



First decay-time-dependent analysis of $B^0 \rightarrow K^0 \pi^0$ decays at Belle II

(Belle II Collaboration)

Abstract

We report measurements of the branching fraction (\mathcal{B}) and direct CP -violating asymmetry (\mathcal{A}_{CP}) of the charmless decay $B^0 \rightarrow K^0 \pi^0$ at Belle II. A sample of e^+e^- collisions, corresponding to 189.8 fb^{-1} of integrated luminosity, recorded at the $\Upsilon(4S)$ resonance is used for the first Belle II decay-time-dependent analysis of these decays. We reconstruct about 135 signal candidates, and measure $\mathcal{B}(B^0 \rightarrow K^0 \pi^0) = [11.0 \pm 1.2(\text{stat}) \pm 1.0(\text{syst})] \times 10^{-6}$ and $\mathcal{A}_{CP}(B^0 \rightarrow K^0 \pi^0) = -0.41_{-0.32}^{+0.30}(\text{stat}) \pm 0.08(\text{syst})$.

16 **1. INTRODUCTION**

17 The $B^0 \rightarrow K^0 \pi^0$ decay is mediated by flavour-changing neutral currents. In the standard
 18 model (SM), the dominant decay amplitude is given by the $b \rightarrow s d \bar{d}$ loop, which is dominated
 19 by the top quark contribution and carries a weak phase $\arg(V_{tb} V_{ts}^*)$. Here, V_{ij} denote the
 20 CKM matrix elements. Such processes are suppressed in the SM and provide an indirect
 21 route to search for beyond-the-SM particles that might be exchanged in the loop. In the
 22 $B^0 \rightarrow K^0 \pi^0$ decay, CP violation can occur either directly in the decay amplitude (\mathcal{A}_{CP})
 23 or via the interference between decays with and without $B^0-\bar{B}^0$ mixing (\mathcal{S}_{CP}). Neglecting
 24 subleading contributions to the amplitude, \mathcal{S}_{CP} is expected to be equal to $\sin 2\beta$ and $\mathcal{A}_{CP} \approx$
 25 0, where $\beta \equiv \arg(-V_{cd} V_{cb}^*/V_{td} V_{tb}^*)$. Deviations from these expectations could be due to
 26 larger-than-expected subleading SM contributions or by non-SM physics.

27 Combining measurements from Belle and BaBar [1, 2], particle data group find $\mathcal{A}_{CP}(B^0 \rightarrow$
 28 $K^0 \pi^0)$ to be consistent with zero within 13% precision. This uncertainty is limiting the
 29 overall precision of a sum rule that combines B -meson lifetimes (τ) with branching fractions
 30 (\mathcal{B}) and CP asymmetries of four $B \rightarrow K\pi$ decays, related by isospin symmetry. The sum
 31 rule,

$$I_{K\pi} = \mathcal{A}_{CP}(K^+ \pi^-) + \mathcal{A}_{CP}(K^0 \pi^+) \frac{\mathcal{B}(K^0 \pi^+) \tau_{B^0}}{\mathcal{B}(K^+ \pi^-) \tau_{B^+}} \quad (1)$$

$$- 2\mathcal{A}_{CP}(K^+ \pi^0) \frac{\mathcal{B}(K^+ \pi^0) \tau_{B^0}}{\mathcal{B}(K^+ \pi^-) \tau_{B^+}} - 2\mathcal{A}_{CP}(K^0 \pi^0) \frac{\mathcal{B}(K^0 \pi^0)}{\mathcal{B}(K^+ \pi^-)} = 0,$$

32 is expected to hold with an uncertainty below 1% and provides an important consistency test
 33 of the SM [3]. Deviations from the isospin sum rule can indicate contributions of non-SM
 34 physics in the loops, or enhancements of color suppressed SM tree amplitudes. The current
 35 measurement of $I_{K\pi}$ value is 0.03 ± 0.08 [4]. The dominant uncertainty on $I_{K\pi}$ sensitivity
 36 comes from the uncertainty of $\mathcal{A}_{CP}(K^0 \pi^0)$. Therefore a precise measurement of $\mathcal{A}_{CP}(K^0 \pi^0)$
 37 is very important for the consistency test of SM.

