

Results and Prospects of Radiative and Electroweak Penguin Decays at Belle II

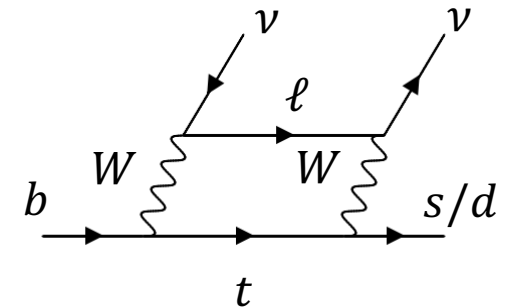
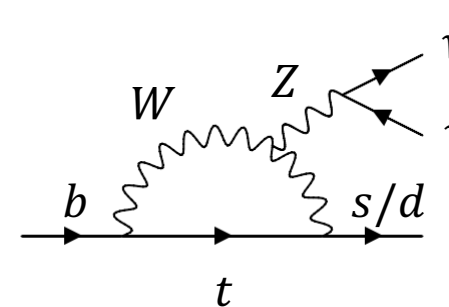
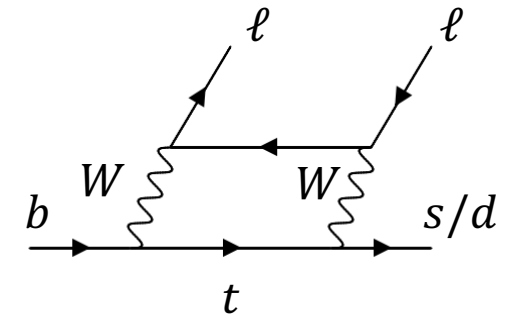
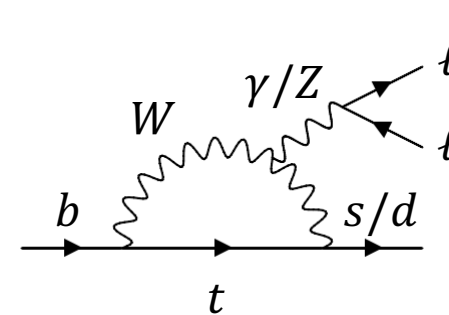
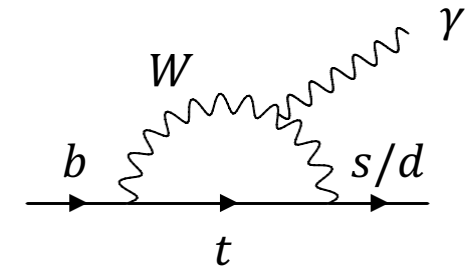
Yo Sato on behalf of Belle II collaboration

Tohoku University

ICHEP 2020, July 30th

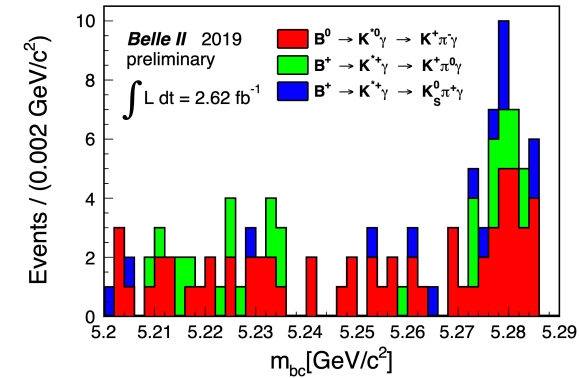
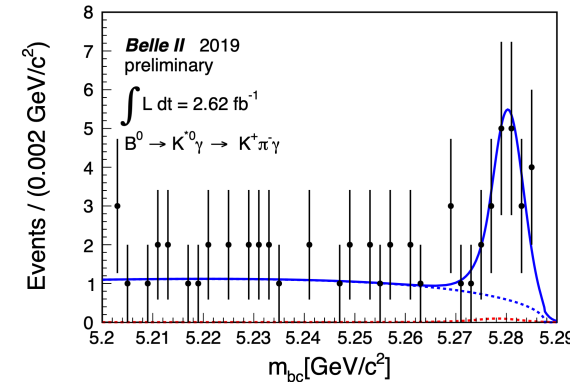


- Flavour-changing neutral current (FCNC) $b \rightarrow s$ and $b \rightarrow d$ processes continue to be a great probe for new physics beyond the standard model.
- Radiative and electroweak (EW) penguin decays are theoretically and experimentally clean because the final states include color single particle(s), γ , $\ell^+ \ell^-$, $\nu \bar{\nu}$.
- The anomalies in $B \rightarrow K^{(*)} \ell^+ \ell^-$ decays motivate further studies on this field.
[LHCb : [1](#), [2](#), [3](#)] [Belle : [4](#)]



Belle II program on the channels includes

- Time dependent CP violation in radiative decays.
 - New physics can induce much larger decay rate of $b_L \rightarrow s_R \gamma_R$ which introduce large mixed-induced CP violation.
 - Rediscovery of $B \rightarrow K^* \gamma$ at Belle II. Update with new dataset is in progress.
- Measurements on inclusive $B \rightarrow X_s \ell^+ \ell^-$ decays to shed further light on the anomalies of exclusive $B \rightarrow K^{(*)} \ell^+ \ell^-$.
- Discovery of the channels involving neutrino like $B \rightarrow K^{(*)} \nu \bar{\nu}$.



