



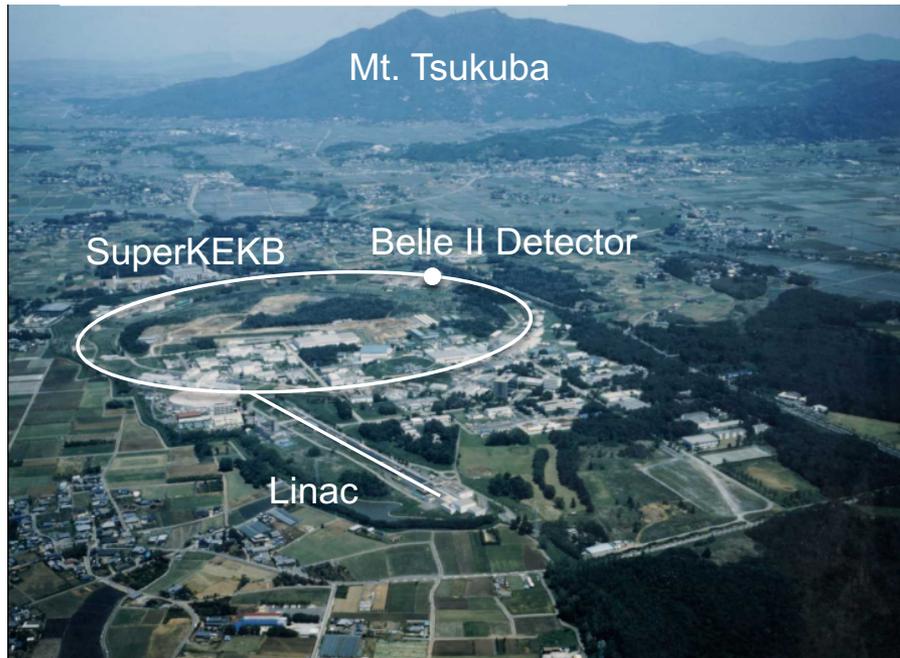
# Towards first CKM measurements at Belle II



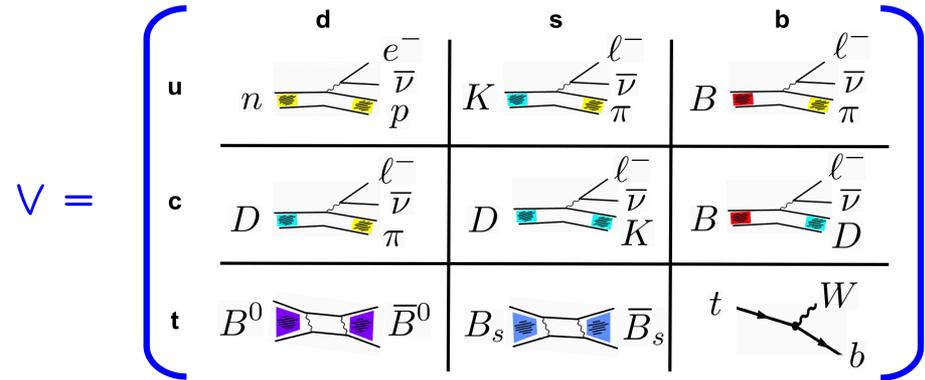
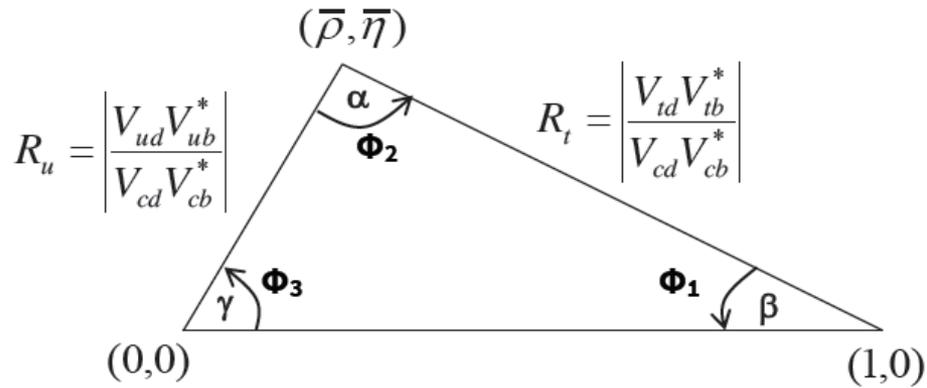
*Mario Merola (Università di Napoli Federico II and INFN)*

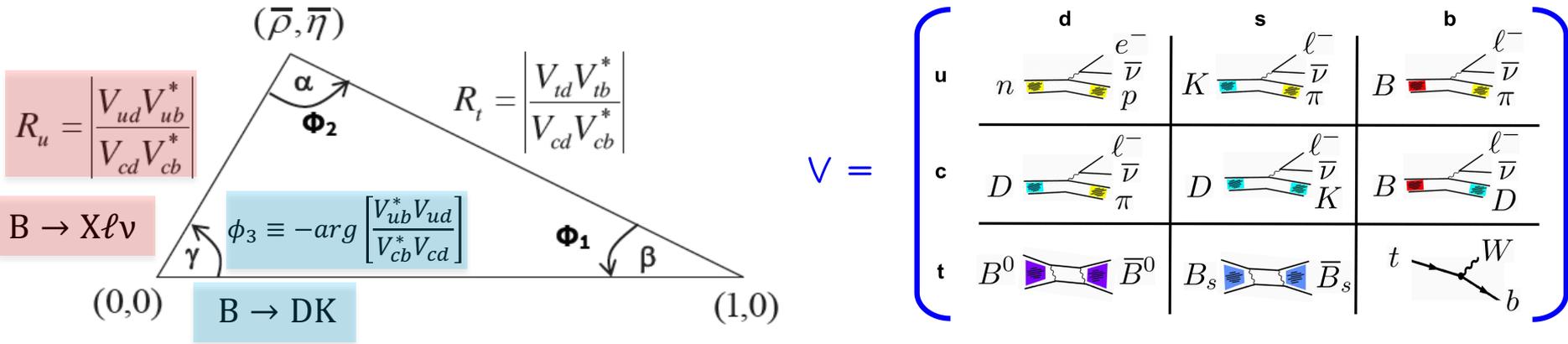
*On behalf of the Belle II Collaboration*

*FPCP2020, 8-12 June 2020*



# 'Standard' Unitarity Triangle: sides and angles





In this talk will focus on  $R_u \sim |V_{ub}|/|V_{cb}|$  and  $\phi_3$ :

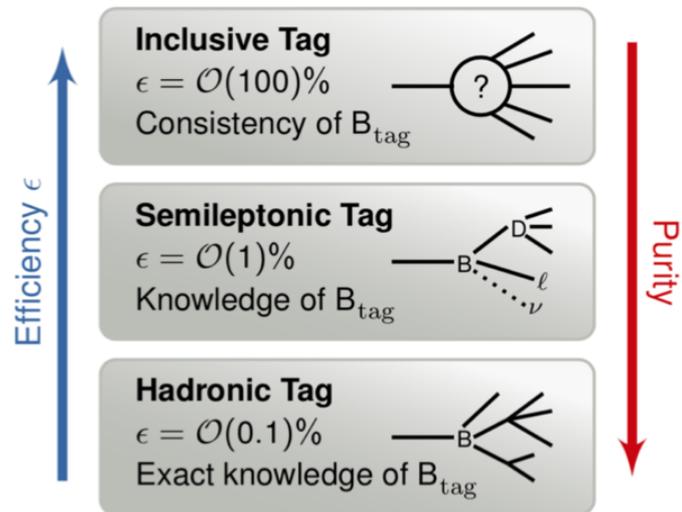
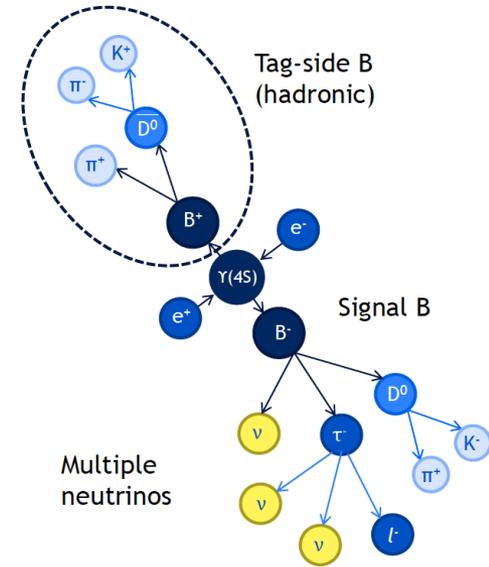
- Semileptonic B decays with missing energy  $B \rightarrow X_{u(c)} \ell \nu$
- Hadronic B decays into charm  $B \rightarrow DK$