38 Preliminary results on \mathcal{B} and \mathcal{A}_{CP} of $B^0 \rightarrow K^0 \pi^0$ decays have been reported by Belle II
 39 using a data sample corresponding to 62.8 fb^{-1} . In this analysis, we extend over those mea-
 40 surements by using a larger sample (189.8 fb^{-1}) complemented by a decay-time-dependent
 41 analysis that enhances our sensitivity to \mathcal{A}_{CP} .

42 At Belle II, pairs of neutral B mesons are coherently produced in the process $e^+ e^- \rightarrow$
 43 $\Upsilon(4S) \rightarrow B^0 \bar{B}^0$. When one of the B mesons decays to a CP eigenstate f_{CP} , such as $K_s^0 \pi^0$,
 44 and the other to a flavor-specific final state f_{tag} , the time-dependent decay rate is given by

$$\mathcal{P}(\Delta t) = \frac{e^{-|\Delta t|/\tau_{B^0}}}{4\tau_{B^0}} [1 + q\{\mathcal{A}_{CP} \cos(\Delta m_d \Delta t) + \mathcal{S}_{CP} \sin(\Delta m_d \Delta t)\}], \quad (2)$$

45 where $\Delta t = t_{CP} - t_{\text{tag}}$ is the proper time difference between the decays into f_{CP} and f_{tag} ,
 46 q equals +1 (-1) for the B^0 (\bar{B}^0) decay to f_{tag} , and Δm_d is the $B^0-\bar{B}^0$ mixing frequency.
 47 The key challenge for this analysis is to find the CP side vertex position, for that K_s^0 -flight
 48 direction is project back to the interaction region and put a criteria on K_s^0 to decay inside the
 49 vertex detector. The signal yield and CP asymmetry are obtained from a four-dimensional
 50 fit. The full analysis is developed and tested with simulation, and validated with data
 51 samples in control decay before inspecting on data to measure the physics observables. Due
 52 to the limited sensitivity provided by the available data sample, we measure \mathcal{A}_{CP} by fixing
 53 \mathcal{S}_{CP} , Δm_d and τ_{B^0} to their known values [5].

54 2. THE BELLE II DETECTOR AND DATA SAMPLE

55 Belle II [6] is a particle spectrometer having almost 4π solid-angle coverage, designed to
56 reconstruct final-state particles of e^+e^- collisions delivered by the SuperKEKB asymmetric-
57 energy collider [7]. It is located at the KEK laboratory in Tsukuba, Japan. The energies
58 of the positron and electron beams are 4 and 7 GeV, respectively. Belle II comprises a
59 number of subdetectors surrounding the interaction region in a cylindrical geometry. The
60 innermost one is the vertex detector (VXD), which uses position-sensitive silicon layers to
61 sample the trajectories of charged particles (‘tracks’) in the vicinity of the interaction region
62 to determine the decay positions of their long-lived parent particles. The VXD includes
63 two inner layers of pixel sensors and four outer layers of double-sided microstrip sensors.
64 The second pixel layer is currently incomplete covering one sixth of the azimuthal angle.
65 Charged-particle momenta and charges are measured by a large-radius, small-cell, helium-
66 ethane central drift chamber (CDC), which also offers particle-identification information via
67 a measurement of specific ionization. A Cherenkov-light angle and time-of-propagation de-
68 tector surrounding the CDC provides charged-particle identification in the central detector
69 volume, supplemented by proximity-focusing, aerogel, ring-imaging Cherenkov detectors in
70 the forward region with respect to the electron beam. A CsI(Tl)-crystal electromagnetic
71 calorimeter (ECL) provides energy measurements of electrons and photons. A solenoid sur-
72 rounding the ECL generates a uniform axial 1.5 T magnetic field filling its inner volume.
73 Layers of plastic scintillators and resistive-plate chambers, interspersed between the mag-
74 netic flux-return iron plates, allow for the identification of K_L^0 mesons and muons. The
75 subdetectors most relevant for our study are the VXD, CDC, and ECL.

76 We use all good quality collision data collected, at a center-of-mass (CM) energy near
77 the $\Upsilon(4S)$ resonance, corresponding to an integrated luminosity of 189.8 fb^{-1} . We use large
78 samples of simulated $e^+e^- \rightarrow q\bar{q}$ ($q = u, d, s, c$), $\Upsilon(4S) \rightarrow B^0\bar{B}^0$ and B^+B^- events to
79 optimize the event selection and study possible background contributions. We also use
80 simulated signal events to determine signal models and estimate the selection efficiency.
81 The B -meson decays are simulated using the EVTGEN generator [8], with the effect of final-
82 state radiation incorporated via the PHOTOS package [9]. The simulation of $e^+e^- \rightarrow q\bar{q}$
83 continuum background uses the KKMC generator [10] interfaced to PYTHIA [11]. The
84 interactions of final-state particles with the detector are simulated using GEANT4 [12].