BELLE2-NOTE-PL-2019-021

Observables	Belle	Belle II	
	(2017)	5 ab ⁻¹	50 ab ⁻¹
$\mathcal{B}(B \rightarrow K^{*+} \nu \bar{\nu})$	$< 40 \times 10^{-6}$	25%	9%
$\mathcal{B}(B \rightarrow K^+ \nu \bar{\nu})$	$< 19 \times 10^{-6}$	30%	11%
$A_{CP}(B \rightarrow X_{s+d} \gamma) [10^{-2}]$	$2.2 \pm 4.0 \pm 0.8$	1.5	0.5
$S(B \rightarrow K_S^0 \pi^0 \gamma)$	$-0.10 \pm 0.31 \pm 0.07$	0.11	0.035
$S(B \rightarrow \rho \gamma)$	$-0.83 \pm 0.65 \pm 0.18$	0.23	0.07
$A_{FB}(B \rightarrow X_s \ell^+ \ell^-) (1 < q^2 < 3.5 \text{ GeV}^2/c^4)$	26%	10%	3%
$Br(B \rightarrow K^+ \mu^+ \mu^-) / Br(B \rightarrow K^+ e^+ e^-)$	28%	11%	4%
$Br(B \rightarrow K^{*+} (892) \mu^+ \mu^-) / Br(B \rightarrow K^{*+} (892) e^+ e^-) (1 < q^2 < 6 \text{ GeV}^2/c^4)$	24%	9%	3%
$\mathcal{B}(B_s \rightarrow \gamma \gamma)$	$< 8.7 \times 10^{-6}$	23%	—
$\mathcal{B}(B_s \rightarrow \tau \tau) [10^{-3}]$	—	< 0.8	—

The Belle II Physics Book, PTEP 2019 (2019) 12 hereinafter referred to as B2TiP

In the SM,

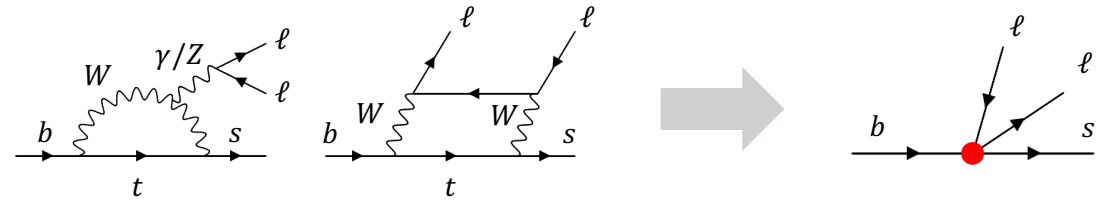
- $b \rightarrow s \ell^+ \ell^-$: C_7 , C_9 , and C_{10} .
- $C_7 \sim -0.3$, $C_9 \sim 4$, $C_{10} \sim -4$.
- Lepton Flavor Universality (LFU), $C_e = C_\mu$.

$$\mathcal{H}_{\text{eff}} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \sum_i C_i \mathcal{O}_i$$

$$\mathcal{O}_7 = \frac{e}{16\pi^2} m_b (\bar{s} \sigma_{\mu\nu} P_R b) F^{\mu\nu},$$

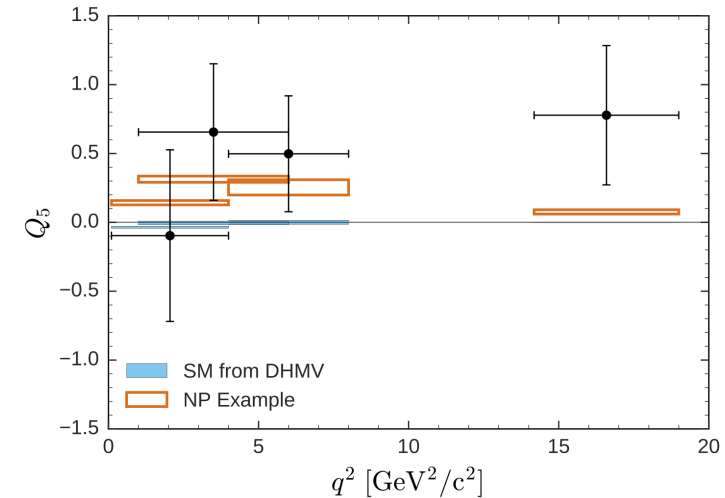
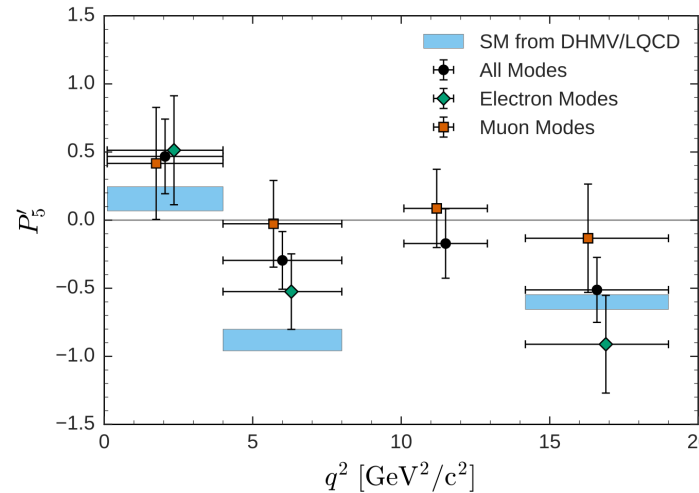
$$\mathcal{O}_{9\ell} = \frac{e^2}{16\pi^2} (\bar{s} \gamma_\mu P_L b) (\bar{\ell} \gamma^\mu \ell),$$

$$\mathcal{O}_{10\ell} = \frac{e^2}{16\pi^2} (\bar{s} \gamma_\mu P_L b) (\bar{\ell} \gamma^\mu \gamma_5 \ell),$$



