

Measurement of the Branching Fraction of $\Lambda_c^+ \rightarrow pK_S^0\pi^0$ at Belle

We report a precise measurement of the ratio of branching fractions $\mathcal{B}(\Lambda_c^+ \rightarrow pK_S^0\pi^0)/\mathcal{B}(\Lambda_c^+ \rightarrow pK^-\pi^+)$ using 980 fb⁻¹ of e^+e^- collision data from the Belle experiment. We obtain a value of $\mathcal{B}(\Lambda_c^+ \rightarrow pK_S^0\pi^0)/\mathcal{B}(\Lambda_c^+ \rightarrow pK^-\pi^+) = 0.339 \pm 0.002 \pm 0.009$, where the first and second uncertainties are statistical and systematic, respectively. This measurement is consistent with the previous measurement from the CLEO experiment but has a fivefold improvement in precision. By combining our result with the world average $\mathcal{B}(\Lambda_c^+ \rightarrow pK^-\pi^+)$, we obtain the absolute branching fraction $\mathcal{B}(\Lambda_c^+ \rightarrow pK_S^0\pi^0) = (2.13 \pm 0.01 \pm 0.05 \pm 0.11)\%$, where the uncertainties are statistical, general systematic, and specific systematic due to the uncertainty in $\mathcal{B}(\Lambda_c^+ \rightarrow pK^-\pi^+)$, respectively. This measurement can shed light on hadronic decay mechanisms in charmed baryon decays.

I. INTRODUCTION

The nonleptonic weak decays of Λ_c^+ provide a unique testing ground for understanding the factorization scheme involving the $c \rightarrow s$ transition and the final-state interactions. Among the possible final states, $N\bar{K}\pi$ decays are particularly useful for examining the isospin properties of the weak interaction in Λ_c^+ decay [1]. The $\Delta S = 1$ Cabibbo-allowed transition is governed by $c \rightarrow s\bar{u}\bar{d}$, so iso-singlet Λ_c^+ decays result in a final state with $I = I_3 = 1$. In the $\Lambda_c^+ \rightarrow N\bar{K}\pi$ decays, the $N\bar{K}$ state can have isospin 0 or 1. Thus, the sum of isospin amplitudes of the three decay modes, $\sqrt{2}\mathcal{A}(p\bar{K}^0\pi^0) + \mathcal{A}(pK^-\pi^+) + \mathcal{A}(n\bar{K}^0\pi^+)$, is zero according to isospin symmetry [2–4], which imposes useful constraints on the branching ratios of the nonleptonic decay channels. In the quark-diagram schemes for $\Lambda_c^+ \rightarrow N\bar{K}\pi$ decays, as shown in Fig. 1, direct π^+ emission can involve a color-allowed factorizable process with external W^+ emission (Fig. 1(c)) but a π^0 cannot be produced in this process. The dominant contributions in the $N\bar{K}\pi^0$ decays instead come from color-suppressed internal W^+ emission and internal flavor conversion involving the subprocess $cd \rightarrow su$ with W^+ exchange.

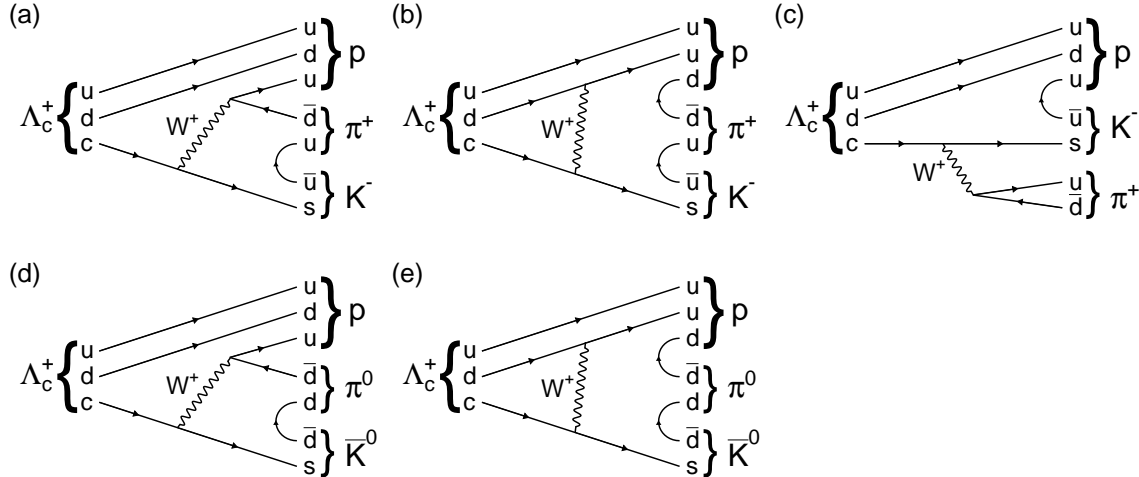


FIG. 1. Typical Feynman diagrams for internal W emission processes in $\Lambda_c^+ \rightarrow pK^-\pi^+$ (a) and $\Lambda_c^+ \rightarrow pK_S^0\pi^0$ (d), internal W exchange processes in $\Lambda_c^+ \rightarrow pK^-\pi^+$ (b) and $\Lambda_c^+ \rightarrow pK_S^0\pi^0$ (e), and external W emission process in $\Lambda_c^+ \rightarrow pK^-\pi^+$ (c).

18 Since direct π^+ emission leaves the ud diquark in the iso-singlet Λ_c^+ as a spectator, the sud
 19 cluster in the final state is a pure $I = 0$ state, thus favoring the $I = 0 \bar{K}N$ state [5, 6]. Hence,
 20 if the direct π^+ emission process is dominant, the two-body decay $\Lambda_c^+ \rightarrow \Lambda\pi^+$ should be
 21 greatly favored over $\Lambda_c^+ \rightarrow \Sigma^0\pi^+$. Moreover, as the Λ_c^+ contains an anti-symmetric quark pair
 22 ($ud - du$) c , factorizable processes are suppressed for Λ_c^+ decays involving a baryon decuplet
 23 with totally flavor symmetric quark content [7]. However, the experimentally determined
 24 branching fractions for the two decays are comparable, indicating that the contributions
 25 from color-suppressed W^+ emission and W^+ exchange processes are large. The subsequent
 26 rescattering of the $N\pi$ pair can populate $N(1535)$ and $N(1650)$ resonances, and the $N\bar{K}$
 27 final-state interaction generates $\Lambda(1405)$ and $\Lambda(1670)$ states [8].