85 3. RECONSTRUCTION AND SELECTION

86 Tracks are reconstructed with the VXD and CDC. Photons are identified as isolated ECL
87 clusters that are not matched to any track. Candidates K_S^0 are reconstructed from pairs of
88 opposite charged particles with dipion mass between 482 and 513 MeV/c^2 . We reconstruct π^0
89 candidates from pairs of photons that have energies greater than 80 (223) MeV if detected in
90 the barrel (endcap) ECL. We apply different energy thresholds between barrel and endcap
91 to suppress beam background, which is higher in the endcap compared to barrel region. The
92 selection also requires the diphoton mass to lie between 119 and 150 MeV/c^2 and the absolute
93 cosine of its helicity angle to be less than 0.953. These criteria suppress contributions from
94 misreconstructed π^0 candidates.

95 The B -meson candidate is reconstructed by combining a K_S^0 with a π^0 candidate. For
96 this purpose, we use two kinematic variables, the beam-energy-constrained mass (M_{bc}) and

97 the energy difference (ΔE),

$$\begin{aligned}
 M_{\text{bc}} &= \sqrt{E_{\text{beam}}^2 - \vec{p}_B^2}, \\
 \Delta E &= E_B - E_{\text{beam}},
 \end{aligned}
 \tag{3}$$

98 where E_{beam} is the beam energy, and E_B and \vec{p}_B are respectively the reconstructed energy
 99 and momentum of the B meson; all calculated in the CM frame.

100 The presence of a high momentum π^0 causes a nontrivial correlation between M_{bc} and
 101 ΔE due to the shower leakage of final-state photons. To reduce the correlation with ΔE ,
 102 we use a modified version of M_{bc} that is defined in terms of the beam energy and momenta
 103 of final-state particles as

$$M'_{\text{bc}} = \sqrt{E_{\text{beam}}^2 - \left(\vec{p}_{K_S^0} + \frac{\vec{p}_{\pi^0}}{|\vec{p}_{\pi^0}|} \sqrt{(E_{\text{beam}} - E_{K_S^0})^2 - m_{\pi^0}^2} \right)^2},
 \tag{4}$$

104 where all kinematic quantities are again calculated in the CM frame. We retain candidate
 105 events satisfying $5.24 < M'_{\text{bc}} < 5.29$ GeV/ c^2 and $|\Delta E| < 0.30$ GeV.

106 To measure the proper time difference Δt , we determine the signal and tag-side B de-
 107 cay vertices. The signal B vertex is obtained by projecting the flight direction of the K_S^0
 108 candidate back to the interaction region. The K_S^0 flight direction is determined from its
 109 decay vertex and momentum. The intersection of the K_S^0 -flight projection with the inter-
 110 action region provides a good approximation of the signal B decay vertex, since both the
 111 transverse flight length of the B^0 meson and the transverse size of the interaction region
 112 are small compared to the B^0 flight length along the boost direction. The tag-side vertex
 113 is obtained with tracks that are not associated to the $B^0 \rightarrow K_S^0 \pi^0$ decay. We obtain the Δt
 114 value by dividing the longitudinal distance between signal and tag vertices by the speed of
 115 light and the Lorentz boost of the $\Upsilon(4S)$ system in the lab frame. Signal candidates with
 116 poorly measured Δt , mainly due to K_S^0 mesons decaying outside of the VXD acceptance,
 117 are suppressed by requiring the estimated uncertainty on Δt to be below 2.5 ps. This re-
 118 quirement removes about 50% of signal candidates, which contribute negligible information
 119 for the decay-time-dependent analysis.

