

# Two-Photon Physics results from Belle and perspectives for Belle II

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PhiPsi2017 @ Mainz



PHIPSI: INTERNATIONAL WORKSHOP  
on  $e^+e^-$  collisions from Phi to Psi 2017

**Phi<sup>17</sup>**  
Psi

26-29 June 2017  
Mainz, Germany

**BELLE**

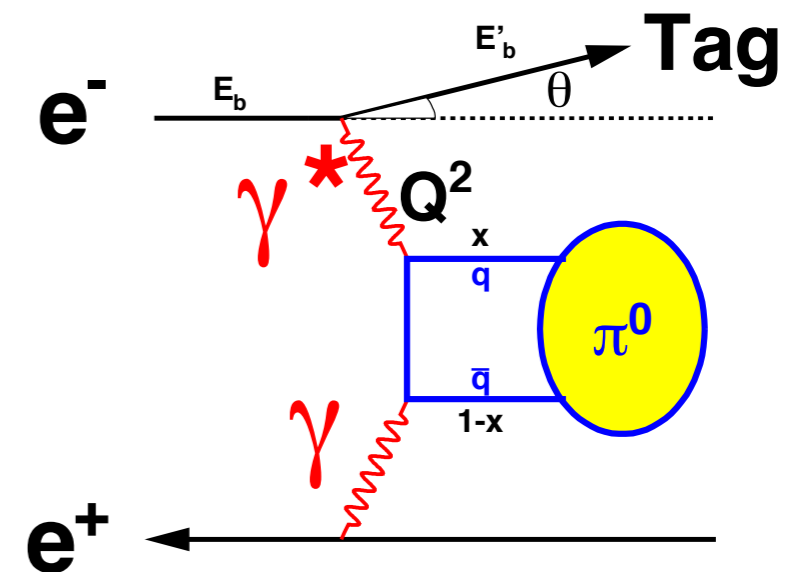
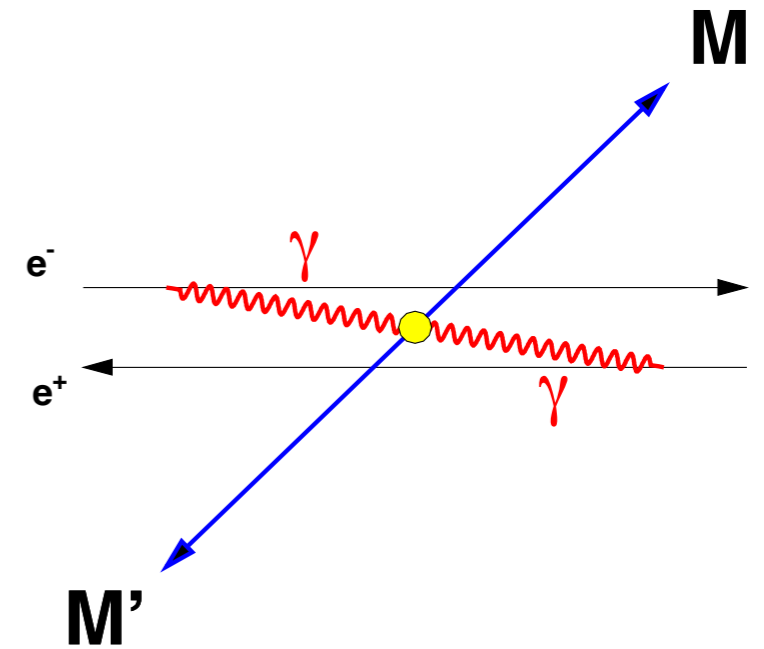
The banner features a dark background with a technical illustration of a particle detector on the left and a line graph on the right. The text is overlaid in white and red. The Belle logo is prominently displayed on a blue rectangular background on the right side.

# Contents

★ Two-Photon Physics at Belle

★ No-tag measurements

★ Single-tag measurements



# Two-Photon Process at Belle

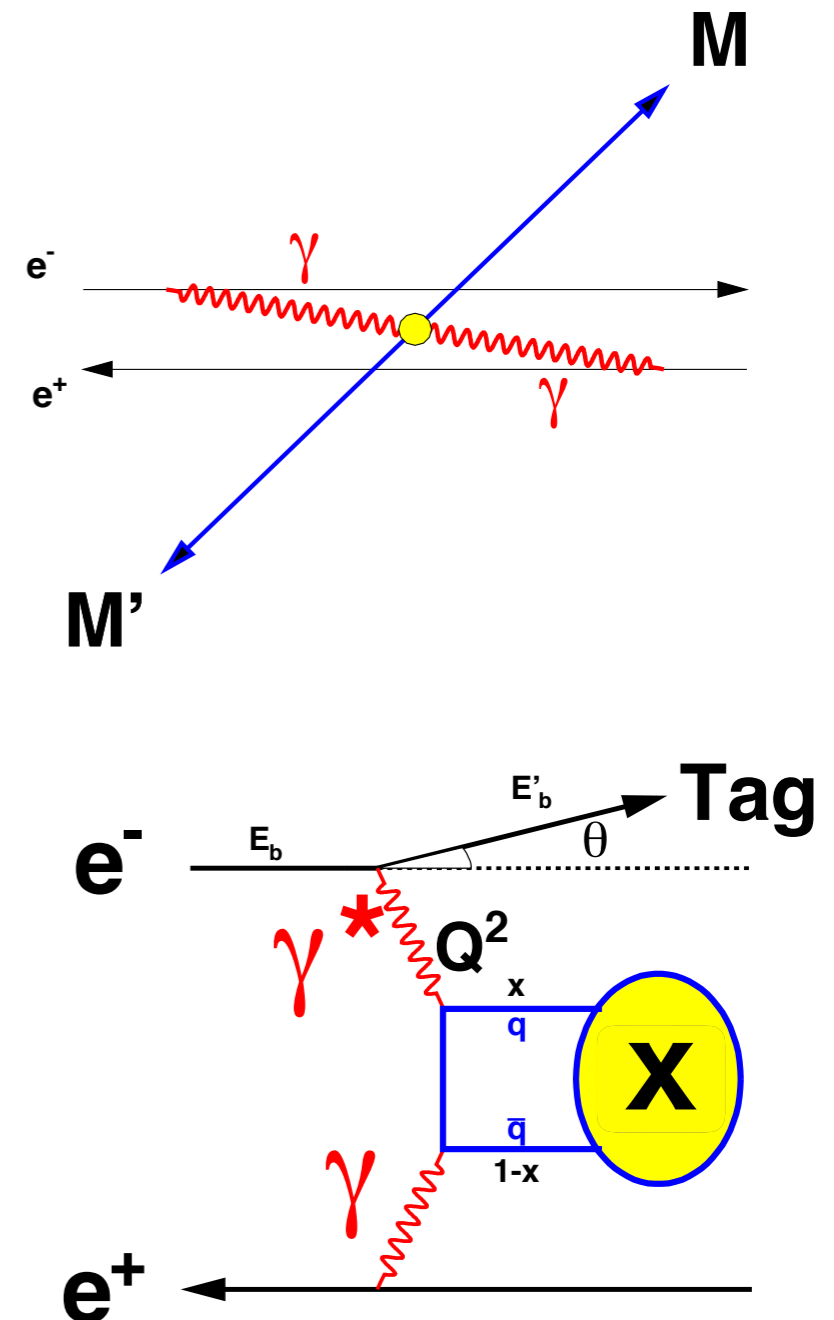
★ Reaction by virtual photons from each beam particle