For  $\phi_1, \phi_2$  measurements see Fernando Abudinén's [talk](#) today

- Reconstruct one B ( $\mathbf{B}_{\text{tag}}$ ) and constrain the 4-momentum of the other ( $\mathbf{B}_{\text{sig}}$ )

$$p_\nu = p_{e^+e^-} - p_{B_{\text{tag}}} - p_{B_{\text{sig}}}$$

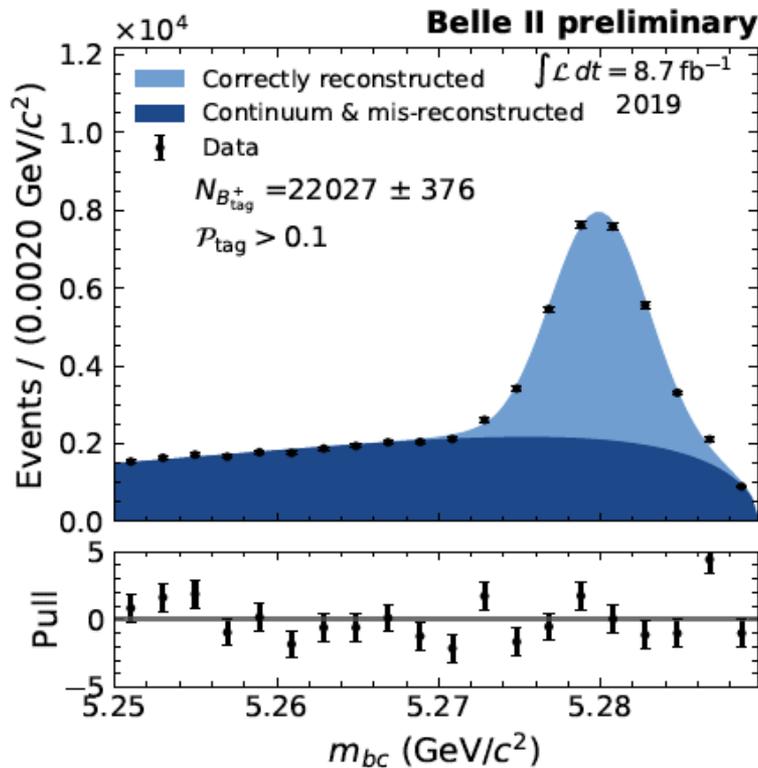
- The FEI uses a **multivariate technique** to reconstruct the B-tag side (semileptonic or hadronic) through  $O(10^3)$  decay modes in a Y(4S) decay.



Performances on Belle MC with hadronic tag @10% purity

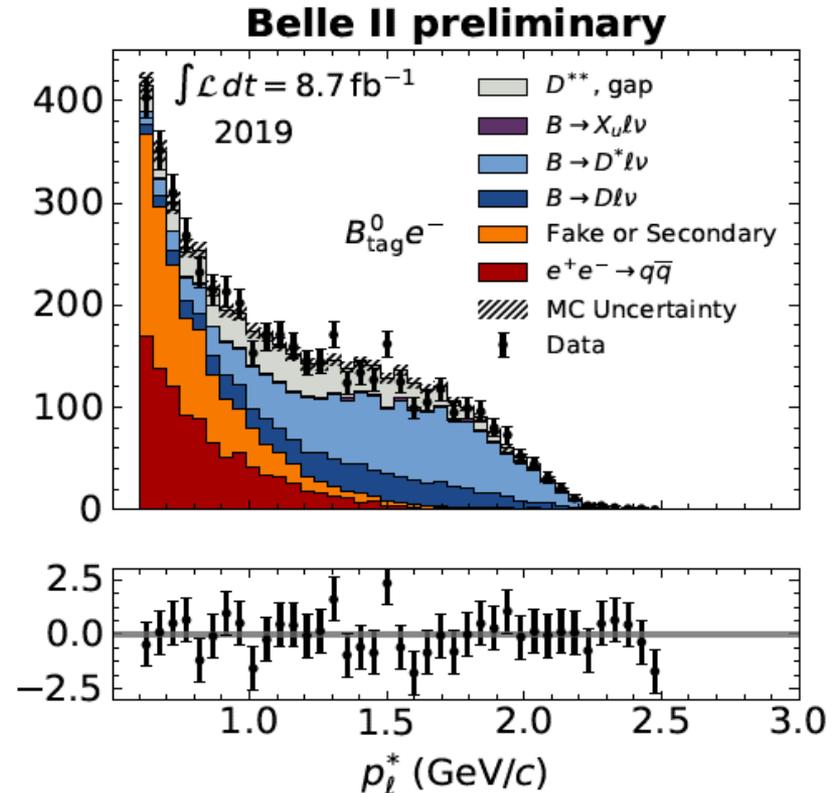
Tag algorithm	Efficiency $B^\pm/B^0$ (%)
Belle algorithm	0.28/0.18
Belle II FEI	0.76/0.46

**Belle algorithm:** NIM A 654, 432-440 (2011)  
**Belle II FEI:** Keck, T., Abudinén, F., Bernlochner, F.U. et al. Comput Softw Big Sci (2019) 3: 6.  
<https://doi.org/10.1007/s41781-019-0021-8>



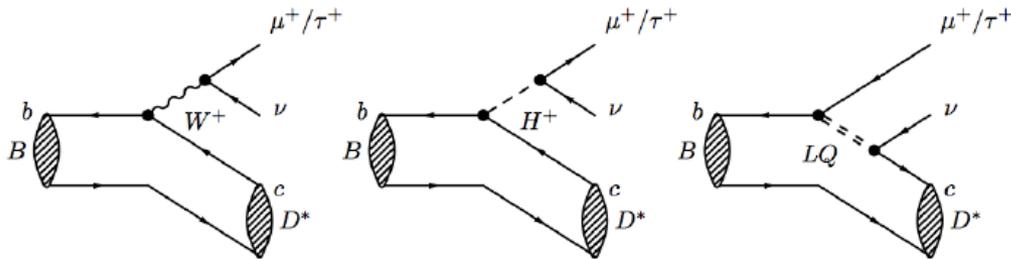
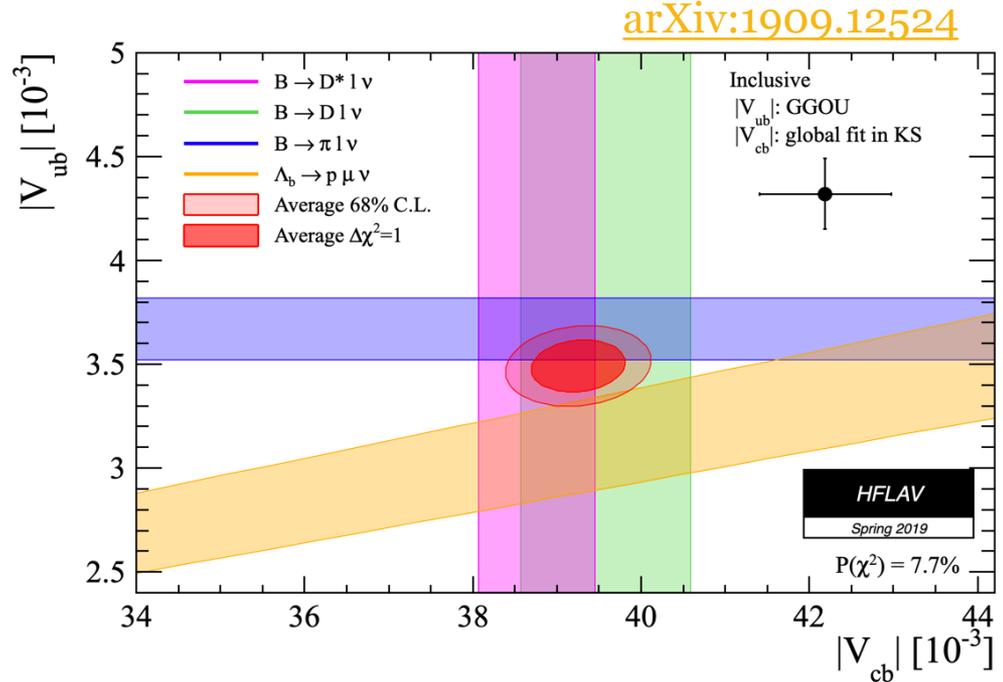
- **Tag side** reconstructed in hadronic modes

$$M_{bc} = \sqrt{s/4 - (p_B^*)^2}$$



- Select a lepton and sum the remaining particles' kinematics on the signal side
- Check consistency with the well-known **B** → **X**ℓν
- Also used to calibrate FEI

- Current precision is **2% on  $|V_{cb}|$**  and **5-6% on  $|V_{ub}|$**
- **Tension** between inclusive and exclusive determinations:  $\sim 3\sigma$  for  $|V_{cb}|$  and  $\sim 3.5\sigma$  for  $|V_{ub}|$
- $X_c\ell\nu$  decays are a clear test of the SM LFU: **NP** (charged Higgs in 2HDM models or Leptoquarks) can affect the BR and  $|V_{cb}|$