120 Events from continuum $e^+e^- \rightarrow q\bar{q}$ production are suppressed using a boosted-decision-
 121 tree (BDT) classifier [13] that exploits 39 event-topology variables known to have discrim-
 122 ination between B -meson signal and continuum background. The following variables are
 123 those offering most discrimination between signal and continuum: modified Fox-Wolfram
 124 moments [14], CLEO cones [15], the magnitude of thrust axis for the reconstructed B can-
 125 didate and the cosine of the angle between the thrust axis of signal B and that of rest of
 126 events. The BDT is trained on samples of simulated $e^+e^- \rightarrow q\bar{q}$, $B^0\bar{B}^0$ and B^+B^- events,
 127 each equivalent to an integrated luminosity of 1 ab^{-1} . The BDT output distribution (C_{out}) is
 128 shown in Fig. 1. We applied the $C_{\text{out}} = 0.60$ criterion and reject about 89% of the continuum
 129 background with a 18% relative loss in signal efficiency. We translate it into a new variable,
 130

$$C'_{\text{out}} = \ln \left(\frac{C_{\text{out}} - C_{\text{out,min}}}{C_{\text{out,max}} - C_{\text{out}}} \right),
 \tag{5}$$

131 which is conveniently parametrized with Gaussian functions. Here, $C_{\text{out,min}} = 0.60$ and
 132 $C_{\text{out,max}} = 0.99$.

134 After the final selection and background suppression, the average number of B candidates
 135 per event is 1.009. The multiple candidates arise due to a random combination of final-state

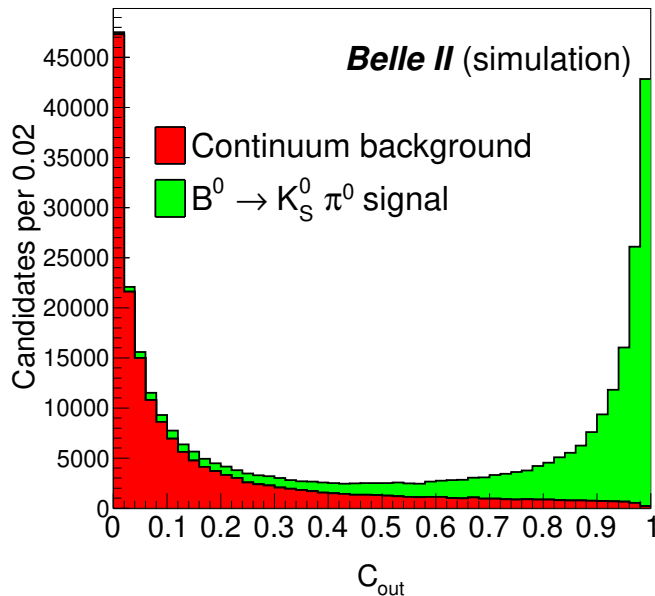


FIG. 1. Distributions of the BDT output C_{out} for simulated signal and $e^+e^- \rightarrow q\bar{q}$ events.

136 particles. To select the best one in an event with multiple candidates, we first compare the
 137 π^0 mass-constrained fit χ^2 probability (‘p-value’). If there are more than one candidates
 138 sharing the same p-value, we choose the one with the best p-value of the fit of the K_S^0
 139 vertex; this is the fit of the decay-chain of the candidate. This selection retains the correct
 140 B candidate in 74% of our simulated events.

141 The signal efficiency (ϵ) of correctly reconstructed events after all the selection is 12.3%.
 142 From simulation we find that signal candidates can be incorrectly reconstructed in 1.5% of
 143 the times by accidentally selecting a particle from the other B meson decay. We consider
 144 those candidates as part of the signal.

145 We determine the flavor of the tag-side B meson (q) from properties of final-state particles
 146 that are not associated with the reconstructed $B^0 \rightarrow K_S^0 \pi^0$ decay. The Belle II flavor tagging
 147 algorithm [16] returns, as the tagging decision, q and the tagging dilution, r , that ranges from
 148 0 (no flavor discrimination) to 1 (unambiguous flavor assignment). Multivariate category-
 149 based flavor-tagger algorithm uses the information of B -decay products to determine the
 150 quark-flavor of B mesons.

151 4. DETERMINATION OF BRANCHING FRACTION AND CP ASYMMETRY

152 We obtain the signal yield and CP asymmetry from a four-dimensional extended
 153 maximum-likelihood fit to the unbinned distributions of M'_{bc} , ΔE , C'_{out} , and Δt . For
 154 the signal component, M'_{bc} is modeled with the sum of a Crystal Ball [17] and a Gaussian
 155 function with a common mean; ΔE with the sum of a Crystal Ball and a double Gaussian
 156 function, all three with a common mean; and C'_{out} with the sum of an asymmetric and a

