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6 **Measurements of the branching fraction and direct CP -violating**
7 **asymmetry in $B^0 \rightarrow K^0 \pi^0$ decays**

8 (Belle II Collaboration)

9 **Abstract**

10 We report the measurements of branching fraction (\mathcal{B}) and direct CP -violating asymmetry
11 (\mathcal{A}_{CP}) in the charmless decays $B^0 \rightarrow K^0 \pi^0$ at Belle II. A sample of e^+e^- collisions, corresponding
12 to 189.8 fb^{-1} of integrated luminosity, recorded near the $\Upsilon(4S)$ resonance is used for the study. We
13 find 135 signal candidates, and measure $\mathcal{B}(B^0 \rightarrow K^0 \pi^0) = [11.0 \pm 1.2(\text{stat}) \pm 1.0(\text{syst})] \times 10^{-6}$ and
14 $\mathcal{A}_{CP} = -0.41_{-0.32}^{+0.30}(\text{stat}) \pm 0.08(\text{syst})$.

15 **1. INTRODUCTION**

16 Decays mediated by flavour-changing neutral current transitions are suppressed in the
 17 standard model (SM) and provide an indirect route to search for beyond-the-SM physics.
 18 The latter is accomplished via a consistency check between measurements and corresponding
 19 theory predictions since new particles may enter the quantum loop [1]. Within the SM, CP
 20 violation arises due to an irreducible phase in the Cabibbo-Kobayashi-Maskawa (CKM)
 21 matrix [2]. At an e^+e^- flavor-factory experiment such as Belle II, neutral B meson pairs
 22 are coherently produced in the process $e^+e^- \rightarrow \Upsilon(4S) \rightarrow B^0\bar{B}^0$. When one of these B
 23 mesons decays to a CP eigenstate f_{CP} and the other to a flavor-specific final state f_{tag} , the
 24 time-dependent decay rate is given as

$$\mathcal{P}(\Delta t) = \frac{e^{-|\Delta t|/\tau_{B^0}}}{4\tau_{B^0}} [1 + q\{\mathcal{A} \cos(\Delta m_d \Delta t) + \mathcal{S} \sin(\Delta m_d \Delta t)\}], \quad (1)$$

25 where $\Delta t = t_{CP} - t_{\text{tag}}$ is the proper time difference between the decay into f_{CP} and f_{tag} , q
 26 is the flavor of f_{tag} being +1 (−1) for the B^0 (\bar{B}^0) decay to f_{tag} , Δm_d is the B^0 – \bar{B}^0 mixing
 27 frequency, and τ_{B^0} is the B^0 lifetime. The quantity \mathcal{A} is a measure of direct CP violation,
 28 and \mathcal{S} denotes CP violation due to interference between decays with and without B^0 – \bar{B}^0
 29 mixing.

30 The CKM and color suppression of the tree-level $b \rightarrow su\bar{u}$ transition means that the $B^0 \rightarrow$
 31 $K_S^0\pi^0$ decays are dominated by the top-quark mediated $b \rightarrow sd\bar{d}$ loop diagram, which carries
 32 a weak phase $\arg(V_{tb}V_{ts}^*)$; V_{ij} denote the CKM matrix elements. If subleading contributions
 33 are small, $\mathcal{S}_{K_S^0\pi^0}$ is expected to be equal to $\sin 2\phi_1$ and $\mathcal{A}_{K_S^0\pi^0} \approx 0$. Therefore, a precise
 34 measurement of the direct CP asymmetry (\mathcal{A}) and branching fraction (\mathcal{B}) in this decay
 35 channel represents an important consistency test of the SM. Furthermore, $B^0 \rightarrow K_S^0\pi^0$ is a
 36 key component in improving the sensitivity of an isospin sum-rule proposed by Gronau [3].
 37 The sum rule, given by

$$I_{K\pi} = \mathcal{A}_{K^+\pi^-} + \mathcal{A}_{K^0\pi^+} \frac{\mathcal{B}(K^0\pi^+)}{\mathcal{B}(K^+\pi^-)} \frac{\tau_{B^0}}{\tau_{B^+}} - 2\mathcal{A}_{K^+\pi^0} \frac{\mathcal{B}(K^+\pi^0)}{\mathcal{B}(K^+\pi^-)} \frac{\tau_{B^0}}{\tau_{B^+}} - 2\mathcal{A}_{K^0\pi^0} \frac{\mathcal{B}(K^0\pi^0)}{\mathcal{B}(K^+\pi^-)} = 0, \quad (2)$$