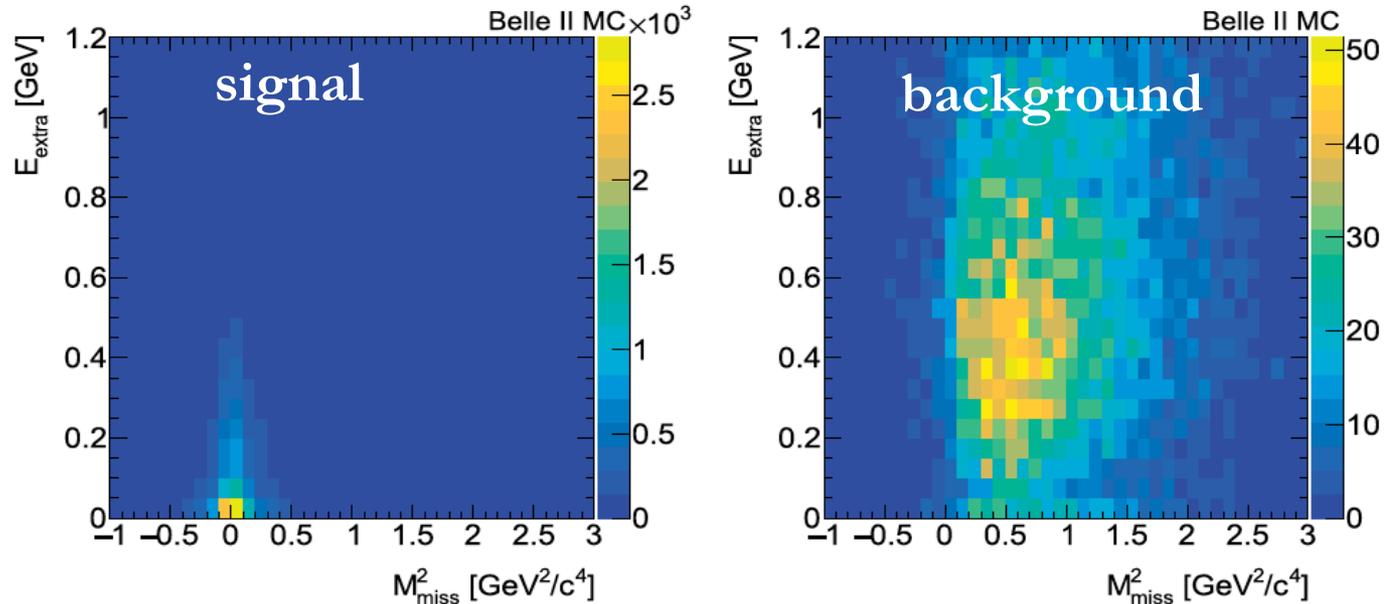
- Complementary to the  $R(D)/R(D^*)$  measurements which factor out the  $|V_{cb}|$  and form factor uncertainties

$$\mathcal{R}(D^{(*)}) = \frac{\mathcal{B}(\bar{B} \rightarrow D^{(*)}\tau^-\bar{\nu}_\tau)}{\mathcal{B}(\bar{B} \rightarrow D^{(*)}\ell^-\bar{\nu}_\ell)} \quad (\ell = e, \mu)$$

Measurement of  $|V_{ub}|$  from inclusive and exclusive B decays

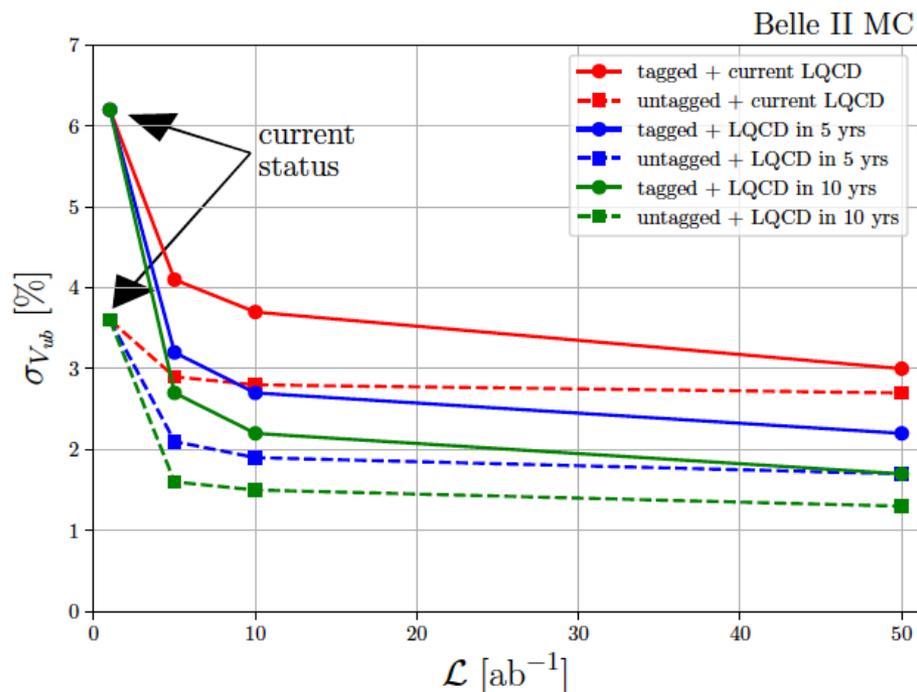
Exclusive:  $B^0 \rightarrow \pi \ell \nu$  decay

- Exploit **missing mass** and **extra energy** in the calorimeter
- $\mathcal{B} \sim f_i |V_{ub}|^2$ . Form factors  $f_i$  computed with LQCD\*



$$M_{miss}^2 = \left( p_{\Upsilon(4S)} - p_{B_{tag}} - p_{\pi} - p_{\ell} \right)^2$$

\* PRD 91,  
074510 (2015) **7**



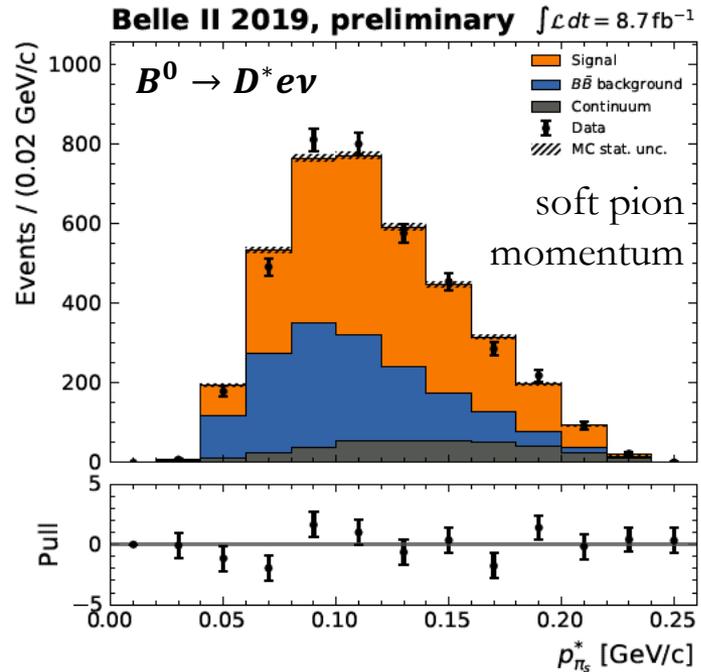
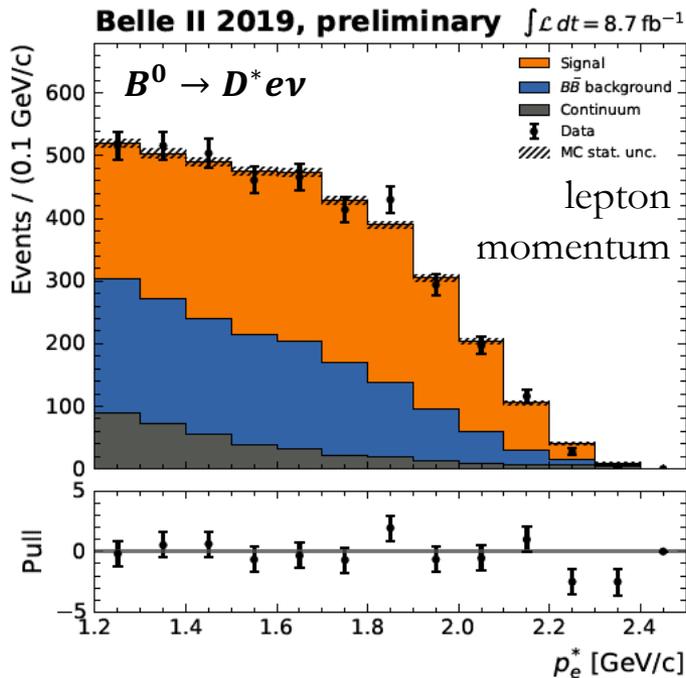
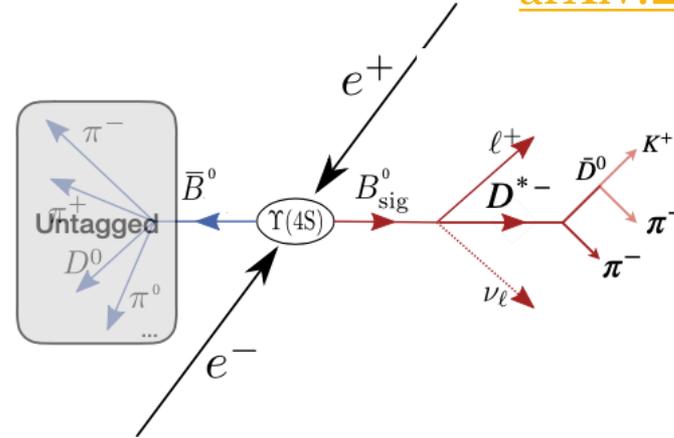
- Projection of  $|V_{ub}|$  uncertainties from  $B^0 \rightarrow \pi \ell \nu$  decay
- Takes advantage from improvements in LQCD

- Precision of  $\sim 1\%$  with full Belle II dataset

$ V_{ub} $ uncert.	Belle II (5 ab <sup>-1</sup> )	Belle II (50 ab <sup>-1</sup> )
Exclusive	(1.2 $\oplus$ 1.7)%	(0.9 $\oplus$ 0.9)%
Inclusive	(2.3 $\oplus$ 2.5-4.5)%	(1.7 $\oplus$ 2.5-4.5)%

Projected errors: (experiment  $\oplus$  theory)