157 regular Gaussian function. Its Δt probability density function (PDF) is given by

$$158 \quad \mathcal{P}_{\text{sig}}(\Delta t, q) = \frac{e^{-|\Delta t|/\tau_{B^0}}}{4\tau_{B^0}} [\{1 - q\Delta w_r + q\mu_r(1 - 2w_r)\} + \{q(1 - 2w_r) + \mu_r(1 - q\Delta w_r)\}] \quad (6)$$

$$159 \quad \{\mathcal{A}_{CP} \cos(\Delta m_d \Delta t) + \mathcal{S}_{CP} \sin(\Delta m_d \Delta t)\} \otimes \mathcal{R}_{\text{sig}},$$

160 where w_r is the fraction of wrongly tagged events, Δw_r is the difference in w_r between B^0
 161 and \bar{B}^0 , μ_r is the difference in their tagging efficiency corresponds to the fraction of events
 162 to which a flavor tag can be assigned, and \mathcal{R}_{sig} is the Δt resolution function, composed
 163 of the sum of two Gaussians with width ≈ 0.9 ps which is parametrized from simulated
 164 events. We set τ_{B^0} to 1.520 ps, Δm_d to 0.507 ps^{-1} , and \mathcal{S}_{CP} to 0.57 [5]. The data are divided
 165 into seven $q \cdot r$ bins with the tagging parameters for each bin (w_r , Δw_r , and μ_r) fixed to
 166 the respective values obtained in Ref. [16]. The effective tagging efficiency, w_r and μ_r are
 (30.0 \pm 1.2)%, (2–47)% and (0.5–11)%, respectively. All signal PDF shapes are fixed to the
 values determined from a $q \cdot r$ binned fit to simulated signal events.

167 For the continuum background component, an ARGUS function [18] is used for M'_{bc} ,
 168 a linear function for ΔE , and the sum of an asymmetric and a regular Gaussian function
 169 for C'_{out} . Its Δt distribution is modeled with an exponential function convolved with a
 170 Gaussian for the tail; we use a double Gaussian for its resolution function ($\mathcal{R}_{q\bar{q}}$). For the
 171 continuum background component, we float the PDF shape parameters, which are found to
 172 be independent of the $q \cdot r$ bins. For the $B\bar{B}$ background component, a two-dimensional
 173 Kernel estimation PDF [19] is used to model the ΔE vs. M'_{bc} distribution, and the sum
 174 of an asymmetric and a regular Gaussian function is used for C'_{out} . Its Δt distribution is
 175 modeled with an exponential function convolved with a Gaussian for the tail; we again use a
 176 double Gaussian for its resolution function ($\mathcal{R}_{B\bar{B}}$). The $B\bar{B}$ background shape parameters
 177 are fixed from a fit to the corresponding simulated sample.

178 The fit parameters are the signal yield N_{sig} ; \mathcal{A}_{CP} ; $B\bar{B}$ background yield, which is Gaussian
 179 constrained to the result of a fit to the ΔE sideband in data; continuum background yield;
 180 M'_{bc} ARGUS parameter; ΔE slope; and C'_{out} relative width for the $q\bar{q}$ component. We
 181 correct the signal M'_{bc} , ΔE , and C'_{out} PDF shapes for possible data–simulation differences,
 182 according to the values obtained with a control sample of $B^+ \rightarrow \bar{D}^0 (\rightarrow K^+ \pi^- \pi^0) \pi^+$ (charge
 183 conjugated modes are implicitly included hereafter). In order to mimic the signal decay, we
 184 use the similar π^0 selection. We use a maximum-likelihood fit to the unbinned distribution
 185 of M'_{bc} , ΔE , and C'_{out} , using PDF shapes similar to that employed in the fit to signal data.
 186 We use a control sample of $B^0 \rightarrow J/\psi (\rightarrow \mu^+ \mu^-) K_S^0$ decays to validate the time-dependent
 187 analysis. To mimic the signal decay, we do not use the two muons coming from the J/ψ
 188 decay to reconstruct the signal B decay vertex. We use a maximum-likelihood fit to the
 189 unbinned distributions of M_{bc} and Δt , using PDF shapes and resolution functions similar
 190 to those employed in the fit to signal data. The B^0 lifetime and \mathcal{A}_{CP} are measured to be
 191 $1.59^{+0.09}_{-0.08}$ ps and -0.03 ± 0.10 , respectively, which are consistent with their known values [5].
 192 This provides convincing data-driven support to the time-dependent part of the analysis.
 193 The same sample is also used to correct the Δt PDF shape parameters for possible data–
 194 simulation differences. The estimator properties (bias, uncertainties) have been thoroughly
 195 studied in simplified and realistic simulated experiments and found to be as expected.