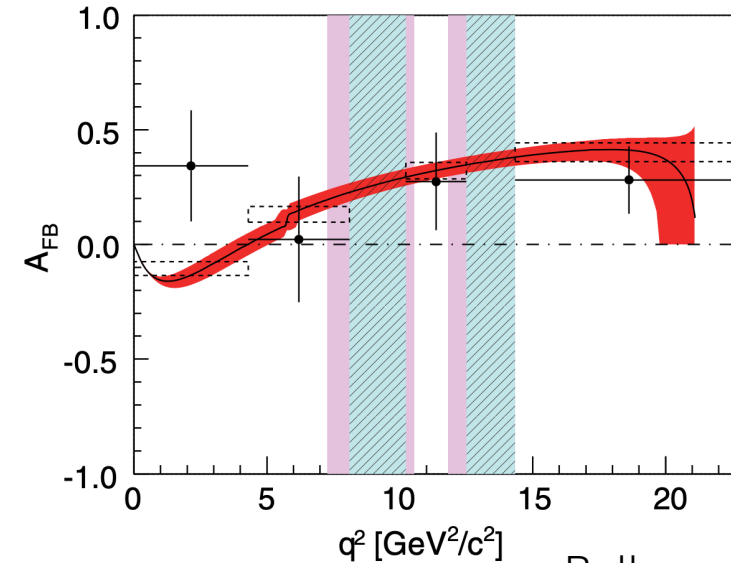
Anomalies in exclusive $B \rightarrow K^{(*)} \ell^+ \ell^-$ imply smaller C_9 , especially for $C_{9\mu}$.

- Angular observable P'_5 in $B \rightarrow K^* \ell^+ \ell^-$.
 - $Q_5 = P_5'^\mu - P_5'^e$.
- LFU violation, R_K, R_{K^*} .



Belle : PRL 118 (2017) 111801

- Hadronic uncertainties are under better control than exclusive $b \rightarrow s \ell^+ \ell^-$.
- Sum-of-exclusive method : Reconstruct as many final states as possible.
- Experimentally challenging due to large backgrounds.
 - All observables are highly statistics limited.

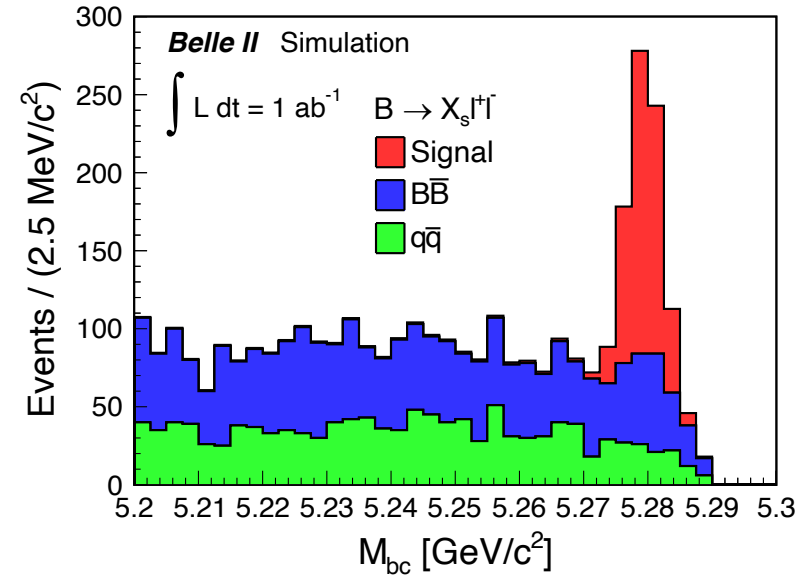


Belle :
Phys. Rev. D 93, 032008

Belle II is the unique experiment to perform an analysis of $B \rightarrow X_s \ell^+ \ell^-$ with large statistics.

▣ Sum-of-exclusive method

- X_s is reconstructed from
 - $Kn\pi$ ($n \leq 4$) and $3K$.
 - at most one K_S^0, π^0 .
 - $M_{X_s} < 2.0 \text{ GeV}/c^2$.
- Background
 - Dominated by $B(\rightarrow X\ell\nu)\bar{B}(\rightarrow X\ell\nu)$.
 - Mis-identified $B \rightarrow Km\pi$ has to be understood.
- Sensitivity of BF and A_{FB} is a few % level in 50 ab^{-1} .

