### Recent leptonic/rare decays results at Belle and Belle II

WG2 + WG3

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Established by the European Co







### Outline

#### Paving the way towards LFU tests:

- Path to  $R_{\kappa}(*)$  in B decays
- τ mass measurement in tau decays

#### Searches for rare/forbidden decays:

- $B^+ \rightarrow \mu^+ \nu$
- $B^0 \rightarrow K^{*0} \tau \tau$
- $B_s \rightarrow \pi^0 \pi^0$
- LFV τ decays

#### Measurement of radiative decay:

• Inclusive  $B \rightarrow X_s \gamma$ 

See also previous talks:

LFV B decays : Gagan Mohanty (WG2) LFU tests in b  $\rightarrow$  clv : Robert Kowalewski (WG3) B  $\rightarrow$  Kvv : Slavomira Stefkova (WG2) B  $\rightarrow \rho\gamma$  : Rahul Tiwar (WG3)

### Outline



### Advantages of Belle (II) for rare decays

• Excellent muon and electron ID efficiency



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- Good hermiticity: useful for modes with missing energy
- Various levels of B-tagging



Hadronic tagging Full knowledge of B<sub>tag</sub> kinematic

Semileptonic tagging Partial knowledge of B<sub>tag</sub> kinematic

Inclusive tagging Indirect knowledge of B<sub>tag</sub> kinematic See e.g. <u>PRL. 127, 181802</u>

#### Data sets





Data available for physics analysis (fb<sup>-1</sup>) :

	Y(4S)	Y(5S)	Off-resonance*	others	Total
Belle	711	121	89	67	980
Belle II	362		42	20	424

\*off resonance data are taken 60MeV below Y(4S)

Unless stated, results presented here are based on full statistics

Towards  $R_{K(*)}$ : BR(B  $\rightarrow$  K\*II)

- First step : observation of  $B \rightarrow K^*II$  decays at Belle II
- Combine B<sup>+</sup> and B<sup>0</sup> channels, using  $K^* \rightarrow K + \pi$ -, Ks  $\pi$ +, K+ $\pi$ 0
- Signal yields obtained from 2D maximum likelihood fit of  $M_{bc}$ and  $\Delta E \qquad M_{bc} = \sqrt{E_{beam}^{*2} - p_B^{*2}} \qquad \Delta E = E_B^* - E_{beam}^*$
- Similar performances for electrons and muons in terms of efficiency and background
- Exclude charmonium resonances and M(e+e-)<0.14GeV
- Using 189fb<sup>-1</sup>, observe 22±6 B  $\rightarrow$  K\*µµ, 18±6 B  $\rightarrow$  K\*ee and 38±9 B  $\rightarrow$  K\*II, giving :

 $\mathcal{B}(B \to K^* \mu^+ \mu^-) = (1.19 \pm 0.31^{+0.08}_{-0.07}) \times 10^{-6},$  $\mathcal{B}(B \to K^* e^+ e^-) = (1.42 \pm 0.48 \pm 0.09) \times 10^{-6},$  $\mathcal{B}(B \to K^* \ell^+ \ell^-) = (1.25 \pm 0.30^{+0.08}_{-0.07}) \times 10^{-6}.$ 









Belle II arXiv:2207.11275

Towards  $R_{K(*)}$ :  $R_{K}(J/\psi)$ 

- Measurement validation using  $B \rightarrow J/\psi K$  decays
- Use both B<sup>+</sup> and B<sup>0</sup> channels, also measure isospin asymmetries



$$R_K(J/\psi) = \frac{\mathcal{B}(B \to J/\psi(\mu^+\mu^-)K)}{\mathcal{B}(B \to J/\psi(e^+e^-)K)}$$

ObservableMeasured value $A_I (J/\psi(ee)K)$  $-0.022 \pm 0.016 \pm 0.030$  $A_I (J/\psi(\mu\mu)K)$  $-0.006 \pm 0.015 \pm 0.030$  $R_{K^+} (J/\psi)$  $1.009 \pm 0.022 \pm 0.008$  $R_{K_S^0} (J/\psi)$  $1.042 \pm 0.042 \pm 0.008$ 