196 Figure 2 shows the four projections of the fit to the seven $q \cdot r$ -integrated data sample.
 197 For each projection the signal enhancing criteria, defined by $5.27 < M'_{\text{bc}} < 5.29 \text{ GeV}/c^2$,
 198 $-0.15 < \Delta E < 0.10 \text{ GeV}$, $|\Delta t| < 10.0 \text{ ps}$, and $C'_{\text{out}} > 0.0$, are applied on all but for the
 199 variable displayed. The obtained signal yield is 135^{+16}_{-15} , where the quoted uncertainty is

200 statistical only. We also find 2214_{-48}^{+49} continuum and 44 ± 5 $B\bar{B}$ background events. We
 201 determine the branching fraction using the following formula:

$$\mathcal{B}(B^0 \rightarrow K^0 \pi^0) = \frac{N_{\text{sig}}}{2 \times N_{B\bar{B}} \times f^{00} \times \epsilon \times \mathcal{B}_s}, \quad (7)$$

202 where $N_{B\bar{B}} = (197.2 \pm 5.70) \times 10^6$, $f^{00} = 0.487 \pm 0.010$, and $\mathcal{B}_s = 0.5$ are the number of
 203 $B\bar{B}$ pairs, $\Upsilon(4S) \rightarrow B^0 \bar{B}^0$ branching fraction, and $K^0 \rightarrow K_S^0 \rightarrow \pi^+ \pi^-$ branching fraction,
 204 respectively. The $B^0 \rightarrow K^0 \pi^0$ branching fraction and direct CP asymmetry are measured
 205 to be $(11.0 \pm 1.2 \pm 1.0) \times 10^{-6}$ and $0.41_{-0.32}^{+0.30} \pm 0.08$, respectively. The first uncertainties are
 206 statistical and the second are systematic (described in Section 5). This extends the previous
 207 measurement [20] of \mathcal{B} and \mathcal{A}_{CP} in $B^0 \rightarrow K^0 \pi^0$ decays, where no information on the proper
 208 time difference had been used.