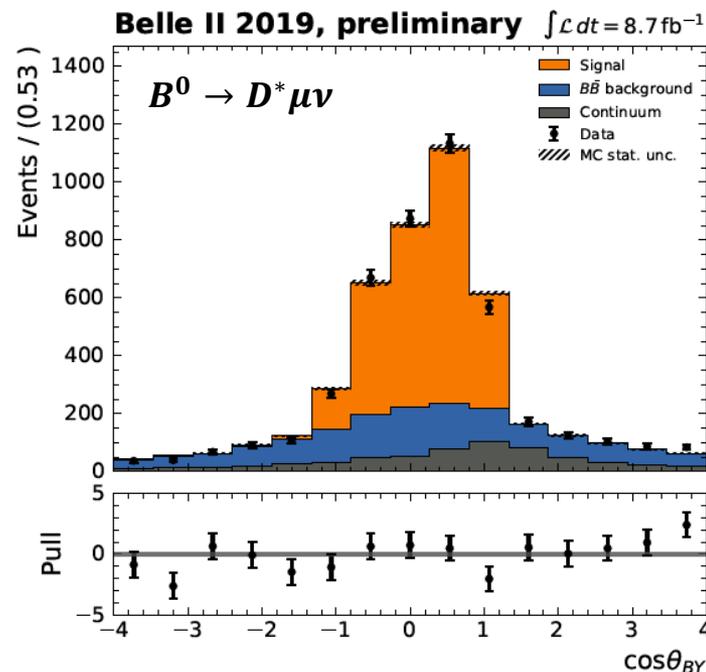
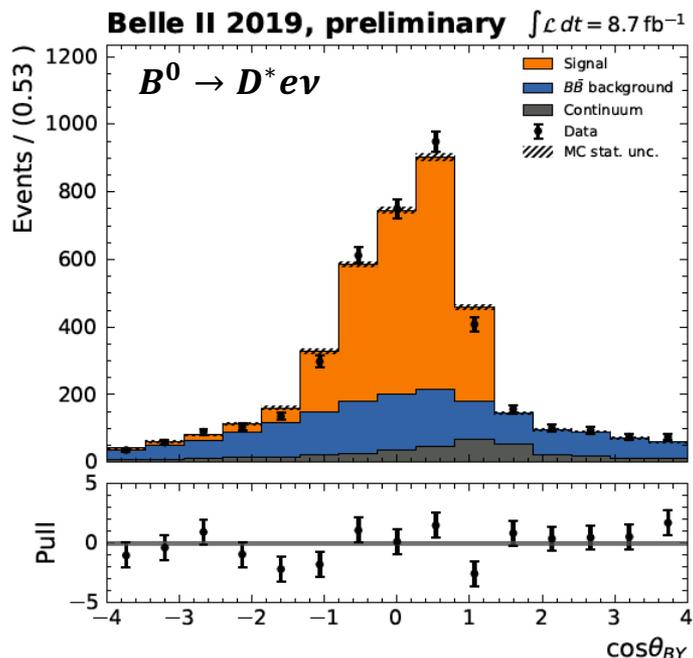
- Flagship decay for the measurement of  $|V_{cb}|$
- Inclusive tagging
- $D^* \rightarrow D^0 \pi_s, D^0 \rightarrow K\pi$



- Angle between the B flight direction and the direction of the  $(D^* \ell)$  system (Y):

$$\cos \theta_{BY} = \frac{2E_B^* E_Y^* - M_B^2 - m_Y^2}{2p_B^* p_Y^*}$$

- Fit to  $\cos \theta_{BY}$  distribution in data to measure the branching ratio



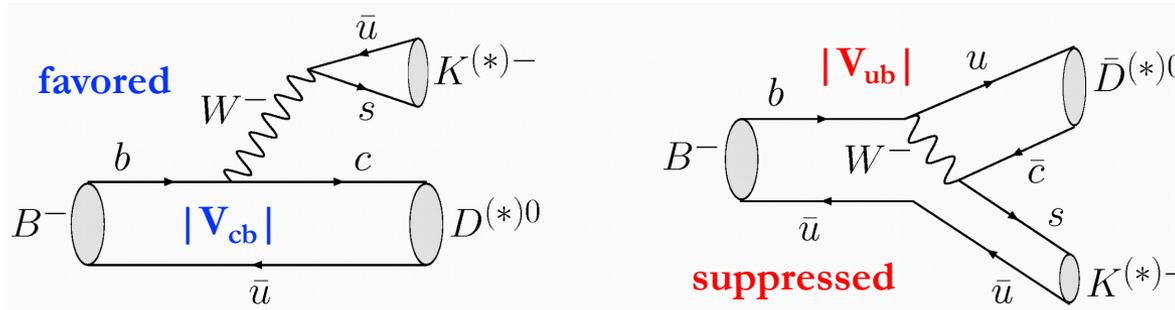
$$\mathcal{B}(\bar{B}^0 \rightarrow D^{*+} e^- \bar{\nu}_e) = (4.55 \pm 0.14(\text{stat}) \pm 0.35(\text{sys}))\%$$

$$\mathcal{B}(\bar{B}^0 \rightarrow D^{*+} \mu^- \bar{\nu}_\mu) = (4.84 \pm 0.13(\text{stat}) \pm 0.37(\text{sys}))\%$$

consistent with the SM within  $1\sigma$

$ V_{cb} $ uncert.	Belle II ( $5 \text{ ab}^{-1}$ )	Belle II ( $50 \text{ ab}^{-1}$ )
Exclusive	1.8%	1.4%

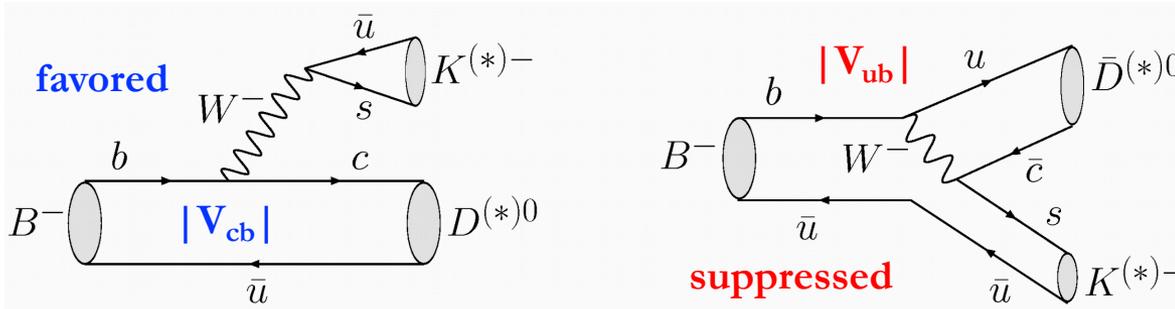
- $\phi_3$  is accessible at tree level: **theoretically very clean**,  $\delta\phi_3/\phi_3 \sim 10^{-7}$ \*
- Measured via the interference between  $B^- \rightarrow D^0 K^-$  and  $B^- \rightarrow \bar{D}^0 K^-$



$$\frac{A^{suppr.}}{A^{favor.}} = r_B e^{i(\delta_B - \phi_3)}$$

$\delta_B$  strong CP conserving phase

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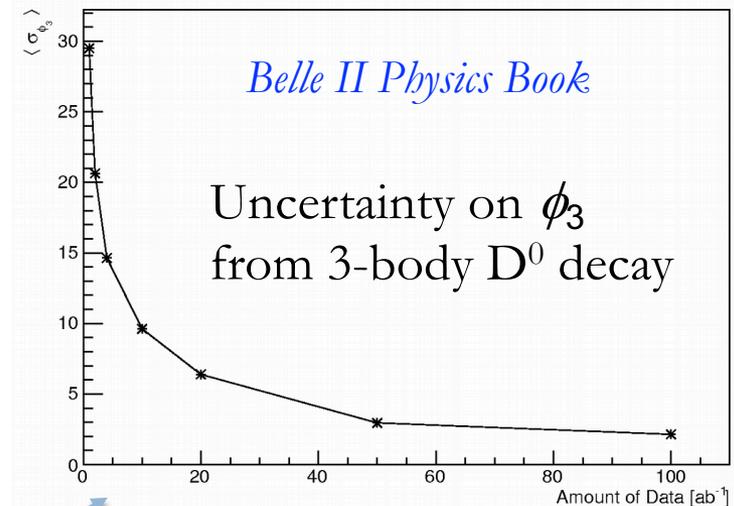