38 properly accounts for subleading amplitudes by combining the \mathcal{B} and \mathcal{A} values measured
 39 in B decays to all four $K\pi$ final states: $K^+\pi^-$, $K^0\pi^+$, $K^+\pi^0$, and $K^0\pi^0$. The rule offers a
 40 stringent null test of the SM. The impact of Belle II’s inputs on the $I_{K\pi}$ determination [4]
 41 is evident from Fig. 1 with the dominant uncertainty arising from the $\mathcal{A}_{K^0\pi^0}$ measurement.
 42 Previous measurements of CP violation in $B^0 \rightarrow K^0\pi^0$ decay have been reported by Belle
 43 and BaBar [5–8]. With the data size anticipated at Belle II, we expect to have significantly
 44 smaller uncertainties compared to what Belle and BaBar have achieved for these quantities.

45 In this document, we report the measurements of \mathcal{B} and \mathcal{A}_{CP} in $B^0 \rightarrow K^0\pi^0$ decays
 46 at Belle II conducted using a time-dependent analysis framework. Owing to the limited
 47 statistics, we are unable to simultaneously measure \mathcal{A}_{CP} and \mathcal{S}_{CP} ; instead we fix the latter
 48 to its world-average value [9].

49 **2. THE BELLE II DETECTOR AND DATA SAMPLES**

50 Belle II [10] is a particle spectrometer with almost 4π solid-angle coverage, designed
 51 to reconstruct the final-state particles of e^+e^- collisions produced by the SuperKEKB

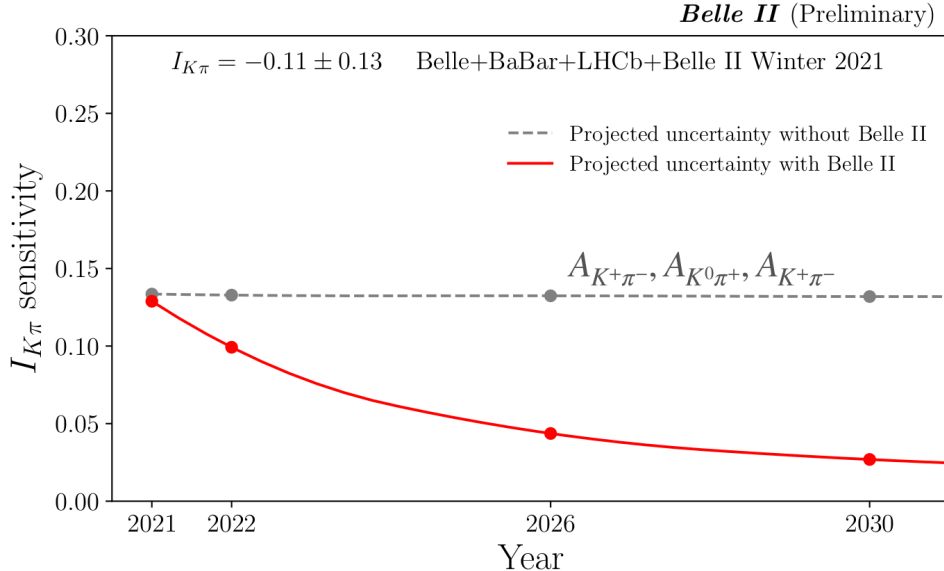


FIG. 1. The projected uncertainty on $I_{K\pi}$ with and without Belle II inputs.