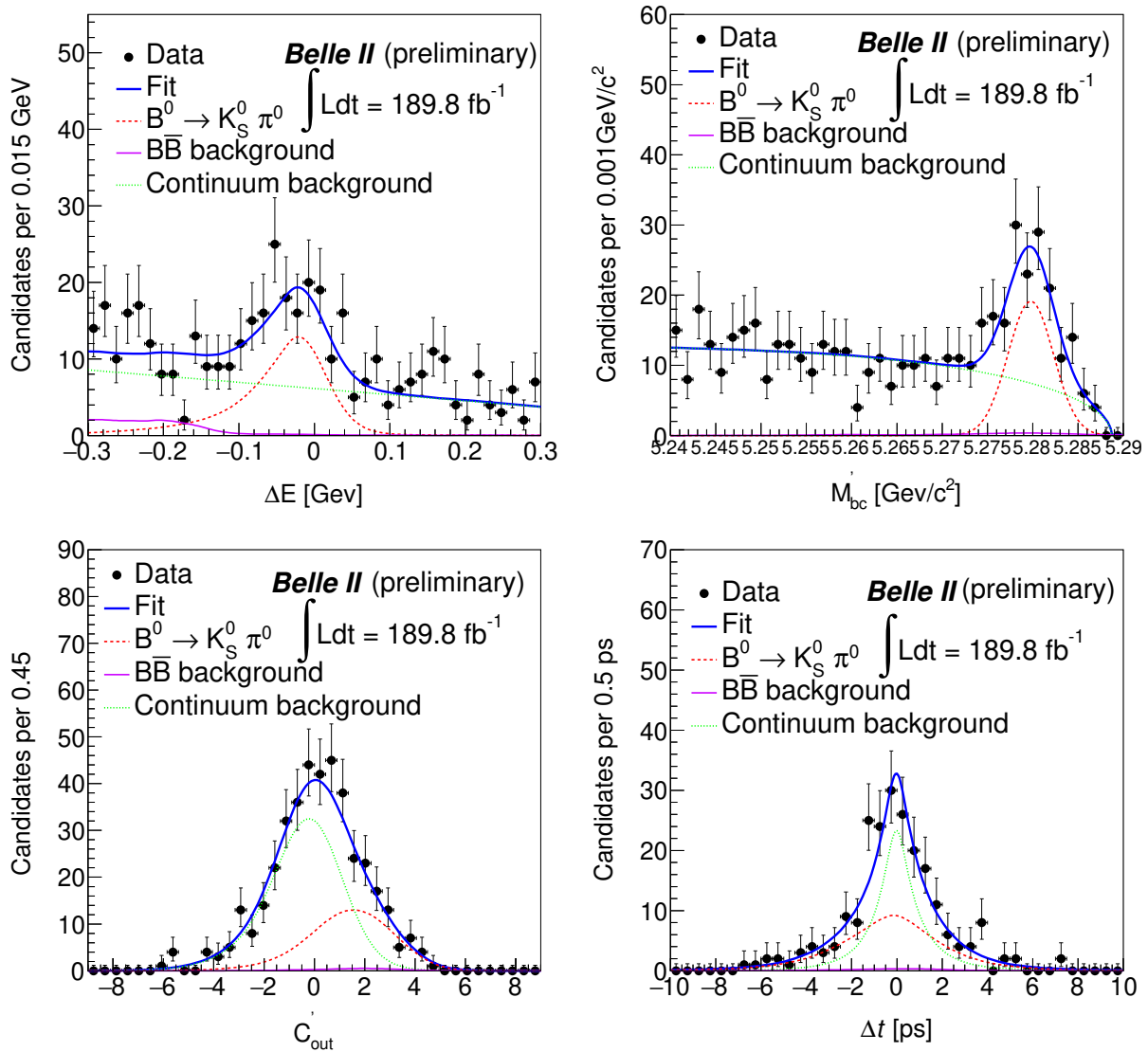


FIG. 2. Signal enhanced fit projections of ΔE (top-left), M'_{bc} (top-right), C'_{out} (bottom-left), and Δt (bottom-right) shown for the sample integrated in the seven $q \cdot r$ bins.

209 **5. SYSTEMATIC UNCERTAINTIES**

210 Various systematic uncertainties contributing to \mathcal{B} and \mathcal{A}_{CP} are listed in Table I. Assum-
 211 ing these sources to be independent, we add their contributions in quadrature to get the
 212 total systematic uncertainty. The systematic uncertainty due to possible differences between
 213 data and simulation in the reconstruction of charged particles is 0.3% per track [21]. We
 214 linearly add this uncertainty corresponding to each of the two pion tracks coming from the
 215 K_s^0 decay in the signal side. From a comparison of the K_s^0 yield in data and simulation,
 216 we find that the ratio of K_s^0 reconstruction efficiency changes approximately linearly as a
 217 function of its flight length [21]. We apply an uncertainty of 0.4% for each centimeter of
 218 the average flight length of K_s^0 candidates resulting in a 4.2% total systematic uncertainty
 219 to \mathcal{B} . We estimate the systematic uncertainty due to possible differences between data and
 220 simulation in the π^0 reconstruction and selection by comparing the inclusive decay sample of
 221 $D^0 \rightarrow K^- \pi^+ \pi^0$ with $D^0 \rightarrow K^- \pi^+$ [22]. The data–simulation efficiency ratio is found to be
 222 close to unity with an uncertainty of 7.5%, which we assign as the systematic uncertainty to
 223 \mathcal{B} . We evaluate possible data–simulation differences in the continuum-suppression efficiency
 224 using the control sample of $B^+ \rightarrow \bar{D}^0 (\rightarrow K^+ \pi^- \pi^0) \pi^+$. As the ratio of efficiencies obtained
 225 in data and simulation is close to unity, the statistical uncertainty on the ratio (1.6%) is
 226 assigned as a systematic uncertainty to \mathcal{B} . We estimate the systematic uncertainty on \mathcal{A}_{CP}
 227 due to wrong tag fraction by varying the parameter individually for each $q \cdot r$ region by its 1σ
 228 uncertainty. The systematic uncertainty due to resolution function is estimated in a similar
 229 fashion. As external inputs τ_{B^0} , Δm_d , and \mathcal{S}_{CP} are fixed to their known values in the fit,
 230 the associated systematic uncertainty is estimated by varying their values by $\pm 1\sigma$. In the
 231 nominal fit, we assume the $B\bar{B}$ -background decays to be CP symmetric. However, there
 232 could be a nontrivial asymmetry arising due to this component. To take such possibility
 233 into account, we use an alternative Δt PDF given by

$$\mathcal{P}_{B\bar{B}}(\Delta t, q) = \frac{e^{-|\Delta t|/\tau_{B^0}}}{4\tau_{B^0}} [1 + q\{\mathcal{A}'_{CP} \cos(\Delta m_d \Delta t) + \mathcal{S}'_{CP} \sin(\Delta m_d \Delta t)\}] \otimes R_{B\bar{B}}. \quad (8)$$