28 An observation of a narrow structure at the $\Lambda\eta$ threshold in the K^-p invariant mass
 29 spectrum in $\Lambda_c^+ \rightarrow pK^-\pi^+$ reported by the Belle collaboration [9] has attracted significant
 30 attention. A recent analysis, attempting to shed light on the nature of the structure, in-
 31 dicates a $\Lambda\eta$ cusp effect, enhanced by the $\Lambda(1670)$ pole [10]. Another study suggests that
 32 the effect giving rise to the narrow structure is enhanced by a triangle singularity involving
 33 rescattering via the near-lying $\Lambda a_0(980)^+$ or $\eta\Sigma(1660)^+$ scattering [11]. In $\Lambda_c^+ \rightarrow pK^-\pi^+$
 34 process, isospin symmetry implies that the partial branching ratio of $\Lambda_c^+ \rightarrow \Sigma^{*+}\pi^0$ equals
 35 that of $\Lambda_c^+ \rightarrow \Sigma^{*0}\pi^+$, whereas the $\Lambda_c^+ \rightarrow \Delta^{++}K^-$ decay is three times larger than the

36 branching fraction of $\Lambda_c^+ \rightarrow \Delta^+ \bar{K}^0$ [7, 12]. In the $\Lambda_c^+ \rightarrow p \bar{K}^0 \pi^0$ decay, only Σ^{*+} resonances
 37 are possible in the $N \bar{K}$ system. Therefore, a precise measurement of the relative branching
 38 fraction for $\Lambda_c^+ \rightarrow p K_S^0 \pi^0$ as well as the investigation of intermediate resonances provides
 39 stringent tests of isospin symmetry and could help to better understand non-factorizable
 40 processes in the non-leptonic decay of charmed baryons.

41 The absolute branching fractions for $\Lambda_c^+ \rightarrow n \bar{K}^0 \pi^+$ and $\Lambda_c^+ \rightarrow p K_S^0 \pi^0$ decays are reported
 42 from BESIII to be $\mathcal{B}(\Lambda_c^+ \rightarrow n K_S^0 \pi^+) = (1.82 \pm 0.25)\%$ and $\mathcal{B}(\Lambda_c^+ \rightarrow p K_S^0 \pi^0) = (1.87 \pm 0.14)\%$,
 43 respectively [3]. The branching fraction of $\Lambda_c^+ \rightarrow p K_S^0 \pi^0$ relative to $\Lambda_c^+ \rightarrow p K^- \pi^+$ reported
 44 from CLEO is 0.33 ± 0.05 [13]. This paper reports a precise measurement of the relative
 45 branching fraction of $\Lambda_c^+ \rightarrow p K_S^0 \pi^0$ compared with $\Lambda_c^+ \rightarrow p K^- \pi^+$ using Belle data. In
 46 addition, we present the first investigation of the intermediate resonances in $\Lambda_c^+ \rightarrow p K_S^0 \pi^0$
 47 decays.

48 II. THE DATA SAMPLE AND THE BELLE DETECTOR

49 The branching fractions are measured based on a full data sample obtained at or near
 50 $\Upsilon(1S)$, $\Upsilon(2S)$, $\Upsilon(3S)$, $\Upsilon(4S)$ and $\Upsilon(5S)$ with the Belle detector at the KEKB asymmetric
 51 energy e^+e^- collider [14]. The full data sample has an integrated luminosity of 980 fb^{-1} .
 52 The Belle detector was a large-solid-angle magnetic spectrometer comprising a silicon vertex
 53 detector (SVD), a central drift chamber (CDC), an array of aerogel threshold Cherenkov
 54 counters (ACC), a barrel-like arrangement of time-of-flight scintillation counters (TOF),
 55 and an electromagnetic calorimeter comprising CsI(Tl) crystals (ECL) located inside a su-
 56 perconducting solenoid that provided a 1.5 T magnetic field. An iron flux return located
 57 outside the coil was employed to detect K_L^0 mesons and identify muons. The Belle detector
 58 is described in detail in Ref. [15].

59 The Monte Carlo (MC) samples used in the simulation studies are generated using Evt-
 60 Gen [16] and PYTHIA [17], and propagated through a virtual GEANT3 model of the
 61 full detector [18]. The final-state radiation process is simulated using the PHOTOS [19]
 62 package in EvtGen. A signal MC sample is generated via $e^+e^- \rightarrow c\bar{c} \rightarrow \Lambda_c^+ + X$ to study the
 63 reconstruction efficiency and signal shape functions. A Belle generic MC sample including
 64 $\Upsilon(4S) \rightarrow B\bar{B}$, $\Upsilon(5S) \rightarrow B_{(s)}^{(*)}\bar{B}_{(s)}^{(*)}$, $\Upsilon(1S, 2S, 3S)$ decays and $e^+e^- \rightarrow q\bar{q}$ ($q = u, d, s, c$) with
 65 the same integrated luminosity as the real data is used to optimize the selection criteria.

III. EVENT SELECTION

We consider the $\Lambda_c^+ \rightarrow pK_S^0\pi^0$ process with subsequent decays $K_S^0 \rightarrow \pi^+\pi^-$ and $\pi^0 \rightarrow \gamma\gamma$. The event selection criteria are optimized using a generic MC sample, with a figure-of-merit (FoM) defined as $N_{\text{sig}}/\sqrt{N_{\text{sig}} + N_{\text{bkg}}}$, where N_{sig} is the number of signal events and N_{bkg} is the number of background events. The latter are obtained in the $pK_S^0\pi^0$ invariant mass region between 2.263 GeV/ c^2 and 2.306 GeV/ c^2 .

The likelihood \mathcal{L}_i ($i = \pi^\pm, K^\pm, p^\pm$) is calculated by combining information from the ACC, CDC, and TOF detectors. The likelihood ratio between hypotheses i and i' is defined as $\mathcal{R}(i|i') = \mathcal{L}_i/(\mathcal{L}_i + \mathcal{L}_{i'})$. Charged tracks must satisfy $\mathcal{R}(p|K) > 0.9$ and $\mathcal{R}(p|\pi) > 0.9$ to be considered as proton candidates. Furthermore, the electron likelihood ratio ($\mathcal{R}(e)$), obtained from ACC, CDC, and ECL information, should be smaller than 0.9 for the proton candidates. In addition, the distance-of-closest-approach (DOCA) to the beam interaction point (IP) must be smaller than 2.0 cm along the beam direction (z) and smaller than 0.1 cm in the transverse direction (r). Furthermore, at least one hit in SVD is required. After applying the selection criteria, the PID efficiency for the proton candidates is 83% in the typical momentum range of the decays.