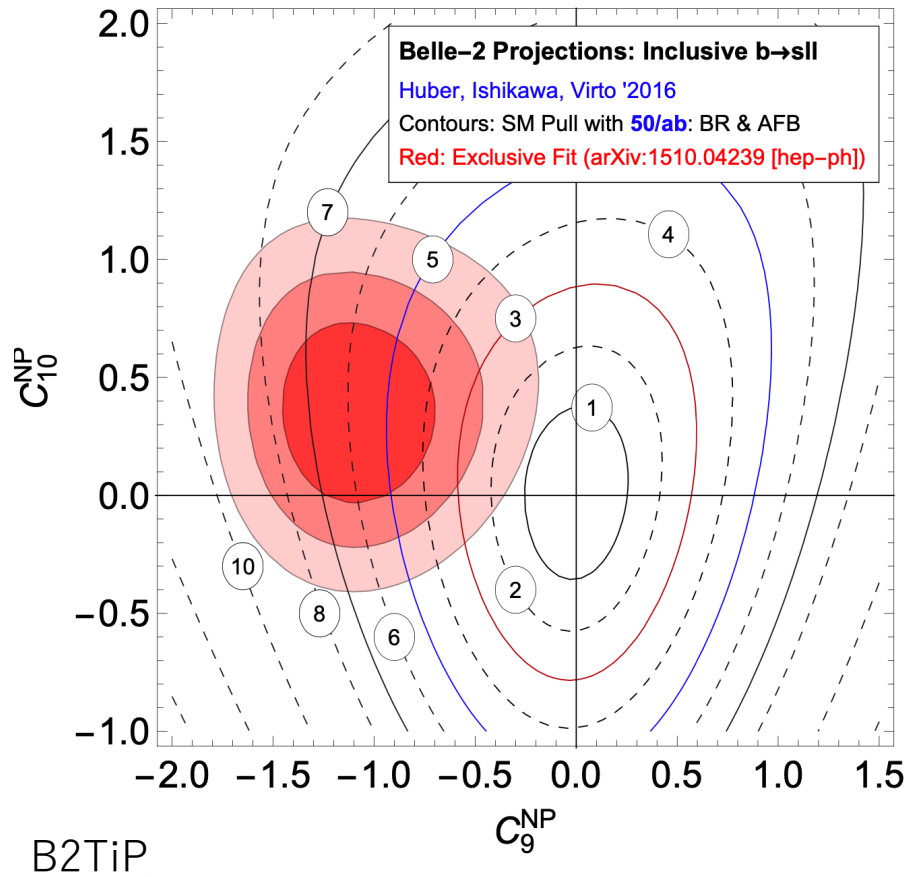


BELLE2-NOTE-PL-2020-007

Observables	Belle 0.71 ab^{-1}	Belle II 5 ab^{-1}	Belle II 50 ab^{-1}
$\text{Br}(B \rightarrow X_s \ell^+ \ell^-)$ ($[1.0, 3.5] \text{ GeV}^2$)	29%	13%	6.6%
$\text{Br}(B \rightarrow X_s \ell^+ \ell^-)$ ($[3.5, 6.0] \text{ GeV}^2$)	24%	11%	6.4%
$\text{Br}(B \rightarrow X_s \ell^+ \ell^-)$ ($> 14.4 \text{ GeV}^2$)	23%	10%	4.7%
$A_{FB}(B \rightarrow X_s \ell^+ \ell^-)$ ($[1.0, 3.5] \text{ GeV}^2$)	26%	9.7%	3.1%
$A_{FB}(B \rightarrow X_s \ell^+ \ell^-)$ ($[3.5, 6.0] \text{ GeV}^2$)	21%	7.9%	2.6%
$A_{FB}(B \rightarrow X_s \ell^+ \ell^-)$ ($> 14.4 \text{ GeV}^2$)	19%	7.3%	2.4%

B2TiP

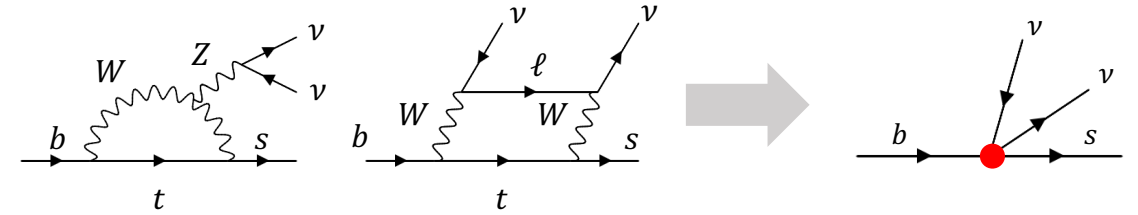
▣ Fully inclusive method will be explored with dedicated simulation studies.



An analysis of inclusive $B \rightarrow X_s\ell^+\ell^-$ with 50 ab^{-1} will exclude the SM by 5σ if the true values of C_9 and C_{10} are at the current best-fit.

- Hadronic uncertainties in the inclusive and exclusive decays are independent. Complementary information can be provided.
- Full angular analysis, not only A_{FB} , can be performed with large statistics.

- Theoretically cleaner than $b \rightarrow s\ell^+\ell^-$ due to the absence of photon mediated contribution.
 - In the SM, only \mathcal{O}_L is relevant.
- Experimentally, the decay has never been observed.
 - Two neutrinos cannot be detected.



$$\mathcal{O}_L = \frac{e^2}{16\pi^2} (\bar{s}\gamma_\mu P_L b) (\bar{\nu}\gamma^\mu (1 - \gamma_5)\nu)$$

Mode	Upper limit
$B^+ \rightarrow K^+ \nu\bar{\nu}$	$< 5.5 \times 10^{-5}$
$B^0 \rightarrow K_s^0 \nu\bar{\nu}$	$< 9.7 \times 10^{-5}$
$B^+ \rightarrow K^{*+} \nu\bar{\nu}$	$< 4.0 \times 10^{-5}$
$B^0 \rightarrow K^{*0} \nu\bar{\nu}$	$< 5.5 \times 10^{-5}$

Belle : [Phys. Rev. D87 \(2013\) 111103](#)