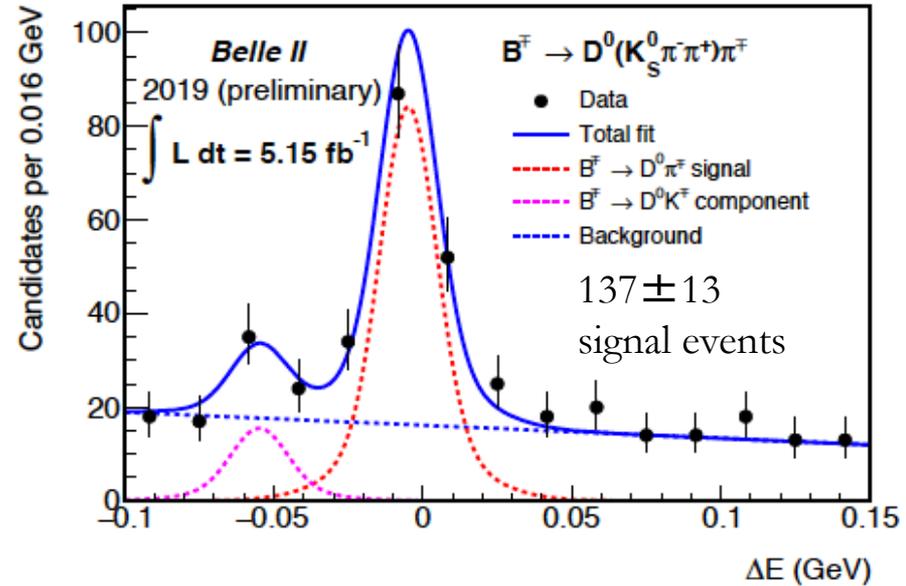
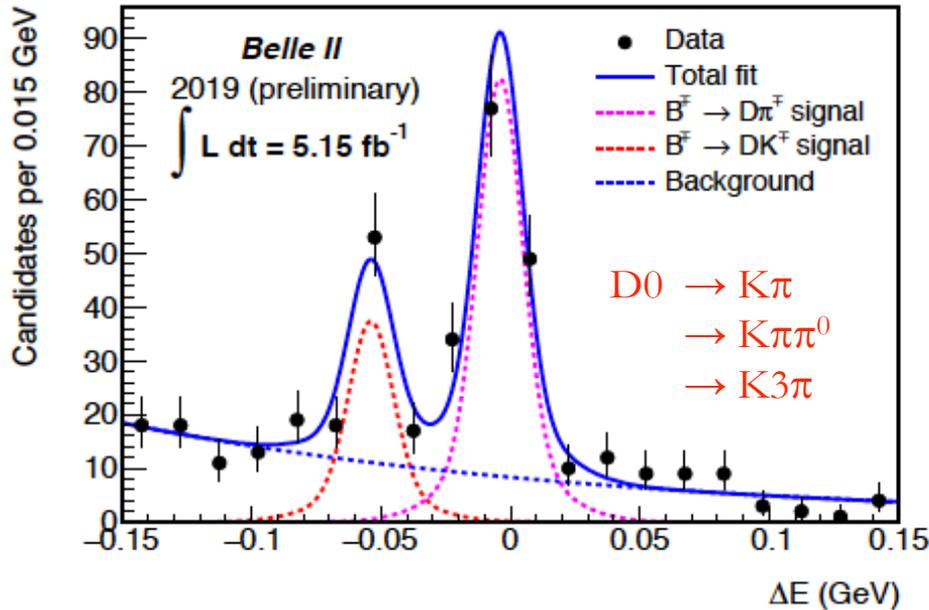
$$\frac{A_{\text{suppr.}}}{A_{\text{favor.}}} = r_B e^{i(\delta_B - \phi_3)}$$

$\delta_B$  strong CP conserving phase

Three approaches depending on  $D^0$  decay channels:

- CP eigenstates:  $K^+ K^-$ ,  $\pi^+ \pi^-$ , etc.
- Doubly Cabibbo suppr.:  $K^+ \pi^-$
- Multi-body** (Dalitz analysis):  $K_S \pi^+ \pi^-$ ,  $K_S \pi^+ \pi^- \pi^0$ . **Improving precision:** model independent approach and strong phase measurements from BESIII.





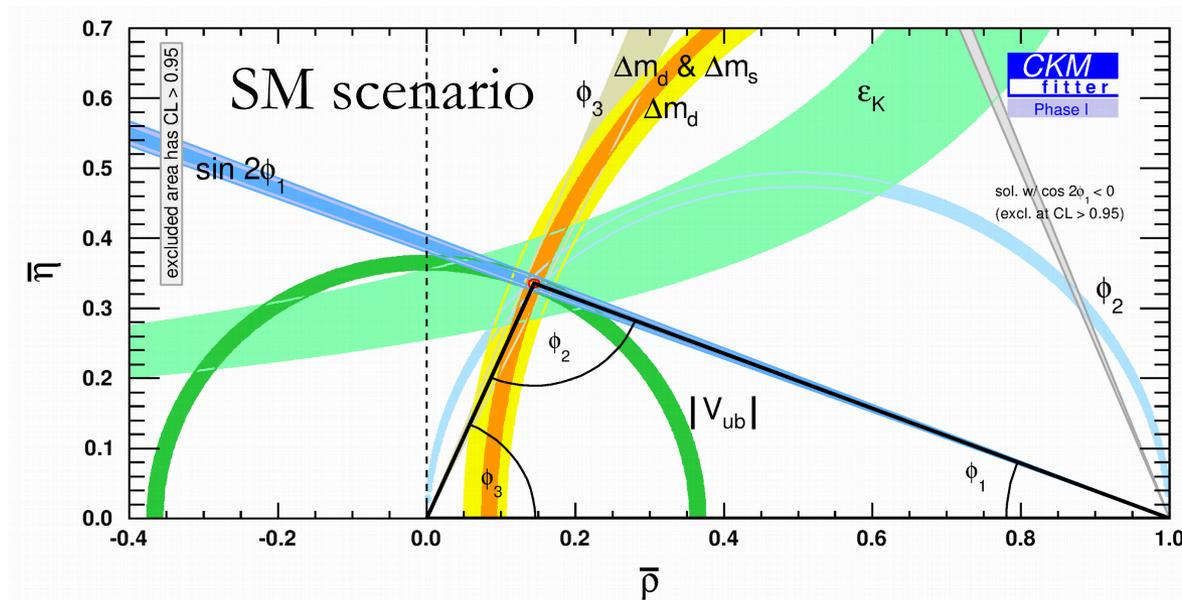
- Exploits multivariate techniques to suppress continuum background and good particle identification performances

$$\Delta E \equiv E_B^* - \sqrt{s}/2$$

- Observation of the golden 3-body decay as well

Ultimate **Belle II** precision on  $\phi_3 < 1.6^\circ$  (combining all the approaches)

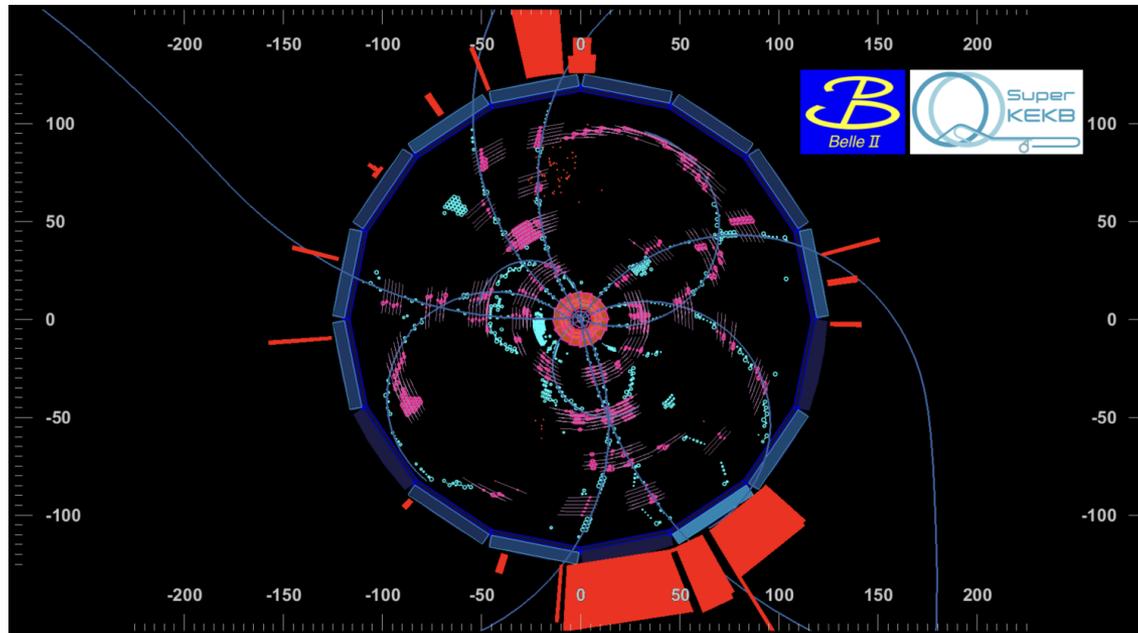
- Within the next years Belle II will be able to address the **inclusive/exclusive  $|V_{cb}|/|V_{ub}|$  tension** by measuring semileptonic B decays with missing energy.
- The use of advanced tagging techniques, i.e. FEI, together with untagged analyses will allow to reach a precision of  **$\sim 1\%$  on  $|V_{ub}|$**  and  **$\sim 1.5\%$  on  $|V_{cb}|$** .
- Belle II will also deliver a high precision measurement of the  $\phi_3$  angle, exploiting the Dalitz analysis of **multi-body  $D^0$  decays in the  $B \rightarrow DK$  process**.



**UT in a decade**

Assumptions:  
 Belle II:  $50 \text{ ab}^{-1}$   
 LHCb:  $23 \text{ fb}^{-1}$

# Thanks !



Summary [talk](#) on Belle II status and prospects  
by Phillip Urquijo on Friday

- FEI Calibration (17)
- $B \rightarrow \pi l \nu$  decay (18)
- $B \rightarrow D^* l \nu$  (19)
- Leptonic B decays (20-23)
- $RD/RD^*$  (24)
- $B \rightarrow s ll$  (25)
- Semileptonic projections (26)
- $\phi_3$  angle (27)