We reconstruct K_S^0 candidates from $K_S^0 \rightarrow \pi^+\pi^-$ decays, which are identified using a neural network algorithm involving the K_S^0 momentum in the laboratory frame, the distance between two charged pion tracks along the z axis, the flight length of K_S^0 projected onto the r plane, the angle between the K_S^0 momentum and the vector from IP to K_S^0 decay vertex in the laboratory frame, longer and shorter DOCAs in the r -direction of charged pions, the angle between the K_S^0 momentum in the laboratory frame and charged the pion momentum in the K_S^0 rest frame, the number of CDC hits from each π^\pm track and the presence or absence of SVD hits [20]. In addition, we perform a mass-constrained fit to the K_S^0 candidates in order to improve the momentum resolution. The χ^2 value of the mass-constrained vertex fit to the π^+ and π^- tracks with a common vertex is required to be smaller than 40.

ECL clusters that do not have matching tracks in the CDC are identified as photons, and the π^0 candidates are reconstructed from photon pairs. For each photon, the energy deposited in the ECL must exceed 50 (100) MeV if the cluster is found in the barrel (end-cap) region [15]. The ratio of energy deposits in the 3×3 array of crystals, centered in the crystal with the highest energy, to that of 5×5 crystal array must exceed 0.9. We

select the π^0 candidates within the $M(\gamma\gamma)$ range from 120 MeV/ c^2 to 150 MeV/ c^2 . The momentum of the π^0 candidate must be greater than 400 MeV/ c in the laboratory frame. A mass-constrained fit is also performed on the π^0 candidates to improve their momentum resolution, requiring the χ^2 value of the fit to be smaller than 100.

As a final step, the proton, K_S^0 , and π^0 candidates are combined to reconstruct Λ_c^+ candidates. The scaled momentum x_p is defined as $x_p = p^*c/\sqrt{s/4 - M^2c^4}$, where p^* is the momentum of the Λ_c^+ candidate in the center-of-mass frame, s is the square of the beam center-of-mass energy and M is invariant mass of the Λ_c^+ candidate. The requirement of $x_p > 0.54$ reduces the combinatorial background, particularly from the B meson decay. We perform a vertex fit to the three decay products requiring a common vertex. The χ^2 value of the vertex fit is required to be smaller than 40.

For $\Lambda_c^+ \rightarrow pK^-\pi^+$ decays, we reconstruct Λ_c^+ candidates using the event selection criteria typically used in other Λ_c^+ analyses with Belle [9], except that the x_p cut-off value is the same as in $\Lambda_c^+ \rightarrow pK_S^0\pi^0$ decays. For proton candidates, the same selection criteria are used as in our signal mode. For K^- and π^+ candidates, the requirements on $\mathcal{R}(e)$, DOCAs in z - and r -directions, and SVD hits are identical to those for proton candidates. However, the PID requirements are $\mathcal{R}(K|\pi) > 0.9$ and $\mathcal{R}(K|p) > 0.4$ for K^- and $\mathcal{R}(\pi|K) > 0.4$ and $\mathcal{R}(\pi|p) > 0.4$ for π^+ . We fit the three decay products to a common vertex. The χ^2 value of the vertex fit is required to be smaller than 40.

After applying all the selection criteria to the data, we observe an average of 1.04 and 1.02 candidates per event for the $\Lambda_c^+ \rightarrow pK_S^0\pi^0$ and $\Lambda_c^+ \rightarrow pK^-\pi^+$ modes within the invariant mass ranges $2.263 \text{ GeV}/c^2 < M(pK_S^0\pi^0) < 2.306 \text{ GeV}/c^2$ and $2.274 \text{ GeV}/c^2 < M(pK^-\pi^+) < 2.298 \text{ GeV}/c^2$, respectively. In addition, we find that approximately 4.0% and 1.8% of events in these modes contain multiple signal candidates. Since these multiple candidates do not contribute to the peaking background in the generic MC simulation study, we retain all candidates for further analysis.

IV. SIGNAL EXTRACTION AND EFFICIENCY CORRECTION

Figure 2 shows the $M(pK^-\pi^+)$ and $M(pK_S^0\pi^0)$ distributions after applying the event selection method described in the previous section. We perform an extended maximum likelihood fit to extract the signal decay yields from the invariant mass distributions. The Λ_c^+

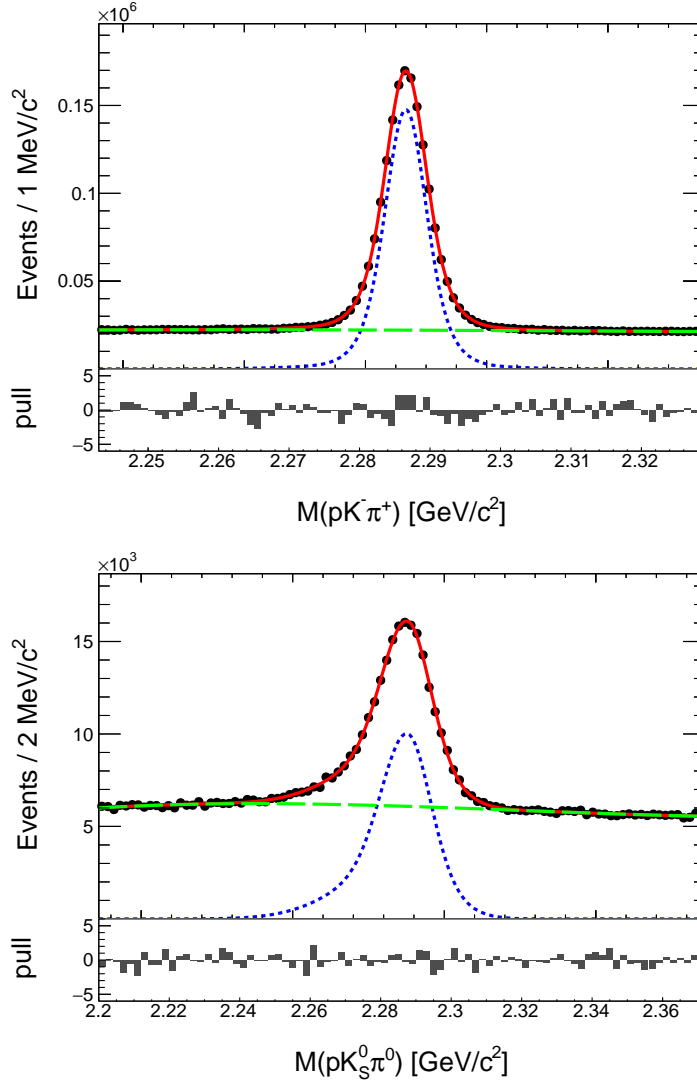


FIG. 2. Invariant mass distributions of Λ_c^+ candidates and fit results for $\Lambda_c^+ \rightarrow pK^-\pi^+$ (top) and $\Lambda_c^+ \rightarrow pK_S^0\pi^0$ (bottom). The total fit, signal, and background are shown by solid red, dashed blue, and long dashed green, respectively.