Low systematic uncertainties thanks to very good control of lepton ID

#### τ mass measurement



- $m_{\tau}$  is one of the fundamental parameter of the SM
- Crucial for SM predictions of BR and LFU tests
- Use kinematic of  $\tau \rightarrow 3\pi v$  decays to measure the pseudomass  $M_{\min} = \sqrt{M_{3\pi}^2 + 2(\sqrt{s}/2 - E_{3\pi}^*)(E_{3\pi}^* - p_{3\pi}^*)} \le m_{\tau}.$

$$\left(\frac{g_{\mu}}{g_{e}}\right)_{\tau} = \sqrt{R_{\mu}\frac{f(m_{e}^{2}/m_{\tau}^{2})}{f(m_{\mu}^{2}/m_{\tau}^{2})}}, \quad R_{\mu} = \frac{\mathcal{B}[\tau^{-} \to \mu^{-}\bar{\nu_{\mu}}\nu_{\tau}]}{\mathcal{B}[\tau^{-} \to e^{-}\bar{\nu_{e}}\nu_{\tau}]}$$
$$f(x) = 1 - 8x + 8x^{3} - x^{4} - 12x^{2}\ln x$$

-  $m_{\tau}$  is extracted from an empirical fit to  $M_{min}$ 



Sharp edge corresponding to  $m_\tau$  value, smeared by momentum resolution and ISR/FSR

Control of beam energy and momentum are crucial (limiting systematics of previous B factory measurements)

#### τ mass measurement

- Beam energy controlled using fully reconstructed B decays
- Momentum scale factor obtained measuring mass from  $D^{*+} \rightarrow D^0(\rightarrow K^-\pi^+)\pi^+$  decays
- Unbinned maximum likelihood fit to  $M_{min} \longrightarrow m_{\tau} = 1777.09 \pm 0.08 \pm 0.11 \text{ MeV}$



Phys. Rev. D 108, 032006



## Search for $B^+ \to \mu^+ \nu$ with inclusive tagging

- CKM and helicity suppressed decay, expected BR in the range 3.8-4.3 x 10<sup>-7</sup>, depending on V<sub>ub</sub> value
- Sensitive to NP contribution such as charged Higgs or leptoquark, or sterile neutrinos
- Analysis strategy based on the monochromaticity of muon in the B rest frame
- Only the muon is explicitly reconstructed, remaining tracks and clusters form the ROE boost in B<sup>+</sup> rest frame



$$\mathcal{B}(B^+ \to \ell^+ \nu_\ell) = \frac{G_F^2 m_B m_\ell^2}{8\pi} \left(1 - \frac{m_\ell^2}{m_B^2}\right)^2 f_B^2 \left|V_{ub}\right|^2 \tau_B$$





## Search for $B^+ \to \mu^+ \nu$ with inclusive tagging

- Resolution is improved with a calibration factor derived from simulation, accounting for particles that escape detection
- Main backgrounds are continuum and semileptonic b → uµv decays, mitigated using a BDT (C<sub>out</sub>) and the muon direction in the B rest frame
- Events separated into 4 categories

<b>-</b>	<i></i>	-	
Category	$C_{ m out}$	$\cos \Theta_{B\mu}$	Signal Efficiency
Ι	[0.98, 1.00)	[-0.13, 1.00)	6.5%
Π	[0.98, 1.00)	[-1.00, -0.13)	5.9%
III 🛉	[0.93, 0.98)	[0.04, 1.00)	7.1%
IV	[0.93, 0.98)	[-1.00, 0.04)	8.3%





Signal enriched



## Search for $B^+ \to \mu^+ \nu$ with inclusive tagging

Phys. Rev. D 101, 032007 (2020)

- Category Category I Continuum 250 200 geV Continuum Entries / (0.050 GeV) 00 001 001 711 fh 0<u>5</u>0.0 150 Entries / 201 sys. unc sys. unc Data Data 2.2 2.2 2.4 2.6 2.8 3.0 3.2 2.6 2.8 3.0 3.2 2.4  $p_{ii}^{B}$  / (GeV)  $p_{\mu}^{B}$  / (GeV)  $B^+ \rightarrow \mu^+ \nu_{\mu}$ relative uncertainty [%] 20.0 🖉 40.017.5 15.0 12.5 nucertainty **Projection of** 35.0 BR(B  $\rightarrow \mu/\tau \nu$ ) 30.0 25.0 uncertainty at 10.0 1.00 . |V<sub>ub</sub>| relative u 20.0 Belle II 15.0 From Snowmass 00 white paper 10.0 arXiv:2207.06307  $\mathcal{B}(B^+$ 2.5 5.0 Belle II 10 50 Integrated Luminosity [ab<sup>-1</sup>]
- BR(B<sup>+</sup>  $\rightarrow \mu^+ \nu)$  obtained from a simultaneous binned fit to  $p^{B}_{\mu}$  in the 4 categories  $\mathcal{B}(B^+ \rightarrow \mu^+ \nu_{\mu}) = (5.3 \pm 2.0 \pm 0.9) \times 10^{-7}$ .
- No significant signal is observed (2.8σ), limit obtained with frequentist approach:

 $\mathcal{B}(B^+ \to \mu^+ \, \nu_{\mu}) < 8.6 \times 10^{-7} \, \mathrm{at} \, 90\% \, \mathrm{CL}$ 

best upper limit to date!

• BR measurement also used to set constraints on 2HDM model and decays to sterile neutrino  $B^+ \rightarrow \mu^+ N$  for masses up to 1.5 GeV

#### Search for $B^0 \to K^{*0} \tau \tau$

- Anomalies seen in violation of LFU suggest a special role of the third family, with enhancement of b→stt decays
- b→sττ decays are much less well known than their e/μ counterparts, experimentally challenging due to at least 2 neutrinos in final state

Decays	SM prediction	Best 90% CL UL			
$B^0 \rightarrow \tau \tau$	(2.22±0.19) 10 <sup>-8</sup> [1]	1.6 10 <sup>-3</sup> [3]			
Β <sub>s</sub> → ττ	(7.73±0.49) 10 <sup>-7</sup> [1]	5.2 10 <sup>-3</sup> [3]			
Β0 → Κ*0ττ	(0.98±0.10) 10 <sup>-7</sup> [2]	This result			
B+ <del>→</del> K+ττ	(1.20±0.12) 10 <sup>-7</sup> [2]	2.25 10 <sup>-3</sup> [4]			

[1] PRL 112(2014)101801
[2] PRL 120(2018)181802
[3] LHCb PRL 118(2017)251802
[4] Babar PRL 118(2017)031802





B. Capdevila, A. Crivellin, S. Descotes-Genon, L. Hofer, et J. Matias, *PRL 120, 181802* 

#### Search for $B^0 \to K^{*0} \tau \tau$



#### Phys. Rev. D 108, L011102 (2023)



- B hadronic tagging based on neural network
- Select event with 4 remaining tracks
- Reconstruct one prong  $\tau$  decays  $\tau \rightarrow e/\mu/\pi$
- Signal yield obtain by fitting the extra ECL energy (clusters not associated with B<sub>sig</sub> or B<sub>tag</sub>)

 $N_{
m sig} = -4.9\pm 6.0$ 

Background only fit with signal superimposed

• Fit procedure validated on  $B \rightarrow Dlv$  decays

Upper limit is set at 3.1 x 10<sup>-3</sup> @90% C.L.

Improvements foreseen at Belle II: FEI,  $\tau \rightarrow \rho$  mode, multivariate analysis. Stay tuned!

## Search for $B_s \to \pi^0 \pi^0$

BELLE



- Decay proceeds through W exchange and penguin annihilation diagram
- Measuring BR is important to understand QCD dynamic and validate theoretical calculations
- BR(B<sub>s</sub>  $\rightarrow \pi^+\pi^-$ ) was measured by LHCb, showing tension with QCDF predictions
- Only a limit was set on  $BR(B_s \rightarrow \pi^0 \pi^0)$  by L3

Decay mode	Measurement	<b>QCDF</b> (× 10 <sup>-7</sup> ) [15]	<b>pQCD</b> (× 10 <sup>-7</sup> )
$B_s \to \pi^+ \pi^-$	$(6.91 \pm 0.54 \pm 0.63 \pm 0.19 \pm 0.4) \times 10^{-7}$ (LHCb, 2017) [13]	$(6.1^{+0.2+0.7}_{-0.4-0.6})$	$\begin{bmatrix} (5.10^{+1.96}_{-1.68} (a_2^{\pi})^{+0.25+1.05+0.29}_{-0.19-0.83-0.20}) \\ [16] \end{bmatrix}$
$B_s \to \pi^0 \pi^0$	< 2.1 × 10 <sup>-4</sup> (L3 Collaboration, 1995) [14]	$(1.3^{+0.1+0.3}_{-0.2-0.3})$	$(2.8^{+0.8+0.9+0.1}_{-0.7-0.5-0.0})$ [17]