★ Beam particles do not annihilate

★ Photon virtuality

$$Q^2 = 4E_b E' \sin^2 \frac{\theta_e}{2}$$

★  $W = M(\gamma\gamma) = M(\text{hadronic system})$



# Two-Photon Measurements at Belle

	GeV	$ \cos\theta^*  <$	fb <sup>-1</sup>	reference	year
$\gamma J/\psi$	3.2 - 3.8		32.6	PLB540, 33	2002
$\pi^+\pi^-$	2.4 - 4.1	0.6	88	PLB15, 39	2005
	0.8 - 1.5	0.6	86	PRD75, 051101	2007
				JPhySocJpn76, 074102	2007
$K^+K^-$	1.4 - 2.4	0.6	67	EPJC32, 323	2003
	2.4 - 4.1	0.6	88	PLB15, 39	2005
ppbar	2.0 - 4.0	0.6	89	PLB621, 41	2005
4 mesons	2.75 - 3.75		395	EPJC53, 1	2006
$K_sK_s$	2.4 - 4.0	0.6	398	PLB651, 15	2007
	1.05 - 4.0	0.8	972	PTEP2013, 123C01	2013
$\pi^0\pi^0$	0.6 - 4.0	0.8	95	PRD78, 052004	2008
	0.6 - 4.1	0.8	223	PRD79, 052009	2009
$\eta\pi^0$	0.84 - 4.0	0.8	223	PRD80, 032001	2009
$\eta\eta$	1.096 - 3.8	1.0	393	PRD82, 114031	2010
$\omega J/\psi$	3.9 - 4.2		694	PRL104, 092001	2010
$\phi J/\psi$	4.2 - 5.0		825	PRL104, 112004	2010
$\omega\omega, \omega\phi, \phi\phi$	thr - 4.0		870	PRL108, 232001	2012
$\eta'\pi^+\pi^-$	1.4 - 3.4		673	PRD86, 052002	2012
$\pi^0$	$Q^2 \in [4, 40] \text{GeV}^2$		759	PRD86, 092007	2012
$\pi^0\pi^0$	$Q^2 < 30 \text{GeV}^2$		759	PRD93, 032003	2016
ppbar $K^+K^-$	3.2 - 5.6		980	PRD93, 112017	2016

# Two-Photon Process by real photons

## No-tag method

★ Collision by two quasi-real photons

★ Dominant two-photon process.  
High Xsec compared with single-tag.

★  $e^+ e^-$  escape to beam pipe with small recoil angle.  
Must not be detected.

★  $\left| \sum_i \vec{p}_t(M_i) \right| \sim 0$  for detected final state particles

★ Translate the result to Xsec by real two-photons

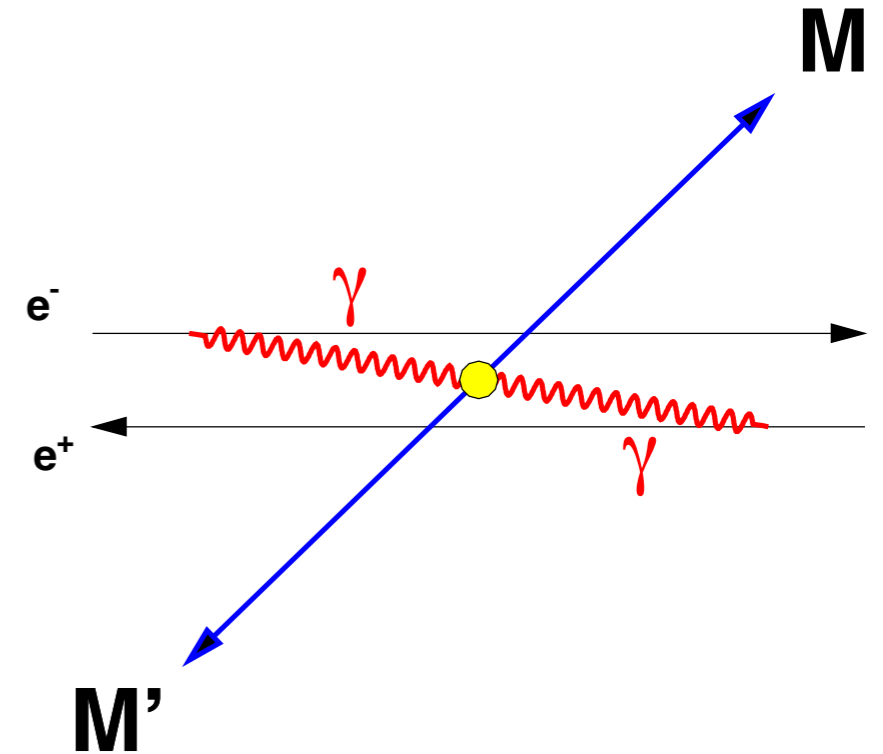
★ W spectrum

★ Final state of  $J^{PC} = 0^{++}, 2^{++}, 3^{++}, \dots$ . **C=+ resonance study.**