127 peak in the $M(pK^-\pi^+)$ distribution is parameterized by a sum of two Gaussian functions and
 128 one bifurcated Gaussian function, with each function sharing a common mean. To accurately
 129 model the energy loss associated with π^0 daughter γ 's in the $\Lambda_c^+ \rightarrow pK_S^0\pi^0$ decay, its signal
 130 function is taken as the sum of two bifurcated Gaussian functions sharing a common mean.
 131 A third-order polynomial function represents the combinatorial backgrounds for $M(pK^-\pi^+)$
 132 and $M(pK_S^0\pi^0)$ fits. The extracted Λ_c^+ yields for $\Lambda_c^+ \rightarrow pK^-\pi^+$ and $\Lambda_c^+ \rightarrow pK_S^0\pi^0$ decays
 133 are $(1.405 \pm 0.003) \times 10^6$ and $(1.283 \pm 0.010) \times 10^5$, respectively, where the uncertainties are

134 purely statistical.

135 The mass resolutions for $\Lambda_c^+ \rightarrow pK^-\pi^+$ decay are parameterized as follows: two Gaussians
 136 with σ values of (3.17 ± 0.02) MeV/ c^2 and (4.80 ± 0.07) MeV/ c^2 respectively, and a bifurcated
 137 Gaussian with $\sigma_{\text{left}} = (19.5 \pm 0.39)$ MeV/ c^2 and $\sigma_{\text{right}} = (10.9 \pm 0.32)$ MeV/ c^2 . The yield
 138 fractions for the two Gaussians are $(50.2 \pm 1.3)\%$ and $(42.3 \pm 0.6)\%$. For $\Lambda_c^+ \rightarrow pK_S^0\pi^0$ decay,
 139 there are two bifurcated Gaussians with σ_{left} and σ_{right} as follows: (8.19 ± 0.23) MeV/ c^2
 140 and (7.31 ± 0.27) MeV/ c^2 for the first Gaussian, and (19.5 ± 0.22) MeV/ c^2 and $(11.6 \pm$
 141 $0.30)$ MeV/ c^2 for the second Gaussian. The yield ratio between the two Gaussians is $1.07 \pm$
 142 0.07 . The uncertainties of these values are statistical only.

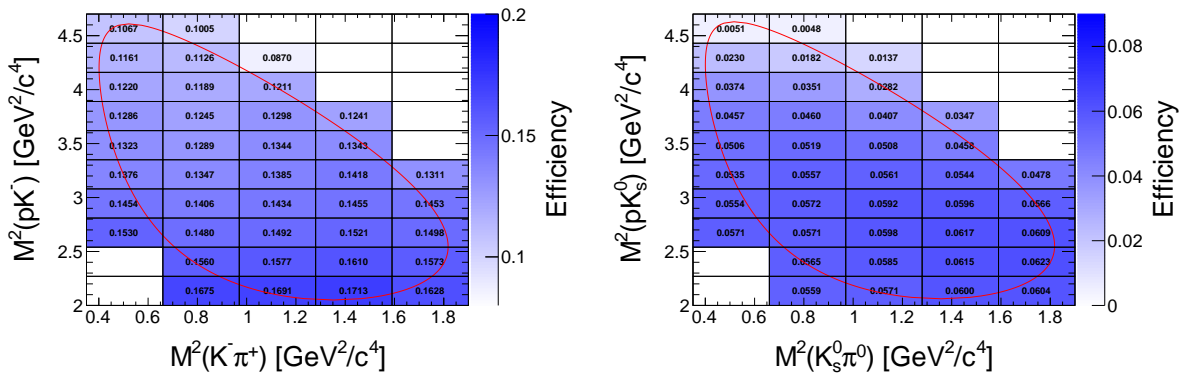


FIG. 3. Distributions of average reconstruction efficiencies over the Dalitz plots divided into the 10×5 bins of $M^2(pK)$ vs. $M^2(K\pi)$ for the $\Lambda_c^+ \rightarrow pK^-\pi^+$ (left) and the $\Lambda_c^+ \rightarrow pK_S^0\pi^0$ (right). Red contours represent the kinematic boundaries of the Dalitz plot, assuming the nominal Λ_c^+ mass.

143 As the reconstruction efficiency varies across the phase space of the Dalitz plot, as shown
 144 in Fig. 3, we perform a bin-by-bin correction to estimate the efficiency-corrected yields of
 145 both decays. To improve the resolution of the Dalitz plots, we fit the trajectories of the Λ_c^+
 146 daughters to a common vertex and use a Λ_c^+ mass constraint. The efficiency-corrected yield
 147 y^{corr} calculated via $y^{\text{corr}} = \sum_i \frac{y_i}{\epsilon_i}$, where y_i and ϵ_i are the extracted yield and reconstruction
 148 efficiency of i -th bin in the Dalitz plots, respectively. In this correction, the Dalitz plots are
 149 divided into 5×10 bins for both decays, as shown in Fig. 4. Note that the bin width of the
 150 Dalitz plots is much larger than the resolution of the data, so the effect of bin migration on
 151 y_i is negligible.

152 The yield for each bin is determined using the same functions employed for the overall

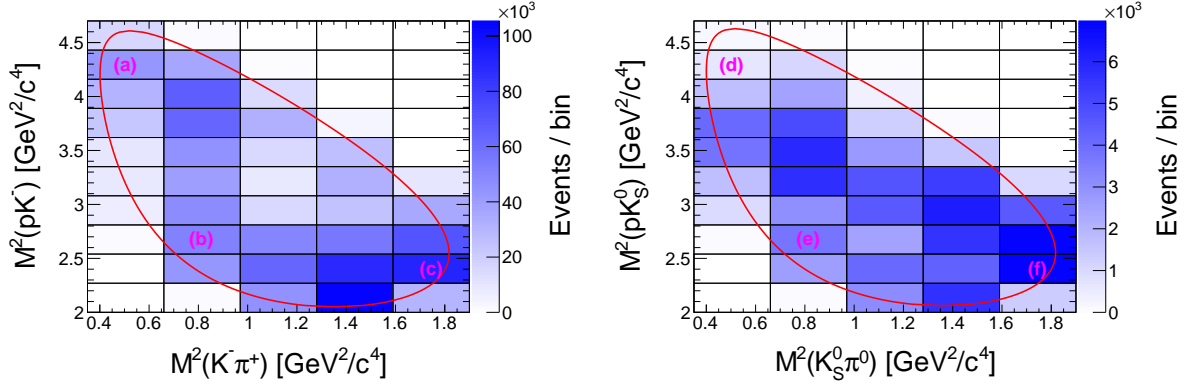


FIG. 4. Extracted signal yield for each Dalitz bin for $\Lambda_c^+ \rightarrow pK^-\pi^+$ (left) and $\Lambda_c^+ \rightarrow pK_S^0\pi^0$ (right). Fit results in the sample bins labeled from (a) to (f) are shown in Fig. 5. Red contours represent the Dalitz plot boundaries assuming the nominal Λ_c^+ mass.