[13] Aaij, et al., PRL 118 (2017)

[14] Acciarri, et al., Physical Letters B 363 (1995)

[15] Chang, et al., Physical Letters B 740 (2015)

[16] Xiao, et al., PRD 85 (2012) 94003

[17] Ali, et al., PRD 76 (2007)

# <u>arXiv:2301.08587</u>

## Search for $B_s \to \pi^0 \pi^0$

- Analysis using 121 fb<sup>-1</sup> of Y(5S) data, just above the B<sub>s</sub>B<sub>s</sub>\* threshold
- Blind analysis, overall signal efficiency is 12.7%
- Signal yield obtained from a 3D fit using  $M_{bc}$ ,  $\Delta E$  and a neural network output C' against continuum backgrounds  $M_{bc} = \frac{\sqrt{(E_{beam})^2 |\vec{p}_{reco}|^2 c^2}}{c^2}, \quad \Delta E = E_{reco} E_{beam} + M_{bc}c^2 m_{B_s^0}c^2$
- Signal PDF is the sum of all 3 production modes



### Search for $\tau$ LFV decays

- LFV decays expected at rate 10<sup>-50</sup> in SM, observation would be a clear sign of NP
- Some channels are particularly sensitive to leptoquark models, ex: τ→ ℓφ in the U(1) vector leptoquark hypothesis
- Most of best LFV limits have been set by Belle in the past using a selection based on the topology







#### Search for $\tau \rightarrow \ell V^0$

- New Belle analysis using 980 fb<sup>-1</sup>
- Use 3-prong decays of tagged τ in addition to 1-prong, and a BDT selection to suppress continuum background
- Signal is searched in 2D plane:  $M_{\tau sig}$  and  $\Delta E = E_{sig} E_{beam}$

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	Mode	$\varepsilon$ (%)	$N_{ m BG}$	$\sigma_{\rm syst}$ (%)	$N_{ m obs}$	$\mathcal{B}_{ m obs}~( imes 10^{-8})$
	$ au^\pm  o \mu^\pm  ho^0$	7.78	$0.95 \pm 0.20$ (stat.) $\pm 0.15$ (syst.)	4.6	0	< 1.7
	$\tau^\pm \to e^\pm \rho^0$	8.49	$0.80 \pm 0.27 (stat.) \pm 0.04 (syst.)$	4.4	1	< 2.2
	$\tau^\pm \to \mu^\pm \phi$	5.59	$0.47 \pm 0.15 (stat.) \pm 0.05 (syst.)$	4.8	0	< 2.3 *
	$\tau^\pm \to e^\pm \phi$	6.45	$0.38 \pm 0.21$ (stat.) $\pm 0.00$ (syst.)	4.5	0	< 2.0 *
	$ au^\pm  o \mu^\pm \omega$	3.27	$0.32 \pm 0.23$ (stat.) $\pm 0.19$ (syst.)	4.8	0	< 3.9 *
	$\tau^\pm \to e^\pm \omega$	5.41	$0.74 \pm 0.43$ (stat.) $\pm 0.06$ (syst.)	4.5	0	< 2.4 *
	$\tau^\pm \to \mu^\pm K^{*0}$	4.52	$0.84 \pm 0.25 (stat.) \pm 0.31 (syst.)$	4.3	0	< 2.9 *
	$\tau^\pm \to e^\pm K^{*0}$	6.94	$0.54 \pm 0.21$ (stat.) $\pm 0.16$ (syst.)	4.1	0	< 1.9 🔺
	$\tau^{\pm} \to \mu^{\pm} \overline{K}{}^{*0}$	4.58	$0.58 \pm 0.17 (stat.) \pm 0.12 (syst.)$	4.3	1	< 4.3 *
	$\tau^{\pm} \rightarrow e^{\pm} \overline{K}^{*0}$	7.45	$0.25 \pm 0.11$ (stat.) $\pm 0.02$ (syst.)	4.1	0	< 1.7 *

