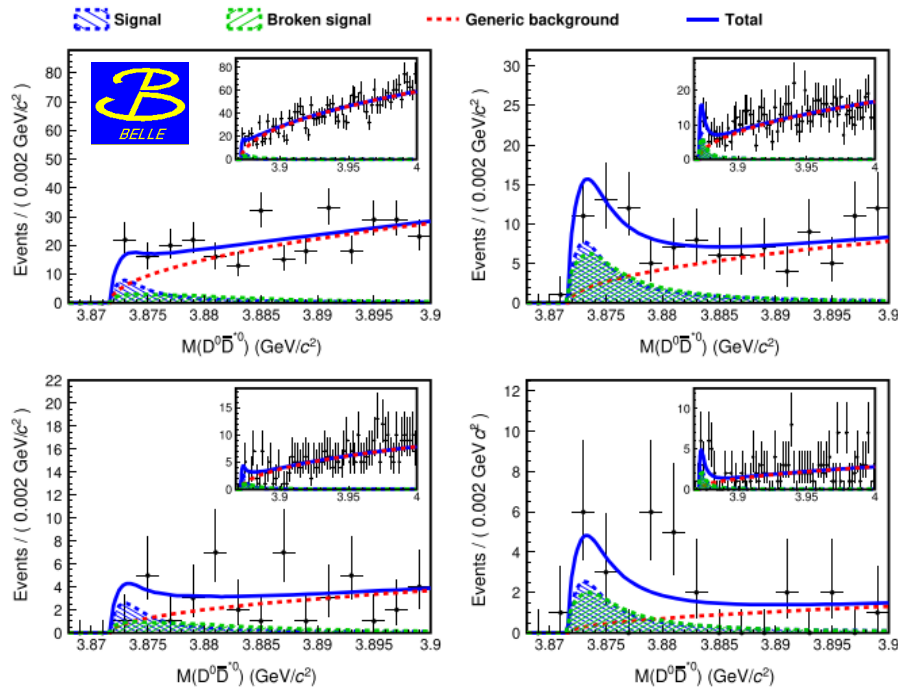
- $\sigma(e^+e^- \rightarrow \omega\eta_b(1s)) < 2.5 \text{ pb}$  \*  $\sigma(e^+e^- \rightarrow \Upsilon(2S)\pi^+\pi^-) = \sim 3 \text{ pb}$

→ These results do not support the tetraquark prediction of  $\Upsilon(10753)$ .

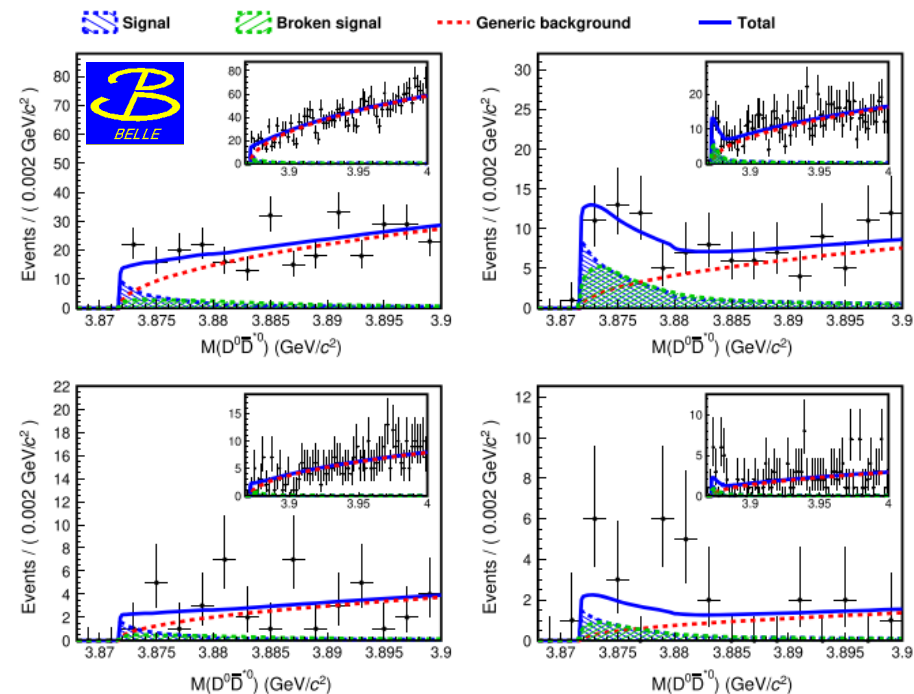
# New Peak Structures near the Mass Thresholds

- New peak structures have been observed near the mass threshold.
  - They do not always indicate new hadron resonances.
    - New hadron resonance or threshold cusp
    - Lineshape analysis is required to identify the structure.
- $X(3872)$  structure near  $D^0\bar{D}^{*0}$  threshold