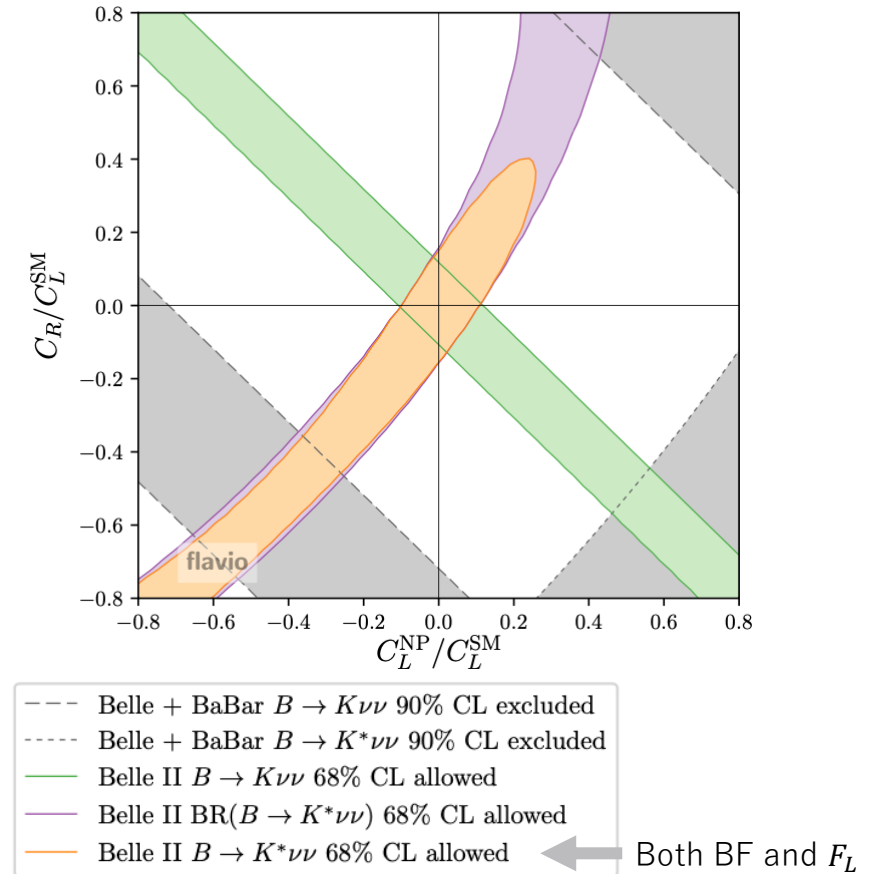
$$\begin{aligned} \text{BR}(B^+ \rightarrow K^+ \nu\bar{\nu})_{\text{SM}} &= (3.98 \pm 0.43 \pm 0.19) \times 10^{-6}, \\ \text{BR}(B^0 \rightarrow K^{*0} \nu\bar{\nu})_{\text{SM}} &= (9.19 \pm 0.86 \pm 0.50) \times 10^{-6}, \\ F_L^{\text{SM}} &= 0.47 \pm 0.03, \end{aligned}$$

Buras, Girschbach-Noe, Niehoff and Straub, [JHEP 02 184 \(2015\)](#)

Belle II can observe the $B \rightarrow K^{(*)}\nu\bar{\nu}$ at early stage (several ab^{-1}).

- Hadronic and Semi-leptonic tagging with FEI [T. Keck et al. Comput. Softw. Big. Sci. (2019)3: 6].
- Sensitivity on the BF is 10% level with 50 ab^{-1} .
- The longitudinal polarization fraction $F_L(K^*)$ can be measured with 20% precision.
- Combining measurements of $B \rightarrow K\nu\bar{\nu}$ and $K^*\nu\bar{\nu}$ will exclude a large portion of the allowed parameter space.

New analysis method with current data in progress for publication.



B2TiP

$$\mathcal{O}_L = \frac{e^2}{16\pi^2} (\bar{s}\gamma_\mu P_L b) (\bar{\nu}\gamma^\mu (1 - \gamma_5)\nu),$$

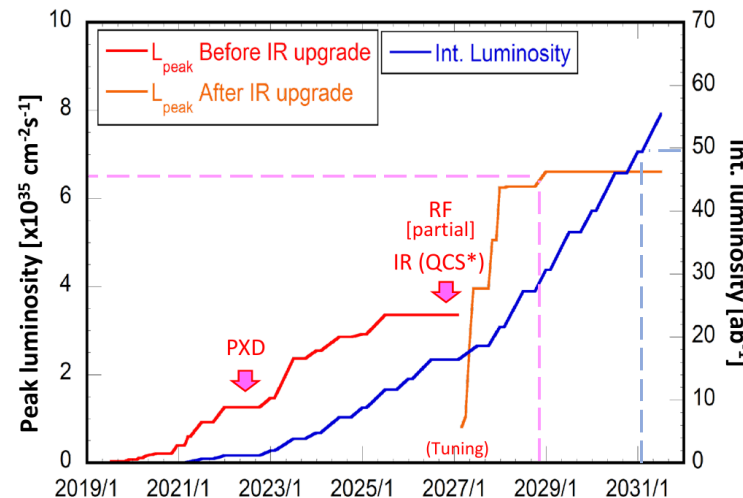
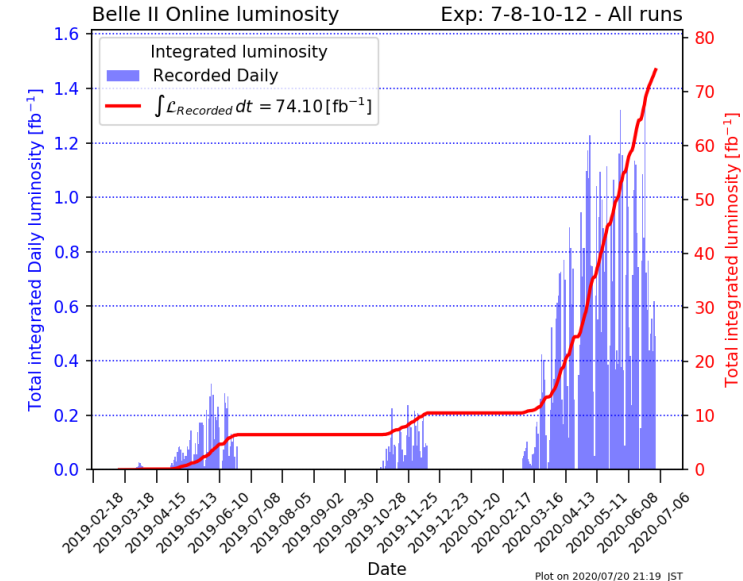
$$\mathcal{O}_R = \frac{e^2}{16\pi^2} (\bar{s}\gamma_\mu P_R b) (\bar{\nu}\gamma^\mu (1 - \gamma_5)\nu).$$