## FEI validated on Belle data

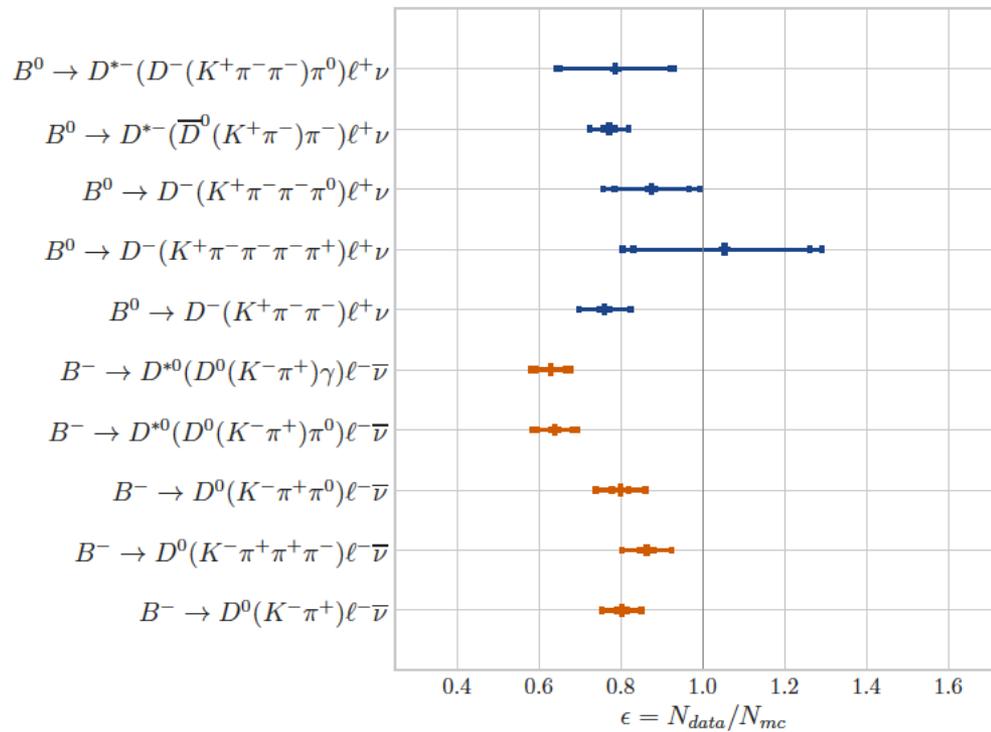
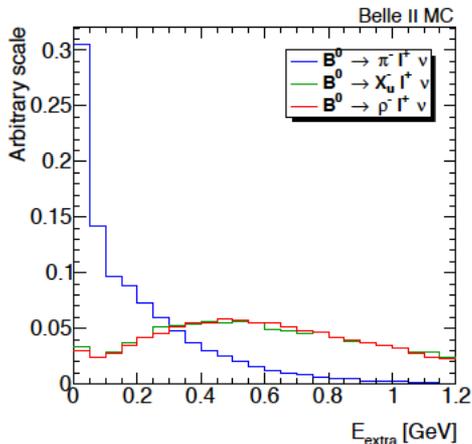
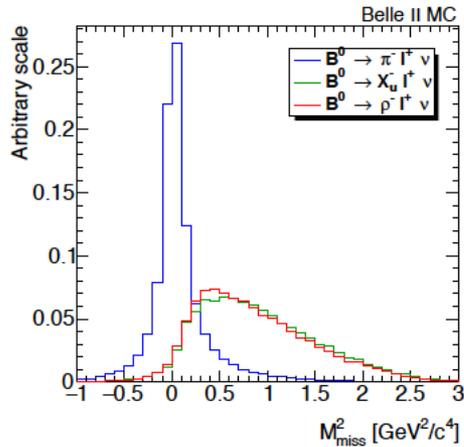


Figure 4.18.: The overall efficiency correction calculated by measuring the known branching fractions of 10 control channels on converted Belle data [76].



**Table 53.** Summary of systematic uncertainties on the branching fractions of  $B^0 \rightarrow \pi^- \ell^+ \nu_\ell$  decays in hadronic tagged and untagged Belle analyses with  $711 \text{ fb}^{-1}$  [84] and  $605 \text{ fb}^{-1}$  [299] data samples, respectively. The estimated precision limit for some sources of systematic uncertainties is given in parentheses.

Source	Error (limit) [%]	
	Tagged	Untagged
Tracking efficiency	0.4	2.0
Pion identification	—	1.3
Lepton identification	1.0	2.4
Kaon veto	0.9	—
Continuum description	1.0	1.8
Tag calibration and $N_{B\bar{B}}$	4.5 (2.0)	2.0 (1.0)
$X_u \ell \nu$ cross-feed	0.9	0.5 (0.5)
$X_c \ell \nu$ background	—	0.2 (0.2)
Form factor shapes	1.1	1.0 (1.0)
Form factor background	—	0.4 (0.4)
<b>Total</b>	<b>5.0</b>	<b>4.5</b>
<b>(reducible, irreducible)</b>	<b>(4.6, 2.0)</b>	<b>(4.2, 1.6)</b>

LQCD: current is the world average by FLAG group

- 5 yr w/o EM: We assume a factor of 2 reduction of the lattice QCD uncertainty in the next five years and that the uncertainty of the EM correction is negligible (e.g. for processes insensitive to the EM correction).

- **5 yr w/ EM:** The lattice QCD uncertainty is reduced by a factor of 2, but we add in quadrature 1% uncertainty from the EM correction.

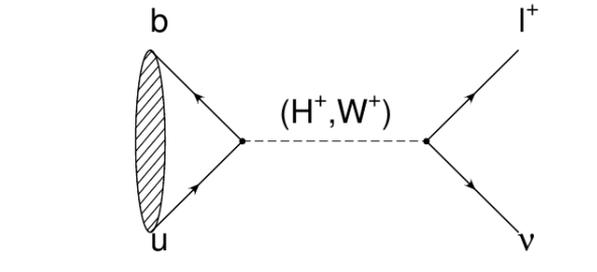
- 10 yr w/o EM: We assume a factor of 5 reduction of the lattice QCD uncertainty in the next ten years. It is also assumed that the EM correction will be under control and its uncertainty is negligible.

- **10 yr w/ EM:** We assume lattice QCD uncertainties reduced by a factor of 5, but add in quadrature 1% uncertainty from the EM correction.

Source	Relative uncertainty (%)	
	$\bar{B}^0 \rightarrow D^{*+} e^- \bar{\nu}_e$	$\bar{B}^0 \rightarrow D^{*+} \mu^- \bar{\nu}_\mu$
Lepton-ID, PDF	0.09	0.08
MC statistics, PDF	0.64	0.55
$\mathcal{B}(\bar{B} \rightarrow D^{**} l \bar{\nu})$	0.18	0.08
Efficiency momentum dependence	0.1	0.1
PDF binning	0.5	0.5
Lepton-ID, efficiency	1.8	2.2
MC statistics, efficiency	0.13	0.13
Tracking of $K, \pi, \ell$	2.5	2.5
Tracking of $\pi_s$	6.0	6.0
$N_{B^0}$	3.3	3.3
Charm branching fractions	1.1	1.1
Total	7.64	7.73

- Helicity suppressed decays

$$BR_{SM}(B \rightarrow \ell \nu) = \frac{G_F^2 m_B \tau_B}{8\pi} f_B^2 |V_{ub}|^2 m_\ell^2 \left[ 1 - \frac{m_\ell^2}{m_B^2} \right]^2$$



- Sensitive to NP contributions, e.g. type III Higgs doublet model [[PhysRevD.86.054014](#)]

SM Prediction	
$\mathcal{B}(B^+ \rightarrow e^+ \nu_e)$	$(1.09 \pm 0.21) \cdot 10^{-11}$
$\mathcal{B}(B^+ \rightarrow \mu^+ \nu_\mu)$	$(4.65 \pm 0.91) \cdot 10^{-7}$
$\mathcal{B}(B^+ \rightarrow \tau^+ \nu_\tau)$	$(1.03 \pm 0.2) \cdot 10^{-4}$

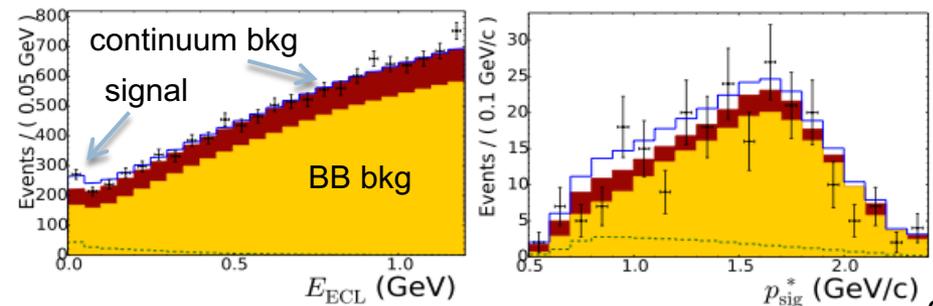
- Clean theoretically, hard experimentally: only  $B \rightarrow \tau \nu$  has been measured

Belle combination

$$\mathcal{B} = [0.91 \pm 0.19(\text{stat.}) \pm 0.11(\text{syst.})] \times 10^{-4}$$

(evidence at  $\sim 4.6 \sigma$  level)

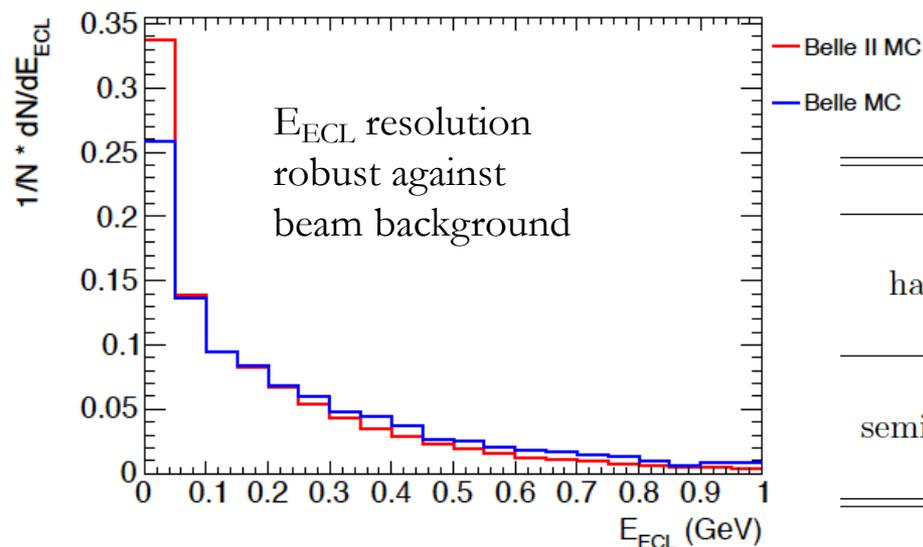
Belle PRD 92, 051102 (2015), SL tag



## Belle II full simulation study

- Hadronic tag with FEI
- 1-prong  $\tau$  decays ( $\mu\nu\nu$ ,  $e\nu\nu$ ,  $\pi\nu$ ,  $\rho\nu$ )
- Dedicated study on machine background impact
- ML fit to extra energy  $E_{\text{ECL}}$