## Breit-Wigner model



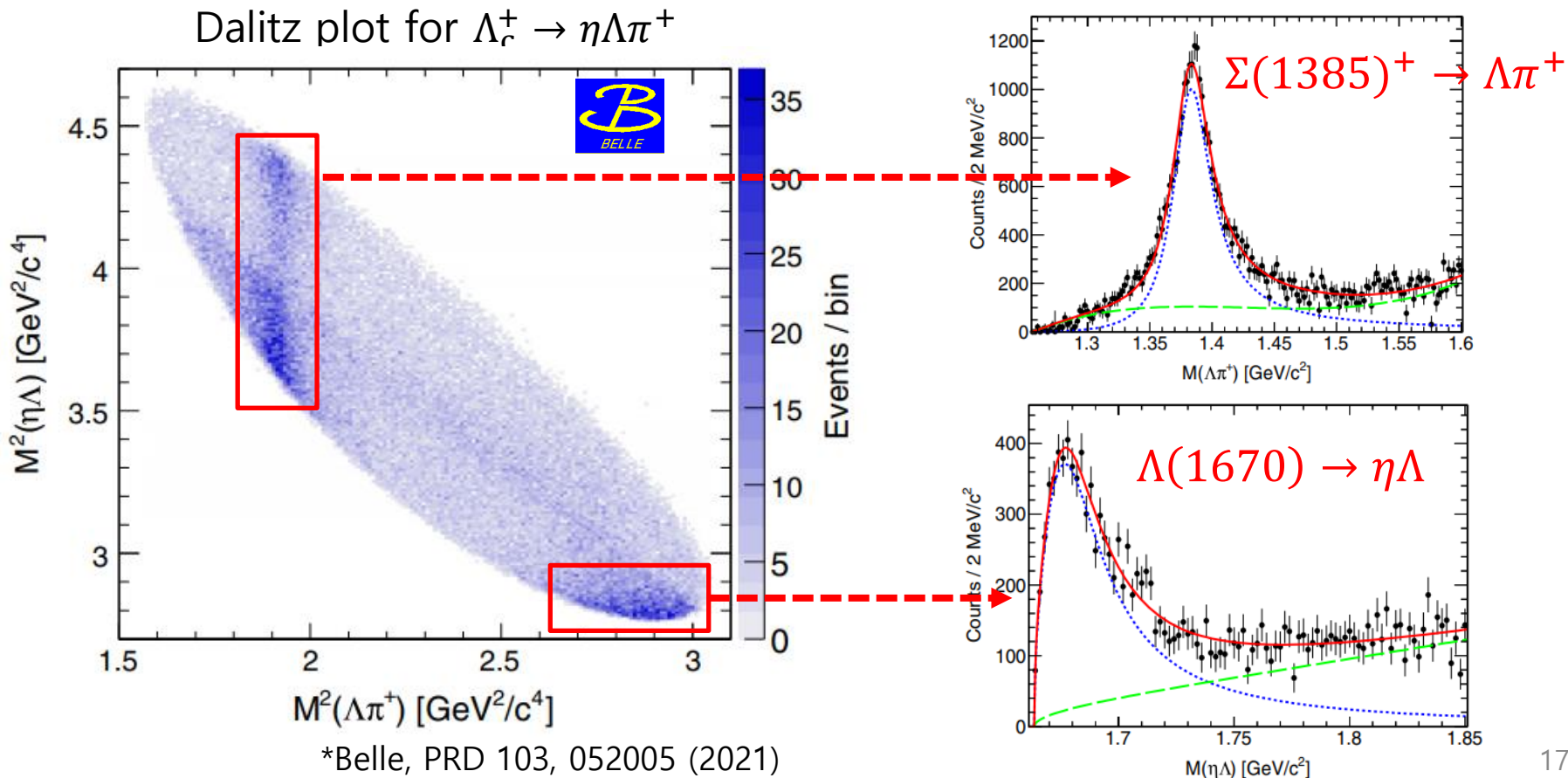
## Flatté model





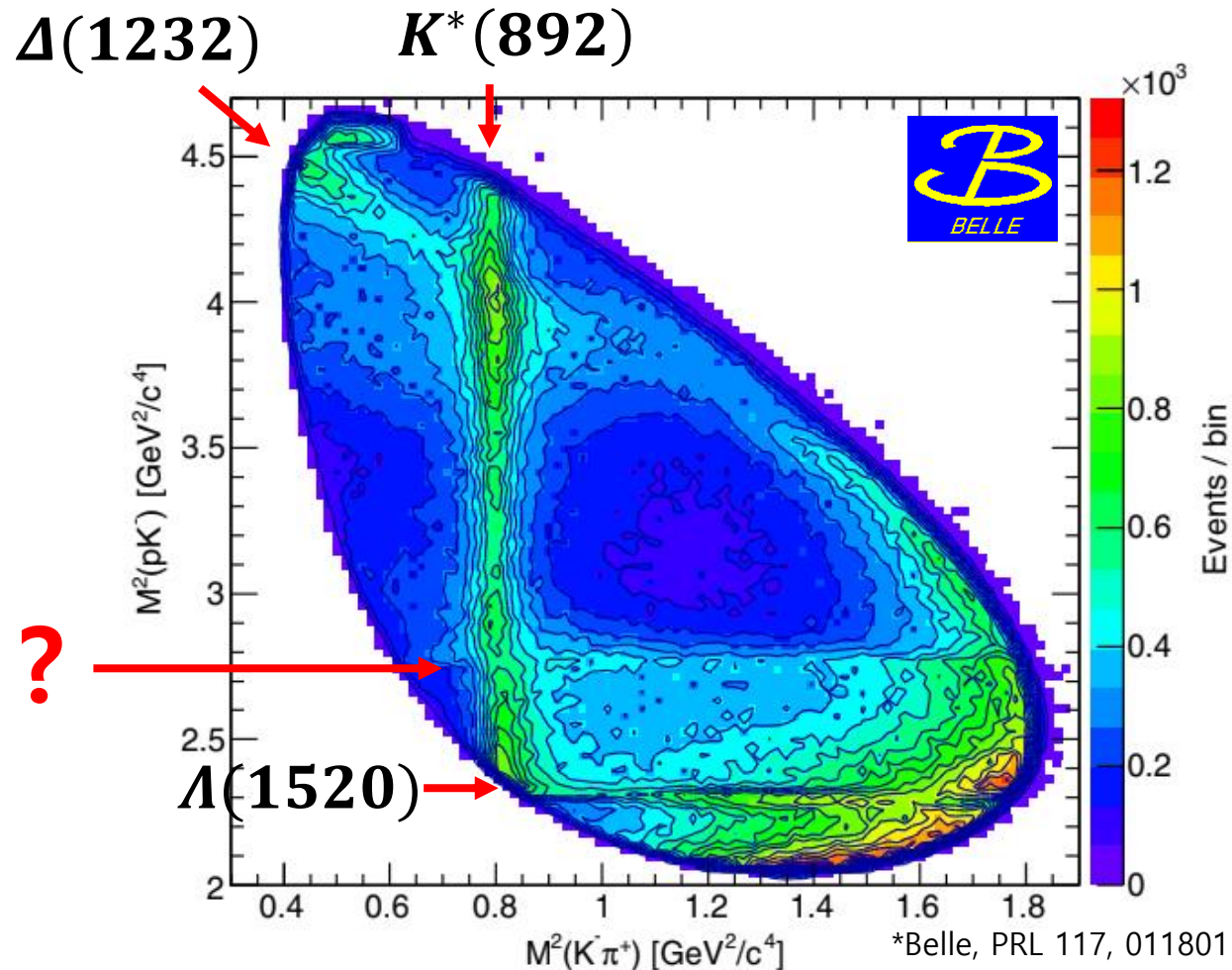
# Hyperons in Charmed Baryon Decays

- Better S/N ratio compared to  $e^+e^- \rightarrow q\bar{q}$  production.
- Possible to choose a suitable decay channel.