Belle II collected 74.10 fb⁻¹ integrated luminosity

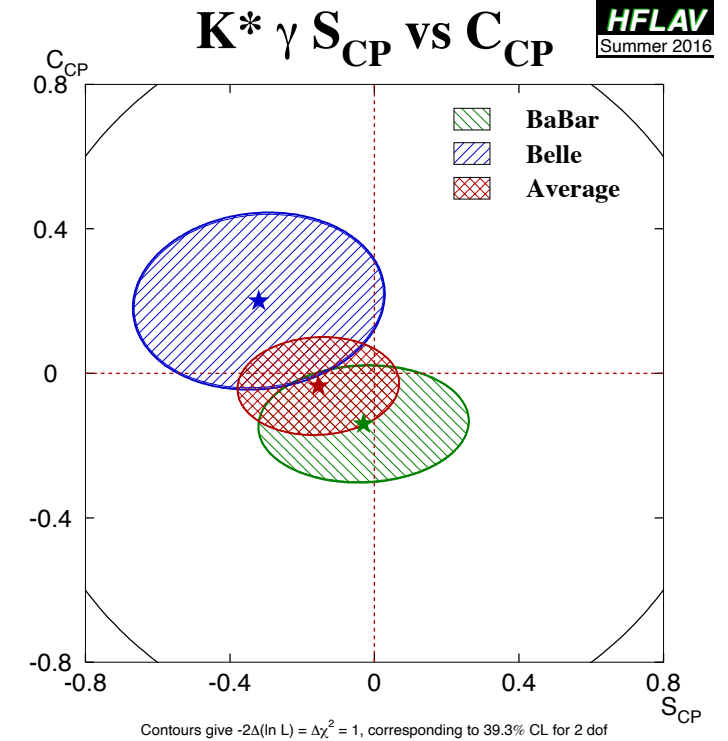
- ~10 times more in this summer than last year.
- Measurements in various processes have been started.
 - Rediscovery of $B \rightarrow K^* \gamma$.
- First results in $b \rightarrow s \ell^+ \ell^-$ and $b \rightarrow s \nu \bar{\nu}$ in progress.

Goal : L = 50 ab⁻¹ by ~2030

- Confirm or exclude the anomalies with $B \rightarrow X_s \ell^+ \ell^-$.
- Discover $B \rightarrow K^{(*)} \nu \bar{\nu}$ at early stage and precise measurements will be performed.



- $b_L \rightarrow s_R \gamma_R$ is helicity suppressed (m_s/m_b) compared to $b_R \rightarrow s_L \gamma_L$.
- Interference between $B \rightarrow f_{CP} \gamma_R$ and $B \rightarrow \bar{B} \rightarrow f_{CP} \gamma_R$ arises from only the helicity suppressed $b_L \rightarrow s_R \gamma_R$ decay.
- SM : $S_{K_S^0 \pi^0 \gamma}^{\text{SM}} \sim -s \frac{m_s}{m_b} \sin 2\phi_1 = -(2.3 \pm 1.6)\%$.
- Current world average : $S_{K_S^0 \pi^0 \gamma}^{\text{exp}} = -0.16 \pm 0.22$.
- New physics can enhance the $b_L \rightarrow s_R \gamma_R$ decay rate.



Experimentally,

- $B \rightarrow K^* \gamma$ has the largest BF. At several ab^{-1} , tension from SM will be observed if the true values are at world average.
- $B \rightarrow \rho \gamma$ will be explored with high statistics.