Extra energy in the calorimeter



Main **systematic uncertainties**:

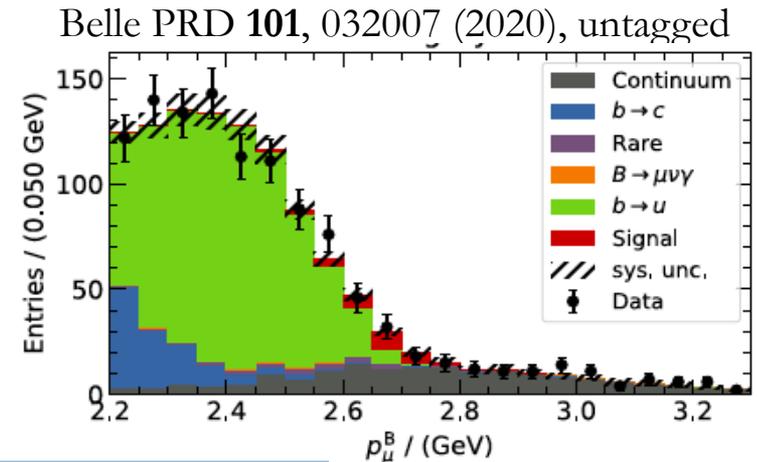
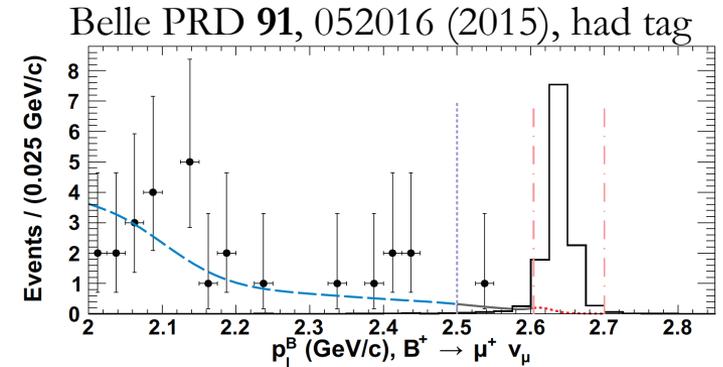
background  $E_{\text{Extra}}$  PDF, branching fractions of the peaking backgrounds, tagging efficiency, and  $K^0_L$  veto efficiency

	Integrated Luminosity ( $\text{ab}^{-1}$ )	1	5	50
hadronic tag	statistical uncertainty (%)	29.2	13.0	4.1
	systematic uncertainty (%)	12.6	6.8	4.6
	total uncertainty (%)	31.6	14.7	6.2
semileptonic tag	statistical uncertainty (%)	19.0	8.5	2.7
	systematic uncertainty (%)	17.9	8.7	4.5
	total uncertainty (%)	26.1	12.2	5.3

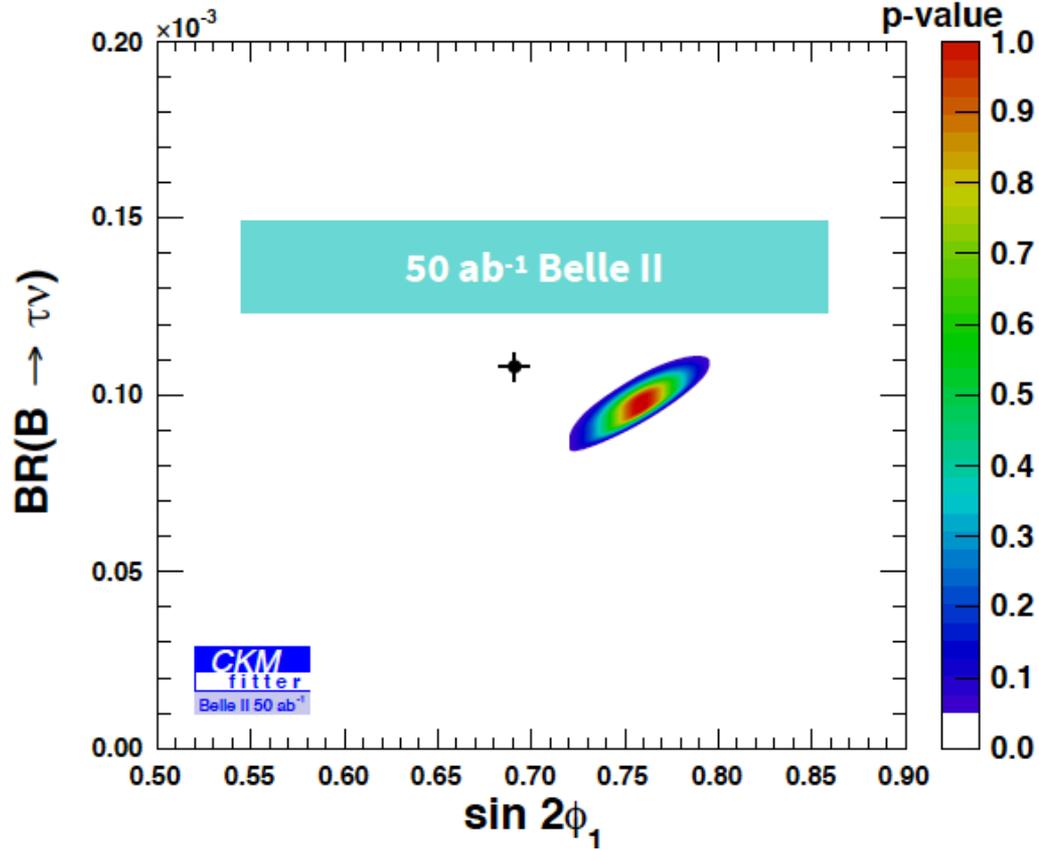
Observation at  $\sim 3 \text{ ab}^{-1}$

$$B \rightarrow \mu \nu$$

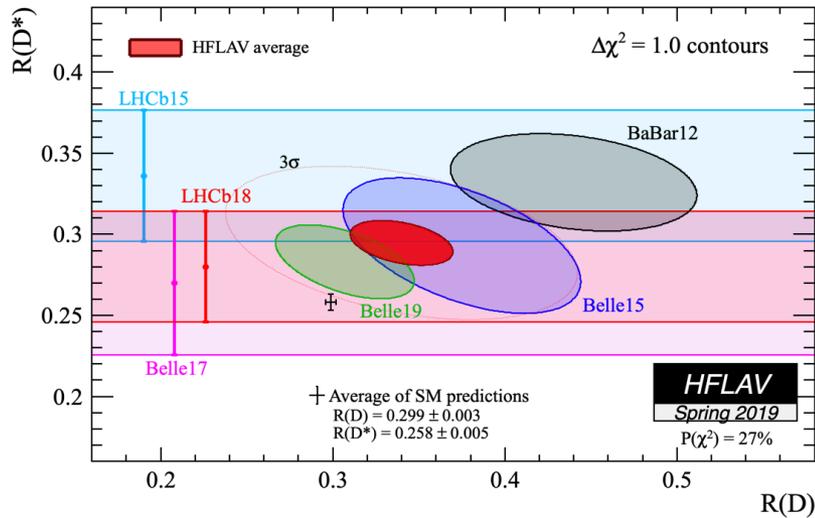
- Two body decay:  $p_{\mu}^* = m_B/2$  in B rest frame
- Tagging  $\rightarrow$  better  $p_{\mu}^*$  resolution but small statistics
- Untagged measurement (2020):
  - $2.8\sigma$  precision on the BR
  - 20% uncertainty on  $|V_{ub}|$



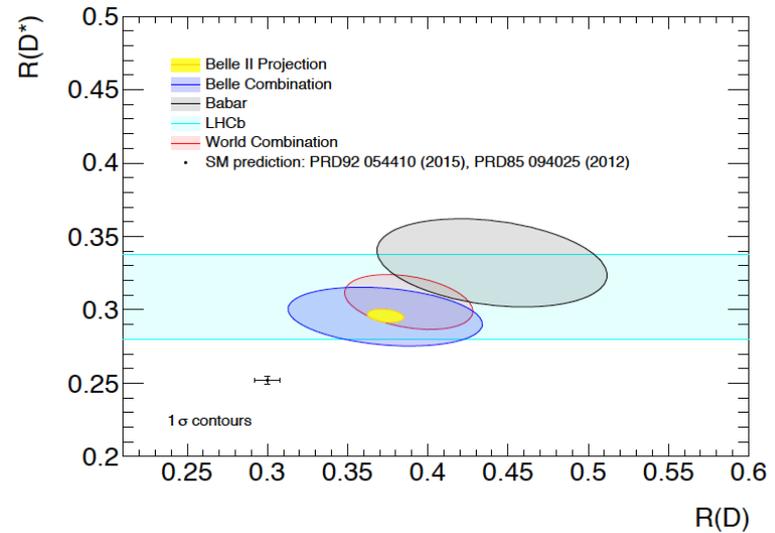
Unc. on $ V_{ub} $	Belle II @5ab <sup>-1</sup>	Belle II @50 ab <sup>-1</sup>
$B \rightarrow \tau \nu$	5%	1.5 - 2 %
$B \rightarrow \mu \nu$	10%	5%