- $\Lambda(1670)$  in  $\Lambda_c^+ \rightarrow \eta\Lambda\pi^+$  decays
  - First observation of a peak structure of  $\Lambda(1670)$

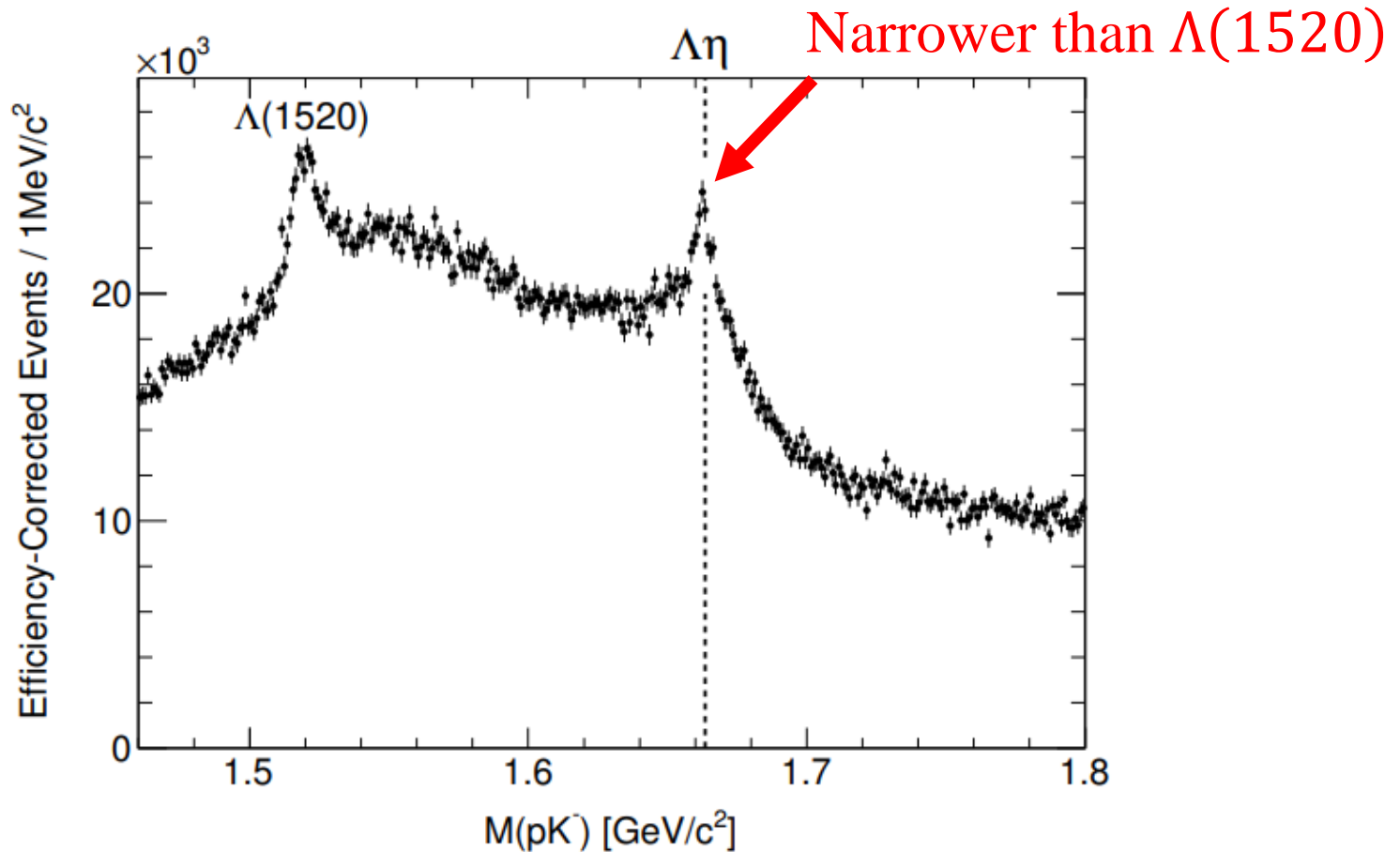


## $\Lambda\eta$ Threshold Cusp in $pK^-$ System

- Full data sample of Belle,  $980 \text{ fb}^{-1}$
- Dalitz plot for  $\Lambda_c^+ \rightarrow pK^- \pi^+$ ,