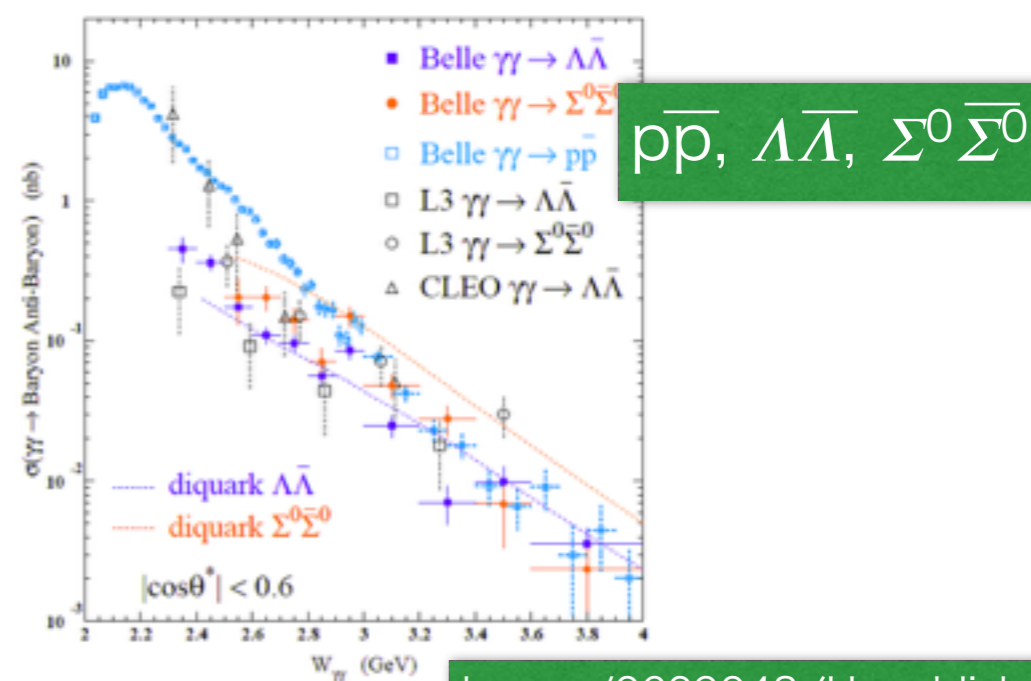
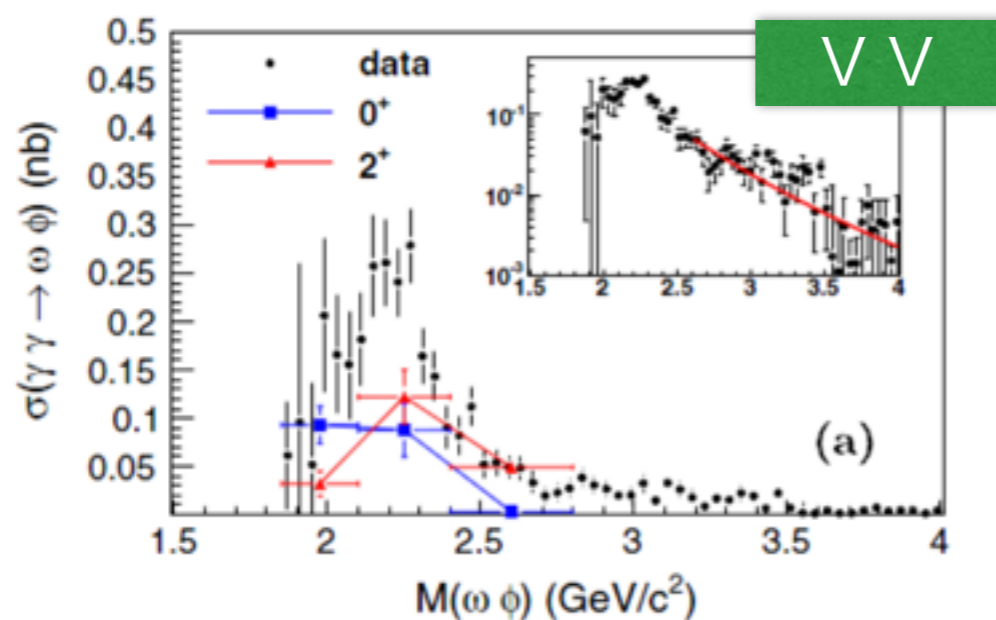
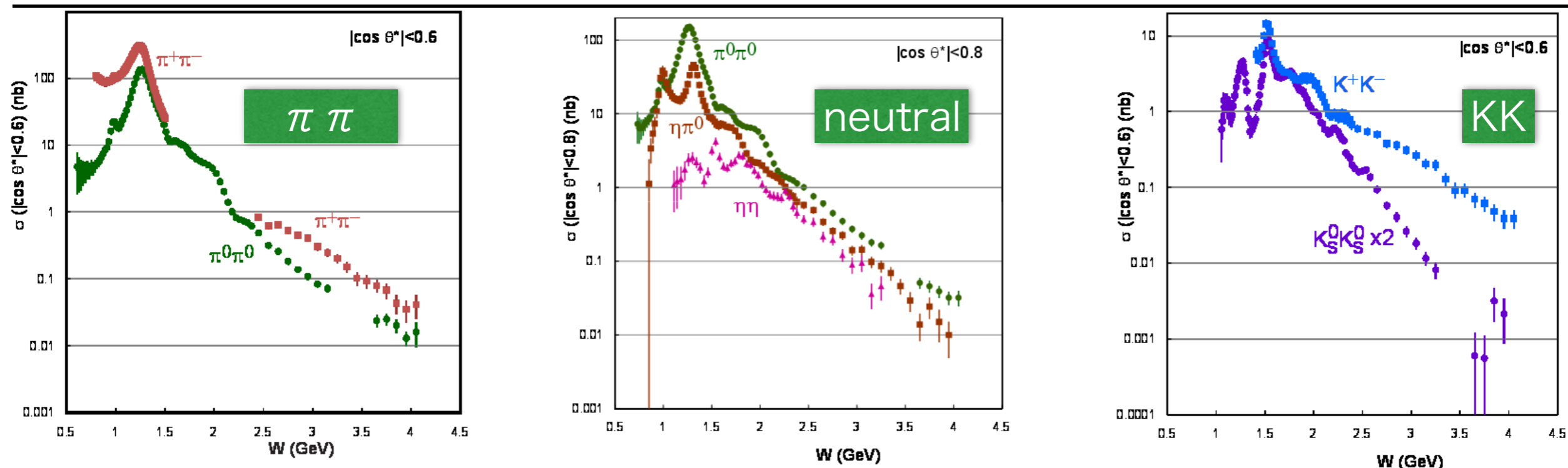
★ Hadron Pair production

$$\frac{d\sigma}{d|\cos\theta^*|} = \frac{\Delta N}{\Delta W \Delta|\cos\theta^*| \frac{dL_{\gamma\gamma}}{dW} \epsilon(W, |\cos\theta^*|) \int \mathcal{L} dt}$$

$$\sigma(e^+e^- \rightarrow e^+e^- X) = \int \sigma(\gamma\gamma \rightarrow X; W) \frac{dL_{\gamma\gamma}}{dW} dW$$



# Cross Sections for hadron pair production in no-tag measurements



hep-ex/0609048 (Unpublished)

Wide  $W$  region can be measured at once

# Light Meson Study using Partial Wave Analysis

## No-tag measurements in lower W region ( $W < 3\text{GeV}$ )

$$\begin{aligned}\frac{d\sigma}{4\pi d|\cos\theta^*|}(\gamma\gamma \rightarrow MM') &= |SY_0^0 + D_0Y_2^0 + G_0Y_4^0|^2 + |D_2Y_2^2 + G_2Y_4^2|^2 \\ &= \hat{S}^2|Y_0^0|^2 + \hat{D}_0^2|Y_2^0|^2 + \hat{D}_2^2|Y_2^2|^2 + \hat{G}_0^2|Y_4^0|^2 + \hat{G}_2^2|Y_4^2|^2\end{aligned}$$

- ★ Two-photon spin-helicity state  $(J, \lambda) = (0, 0), (2, 0), (2, \pm 2)$
- ★  $S, D_\lambda, G_\lambda$  waves for final hadronic systems
- ★  $S, D_\lambda, G_\lambda$  have W dependence;  
Breit-Wigner + Non-resonant component

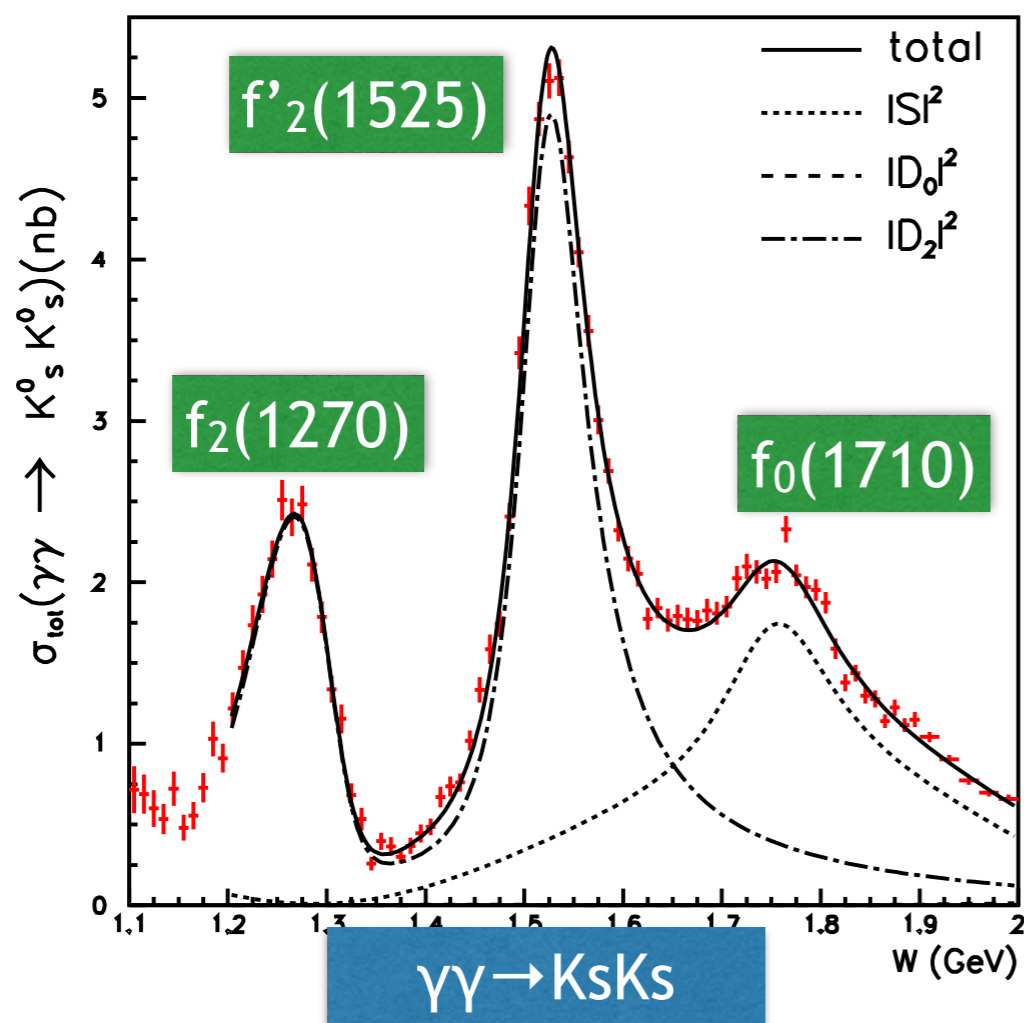
$$A(f_0) = \sqrt{\frac{8\pi m_{f_0}}{W} \frac{\sqrt{\Gamma_{f_0}\Gamma_{\gamma\gamma}(f_0)\mathcal{B}(K\bar{K})}}{m_{f_0}^2 - W^2 - im_{f_0}\Gamma_{f_0}}}$$