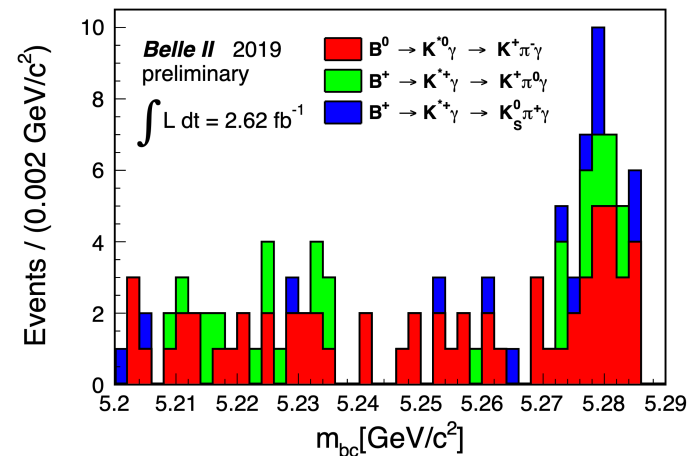
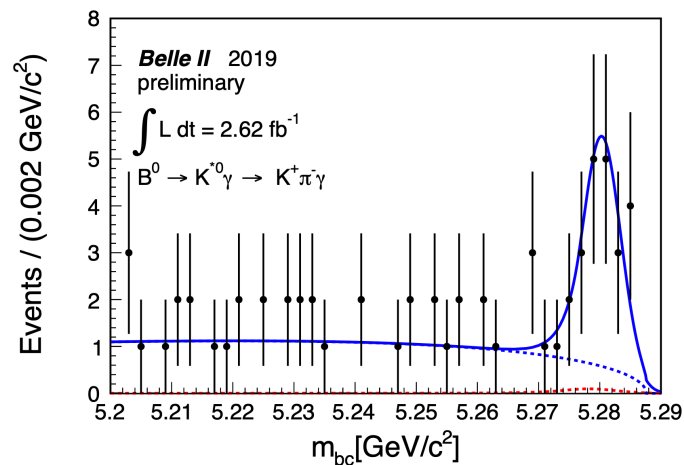
Int. Lum. ab^{-1}	Stat(S)	Stat(A)
2	0.15	0.10
10	0.07	0.05
50	0.031	0.021

Sensitivity on S and $A(C)$ for $B \rightarrow K^* \gamma$ at Belle II, B2TiP

Search for $B \rightarrow K^* \gamma$ decay using three decay modes.

- Clear peak is observed in the beam-constrained mass $M_{bc} = \sqrt{E_{\text{beam}}^{*2} - p_B^{*2}}$ distribution.
- Signal yields agree with world average branching fraction.
- Combined significance exceeds 5σ .

Rediscovery of radiative penguin decay at Belle II.



	Signal yield (stat. error)	Significance
$B^0 \rightarrow K^{*0} [K^+ \pi^-] \gamma$	19.2 ± 5.2	4.4σ
$B^+ \rightarrow K^{*+} [K^+ \pi^0] \gamma$	9.8 ± 3.4	3.7σ
$B^+ \rightarrow K^{*+} [K_S^0 \pi^+] \gamma$	6.6 ± 3.1	2.1σ

BELLE2-NOTE-PL-2019-021

The double differential decay rate for $B \rightarrow X_s \ell^+ \ell^-$.

$$\frac{d^2\Gamma}{dq^2 dz} = \frac{3}{8} [(1+z^2)H_T(q^2) + 2zH_A(q^2) + 2(1-z^2)H_L(q^2)].$$

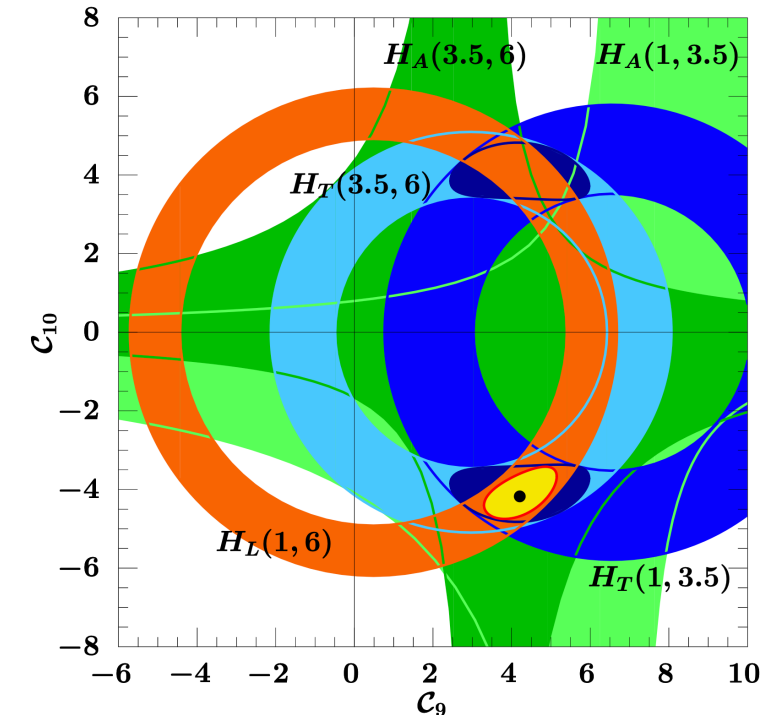
$q^2 = (p_{\ell^+} + p_{\ell^-})^2$, $z = \cos\theta$ (θ is the angle between ℓ^- and B in the di-lepton center-of-mass frame).

$$\frac{d\Gamma}{dq^2} = H_T(q^2) + H_L(q^2),$$

$$\frac{dA_{\text{FB}}}{dq^2} = \frac{3}{4}H_A(q^2).$$

Helicity decomposition gives third observables. Third independent constraint can be set.