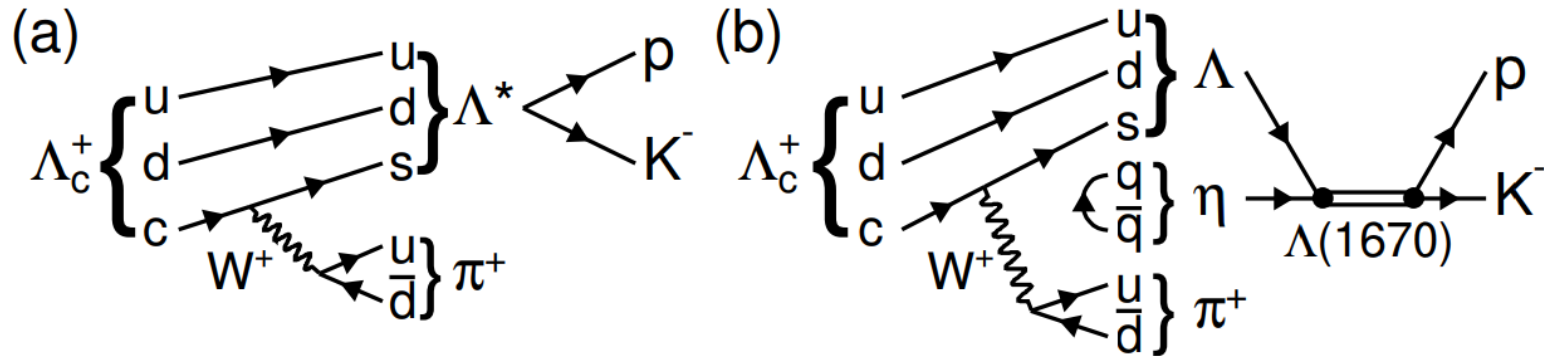


- $M(pK^-)$  Distribution of  $\Lambda_c^+ \rightarrow pK^- \pi^+$  decays



→ A new narrow peak structure near the  $\Lambda\eta$  threshold

- Two approaches to explain the narrow peaking structure.



(a) Breit-Wigner function: a new resonance

(b) Flatté function : a visible cusp enhanced by  $\Lambda(1670)$  pole

$$\frac{dN}{dm} \propto |f(m)|^2 = \left| \frac{1}{m - m_f + \frac{i}{2} (\Gamma' + \bar{g}_{\Lambda\eta} k)} \right|^2,$$

where  $m_f$ : Flatté mass

$\Gamma'$ : a sum of partial widths other than  $\Lambda\eta$  decay

$\bar{g}_{\Lambda\eta}$ : coupling constant of  $\Lambda\eta$  channel

$k$ :  $\sqrt{2\mu_{\Lambda\eta}(m - m_{\Lambda} - m_{\eta})}$ , \* $k$  is imaginary when  $m < m_{\Lambda} + m_{\eta}$

- Interference effects with other resonances:

Breit-Wigner and Flatté functions with a constant coherently added.

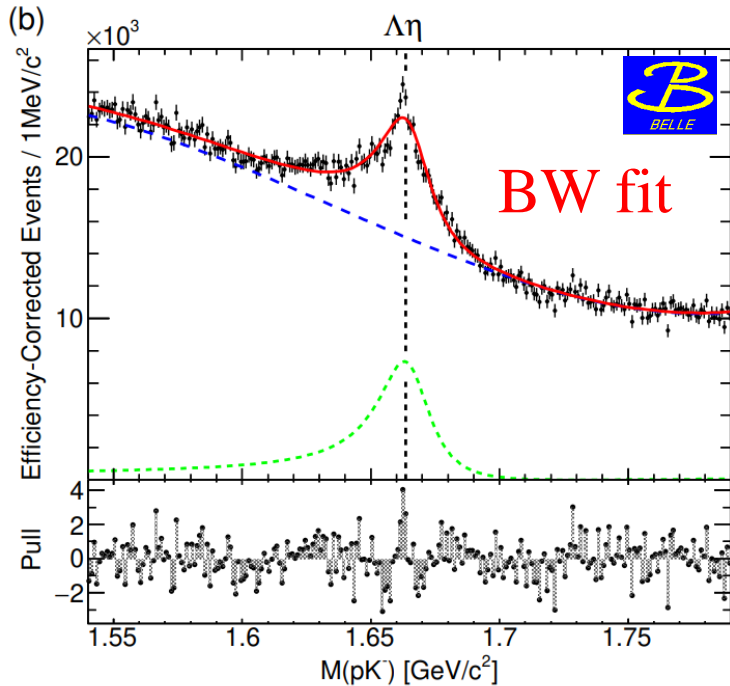
- The cusp shape is unaffected by resonances in higher partial waves.
- The interference term with different  $L$  vanishes with an integral over the decay angle.
- $S$ -wave resonances such as  $\Lambda(1405)$  can make an interference effect. As they are rather far away, and their effect are approximated as a constant.

→ Then,  $\frac{dN}{dm} \propto |f(m) + r e^{i\theta}|^2$  is a reasonable choice.