- ★ Two-photon decay width  $\Gamma_{\gamma\gamma}$ 
  - ★ Useful to study the nature of the resonance  
glueballs, four quark states, ...

# Light Meson Study using Partial Wave Analysis

## No-tag measurements in lower W region ( $W < 3\text{GeV}$ )

- ★ Abundant data in this region but too many parameters.
- ★ Needs more data.



Mode	Resonance	Mass (MeV/c <sup>2</sup> )	Width (MeV)	$\Gamma_{\gamma\gamma}$ (eV), $(J, \lambda) = \begin{cases} (2, 2) \\ (0, 0) \end{cases}$
$\pi^+\pi^-$	$f_0(980)$	$985.6^{+1.2+1.1}_{-1.5-1.6}$	$34.2^{+13.9+8.8}_{-11.8-2.5}$	$205^{+95+147}_{-83-117}$
	$\eta'(958)$	$B(\pi^+\pi^-) < 2.9 \times 10^{-3}$ (with interference), $3.3 \times 10^{-4}$ (without)		
$K^+K^-$	$f'_2(1525)$	$1518 \pm 1 \pm 3$	$82 \pm 2 \pm 3$	$28.2 \pm 2.4 \pm 5.8/B$
	$f_J/f_0/a_2$	$1737 \pm 5 \pm 7$	$151 \pm 22 \pm 24$	$\begin{cases} 10.3 \pm 2.1 \pm 2.3/B \\ 76 \pm 15 \pm 17/B \end{cases}$
	$f_2(2010)$	$1980 \pm 2 \pm 14$	$297 \pm 12 \pm 6$	$61 \pm 2 \pm 3/B$
	$f_J/f_2$	$2327 \pm 9 \pm 6$	$275 \pm 36 \pm 20$	$\begin{cases} 22 \pm 3 \pm 6/B \\ 161 \pm 22 \pm 48/B \end{cases}$
$K_S^0 K_S^0$	$f'_2(1525)$	$1525.3^{+1.2+3.7}_{-1.4-2.1}$	$82.9^{+2.1+3.1}_{-2.2-2.0}$	$48^{+67+108}_{-8-12}/B(K\bar{K})$
	$f_0(1710)$	$1750^{+6+29}_{-7-18}$	$139^{+11+96}_{-12-50}$	$12^{+3+227}_{-2-8}/B(K\bar{K})$
	$f_2(2200)$	$2243^{+7+3}_{-6-29}$	$145 \pm 12^{+27}_{-34}$	$3.2^{+0.5+1.3}_{-0.4-2.2}/B(K\bar{K})$
$\pi^0\pi^0$	$f_0(2500)$	$2539 \pm 14^{+38}_{-14}$	$274^{+77+126}_{-61-163}$	$40^{+9+17}_{-7-40}/B(K\bar{K})$
	$f_0(980)$	$982.2 \pm 1.0^{+8.1}_{-8.0}$		$286 \pm 17^{+211}_{-70}$
	$f_2(1270)$	fixed	fixed	$B(f_2 \rightarrow \gamma\gamma) = (1.57 \pm 0.01^{+1.39}_{-0.14}) \times 10^{-5}$
	$f_0(Y)$	$1470^{+6+72}_{-7-255}$	$90^{+2+50}_{-1-22}$	$11^{+4+603}_{-2-7}/B$
	$f_2(1950)$	$2038^{+13}_{-11}$	$441^{+27}_{-25}$	$54^{+23}_{-14}/B$
	$f_4(2050)$	$1884^{+14+218}_{-13-25}$	$453 \pm 20^{+31}_{-129}$	$136^{+24+415}_{-22-91}$
	$\eta\pi^0$	$a_0(980)$	$982.3^{+0.6+3.1}_{-0.7-4.7}$	$75.6 \pm 1.6^{+17.4}_{-10.0}$
$a_0(Y)$		$1316.8^{+0.7+24.7}_{-1.0-4.6}$	$65.0^{+2.1+99.1}_{-5.4-32.6}$	$432 \pm 6^{+1073}_{-256}/B$
$a_2(1320)$		fixed	fixed	$145^{+97}_{-34}/B$
$\eta\eta$	$f_0(Y)$	$1262^{+51+82}_{-78-103}$	$484^{+246+246}_{-170-263}$	$121^{+133+169}_{-53-106}/B$
	$f_2(1270)$	fixed	fixed	$11.5^{+1.8+4.5}_{-2.0-3.7}/B$
	$f_2(X)$	$1737 \pm 9^{+198}_{-65}$	$228^{+21+234}_{-20-153}$	$5.2^{+0.9+37.3}_{-0.8-4.5}/B$



# W-dependence of Xsec, $\sigma_0 \propto W^{-n}$

## No-tag measurements in higher W region

- ★ Resonance effects small above 3.0 GeV
- ★ Good place to study (p)QCD
- ★ pQCD prediction

$$\mathcal{M}_{\lambda_1 \lambda_2}(W^2, \theta^*) = \int_0^1 \int_0^1 dx dy \phi_M(x, Q_x) \phi_{M'}(y, Q_y) T_{\lambda_1 \lambda_2}(x, y, \theta^*)$$

PRD24, 1808

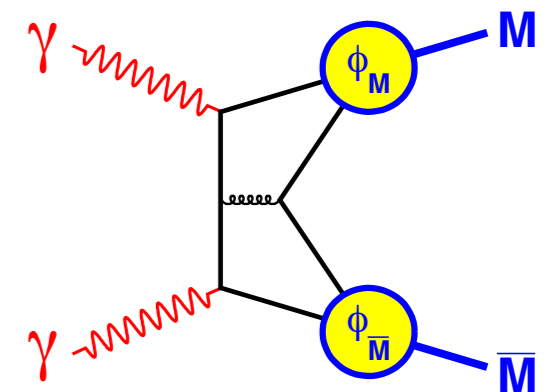
$$\frac{d\sigma}{d|\cos \theta^*|} = 16\pi\alpha^2 \frac{|F_M(W^2)|^2}{W^2} \left\{ \frac{(e_1 - e_2)^4}{\sin^4 \theta^*} + \frac{2e_1 e_2 (e_1 - e_2)^2}{\sin^2 \theta^*} g(\theta^*) + 2e_1^2 e_2^2 g^2(\theta^*) \right\}$$