#### JHEP06(2023)118



Limits improved by ~30% wrt previous Belle results

#### Search for $\tau \rightarrow \ell \phi$

- Novel inclusive strategy developed at Belle II on 190fb<sup>-1</sup>
- Reconstruct only the signal τ
- Use Rest-of-Event properties to discriminate background









Quantity	Dorion	Mode				
Quantity	negion	$e\phi$	$\mu\phi$			
Signal efficiency $\varepsilon_{\ell\phi}$	SR	$(6.1 \pm 0.9 \text{ (syst)})\%$	$(6.5 \pm 0.6 \text{ (syst)})\%$			
$r_{ m MC}$	$\mathbf{SR} \ / \ \mathbf{RSB}$	$0.23^{+0.16}_{-0.10} \text{ (stat)}$	$0.12^{+0.07}_{-0.04}$ (stat)			
$N_{ m data}$	RSB	$1.0^{+2.3}_{-0.8} (\text{stat})$	$3.0^{+2.9}_{-1.6}$ (stat)			
$N_{\mathrm{exp}}$	$\mathbf{SR}$	$0.23^{+0.55}_{-0.21}$ (stat)	$0.36^{+0.39}_{-0.23}$ (stat)			
$N_{\rm obs}$	$\mathbf{SR}$	$2.0^{+2.6}_{-1.3}$ (stat)	$0.0^{+1.8}_{-0.0}$ (stat)			

Obs.  $B_{\text{UL}}(\tau \to e\phi) = 23 \times 10^{-8}$  Obs.  $B_{\text{UL}}(\tau \to \mu\phi) = 9.7 \times 10^{-8}$ Exp.  $B_{\text{III.}}(\tau \rightarrow e\phi) = 15 \times 10^{-8}$ 

Exp.  $B_{\text{III.}}(\tau \to \mu \phi) = 9.9 \times 10^{-8}$ 

Promising technique for coming Belle II statistics

Inclusive  $B \rightarrow X_{\varsigma} \gamma$ 

- Measurement only possible in clean environment of B factories, highly sensitive to NP particles in the loop
- Based on the full reconstruction of the other B in a hadronic mode thanks to the *Full Event Interpretation* 
  - Tagging efficiency is (0.44±0.02)%
- Knowledge of flavour and momentum of  $B_{tag}$  allows to access the photon energy in the  $B_{sig}$  frame,  $E_{v}^{B}$
- Moments of  $E_{\gamma}{}^{B}$  gives information on HQE parameters  $m_{b}$  and  $\mu_{\pi}{}^{2}$
- Inclusive and high purity reconstruction also allows measurement of CP and isospin asymmetries





arXiv:2210.10220

### Inclusive $B \rightarrow X_s \gamma$

- Measure B(B  $\rightarrow$  X<sub>s</sub> $\gamma$ ) with 189 fb<sup>-1</sup> in 8 bins of E<sub> $\gamma$ </sub><sup>B</sup>, for E<sub> $\gamma$ </sub><sup>B</sup> > 1.8 GeV
- Fit of the tag side M<sub>bc</sub> in bins of E<sub>γ</sub><sup>B</sup> to determine yields of correctly reconstructed B events, continuum and combinatorial B background

$$M_{
m bc}=\sqrt{(\sqrt{s}/2)^2-p_{
m tag}^2}$$

• Differential BR computed as:

Unfolding factor

$$\frac{1}{\Gamma_B} \frac{d\Gamma_i}{dE_{\gamma}^B} = \frac{\mathcal{U}_i \times (N_i^{\text{DATA}} - N_i^{\text{BKG, MC}} - N_i^{B \to X_d \gamma})}{\varepsilon_i \times N_B},$$

- Non signal B subtracted using simulation
- $b \rightarrow d\gamma$  contribution removed assuming same shape and selection efficiency as signal, with a factor

$$V_{td}/V_{ts}|^2 \approx 4.3\%$$







### Inclusive $B \rightarrow X_s \gamma$

#### arXiv:2210.10220



$E_{\gamma}^{B}$ threshold [GeV]	$\mathcal{B}(B \to X_s \gamma) \ [10^{-4}]$	Observed signal yield (tot. unc.)
1.8	$3.54 \pm 0.78$ (stat.) $\pm 0.83$ (syst.)	$343 \pm 122$
2.0	$3.06 \pm 0.56$ (stat.) $\pm 0.47$ (syst.)	$285\pm68$
2.1	$2.49\pm0.46$ (stat.) $\pm$ 0.35 (syst.)	$219\pm50$