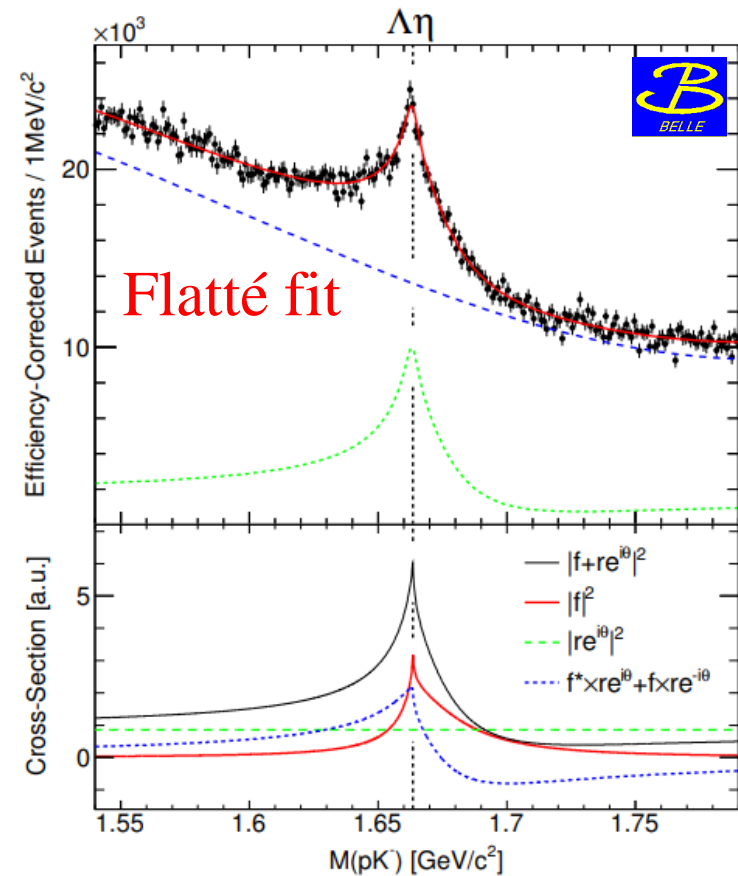
\*Flatté function:  $|f(m)|^2 = \left| \frac{1}{m - m_f + \frac{i}{2}(\Gamma + \bar{g}_{\Lambda\eta}k)} \right|^2$

- One-dimensional fit results

\* $m_f = 1674.4 \text{ MeV}/c^2$  and  $\theta = \pi$  fixed.



\*Belle, PRD 108, L031104 (2023)



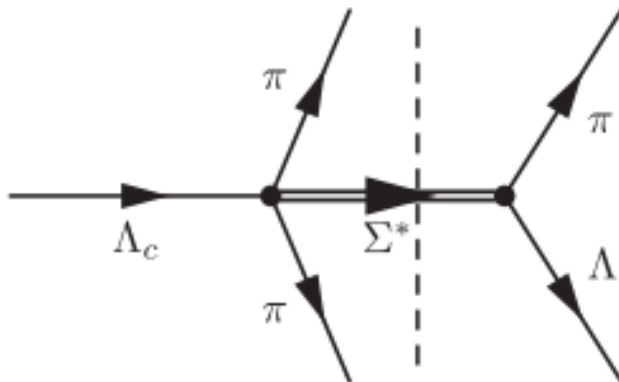
Mass ( $\text{MeV}/c^2$ )	Width (MeV)	$\chi^2/ndf$
$1665.4 \pm 0.5$	$23.8 \pm 1.2$	<b>1.27 (308/243)</b>

$m_f$ ( $\text{MeV}/c^2$ )	$\Gamma'$ (MeV)	$\bar{g}_{\Lambda\eta}$	$\chi^2/ndf$
1674.4 (fixed)	$27.2 \pm 1.9^{+5.0}_{-3.9}$	$0.258 \pm 0.023^{+61}_{-75}$	<b>1.06 (257/243)</b>

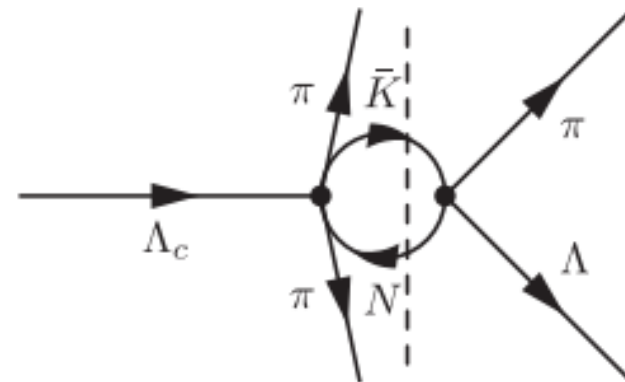
→ Flatté function is significantly favored than Breit-Wigner function.

## New peak structures near $\bar{K}N$ threshold in $\Lambda\pi$ system

- New  $\Lambda\pi$  peak structures near  $\bar{K}N(I = 1)$  threshold in  $\Lambda_c^+ \rightarrow \Lambda\pi^+\pi^-\pi^+$  decays
  - No prediction from standard quark model  $\Lambda_c^+ \rightarrow \Lambda\pi^+\pi^-\pi^+$ 
    - Exotic hadron?
    - Threshold cusp whose shape reflects the scattering length of  $\bar{K}N(I = 1)$  interaction?