$F_M$  Meson form factor.  $\sim 1/W^2$  at leading term

$\phi_M$  Meson distribution amplitude (DA)

$T_{\lambda_1 \lambda_2}$  Hard Scattering amplitude for

$g(\theta^*)$  Only unknown, non-perturbative factor



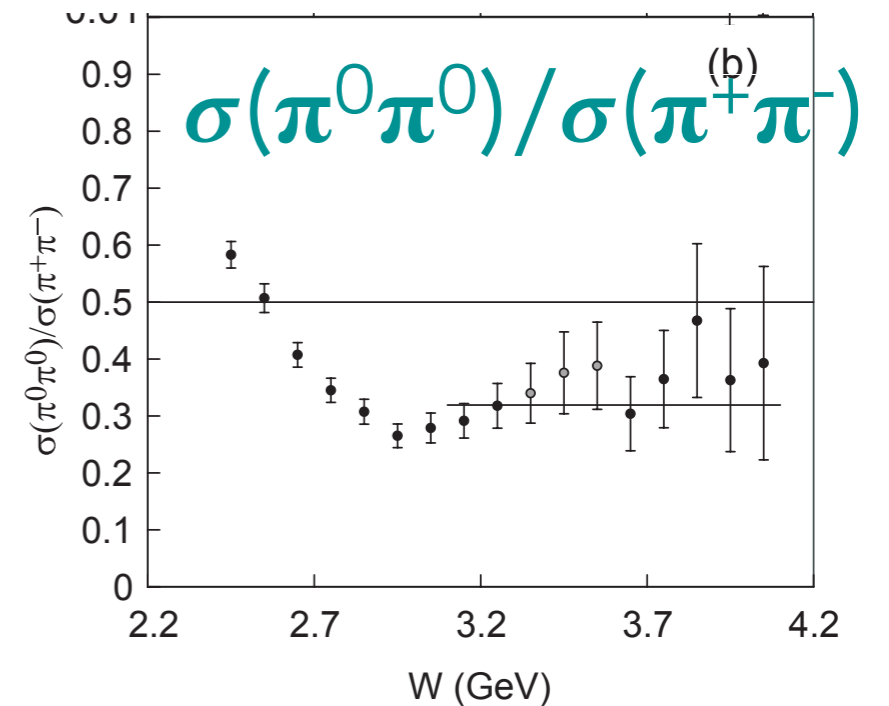
- $\sigma \sim W^{-6}$  for charged pair,  $\sigma \sim W^{-10}$  for neutral and ppbar
- At which energy is enough high to apply pQCD?

# W-dependence of Xsec, $\sigma_0 \propto W^{-n}$

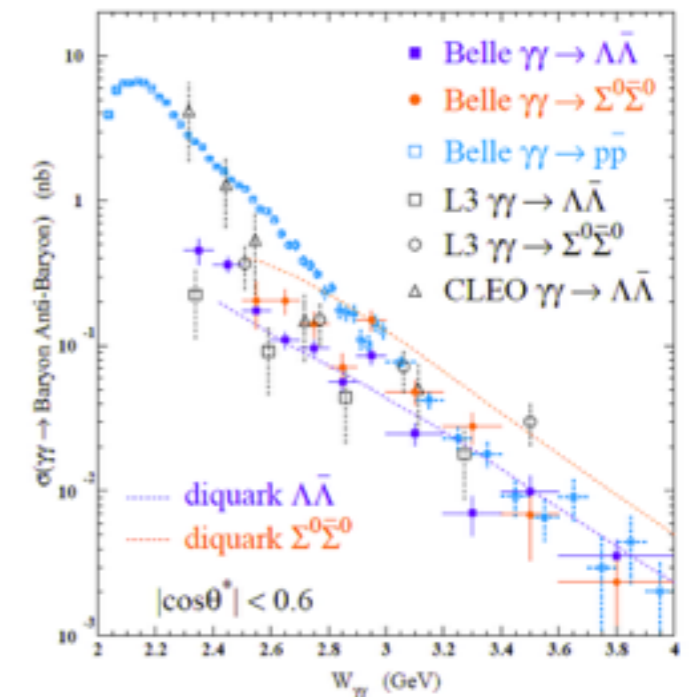
## No-tag measurements in higher W region

	pQCD[2]	Belle	W(GeV)	$ \cos\theta^*  <$
$\pi^+\pi^-$	6	$7.9 \pm 0.4 \pm 1.5$	3.0-4.1	0.6
K <sup>+</sup> K <sup>-</sup>	6	$7.3 \pm 0.3 \pm 1.5$	3.0-4.1	0.6
KsKs	10	$10.5 \pm 0.6 \pm 0.5$	2.4-4.0	0.6
KsKs	10	$11.0 \pm 0.4 \pm 0.4$	2.6-4.0	0.8
$\pi^0\pi^0$	10	$8.0 \pm 0.5 \pm 0.4$	3.1-4.1	0.8
ppbar	10	$12.4 \pm 2.4 \pm 2.3$	3.2-4.0	0.6

pQCD: PRD24,1808(1981), NPB329,285(1990)