52 asymmetric-energy collider [11], located at the KEK laboratory in Tsukuba, Japan. The
 53 energies of the electron and positron beams are 7 GeV and 4 GeV, respectively. Belle II
 54 comprises several subdetectors surrounding the interaction point in a cylindrical geometry.
 55 The innermost subdetector is the vertex detector (VXD), which uses position-sensitive sil-
 56 icon layers to sample the trajectories of charged particles (tracks) in the vicinity of the
 57 interaction region to extrapolate the decay positions of their long-lived parent particles.
 58 The VXD includes two inner layers of DEPFET-based pixel sensors and four outer layers
 59 of double-sided silicon microstrip sensors. The second pixel layer is currently incomplete
 60 covering only one sixth of the azimuthal angle. Charged-particle momenta and charges are
 61 measured by a large-radius, helium-ethane, small-cell central drift chamber (CDC), which
 62 also offers charged-particle-identification information via a measurement of specific ioniza-
 63 tion. A Cherenkov-light angle and time-of-propagation (TOP) detector surrounding the
 64 CDC provides charged-particle identification in the central detector volume, supplemented
 65 by proximity-focusing, aerogel, ring-imaging Cherenkov (ARICH) detectors in the forward
 66 region with respect to the electron beam. A CsI(Tl)-crystal electromagnetic calorimeter
 67 (ECL) provides electron-energy measurements and photon reconstruction. A solenoid sur-
 68 rounding the calorimeter generates a uniform axial 1.5 T magnetic field filling its inner
 69 volume. Layers of plastic scintillators and resistive-plate chambers, interspersed between
 70 the magnetic flux-return iron plates, allow for the identification of K_L^0 and muons. The
 71 subdetectors most relevant for this study are the VXD, CDC, and ECL.

72 The data sample used in the study consists of all good-quality runs collected at a center-
 73 of-mass (CM) energy at the $\Upsilon(4S)$ resonance, corresponding to an integrated luminosity of
 74 189.8 fb^{-1} . We use Monte Carlo (MC) simulated data to optimize the event selection and
 75 study possible background contributions. We use signal-only simulated data to determine
 76 the signal models and estimate the selection efficiency. The so-called generic MC sample
 77 consists of simulated events that include $q\bar{q}$ ($q = u, d, s, c$), $B^0\bar{B}^0$ and B^+B^- events in
 78 realistic proportions, corresponding to more than 10 times that of the $\Upsilon(4S)$ data. The
 79 latter sample is used to study background and make comparisons with the data. The

80 B -meson decays are simulated with the EvtGen generator [12] and the effect of final-state
 81 electromagnetic radiation is simulated by the Photos package [13]. The simulation of the
 82 continuum $e^+e^- \rightarrow q\bar{q}$ background process is carried out with the KKMC generator [14]
 83 interfaced to Pythia [15]. The interactions of particles with the detector are simulated using
 84 Geant4 [16].

85 3. RECONSTRUCTION AND SELECTION

86 Charged particle tracks are reconstructed with the SVD and CDC. Photons are identified
 87 as isolated ECL clusters that are not matched to any charged particle track. The K_S^0
 88 candidates are reconstructed from pairs of oppositely charged tracks having invariant mass
 89 between 482 and 513 MeV/ c^2 . We reconstruct π^0 candidates from pairs of photons that have
 90 energies larger than the thresholds of 80 and 223 MeV for final-state photons detected in
 91 the barrel and endcap, respectively, of the ECL. The selection also requires π^0 mass to lie
 92 between 119 and 150 MeV/ c^2 and the absolute cosine of the π^0 helicity angle to be less than
 93 0.953. These criteria suppress contributions from misreconstructed π^0 candidates.

94 The B -meson candidate is reconstructed by combining a K_S^0 with a π^0 candidate. For
 95 this purpose, we use two kinematic variables: the beam-energy-constrained mass (M_{bc}) and
 96 the energy difference (ΔE), defined as

$$M_{bc} = \sqrt{E_{\text{beam}}^2 - \vec{p}_B^2}, \quad (3)$$

$$\Delta E = E_B - E_{\text{beam}},$$

97 where E_{beam} is the beam energy, E_B and \vec{p}_B are respectively the reconstructed energy and
 98 momentum of the B meson; all calculated in the CM frame. We retain candidate events
 99 satisfying $|\Delta E| < 0.3$ GeV and $5.24 < M_{bc} < 5.29$ GeV/ c^2 .

100 The presence of a high momentum π^0 causes a nontrivial correlation between ΔE and
 101 M_{bc} owing to the shower leakage of final-state photons. To minimize the impact of such
 102 correlation, we introduce a modified M'_{bc} , calculated from the beam energy and momenta of
 103 final-state particles as:

$$M'_{bc} = \sqrt{E_{\text{beam}}^2 - \left(\vec{p}_{K_S^0} + \frac{\vec{p}_{\pi^0}}{|\vec{p}_{\pi^0}|} \sqrt{(E_{\text{beam}} - E_{K_S^0})^2 - m_{\pi^0}^2} \right)^2}, \quad (4)$$

104 where all kinematic quantities are calculated in the CM frame. We find that the linear
 105 correlation coefficient has been reduced for all event categories with the introduction of the
 106 modified M'_{bc} , which we will refer to as just M_{bc} henceforth in this document. As shown in
 107 Eq. (1), one of the most important parameters to estimate the decay rate is Δt . It is found
 108 that the error on it (Δt_{err}) has a significant tail (Fig. 2), caused by the events with poor
 109 decay time resolution. We apply a selection $\Delta t_{\text{err}} < 2.5$ ps to suppress such events.