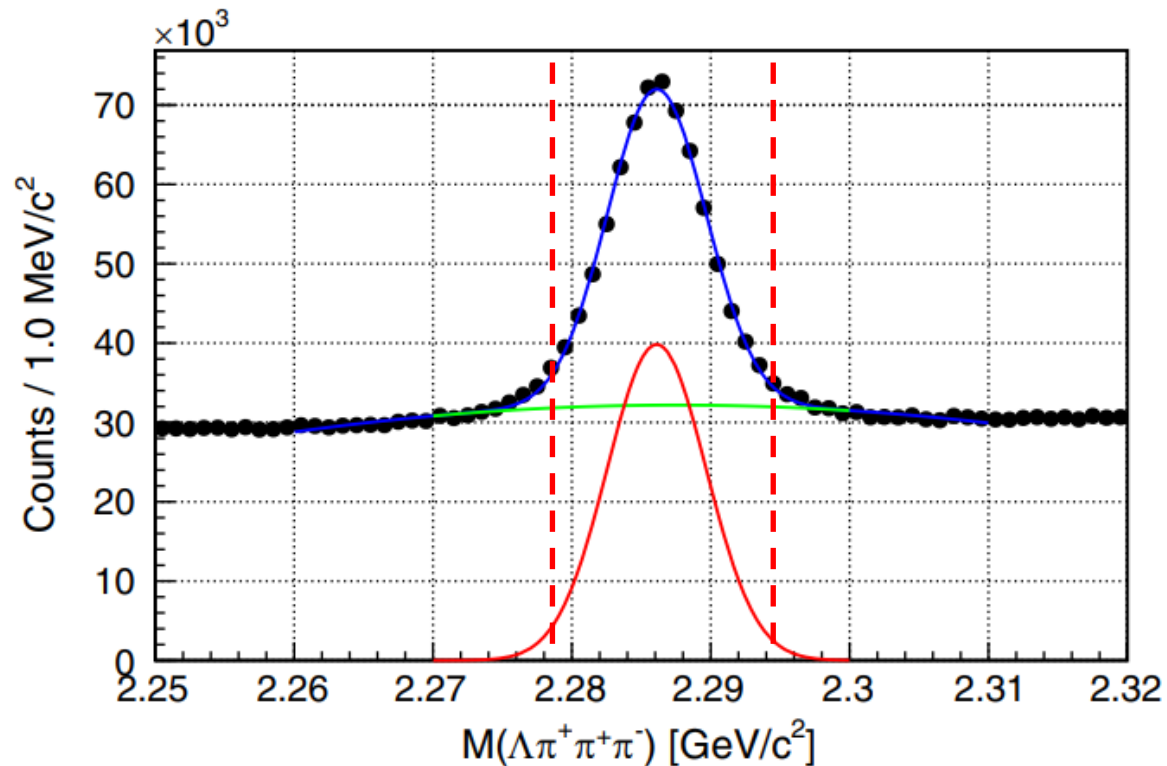
$\Sigma^*$  resonance



$\bar{K}N$  scattering with a cusp

\*Belle, PRL 130, 151903 (2023)

- Full data sample of Belle,  $980 \text{ fb}^{-1}$
- Distribution of  $M(\Lambda\pi^+\pi^-\pi^+)$ 
  - clear peak structure of  $\Lambda_c^+$  is seen.
  - Mass window  $|M(\Lambda\pi^+\pi^-\pi^+) - M_{\Lambda_c^+}| < 8 \text{ MeV}/c^2$

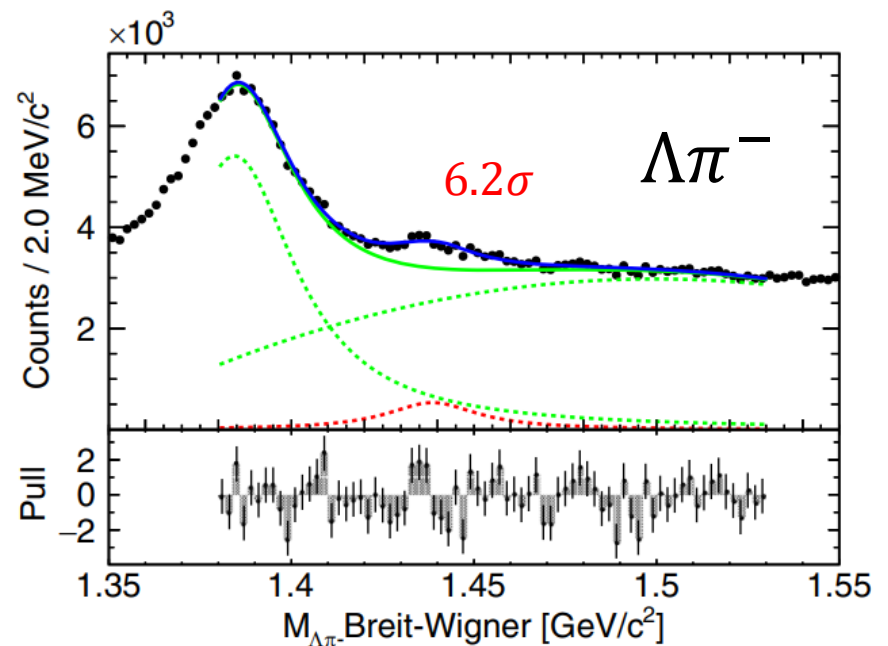
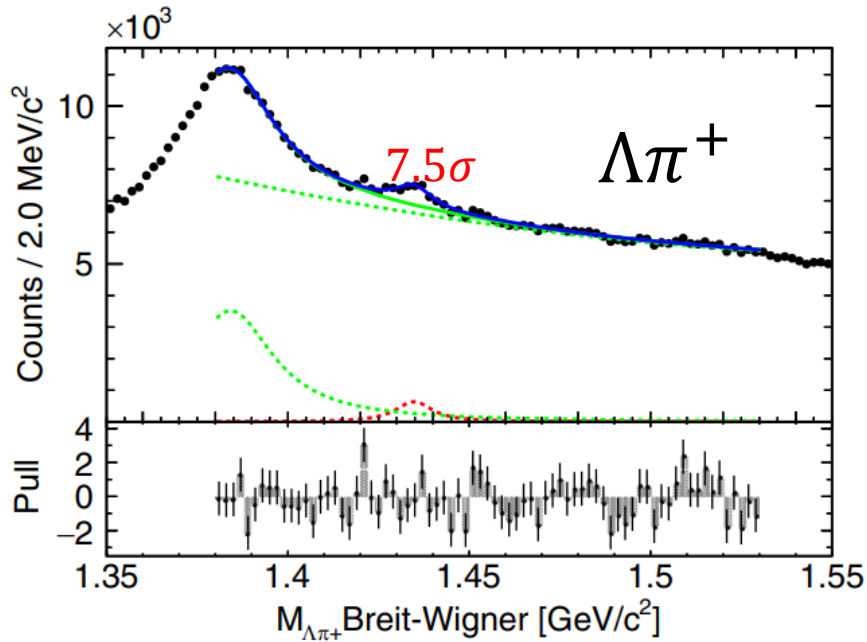
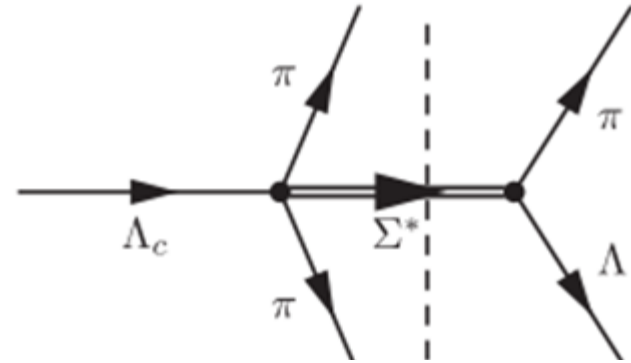