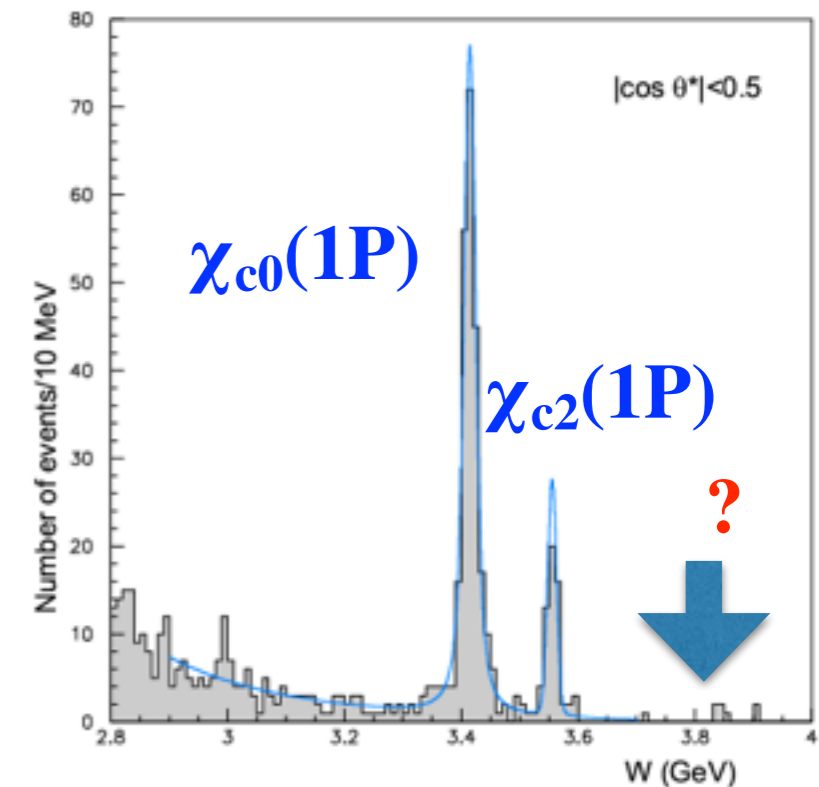
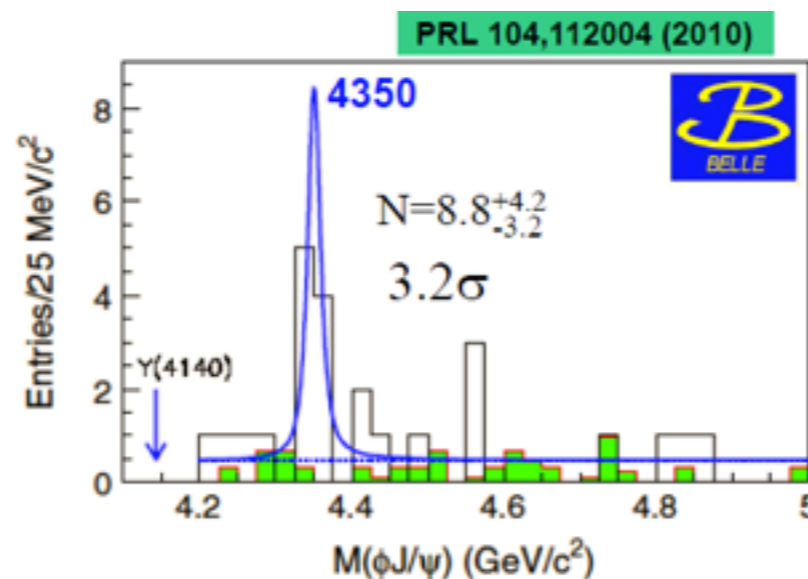
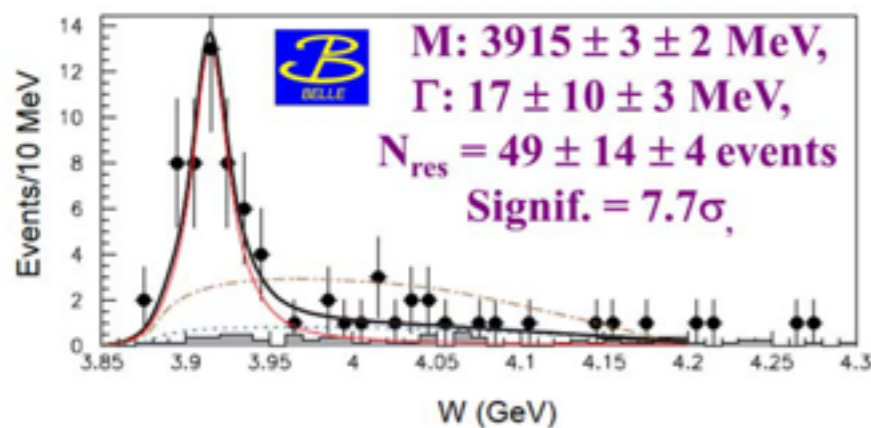
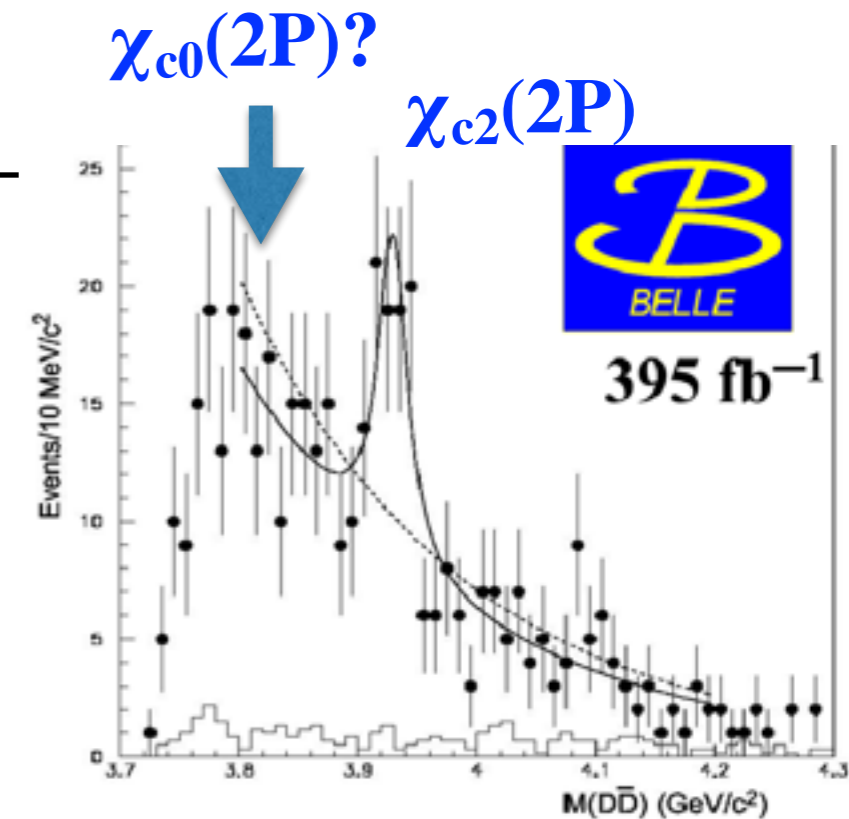


- ★  $\sigma(\pi^0\pi^0)/\sigma(\pi^+\pi^-) \sim$  constant. Disagree with pQCD.
- ★  $\sigma(\Lambda\Lambda)/\sigma(\text{ppbar}) \sim 1$ . Possible for different quark charge?
- ★ At Belle  $W < 4.0$ . At Belle II, as large W as possible, but e<sup>+</sup>e<sup>-</sup> annihilation bkg significant
- ★ Neutral modes relatively clean, but low Xsec