111 The most dominant source of background is from $e^+e^- \rightarrow q\bar{q}$ ($q = u, d, s, c$) continuum
 112 process. These events result in final-state particles collimated into two back-to-back jets,
 113 whereas those from $e^+e^- \rightarrow \Upsilon(4S) \rightarrow B\bar{B}$ are uniformly distributed over the 4π solid angle.
 114 We exploit this difference in event topology to suppress the continuum background. We
 115 combine a set of 39 variables, known to provide discrimination between B -meson signal
 116 and continuum background, using a boosted decision tree (BDT) [17] classifier. We use
 117 $e^+e^- \rightarrow q\bar{q}$, $B^0\bar{B}^0$ and B^+B^- MC events, each equivalent to an integrated luminosity of

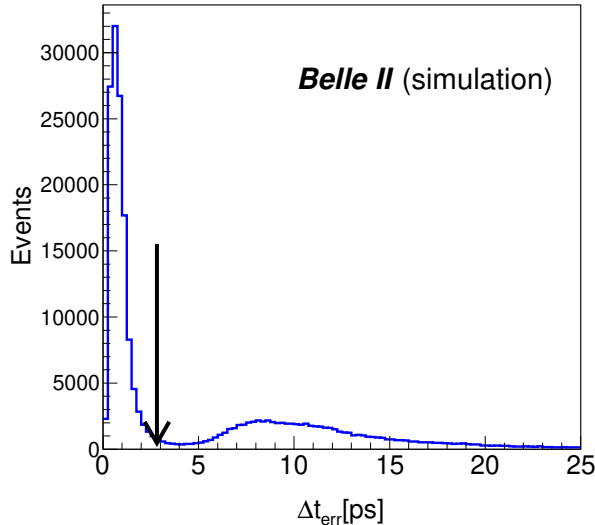


FIG. 2. Distribution of Δt_{err} .

118 1 ab^{-1} , for this purpose. The BDT output clearly discriminate the signal from background
 119 events. As it is difficult to model the BDT output distribution (C_{out}) analytically, we
 120 translate it into a new variable:

$$C'_{\text{out}} = \ln \left(\frac{C_{\text{out}} - C_{\text{out,min}}}{C_{\text{out,max}} - C_{\text{out}}} \right), \quad (5)$$

121 which can be parametrized by one or more Gaussian functions. Here, $C_{\text{out,min}} = 0.6$ and
 122 $C_{\text{out,max}} \simeq 1$. With the $C_{\text{out,min}}$ criterion, we reject about 89% of the continuum background
 123 at a 18% relative loss in signal efficiency.

124 After the final selection and background suppression, we find that the number of B
 125 candidates per event is 1.009. The multiple candidates mostly arises due to a random
 126 combination of final-state particles. In order to find the best candidate in events with
 127 multiple candidates, we first compare the π^0 mass-constrained fit χ^2 probability (p-value).
 128 The K_s^0 vertex fit p-value is served as the second indicator of the validity of the candidate.
 129 The candidate with the larger p-value is retained as the best candidate in an event. This
 130 method retains the correct B candidate out of the events with more than one B candidates
 131 74% of the times. The efficiency of correctly reconstructed signal events after all the selection
 132 is found to be 12.3% and the fraction of self cross-feed (SCF) events are 1.5%. As the SCF
 133 fraction is small, we consider both correctly reconstructed and SCF events as part of the
 134 signal.