\*Belle, PRL 130, 151903 (2023)



- Fit results with Breit-Wigner model

\*Belle, PRL 130, 151903 (2023)



Mode	$E_{\text{BW}}$ (MeV/c <sup>2</sup> )	$\Gamma$ (MeV/c <sup>2</sup> )	$\chi^2/\text{NDF}$
$\Lambda\pi^+$	$1434.3 \pm 0.6$	$11.5 \pm 2.8$	74.4/68
$\Lambda\pi^-$	$1438.5 \pm 0.9$	$33.0 \pm 7.5$	92.3/68

- Parameterization of Dalitz model
  - Neglecting the  $\Lambda_c^+$  form factor
  - $\bar{K}$ - $N$  complex scattering length:  $a + bi$

$$f_D = \frac{4\pi b}{(1 + kb)^2 + (ka)^2}, \quad E > m_{\bar{K}N}$$

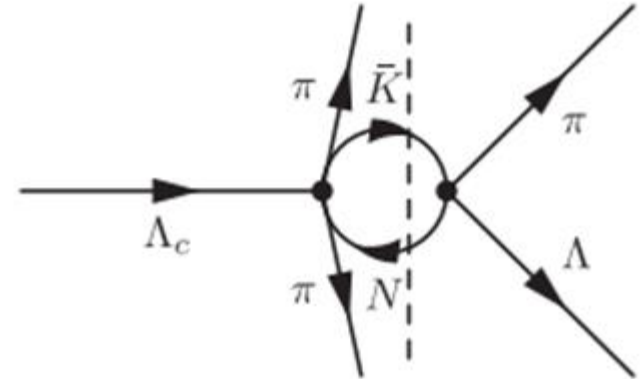
$$= \frac{4\pi b}{(1 + \kappa a)^2 + (\kappa b)^2}, \quad E < m_{\bar{K}N},$$

where

$$\kappa = \sqrt{2\mu(E - m_{\bar{K}N})},$$

$$k = \sqrt{2\mu_{\Lambda\eta}(m_{\bar{K}N} - E)},$$

$$\mu = \frac{m_{\bar{K}}m_N}{(m_{\bar{K}} + m_N)}.$$

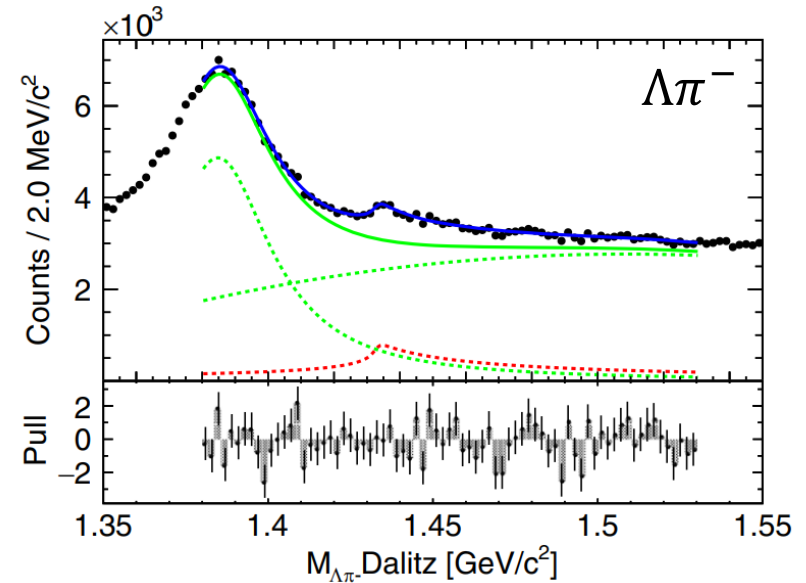
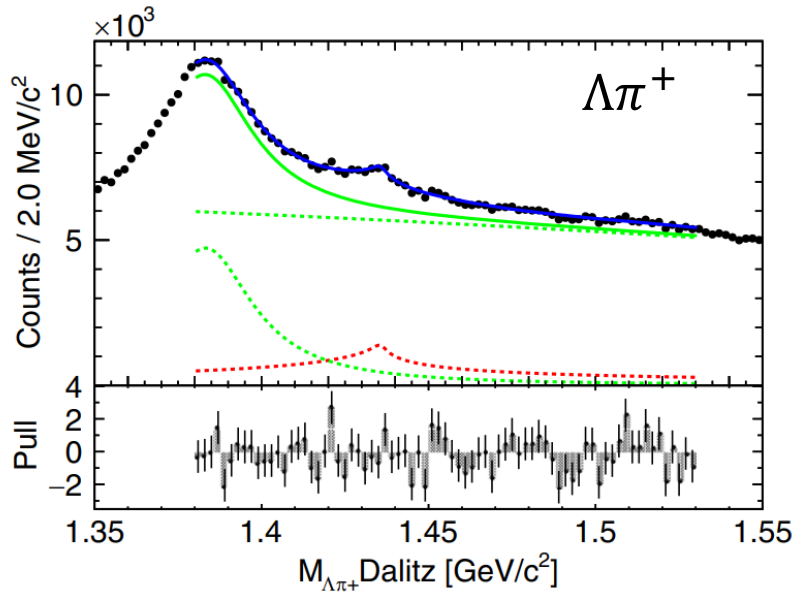


\*Belle, PRL 130, 151903 (2023)

- The Dalitz model is largely consistent with the Flatté model by fixing  $m_f$  far away from  $\bar{K}N$  threshold.