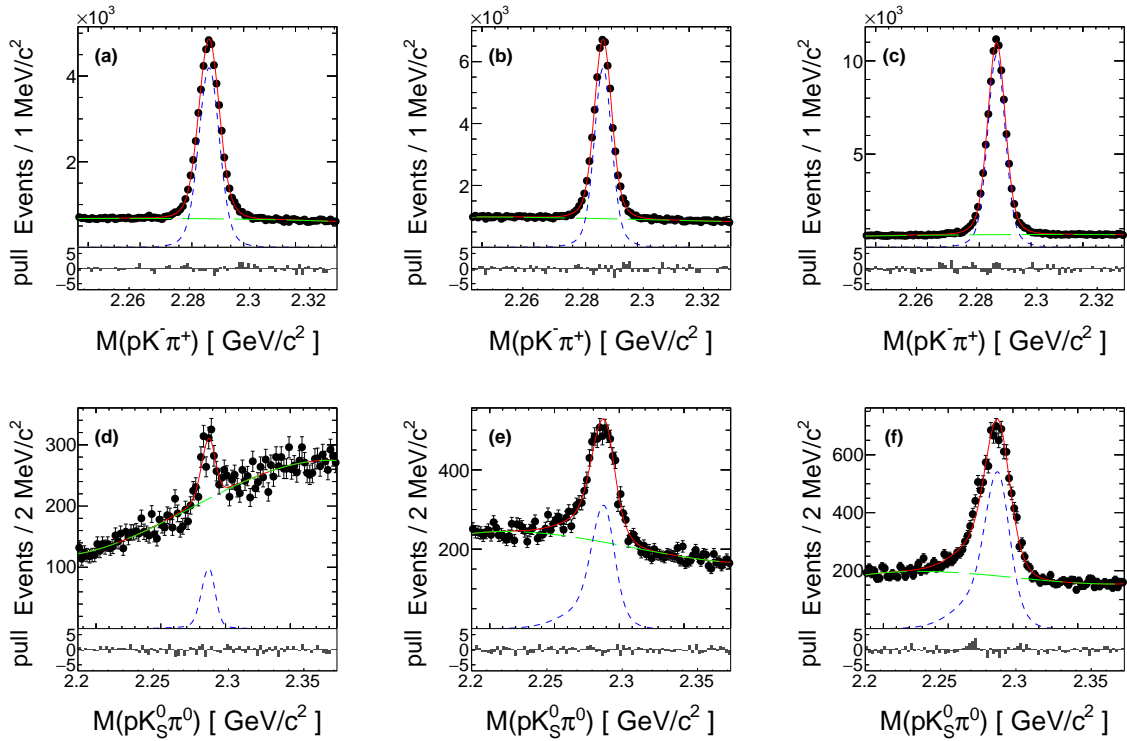


FIG. 5. Fit results (red curves) in the sample Dalitz plot bins specified in Fig. 4 for (a-c) $\Lambda_c^+ \rightarrow pK^-\pi^+$ and (d-f) $\Lambda_c^+ \rightarrow pK_S^0\pi^0$ decays. The dashed blue and long dashed green curves represent the signal and background, respectively.

153 event fit. However, all lineshape parameters, except for a common scaling factor applied
 154 to all Gaussian widths, are fixed at the values obtained from corresponding signal MC

155 samples. This scaling factor corrects for the resolution difference between the data and
 156 the MC simulation. The fitting results for typical bins are shown in Fig. 5. We determine
 157 the efficiency-corrected yields as $(9.570 \pm 0.012) \times 10^6$ for $\Lambda_c^+ \rightarrow pK^-\pi^+$ and $(2.221 \pm$
 158 $0.015) \times 10^6$ for $\Lambda_c^+ \rightarrow pK_S^0\pi^0$, where the uncertainties are statistical only. The bin-by-bin
 159 correction method enables the extraction of efficiency-corrected yields, without requiring
 160 specific models for the production of intermediate states.

161 V. BRANCHING FRACTION

162 The relative branching fraction is calculated using the following equation,

$$\frac{\mathcal{B}(\Lambda_c^+ \rightarrow pK_S^0\pi^0)}{\mathcal{B}(\Lambda_c^+ \rightarrow pK^-\pi^+)} = \frac{y^{corr}(\Lambda_c^+ \rightarrow pK_S^0\pi^0)}{y^{corr}(\Lambda_c^+ \rightarrow pK^-\pi^+) \times \mathcal{B}(\pi^0 \rightarrow \gamma\gamma) \times \mathcal{B}(K_S^0 \rightarrow \pi^+\pi^-)}, \quad (1)$$

163 where we use $\mathcal{B}(\pi^0 \rightarrow \gamma\gamma) = (98.823 \pm 0.034)\%$ and $\mathcal{B}(K_S^0 \rightarrow \pi^+\pi^-) = (69.20 \pm 0.05)\%$
 164 from Ref. [21]. By using the Eq. (1) and the efficiency-corrected yields, the relative branching
 165 fraction is determined as follows:

$$\frac{\mathcal{B}(\Lambda_c^+ \rightarrow pK_S^0\pi^0)}{\mathcal{B}(\Lambda_c^+ \rightarrow pK^-\pi^+)} = 0.339 \pm 0.002, \quad (2)$$

166 where the uncertainty is only statistical.