135 The vertex position for the $B^0 \rightarrow K_s^0 \pi^0$ decay is reconstructed using charged pions from
 136 the K_s^0 decay and an IP constraint. The tag side vertex is obtained with well-reconstructed
 137 tracks that are not assigned to the $B^0 \rightarrow K_s^0 \pi^0$ decay. The flavour of the tag side B meson
 138 is determined from properties of particles that are not associated with the reconstructed
 139 $B^0 \rightarrow K_s^0 \pi^0$ decays. We use the standard Belle II flavour tagging algorithm [18] that gives
 140 two parameters, the b -flavor charge, q and its quality factor, r . We get $q = +1$ (-1) when the
 141 tagged B meson is a B^0 (\bar{B}^0). The parameter r is an event-by-event, MC determined flavour-
 142 tagging dilution factor that ranges from 0 (no flavour discrimination) to 1 (unambiguous
 143 flavour assignment). Each event is divided into seven r regions. We also employ the r -bin

144 dependent wrong tag fraction (w_r), the difference in wrong tag fraction between B^0 and \bar{B}^0
 145 (Δw_r), tagging efficiency (ϵ_r), and tagging efficiency difference (μ_r) that are necessary to
 146 extract CP parameters in data.

147 4. SIGNAL EXTRACTION

148 The signal yields are obtained from a four-dimensional (4D) unbinned extended maximum-
 149 likelihood fit to ΔE , M_{bc} , C'_{out} , and Δt . For the signal component, ΔE is modeled with
 150 a sum of a Crystal Ball (CB) [19] and a double Gaussian function with common mean,
 151 M_{bc} with a sum of CB and a Gaussian function, and C'_{out} with a sum of bifurcated and
 152 a Gaussian functions. The Δt PDF is given by Eq. (6), where \mathcal{R}_{sig} is the proper time
 153 resolution function composed of a sum of double Gaussian functions, which takes the finite
 154 vertex resolution into account.

$$P_{sig}(\Delta t, q) = \frac{e^{-|\Delta t|/\tau_{B^0}}}{4\tau_{B^0}} \{ [1 - q\Delta w_r + q\mu_r(1 - 2w_r)] + [q(1 - 2w_r) + \mu_r(1 - q\Delta w_r)] \} \quad (6)$$

$$(\mathcal{A}_{CP} \cos(\Delta m_d \Delta t) + \mathcal{S}_{CP} \sin(\Delta m_d \Delta t)) \otimes \mathcal{R}_{sig},$$

155 where, w_r =wrong tag fraction, Δw_r =wrong tag fraction difference, μ_r = tag efficiency dif-
 156 ference, $\tau_{B^0} = 1.520$ ps and $\Delta m_d = 0.507$ ps $^{-1}$. For the continuum background component,
 157 a linear function is used to model ΔE , an ARGUS function [20] is used for M_{bc} , and a sum
 158 of asymmetric and symmetric Gaussian functions is used to model C'_{out} . The continuum
 159 Δt distribution is modeled with an exponential function convolved with a Gaussian for the
 160 outlier; for resolution function ($\mathcal{R}_{q\bar{q}}$) we use sum of double Gaussian. For the $B\bar{B}$ back-
 161 ground component, a two-dimensional Kernel estimation PDF [21] is used to model both
 162 ΔE and M_{bc} distributions, and a sum of bifurcated and a Gaussian functions is used to
 163 model C'_{out} . The Δt distribution for the $B\bar{B}$ component is modeled with an exponential
 164 function convolved with a Gaussian for outlier; for resolution function ($\mathcal{R}_{B\bar{B}}$) we use sum
 165 of double Gaussian. The signal PDF shapes are fixed to the values determined from a $q \cdot r$
 166 binned signal MC fit. The $B\bar{B}$ background shape are fixed from the overall MC fit. For
 167 the continuum background component we float the PDF shape parameters over the $q \cdot r$
 168 bin. The free parameters in the final fit are the signal yield, \mathcal{A}_{CP} , (Gaussian-constrained)
 169 BB background yield, continuum background yield, ΔE slope, Argus parameter and C'_{out}
 170 relative width for the $q\bar{q}$ component. The \mathcal{S}_{CP} value fixed to the world average value. We
 171 correct the ΔE , M_{bc} and C'_{out} PDF shapes for possible data-MC differences, according to
 172 the values obtained with a high-statistic control sample of $B^+ \rightarrow \bar{D}^0 (\rightarrow K^+ \pi^- \pi^0) \pi^+$.