234 We perform two different fits by setting \mathcal{S}'_{CP} to either +1 or -1, and $\mathcal{A}'_{CP} = 0.0$. We
 235 then calculate the deviations in signal \mathcal{A}_{CP} from its nominal value. These deviations are
 236 assigned as a systematic uncertainty to \mathcal{A}_{CP} due to $B\bar{B}$ background asymmetry. An overall
 237 uncertainty of 3.2% on \mathcal{B} is taken as a systematic uncertainty due to the number of $B\bar{B}$ pairs
 238 used, which includes the uncertainty on f^{00} , cross section, integrated luminosity, and possible
 239 shifts from the peak CM energy as a function of time. The uncertainties due to signal PDF
 240 shape parameters are estimated by varying their correction factors by $\pm 1\sigma$, where σ denote
 241 the corresponding statistical uncertainties. Similarly, the uncertainties due to background
 242 PDF shape are calculated by varying all fixed parameters by $\pm 1\sigma$, determined from the fit to
 243 simulated samples. We fix the M'_{bc} ARGUS endpoint to the value obtained from a fit to the
 244 sideband data. Subsequently we vary it by $\pm 1\sigma$ to assign a systematic uncertainty, where σ
 245 is the uncertainty from the fit. Potential fit bias is checked by performing an ensemble test
 246 comprising 1000 simplified simulated experiments in which signal events are drawn from the
 247 corresponding simulation sample and background events are generated according to their
 248 PDF shapes. We calculate the mean shift of signal yield from the input value and assign it
 249 as a systematic uncertainty. The tag-side flavor is determined from flavor-specific final states
 250 but there exist some flavor nonspecific channels. For example, the flavor-specific $\bar{B}^0 \rightarrow D^+ \pi^-$
 251 is a CKM-favoured channel, whose suppressed counterpart $B^0 \rightarrow D^+ \pi^-$ may exist on the tag

side. As a result, there can be CP violation on the tag side. The systematic uncertainty on \mathcal{A}_{CP} arising due to unaccounted for tag-side interference is taken from Ref. [23]. A possible systematic uncertainty related to VXD misalignment is neglected in this study.

TABLE I. List of systematic uncertainties contributing to the branching fraction and direct CP asymmetry.

Source	$\delta\mathcal{B}$ (%)	$\delta\mathcal{A}_{CP}$
Tracking efficiency	0.6	–
K_S^0 reconstruction efficiency	4.2	–
π^0 reconstruction efficiency	7.5	–
Continuum suppression efficiency	1.6	–
Number of $B\bar{B}$ pairs	3.2	–
Flavor tagging	–	0.040
Resolution function	–	0.050
External inputs	0.4	0.021
$B\bar{B}$ background asymmetry	–	0.002
Signal modelling	1.0	0.015
Background modelling	0.9	0.004
Possible fit bias	2.0	0.010
Tag-side interference	–	0.038
Total	9.6	0.086

6. SUMMARY

We report measurements of the branching fraction and direct CP asymmetry in $B^0 \rightarrow K^0\pi^0$ decays using a data sample, corresponding to 189.8fb^{-1} of integrated luminosity, recorded by Belle II at the $\Upsilon(4S)$ resonance. The observed signal yield is 135_{-15}^{+16} . We measure $\mathcal{B}(B^0 \rightarrow K^0\pi^0) = [11.0 \pm 1.2(\text{stat}) \pm 1.0(\text{syst})] \times 10^{-6}$ and $\mathcal{A}_{CP} = -0.41_{-0.32}^{+0.30}(\text{stat}) \pm 0.08(\text{syst})$. This is the first measurement of \mathcal{A}_{CP} in $B^0 \rightarrow K^0\pi^0$ performed at Belle II using a decay-time-dependent analysis. The results agree with previous determinations [5, 20].

7. ACKNOWLEDGEMENT

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