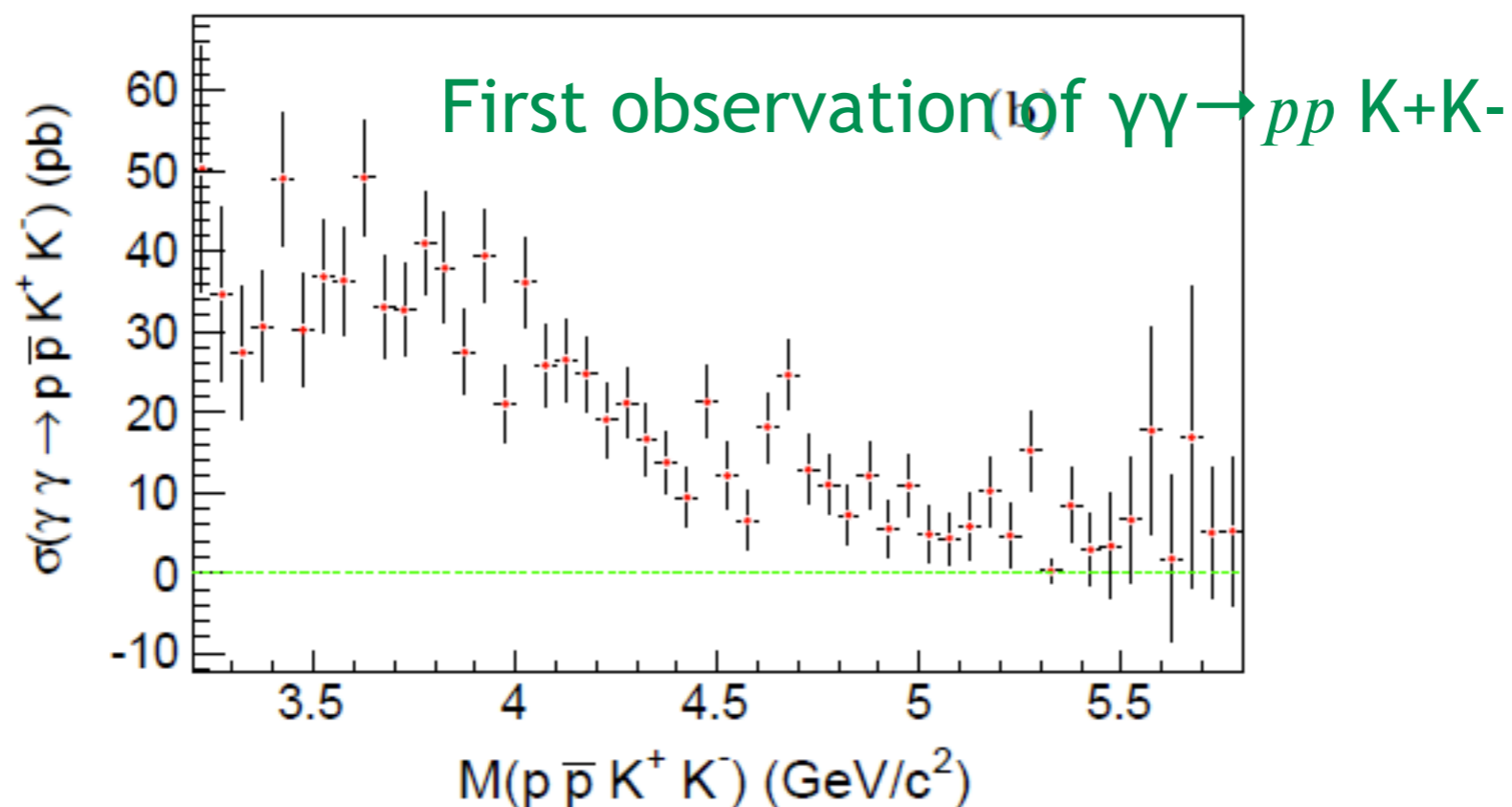
# charmonia and XYZ

- ★ X(3915) and X(4350) found, but nature unknown
- ★ X(3915) is no longer  $\chi_{c0}(2P)$ . Where is it?
- ★  $\chi_{c2}(2P) \rightarrow DD^* \rightarrow DDX$  should be treated carefully

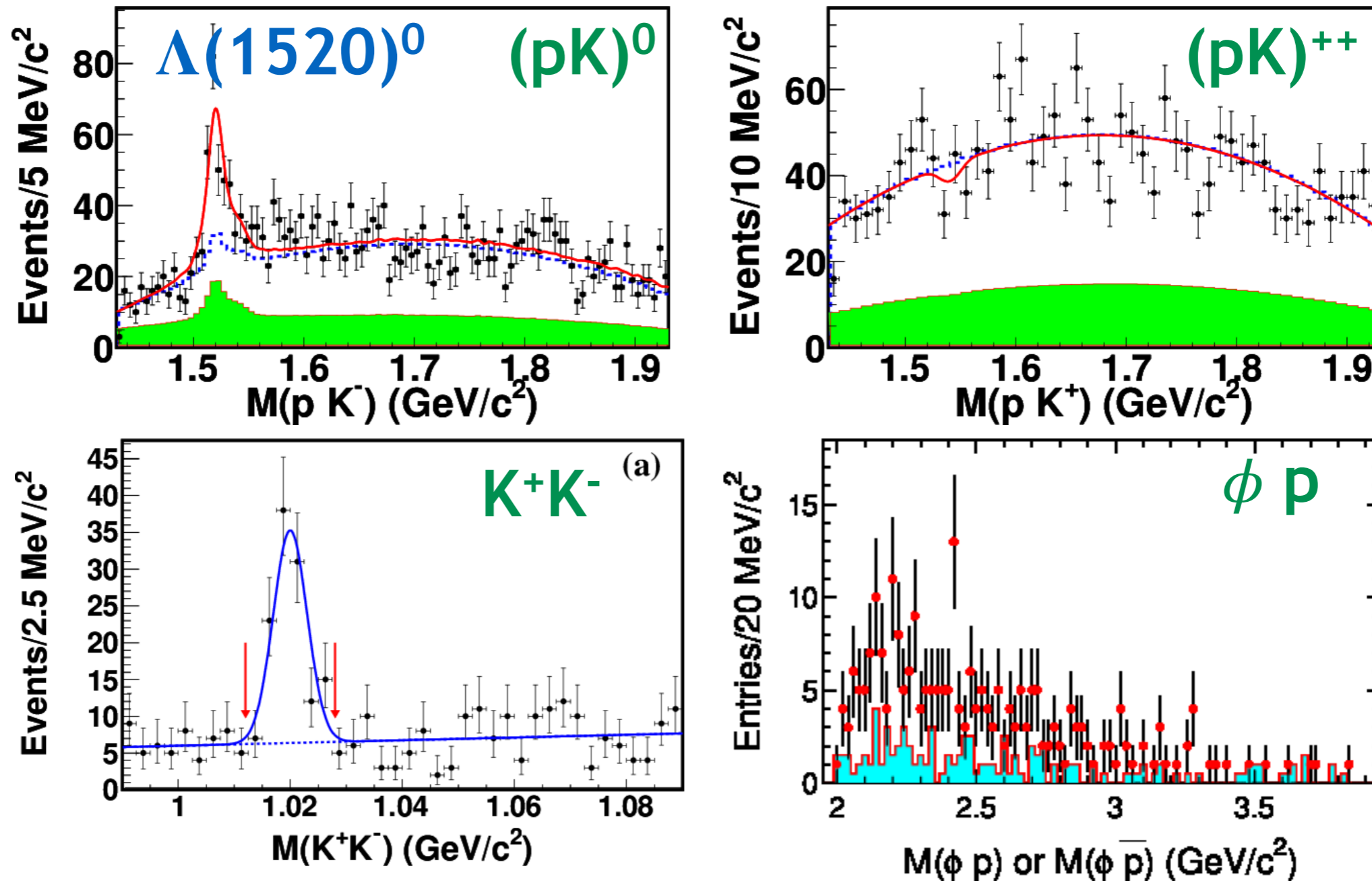


# Search for exotic baryons in $\gamma\gamma \rightarrow pp K^+K^-$

- Search for  $X^+ \rightarrow \phi p$
- $P_c(4380, 4450)^+ \rightarrow J/\psi p$  [LHCb: PRL115,072001(2015)]
- Search for  $\Theta(1540)^0 \rightarrow pK^-$  and  $\Theta(1540)^{++} \rightarrow p K^+$
- First pentaquark "evidence"  $\Theta(1540)^+ \rightarrow n K^+$  [LEPS: PRL91,012002(2003)]



# Search for exotic baryons in $\gamma\gamma \rightarrow pp K+K^-$



★ No evidence of  $s\bar{s}$  partner of  $P_c(4380, 4450)^+$  seen

# $\pi^0$ transition form factor

PRD86, 092007 (2012)

## Single-tag measurement

Transition Form Factor :  $F(Q^2) = \frac{\sqrt{2}f_\pi}{3} \int T_H(x, Q^2, \mu) \phi_\pi(x, \mu) dx$

pQCD: Agaev et.al.  
PRD22, 2157 (1980)