173 We use a high-statistic control sample $B^0 \rightarrow J/\psi K_S^0$ to validate our time-dependent
 174 analysis framework. To mimic the signal decay, we do not vertex the two charged leptons
 175 coming from the J/ψ decay. The obtained values of the B^0 lifetime, \mathcal{A}_{CP} and \mathcal{S}_{CP} are found
 176 to be consistent with the PDG values. The same control sample is also used to correct the
 177 Δt PDF shape parameters for possible data-MC differences.

178 Figure 3 shows the signal-enhanced projections for the $q \cdot r$ -integrated 4D fit. The obtained
 179 signal yield is 135^{+16}_{-15} , where the quoted uncertainty is statistical only. We also obtain
 180 2214^{+49}_{-48} events for $q\bar{q}$ and 44 ± 5 events for BB backgrounds. The obtained $B^0 \rightarrow K^0 \pi^0$
 181 branching fraction is $(11.0 \pm 1.2 \pm 1.0) \times 10^{-6}$, where the first uncertainty is statistical and
 182 the second is systematic (described below). The measured direct CP -violating asymmetry
 183 is $\mathcal{A}_{CP} = -0.41^{+0.30}_{-0.32}(\text{stat}) \pm 0.08(\text{syst})$. This is an improved measurement of \mathcal{B} and \mathcal{A}_{CP} in

184 $B^0 \rightarrow K^0 \pi^0$ decays compared to the previous Belle II result [22] where a time-integrated
 185 study was performed to extract the \mathcal{A}_{CP} value.