- Fit results with Dalitz model

\*Belle, PRL 130, 151903 (2023)



Mode	$a$ (fm)	$b$ (fm)	$\chi^2/\text{NDF}$
$\Lambda\pi^+$	$0.48 \pm 0.32$	$1.22 \pm 0.83$	68.9/68
$\Lambda\pi^-$	$1.24 \pm 0.57$	$0.18 \pm 0.13$	78.1/68

- The scattering length is larger than the previous results  
 $\rightarrow$  The effect of the neglected decay form factor?

- Comparing to Breit-Wigner results, we can't identify them.

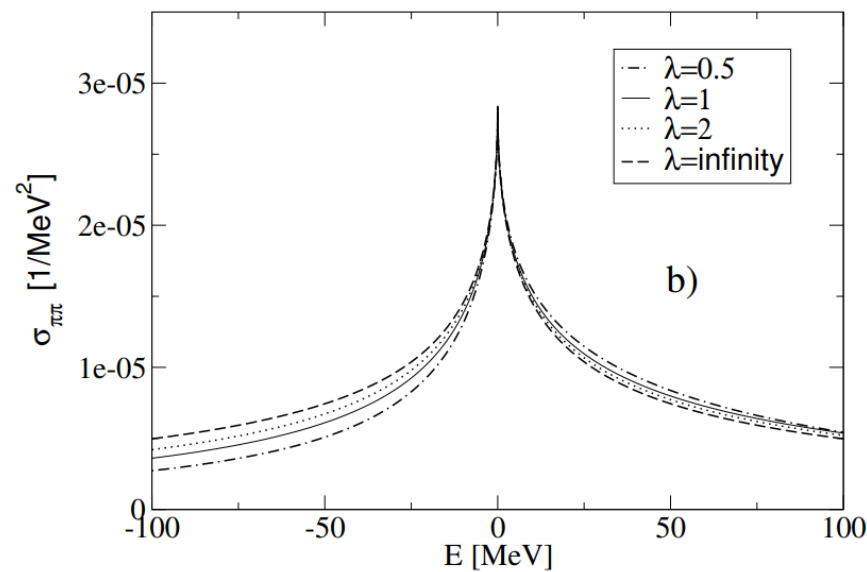
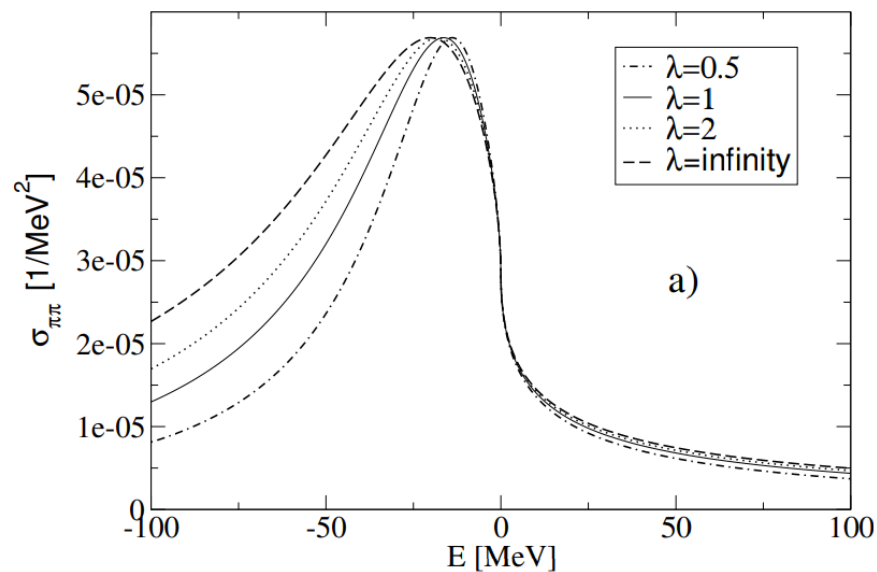
- Bottomonium: Transitions of  $\Upsilon(10753)$ 
  - $\Upsilon(10753) \rightarrow \chi_{bJ}(1P)\omega$  decays are observed.
  - No significant signals of  $\Upsilon(10753) \rightarrow \chi_{b0}(1P)\omega$  and  $\omega\eta_b(1S)$  decays are observed.
  
- Hyperon: New peak structures near the mass thresholds
  - A threshold cusp at the  $\Lambda\eta$  threshold is observed in  $pK^-$  system. The peak structure favors the Flatté model significantly.
  - New  $\Lambda\pi$  peaking structures near the  $\bar{K}N$  threshold are observed in  $\Lambda_c^+ \rightarrow \Lambda\pi^+\pi^-\pi^+$  decays. They are not predicted by standard quark model.

\* In Hadron Spectroscopy section (Oct. 17, 12:10PM),  
     ‘Recent results on charmed baryon’ by Suxian Li

**Significant research on hadron spectroscopy  
 is currently in progress at Belle & Belle II !!**

\*Backup Slides

- Flatté model



$$f_{\text{el}} = -\frac{1}{2q} \frac{\Gamma_P}{E - E_{\text{BW}} + i\frac{\Gamma_P}{2} + i\bar{g}_K \frac{k}{2}}$$

where,  $k = \sqrt{m_K(\sqrt{s} - 2m_k)}$  \* $k$  is imaginary when  $m < 2m_K$