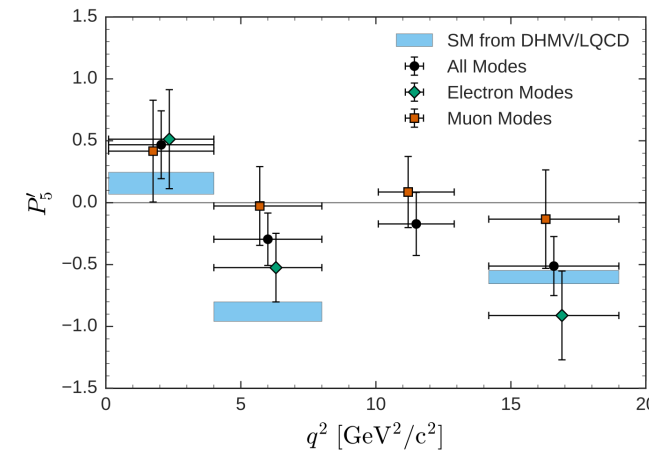
Lee, Ligeti Stewart and Tackmann,
PRD 75, 034016 (2007)



- The uncertainty on P'_5 in $q^2 \in [4,6] \text{ GeV}^2$ bin using both electron and muon modes at $\sim 5 \text{ ab}^{-1}$ will be comparable to the 4.7 fb^{-1} LHCb result that used the muon mode only.
- Precise measurement of $B \rightarrow K^* e^+ e^-$ in the low- q^2 and high- q^2 region at Belle II, provides important information to the anomaly in $B \rightarrow K^* \mu^+ \mu^-$.

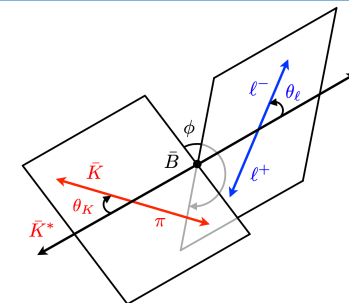
Observables	Belle 0.71 ab^{-1}	Belle II 5 ab^{-1}	Belle II 50 ab^{-1}
P'_5 ($[1.0, 2.5] \text{ GeV}^2$)	0.47	0.17	0.054
P'_5 ($[2.5, 4.0] \text{ GeV}^2$)	0.42	0.15	0.049
P'_5 ($[4.0, 6.0] \text{ GeV}^2$)	0.34	0.12	0.040
P'_5 ($> 14.2 \text{ GeV}^2$)	0.23	0.088	0.027

B2TiP

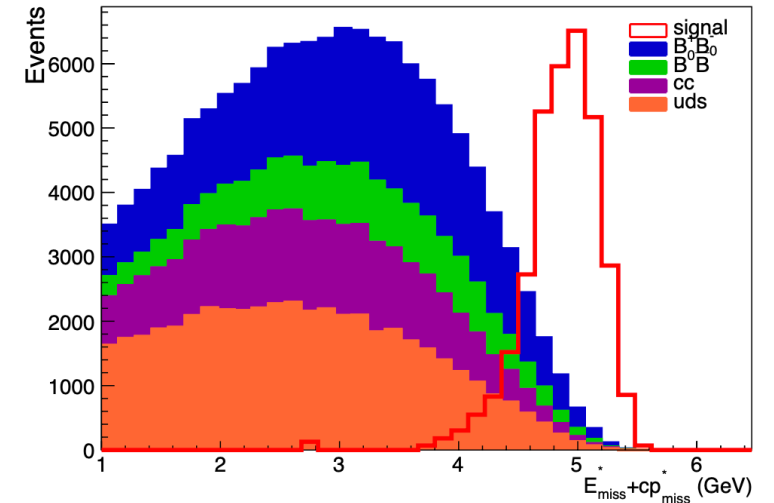


$$\frac{1}{d\Gamma/dq^2 d\cos\theta_\ell d\cos\theta_K d\phi dq^2} \frac{d^4\Gamma}{dq^2} = \frac{9}{32\pi} \left[\frac{3}{4}(1 - F_L) \sin^2 \theta_K + F_L \cos^2 \theta_K + \frac{1}{4}(1 - F_L) \sin^2 \theta_K \cos 2\theta_\ell \right. \\ \left. - F_L \cos^2 \theta_K \cos 2\theta_\ell + S_3 \sin^2 \theta_K \sin^2 \theta_\ell \cos 2\phi \right. \\ \left. + S_4 \sin 2\theta_K \sin 2\theta_\ell \cos \phi + S_5 \sin 2\theta_K \sin \theta_\ell \cos \phi \right. \\ \left. + S_6 \sin^2 \theta_K \cos \theta_\ell + S_7 \sin 2\theta_K \sin \theta_\ell \sin \phi \right. \\ \left. + S_8 \sin 2\theta_K \sin 2\theta_\ell \sin \phi + S_9 \sin^2 \theta_K \sin^2 \theta_\ell \sin 2\phi \right],$$

$$P'_{i=4,5,6,8} = \frac{S_{j=4,5,7,8}}{\sqrt{F_L(1 - F_L)}}.$$



- By reconstructing the other B meson (tag-side) and using the initial state of e^+e^- , the missing energy and momentum can be used to distinguish signal from backgrounds.
- Tagging efficiency
 - Hadronic tag : $O(0.1)\%$.
 - Semi-leptonic tag : $O(1)\%$.
- Analysis with new tagging method gives comparable sensitivity with current data set.
 - Inclusive tag : Higher tagging efficiency.



Missing $E + p$ in the CM frame for $B^0 \rightarrow K^{*0}[K^+\pi^-]\nu\bar{\nu}$. Backgrounds correspond to 1 ab^{-1} , while the signal normalization is arbitrary. [B2TiP](#)

- [1] LHCb Collaboration, [JHEP 08 \(2017\) 055](#)
- [2] LHCb Collaboration, [Phys.Rev.Lett. 122 \(2019\) 19, 191801](#)
- [3] LHCb Collaboration, [Phys.Rev.Lett. 125 \(2020\) 1, 011802](#)
- [4] Belle Collaboration, [Phys.Rev.Lett. 118 \(2017\) 11, 111801](#)