167 By assuming that the sum of the amplitudes, $\sqrt{2}\mathcal{A}(p\bar{K}^0\pi^0) + \mathcal{A}(pK^-\pi^+) + \mathcal{A}(n\bar{K}^0\pi^+)$,
 168 is zero as described above, we can express the amplitudes in terms of two components, \mathcal{A}_0
 169 and \mathcal{A}_1 , corresponding to the isospin amplitudes of the $I = 0$ and $I = 1$ states of the $N\bar{K}$
 170 system, respectively [2, 3]. Defining a relative phase difference (δ), between \mathcal{A}_0 and \mathcal{A}_1 as
 171 $\mathcal{A}_1/\mathcal{A}_0 = |\mathcal{A}_1/\mathcal{A}_0|e^{i\delta}$, the branching fractions are expressed as following equations:

$$\mathcal{B}(\Lambda_c^+ \rightarrow p\bar{K}^0\pi^0) = \frac{1}{2}|\mathcal{A}_1|^2, \quad (3)$$

$$\mathcal{B}(\Lambda_c^+ \rightarrow pK^-\pi^+) = \frac{1}{2}|\mathcal{A}_0|^2 + \frac{1}{4}|\mathcal{A}_1|^2 - \frac{1}{\sqrt{2}}|\mathcal{A}_0||\mathcal{A}_1|\cos\delta, \quad (4)$$

and

$$\mathcal{B}(\Lambda_c^+ \rightarrow n\bar{K}^0\pi^+) = \frac{1}{2}|\mathcal{A}_0|^2 + \frac{1}{4}|\mathcal{A}_1|^2 + \frac{1}{\sqrt{2}}|\mathcal{A}_0||\mathcal{A}_1|\cos\delta. \quad (5)$$

172 With the measured value of $\mathcal{B}(\Lambda_c^+ \rightarrow pK_S^0\pi^0)/\mathcal{B}(\Lambda_c^+ \rightarrow pK^-\pi^+)$ and the world aver-
 173 age $\mathcal{B}(\Lambda_c^+ \rightarrow n\bar{K}^0\pi^+)/\mathcal{B}(\Lambda_c^+ \rightarrow pK^-\pi^+) = 0.581 \pm 0.084$ [21], $|\delta|$ was determined to be

174 1.84 ± 0.07 , while the relative strength ($|\mathcal{A}_1|/|\mathcal{A}_0|$) was found to be 1.23 ± 0.06 , where the
 175 uncertainty is the sum in quadrature of the statistical uncertainty and the uncertainty in
 176 $\mathcal{B}(\Lambda_c^+ \rightarrow n\bar{K}^0\pi^+)/\mathcal{B}(\Lambda_c^+ \rightarrow pK^-\pi^+)$. The results show that the isospin amplitude \mathcal{A}_1 is not
 177 significantly suppressed compared to \mathcal{A}_0 in Λ_c^+ decays. Here, we note that the calculation
 178 considers only the isospin symmetry of non-resonant contributions [2].

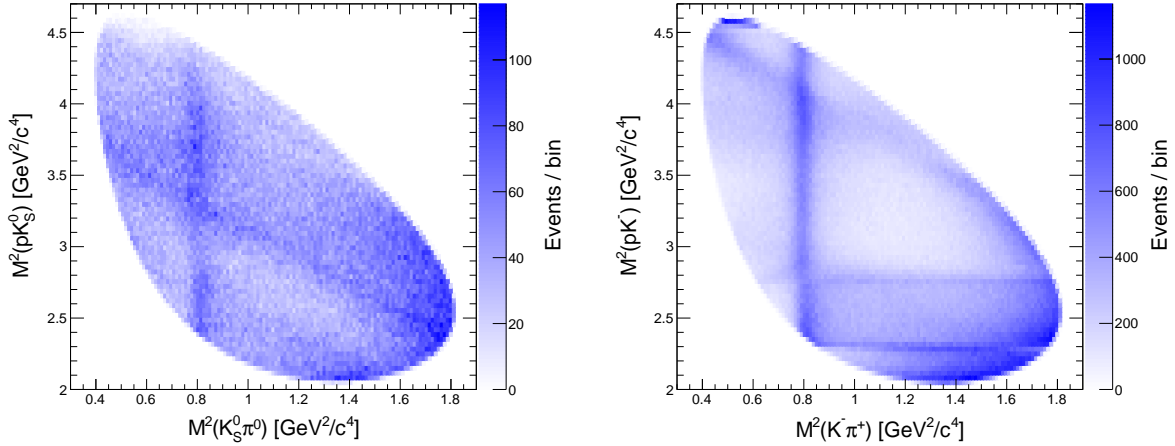


FIG. 6. Dalitz plots of the $\Lambda_c^+ \rightarrow pK_S^0\pi^0$ (left) and $\Lambda_c^+ \rightarrow pK^-\pi^+$ (right) channels within the regions $2.263 \text{ GeV}/c^2 < M(pK_S^0\pi^0) < 2.306 \text{ GeV}/c^2$ and $2.274 \text{ GeV}/c^2 < M(pK^-\pi^+) < 2.298 \text{ GeV}/c^2$, respectively. Both bin widths of x and y axes are $0.02 \text{ GeV}^2/c^4$. Non- Λ_c^+ background events shown in Fig. 2 are included in the Dalitz plots.

179 Figure 6 shows the Dalitz plot, $M^2(K_S^0\pi^0)$ vs. $M^2(pK_S^0)$ for $\Lambda_c^+ \rightarrow pK_S^0\pi^0$ decays, and
 180 several bands corresponding to intermediate resonances are observed in the plot. We inves-
 181 tigate the intermediate resonances by projecting the Dalitz plot onto the one-dimensional
 182 distributions of $M(pK_S^0)$, $M(K_S^0\pi^0)$, and $M(p\pi^0)$. We apply efficiency corrections and then
 183 subtract non- Λ_c^+ background.

184 In the $M(pK_S^0)$ distribution and the Dalitz plot of the $\Lambda_c^+ \rightarrow pK_S^0\pi^0$, as shown in Fig. 7(a)
 185 and the left of Fig. 6, respectively, Σ^* hyperons are not as prominent. However, there are
 186 distinct peak structures that might be tentatively ascribed to $\Lambda(1520)$ and $\Lambda(1670)$ hyperons
 187 in the $M(pK^-)$ distribution, as shown in Fig. 7(b). This finding is in agreement with the
 188 expectation that Λ^* hyperons are preferred over Σ^* hyperons in the π^+ emission decays [5].
 189 This could be attributed to their production dynamics being governed by color-suppressed
 190 factorizable process in the $\Lambda_c^+ \rightarrow pK_S^0\pi^0$ decay.