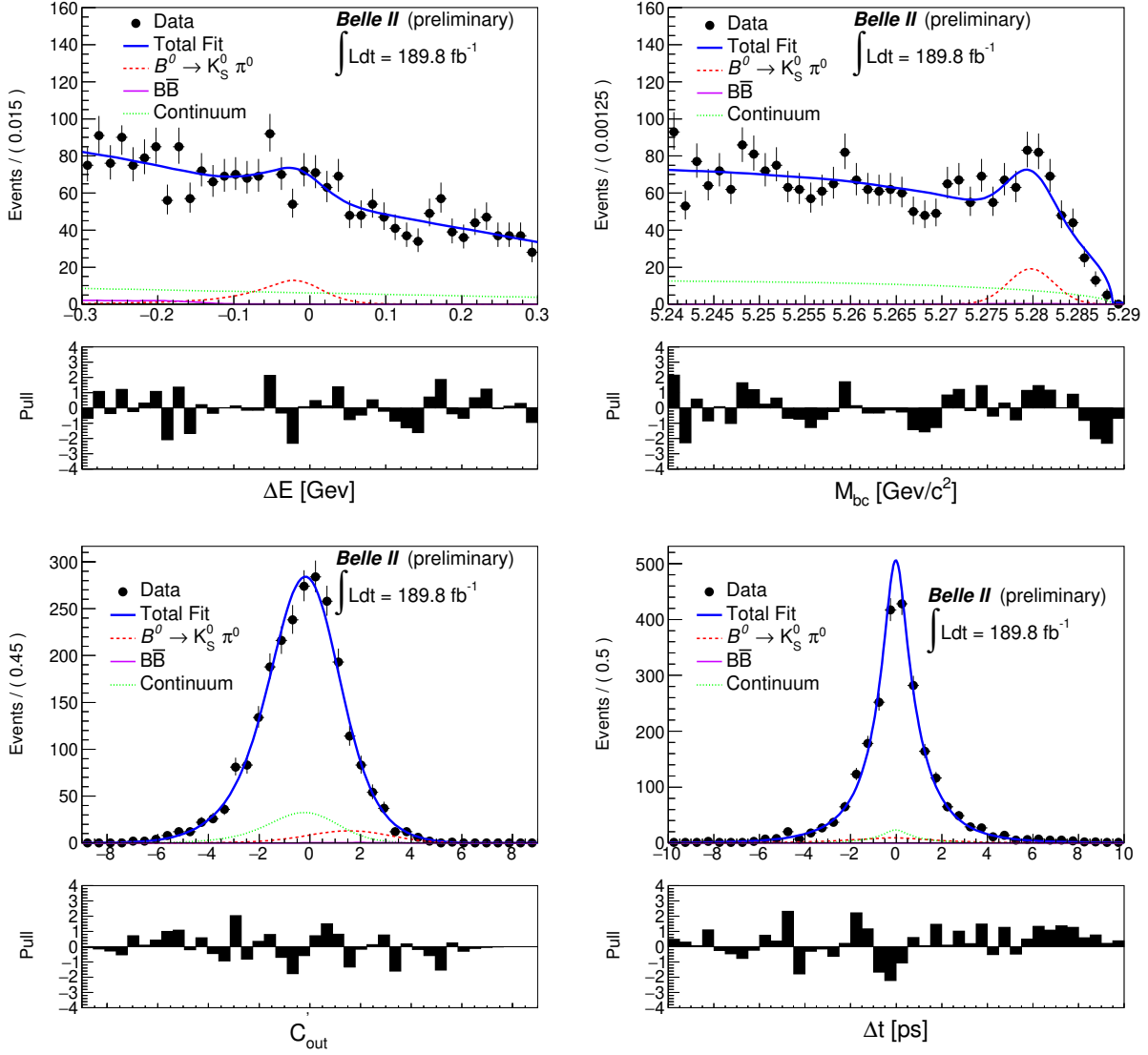


FIG. 3. Signal enhanced 4D fit projections for $q \cdot r$ integrated sample.

186 5. SYSTEMATIC UNCERTAINTIES

187 We consider systematic uncertainties arising from several potential sources. Summary of
 188 systematic uncertainties contributing to the branching fraction and CP asymmetry param-
 189 eters are reported in Table I and II, respectively. We assume the sources to be independent
 190 and add them in quadrature to get the total systematic uncertainty.

191 **5.1. Systematic uncertainties for the branching fraction**

192 **• Tracking efficiency**

193 The systematic uncertainty associated with possible data-MC discrepancies in the
 194 reconstruction of charged particles is 0.30% for per track[23]. We linearly add an
 195 uncertainty corresponding to each of the two pion tracks originating from the K_s^0
 196 decay in the signal side.

197 **• K_s^0 reconstruction efficiency**

198 From a data-MC comparison we observe that the ratio of K_s^0 reconstruction efficiency
 199 changes approximately linearly as a function of the flight distance [23]. We apply an
 200 uncertainty of 0.40% for each centimeter of average flight length of the K_s^0 candidate
 201 resulting in a 4.2% total systematic uncertainty.

202 **• π^0 reconstruction efficiency**

203 We estimate the systematic uncertainty due to possible data-MC discrepancies in the
 204 π^0 reconstruction and selection using inclusive decay samples of $D^0 \rightarrow K^- \pi^+ \pi^0$ and
 205 $D^0 \rightarrow K^- \pi^+$. The data-MC efficiency ratio is found to be close to unity with an
 206 uncertainty of 7.5%, which we allocate as the systematic uncertainty.

207 **• Continuum suppression efficiency**

208 We evaluate possible data-simulation discrepancies in the continuum-suppression dis-
 209 tributions using the control channel $B^+ \rightarrow \bar{D}^0(\rightarrow K^+ \pi \pi^0) \pi^+$. Since the ratio of
 210 selection efficiency obtained in data and MC is close to 1, the statistical uncertainty
 211 (1.6%) on the efficiency ratio is assigned as the systematic uncertainty.

212 **• $B\bar{B}$ pair counting**

213 An overall uncertainty of 3.2% is taken as a systematic uncertainty on the number of
 214 $B\bar{B}$ used [24], which includes the uncertainty on f^{00} , cross section, integrated lumi-
 215 nosity, and potential shifts from the peak CM energy during the run periods.

216 **• Signal and background modeling**

217 The uncertainties due to signal PDF shape are estimated by varying the correction
 218 factors by $\pm 1\sigma$ of their statistical uncertainty. Similarly, the uncertainties due to back-
 219 ground PDF shape are calculated by varying all fixed parameters by $\pm 1\sigma$, determined
 220 from MC component fit.

221 **• Possible fit bias**

222 A potential fit bias is checked by performing an ensemble test comprising 1000 pseu-
 223 doexperiments in which signal events are drawn from the corresponding MC sample
 224 and background events are generated according to their PDF shapes. We calculate the
 225 mean shift of signal yield from the input value and assign it as a systematic uncertainty.

226 **• Physics parameters** Physics parameters τ_{B^0} , Δm_d and \mathcal{S}_{CP} are fixed to the world
 227 average in CP fit. Therefore, the systematic uncertainty is estimated by varying their
 228 error by $\pm 1\sigma$.