## World average

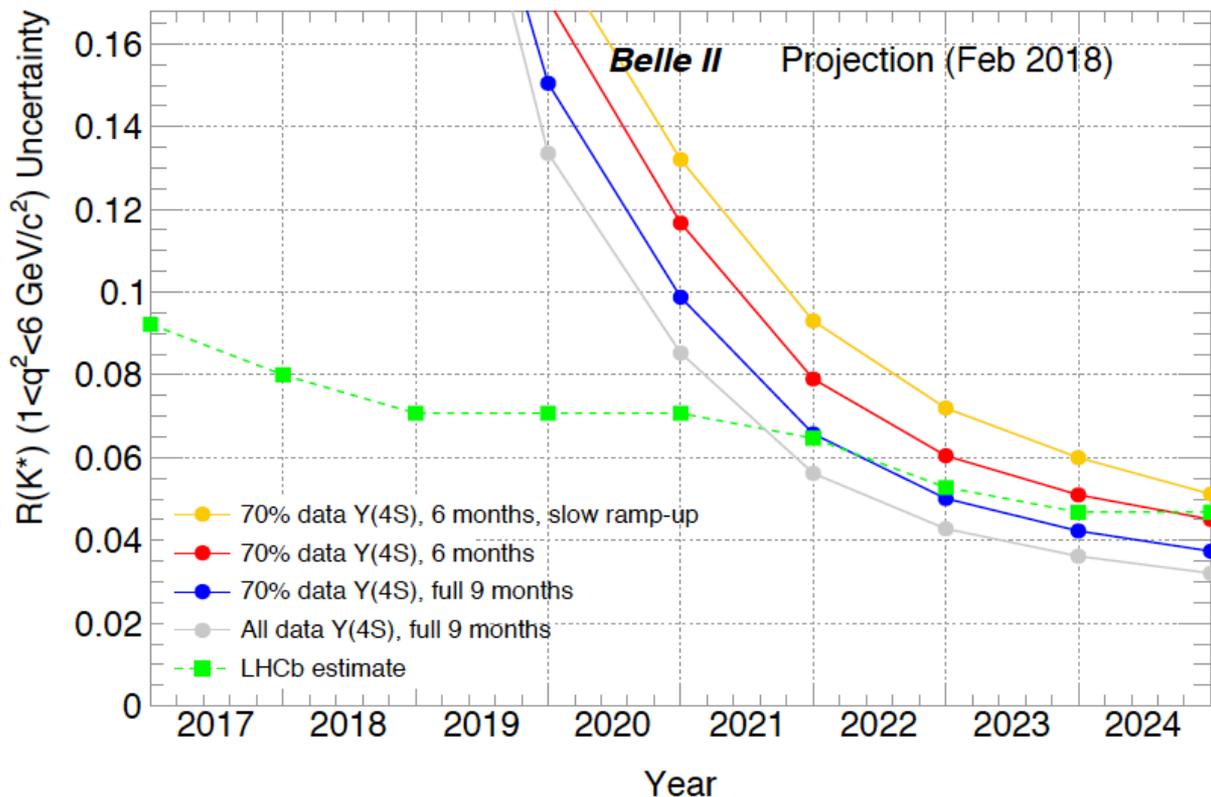


## Belle II projection



	$\Delta R(D)$ [%]			$\Delta R(D^*)$ [%]		
	Stat	Sys	Total	Stat	Sys	Total
Belle 0.7 $ab^{-1}$	14	6	16	6	3	7
Belle II 5 $ab^{-1}$	5	3	6	2	2	3
Belle II 50 $ab^{-1}$	2	3	3	1	2	2

Main systematics:  $D^{**}$  modelling, soft pions, yield of fake  $D^*$  candidates. **Studies of  $B \rightarrow D^{**}lv$  and  $B \rightarrow D^{**}\tau\nu$  planned**



$$R_K^{(*)} = \frac{\mathfrak{B}(B \rightarrow K^{(*)} \mu^+ \mu^-)}{\mathfrak{B}(B \rightarrow K^{(*)} e^+ e^-)}$$

LHCb values based on naive run-1 extrapolation (not official)

Belle II scenarios due to operating conditions at KEK

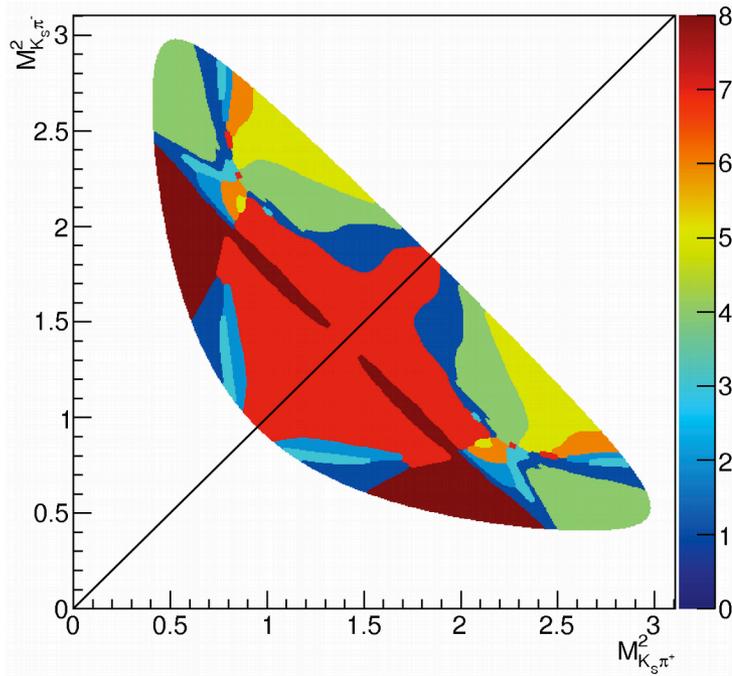
\*\* Consider it as a sketch to show Belle II can provide confirmation of any persistent anomaly.

Observables	Belle 0.71 ab <sup>-1</sup>	Belle II 5 ab <sup>-1</sup>	Belle II 50 ab <sup>-1</sup>
Br(B → X <sub>s</sub> l <sup>+</sup> l <sup>-</sup> ) ([1.0, 3.5] GeV <sup>2</sup> )	29%	13%	6.6%
Br(B → X <sub>s</sub> l <sup>+</sup> l <sup>-</sup> ) ([3.5, 6.0] GeV <sup>2</sup> )	24%	11%	6.4%
Br(B → X <sub>s</sub> l <sup>+</sup> l <sup>-</sup> ) (> 14.4 GeV <sup>2</sup> )	23%	10%	4.7%

Observables	Belle	Belle II	
	(2017)	5 ab <sup>-1</sup>	50 ab <sup>-1</sup>
$ V_{cb} $ incl.	$42.2 \cdot 10^{-3} \cdot (1 \pm 1.8\%)$	1.2%	–
$ V_{cb} $ excl.	$39.0 \cdot 10^{-3} \cdot (1 \pm 3.0\%_{\text{ex.}} \pm 1.4\%_{\text{th.}})$	1.8%	1.4%
$ V_{ub} $ incl.	$4.47 \cdot 10^{-3} \cdot (1 \pm 6.0\%_{\text{ex.}} \pm 2.5\%_{\text{th.}})$	3.4%	3.0%
$ V_{ub} $ excl. (WA)	$3.65 \cdot 10^{-3} \cdot (1 \pm 2.5\%_{\text{ex.}} \pm 3.0\%_{\text{th.}})$	2.4%	1.2%
$\mathcal{B}(B \rightarrow \tau\nu)$ [10 <sup>-6</sup> ]	$91 \cdot (1 \pm 24\%)$	9%	4%
$\mathcal{B}(B \rightarrow \mu\nu)$ [10 <sup>-6</sup> ]	< 1.7	20%	7%
$R(B \rightarrow D\tau\nu)$ (Had. tag)	$0.374 \cdot (1 \pm 16.5\%)$	6%	3%
$R(B \rightarrow D^*\tau\nu)$ (Had. tag)	$0.296 \cdot (1 \pm 7.4\%)$	3%	2%

Process	Observable	Theory	Sys. dom.	(Discovery)	[ab <sup>-1</sup> ]	vs LHCb	vs Belle	Anomaly	NP
● $B \rightarrow \pi l \nu_\ell$	$ V_{ub} $	***	10-20	***	***	***	**	*	
● $B \rightarrow X_u l \nu_\ell$	$ V_{ub} $	**	2-10	***	**	***	*		
● $B \rightarrow \tau\nu$	$Br.$	***	>50 (2)	***	***	*	***		
● $B \rightarrow \mu\nu$	$Br.$	***	>50 (5)	***	***	*	***		
● $B \rightarrow D^{(*)} l \nu_\ell$	$ V_{cb} $	***	1-10	***	**	**	*		
● $B \rightarrow X_c l \nu_\ell$	$ V_{cb} $	***	1-5	***	**	**	**		
● $B \rightarrow D^{(*)} \tau \nu_\tau$	$R(D^{(*)})$	***	5-10	**	***	***	***		
● $B \rightarrow D^{(*)} \tau \nu_\tau$	$P_\tau$	***	15-20	***	***	**	***		
● $B \rightarrow D^{**} l \nu_\ell$	$Br.$	*	-	**	***	**	-		

## Dalitz plot of $K_S\pi^+\pi^-$



## Combination of measurements