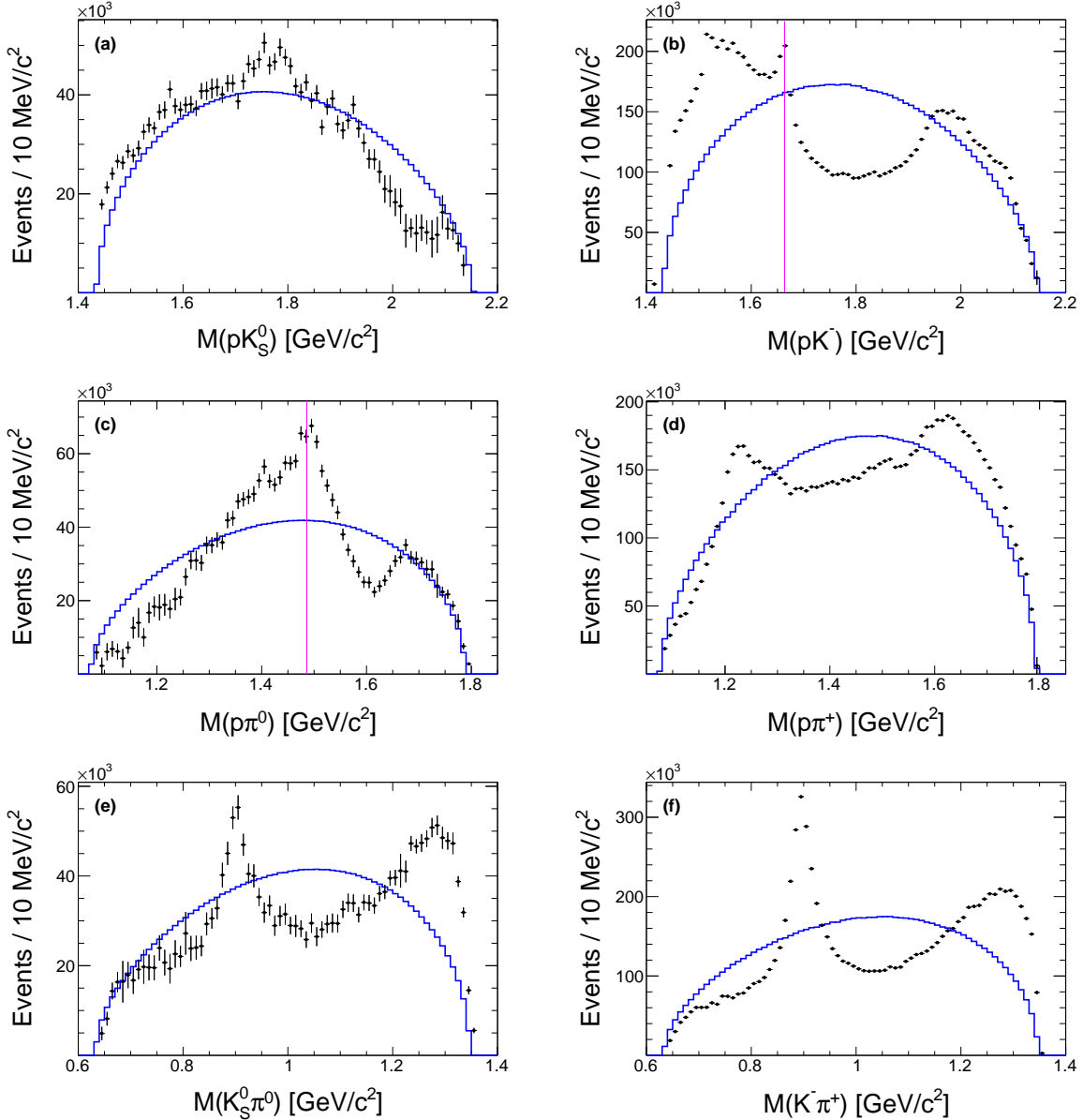


FIG. 7. Mass projection plots of $\Lambda_c^+ \rightarrow pK_S^0\pi^0$ (left) and $\Lambda_c^+ \rightarrow pK^-\pi^+$ (right) after background subtraction and efficiency correction. The projections of signal MC generated with a phase space model are superimposed in blue histograms. A clear peaking structure at the K^* resonance is seen in the $K_S^0\pi^0$ system (e), and a strong enhancement near the $p\eta$ mass threshold is found in (c). The $\Lambda\eta$ and $p\eta$ mass thresholds are marked in (b) and (c), respectively.

191 The peaking structure corresponding to $\Delta(1232)$ is much smaller in the $M(p\pi^0)$ distribu-
 192 tion of the $\Lambda_c^+ \rightarrow pK_S^0\pi^0$ sample (Fig. 7(c)) compared to the one in the $M(p\pi^+)$ distribu-
 193 tion for $\Lambda_c^+ \rightarrow pK^-\pi^+$ decays (Fig. 7(d)). This suppression can be attributed to the preference

194 for the production of the $\Delta^{++}K^-$ channel over the $\Delta^+\bar{K}^0$ channel, as required by isospin
 195 symmetry. Furthermore, a clear peaking structure near the $p\eta$ mass threshold is evident
 196 in the $M(p\pi^0)$ distribution of $\Lambda_c^+ \rightarrow pK_S^0\pi^0$ decay. This peak corresponds to the diagonal
 197 band observed in the Dalitz plot to the left of Fig. 6. The same effect was observed in the
 198 $\Lambda_c^+ \rightarrow pK_S^0\eta$ study in Ref. [22]. The similarity of this effect and the $\Lambda\eta$ threshold cusp, which
 199 was found to be amplified by the $\Lambda(1670)$ in the pK^- system as shown in Fig. 7(b) [10, 23],
 200 suggests that the peak near the $p\eta$ threshold in the Fig. 7(c) may also be attributed to a
 201 threshold cusp enhanced by the $N(1535)^+$.

202 Both $\Lambda_c^+ \rightarrow pK^-\pi^+$ and $\Lambda_c^+ \rightarrow pK_S^0\pi^0$ decays exhibit a peaking structure corresponding
 203 to the vector resonance $K^*(892)^0$, as shown in Fig. 7(e) and (f). In the region where high-
 204 mass K^* mesons are expected, a clear enhancement with respect to phase space is seen in
 205 both decay modes. To further understand the role of isospin symmetry in the Λ_c^+ decays
 206 and extend our understanding of intermediate states such as Λ^* , Σ^* , Δ^* , and N^* resonances,
 207 an amplitude analysis with the helicity formalism of these two channels is planned for the
 208 near future.