TABLE I. List of systematic uncertainties contributing to the measured branching fraction.

Source	$\delta\mathcal{B}(\%)$
Tracking efficiency	0.6
K_S^0 reconstruction efficiency	4.2
π^0 reconstruction efficiency	7.0
Continuum suppression efficiency	1.6
Number of $B\bar{B}$ events	3.2
Signal model	1.0
Continuum background model	0.9
Possible fit bias	2.0
Physics parameters	0.4
Total	9.3

5.2. Systematic uncertainties on the \mathcal{A}_{CP}

• Flavor tagging

Systematic error due to uncertainties in the wrong tag fractions is estimated by varying the parameters individually for each r region within its statistical and systematical variations.

• Resolution function

Systematic error due to uncertainties in the resolution function is estimated by varying each resolution parameter obtained from data by $\pm 1\sigma$ considering both of statistical and systematical variations.

- **Physics parameters** Physics parameters τ_{B^0} , Δm_d and \mathcal{S}_{CP} are fixed to the world average in CP fit. Therefore, the systematic uncertainty is estimated by varying their error by $\pm 1\sigma$.

• B decay background asymmetry

In the nominal fit, we assume the charmless B decay background to be CP symmetric. However, there could be a nontrivial asymmetry arising due to this component. To take such possibility into account, we use an alternative Δt PDF given by

$$P_{B\bar{B}}(\Delta t, q) = \frac{e^{-|\Delta t|/\tau_{B^0}}}{4\tau_{B^0}} [1 + q\{\mathcal{A}_{CP} \cos(\Delta m_d \Delta t) + \mathcal{S}_{CP} \sin(\Delta m_d \Delta t)\}] \otimes R_{B\bar{B}}, \quad (7)$$

instead of RooDecayPDF. We perform two different fits by setting \mathcal{S}_{CP} to either +1 or -1 and $\mathcal{A}_{CP} = 0.0$. We then calculate the deviations in \mathcal{A}_{CP} and \mathcal{S}_{CP} values from the nominal fit. These deviations are assigned as a systematic uncertainty due to B decay background asymmetry. We estimate this systematic in $B^0 \rightarrow J/\psi K_S^0$ data itself.

• Possible fit bias

A potential fit bias is checked by performing an ensemble test comprising 1000 pseudoexperiments in which signal events are drawn from the corresponding MC sample

252 and background events are generated according to their PDF shapes. We calculate
 253 the mean shift of \mathcal{A}_{CP} and \mathcal{S}_{CP} from the input value and assign it as a systematic
 254 uncertainty.

255 • **Tag-side interference**

256 Systematic uncertainties arising due to the tag-side interference is taken from Ref. [25].

257 • **Signal and background modeling**

258 The uncertainties due to signal and background PDF shape are estimated in a manner
 259 similar to the branching fraction case.

260 • **Vertex reconstruction (including VXD misalignment)**

261 The systematic uncertainty is taken from Ref. [26].

TABLE II. List of systematic uncertainties contributing to \mathcal{A}_{CP} .

Source	$\delta\mathcal{A}_{CP}$
Flavor tagging	0.040
Resolution function	0.050
Physics parameter	0.021
B decay background asymmetry	0.002
Possible fit bias	0.010
Tag-side interference	0.008
Background modeling	0.004
Signal modeling	0.015
Vertex reconstruction	0.033
Total	0.076

262 **6. RESULT AND SUMMARY**

263 We report measurements of the branching fraction and direct CP asymmetry (\mathcal{A}_{CP})
 264 based on 189.8 fb^{-1} data sample collected at the $\Upsilon(4S)$ resonance by the Belle II detector.
 265 The observed signal yield is 135_{-15}^{+16} . We measure $\mathcal{A}_{CP} = -0.41_{-0.32}^{+0.30}(\text{stat}) \pm 0.08(\text{syst})$ and
 266 $\mathcal{B}(B^0 \rightarrow K^0\pi^0) = [11.0 \pm 1.2(\text{stat}) \pm 1.0(\text{syst})] \times 10^{-6}$. This is the first measurement of
 267 \mathcal{A}_{CP} in $B^0 \rightarrow K^0\pi^0$ decays reported by Belle II with a time-dependent CP violation analysis
 268 framework. The results agree with previous determinations and show a detector performance
 269 comparable with the best Belle results.

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