The threshold value introduces different biases in the phenomenological interpretation of the moments

Main systematic uncertainties are coming from the fit procedure (B background shape and  $M_{bc}$  endpoint) and simulation statistics



Inclusive  $B \rightarrow X_{s} \gamma$ 



<u>Plot</u> available from <u>latest rare decays HLFAV webpage</u>



### Summary

#### Belle

- First experimental result on  $B^0 \rightarrow K^{*0} \tau \tau$
- Improvement of existing limit on  $B(B_s \rightarrow \pi^0 \pi^0)$  by 2 order of magnitude
- World best limit on  $B^+ \rightarrow \mu^+ \nu$  thanks to an inclusive tagging technique
- Improved limits on  $\tau \rightarrow \ell V^0$

#### Belle II

- Open path towards  $R_{K(^{\ast})}$  measurements with Belle II data
- Most precise measurement of  $\tau$  mass
- New inclusive technique for  $\tau\,$  LFV searches
- First inclusive analysis of  $B \rightarrow X_s \gamma$  showing competitive results with 189 fb<sup>-1</sup>

Belle II already demonstrated excellent tagging performances and control of systematic uncertainties ©





Table III. Relative systematic uncertainties (%) on  $\mathcal{B}(B \to J/\psi K)$ ,  $R_K(J/\psi)$ , and absolute uncertainty on  $A_I(B \to J/\psi K)$ .

Source	$\mathcal{B}\left(B \to KJ/\psi\right)$			$R_K$		$A_I$		
	$K^+$	$K^+$	$K_S^0$	$K_S^0$	$K^+$	$K^0$		
	$e^+e^-$	$\mu^+\mu^-$	$e^+e^-$	$\mu^+\mu^-$			$e^+e^-$	$\mu^+\mu^-$
Number of $B\overline{B}$ events	1.5	1.5	1.5	1.5	_	_	—	—
PDF shape	0.2	0.2	0.2	0.2	0.2	0.2	0.1	0.1
Electron identification	0.6	_	0.6	_	0.6	0.6	_	_
Muon identification	_	0.4	_	0.4	0.4	0.4	_	_
Kaon identification	0.2	0.2	_	_	_	_	0.1	0.1
$K_S^0$ reconstruction	_	_	3.0	3.0	_	_	1.5	1.5
Tracking efficiency	0.9	0.9	1.2	1.2	_	_	0.4	0.4
Simulation sample size	0.1	0.1	0.1	0.1	0.1	0.1	0.1	0.1
$\Upsilon(4S)$ branching fraction	2.6	2.6	2.6	2.6	_	_	2.6	2.6
$( au_{B^+}/ au_{B^0})$					_		0.2	0.2
Total	3.2	3.2	4.4	4.4	0.8	0.8	3.0	3.0

#### Tau mass



Correction factors range from 0.99660 to 1.00077 depending on charge and polar angle

TABLE II. Summary of systematic uncertainties in the  $\tau$ -mass measurement.

Source	Uncertainty (MeV/ $c^2$ )	
Knowledge of the colliding beams:		
Beam-energy correction	0.07	
Boost vector	< 0.01	
Reconstruction of charged particles:		
Charged-particle momentum correction	0.06	
Detector misalignment	0.03	
Fit model:		
Estimator bias	0.03	
Choice of the fit function	0.02	
Mass dependence of the bias	< 0.01	
Imperfections of the simulation:	-	
Detector material density	0.03	
Modeling of ISR, FSR and $\tau$ decay	0.02	
Neutral particle reconstruction efficiency	$\leq 0.01$	
Momentum resolution	< 0.01	
Tracking efficiency correction	< 0.01	
Trigger efficiency	< 0.01	
Background processes	< 0.01	
Total	0.11	

Mostly from uncertainty on BB cross section energy dependence

pT dependence of scale factor, D mass uncertainty, modeling of D0 signal peak, difference in angular distribution of tau and D decays

Obtained from fit to simulation with different tau mass values

Alternative fits with function previously used by Babar/Belle

That can affect the P1 estimator bias

+ consistency checks as function of data taking periods, kinematic regions, tau decay model.