209 VI. SYSTEMATIC UNCERTAINTY

210 The systematic uncertainties of branching fractions are listed in Table I. The K_S^0 recon-
 211 struction imposes a systematic uncertainty that has been estimated using a control sample of
 212 $D^{*\pm} \rightarrow D^0\pi^\pm (D^0 \rightarrow K_S^0\pi^0)$ events. In the control sample study, the momentum-dependent
 213 K_S^0 reconstruction efficiency was compared between the data and MC samples. In a sim-
 214 ilar way, the π^0 reconstruction uncertainty was determined by a study in Ref. [24] using
 215 $\tau^- \rightarrow \pi^-\pi^0\nu_\tau$ events. Here, the difference in efficiency for $M(\gamma\gamma)$ selection between data
 216 and MC samples is also added in quadrature to the systematic uncertainty.

217 The uncertainty due to the background model shown in Fig. 5 is estimated by changing
 218 it to a second-order polynomial and a fourth-order polynomial. We estimate the systematic
 219 uncertainty resulting from the signal functions by performing one thousand fits, in which
 220 we vary the lineshape parameters fixed from the signal MC samples, within their respective
 221 statistical uncertainties. The systematic uncertainty is the standard deviation of the fit
 222 results. The quadratic sum of the systematic uncertainties arising from the background
 223 model and the signal function is referred to as “fit function” in Table I.

TABLE I. Sources of systematic uncertainties for the relative branching fraction, $\mathcal{B}(\Lambda_c^+ \rightarrow pK_S^0\pi^0)/\mathcal{B}(\Lambda_c^+ \rightarrow pK^-\pi^+)$.

Sources	Value (%)
K_S^0 reconstruction	1.57
π^0 reconstruction	1.54
Fit function	0.60
MC statistics	0.58
Dalitz plot binning	0.68
PID of K^- and π^+	0.34
Tracking of K^- and π^+	0.70
Total	2.57

224 We include the statistical uncertainty of the signal MC samples used in the efficiency
 225 corrections across the Dalitz plots as a systematic uncertainty. We estimate the systematic
 226 uncertainties arising from the size of the Dalitz bins by modifying the Dalitz binning from
 227 the initial configuration of 5×10 to include the following configurations: 4×8 , 4×10 ,
 228 5×8 , 5×12 , 6×10 , and 6×12 . The largest difference obtained is attributed to a
 229 corresponding systematic uncertainty.

230 The systematic uncertainty from K^- and π^+ PIDs in $\Lambda_c^+ \rightarrow pK^-\pi^+$ decay is calculated
 231 based on the $D^{*+} \rightarrow D^0\pi^+(D^0 \rightarrow K^-\pi^+)$ control sample. Similar to the K_S^0 reconstruction,
 232 the PID efficiency as a function of momentum and polar angle in the laboratory frame is
 233 compared between data and MC samples. The systematic uncertainty attributed to tracking
 234 is 0.35% for each K^- and π^+ track in $\Lambda_c^+ \rightarrow pK^-\pi^+$ decay.

235 The uncertainties in the PDG values of $\mathcal{B}(\pi^0 \rightarrow \gamma\gamma)$ and $\mathcal{B}(K_S^0 \rightarrow \pi^+\pi^-)$ in Ref. [21]
 236 are negligible, so these contributions are not included in the systematic uncertainty. Other
 237 systematic uncertainties cancel out for the relative branching fraction measurements due
 238 to the similar kinematic distributions of the final state particles from $\Lambda_c^+ \rightarrow pK_S^0\pi^0$ and
 239 $\Lambda_c^+ \rightarrow pK^-\pi^+$ decays.

VII. SUMMARY

We study the $\Lambda_c^+ \rightarrow pK_S^0\pi^0$ decay using the full Belle dataset of 980 fb^{-1} at or near the $\Upsilon(nS)$ ($n = 1, 2, 3, 4,$ and 5) resonances. The branching fraction of $\Lambda_c^+ \rightarrow pK_S^0\pi^0$ relative to $\Lambda_c^+ \rightarrow pK^-\pi^+$ is determined as

$$\frac{\mathcal{B}(\Lambda_c^+ \rightarrow pK_S^0\pi^0)}{\mathcal{B}(\Lambda_c^+ \rightarrow pK^-\pi^+)} = 0.339 \pm 0.002 \pm 0.009, \quad (6)$$

where the uncertainties are statistical and systematic, respectively. Using the PDG value of $\mathcal{B}(\Lambda_c^+ \rightarrow pK^-\pi^+) = (6.26 \pm 0.29)\%$ in Ref. [21], we obtain the following absolute branching fraction for $\Lambda_c^+ \rightarrow pK_S^0\pi^0$:

$$\mathcal{B}(\Lambda_c^+ \rightarrow pK_S^0\pi^0) = (2.13 \pm 0.01 \pm 0.05 \pm 0.11)\%, \quad (7)$$

241 where the uncertainties are statistical, systematic from this experiment and analysis, and
 242 due to the uncertainty in $\mathcal{B}(\Lambda_c^+ \rightarrow pK^-\pi^+)$, respectively. The measured branching fraction
 243 is consistent with the previous measurement by CLEO and has a fivefold improvement in
 244 precision [13].

245 Assuming isospin symmetry, we calculate that the ratio of the isospin amplitudes for $I = 1$
 246 to $I = 0$ in the $N\bar{K}$ system is determined to be $1.23 \pm 0.03 \pm 0.06$, and the relative phase
 247 difference is obtained to be $1.842 \pm 0.001 \pm 0.069$, where the first uncertainty denotes the
 248 total uncertainty and the second uncertainty is from $\mathcal{B}(\Lambda_c^+ \rightarrow n\bar{K}^0\pi^+)/\mathcal{B}(\Lambda_c^+ \rightarrow pK^-\pi^+)$.
 249 These values are consistent with previous results [3]. However, we do not find a strong
 250 enhancement due to Σ^* resonances in the $M(pK_S^0)$ distribution of $\Lambda_c^+ \rightarrow pK_S^0\pi^0$ decay.
 251 These results indicate that factors beyond isospin symmetry, such as resonant contributions,
 252 cannot be neglected.

253 In addition, we observe a clear peaking structure in the $p\pi^0$ system near the $p\eta$ threshold,
 254 which may be attributed to a threshold cusp enhanced by $N(1535)^+$. Further amplitude
 255 analysis is required to understand the contributions of intermediate resonances such as K^* ,
 256 Λ^* , Σ^* , Δ^* , and N^* resonances, as well as to estimate the non-resonant contribution. Such
 257 a comprehensive approach will lead to stringent tests of isospin symmetry by comparing the
 258 partial branching ratios between $\Lambda_c^+ \rightarrow pK^-\pi^+$ and $\Lambda_c^+ \rightarrow pK_S^0\pi^0$ decays. This approach
 259 could also contribute to a better understanding of non-factorizable processes in the non-
 260 leptonic decay of charmed baryons.

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