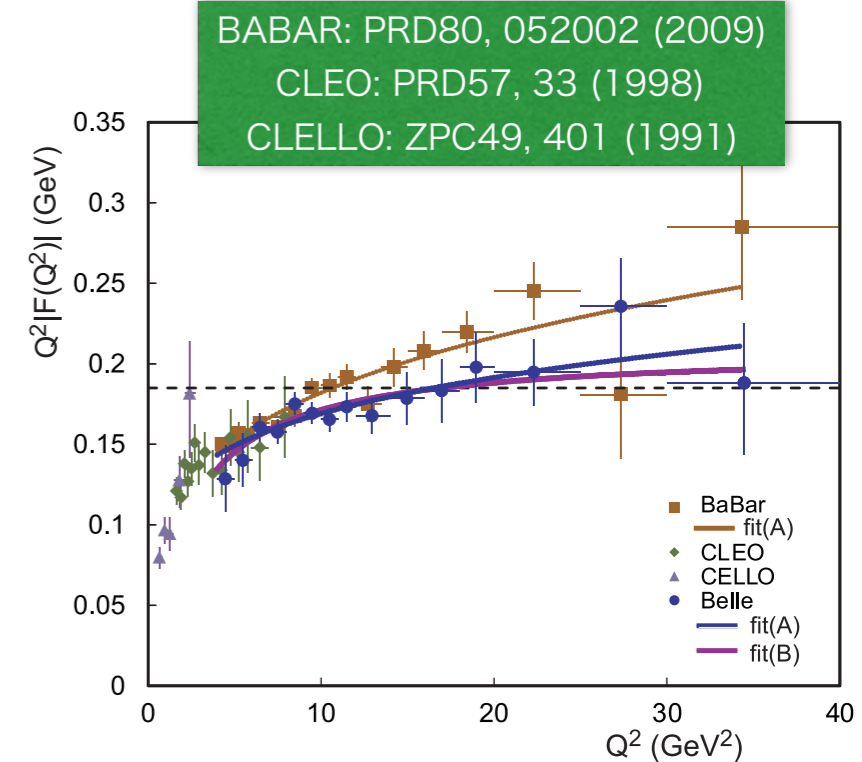
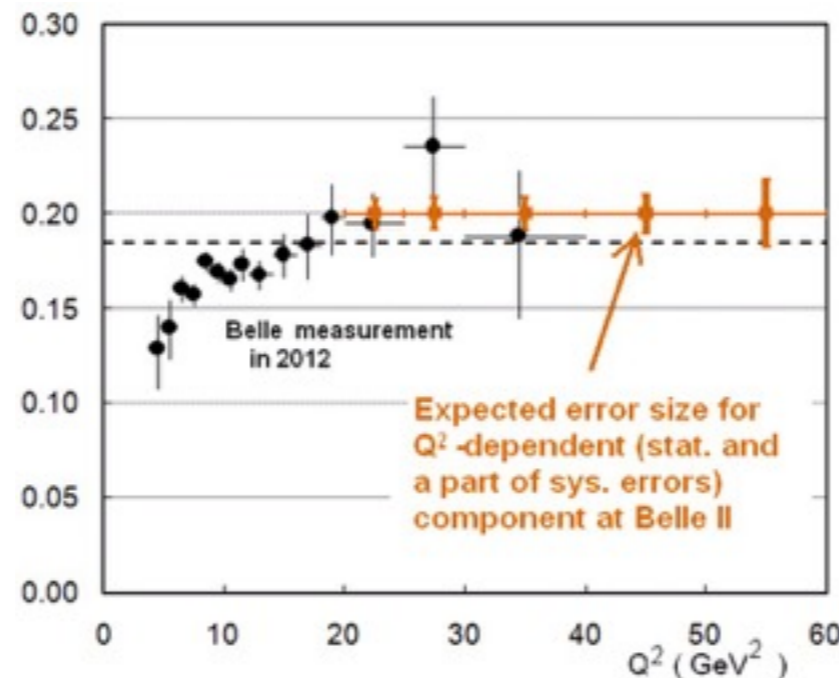
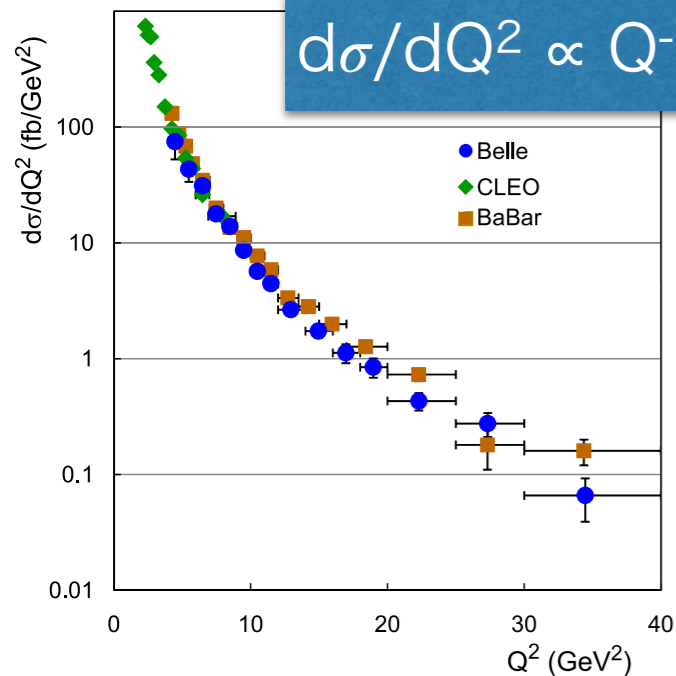
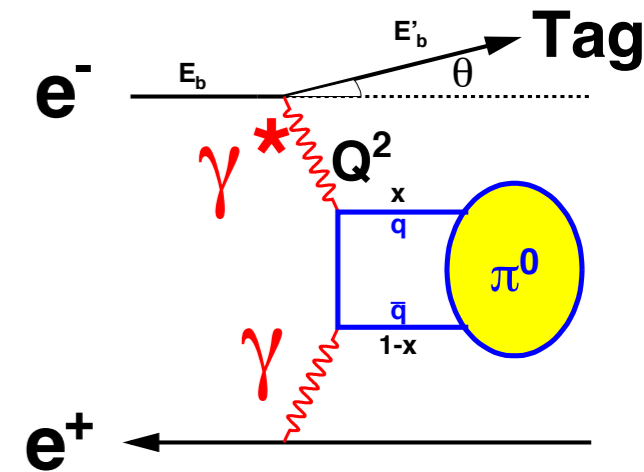
### ★ Extraction from $d\sigma/dQ^2$

$$\frac{d\sigma}{dQ^2} = \frac{N(1 - r_b)}{\int L dt \epsilon \mathcal{B}(\pi^0 \rightarrow \gamma\gamma)(1 + \delta) \Delta Q^2}$$

$\epsilon$	Efficiency
$r_b$	background fraction
$\delta$	radiative correction

2A(Q<sup>2</sup>) from QED  
Brodsky et.al.  
PRD4, 1532(1971)

$$Q^2 |F(Q^2)| = Q^2 \sqrt{(d\sigma/dQ^2)/(2A(Q^2))}$$



# Trigger at Belle II

- ★ At Belle Bhabha trigger caused event loss
- ★ At Belle II more sophisticated trigger
  - ★ Matching between sub trigger components
  - ★ PID at trigger Level: E/p, muon hit. ..
  - ★ benefit to Lowmultiplicity events

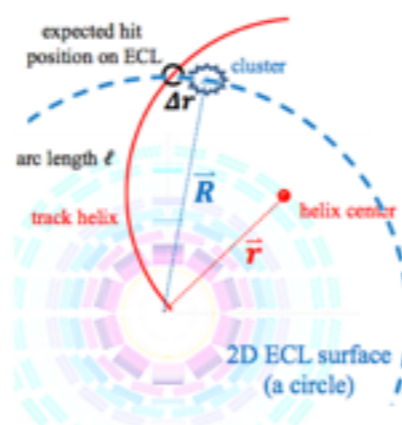
## Trigger Level Analysis

- 2D tracker output from TRGCDC:

- center of track helix:  $\vec{r} = (r, \phi)$
- $p_t$
- Track is extrapolated as a circle/helix inside ECL.

- Output from TRGECL:

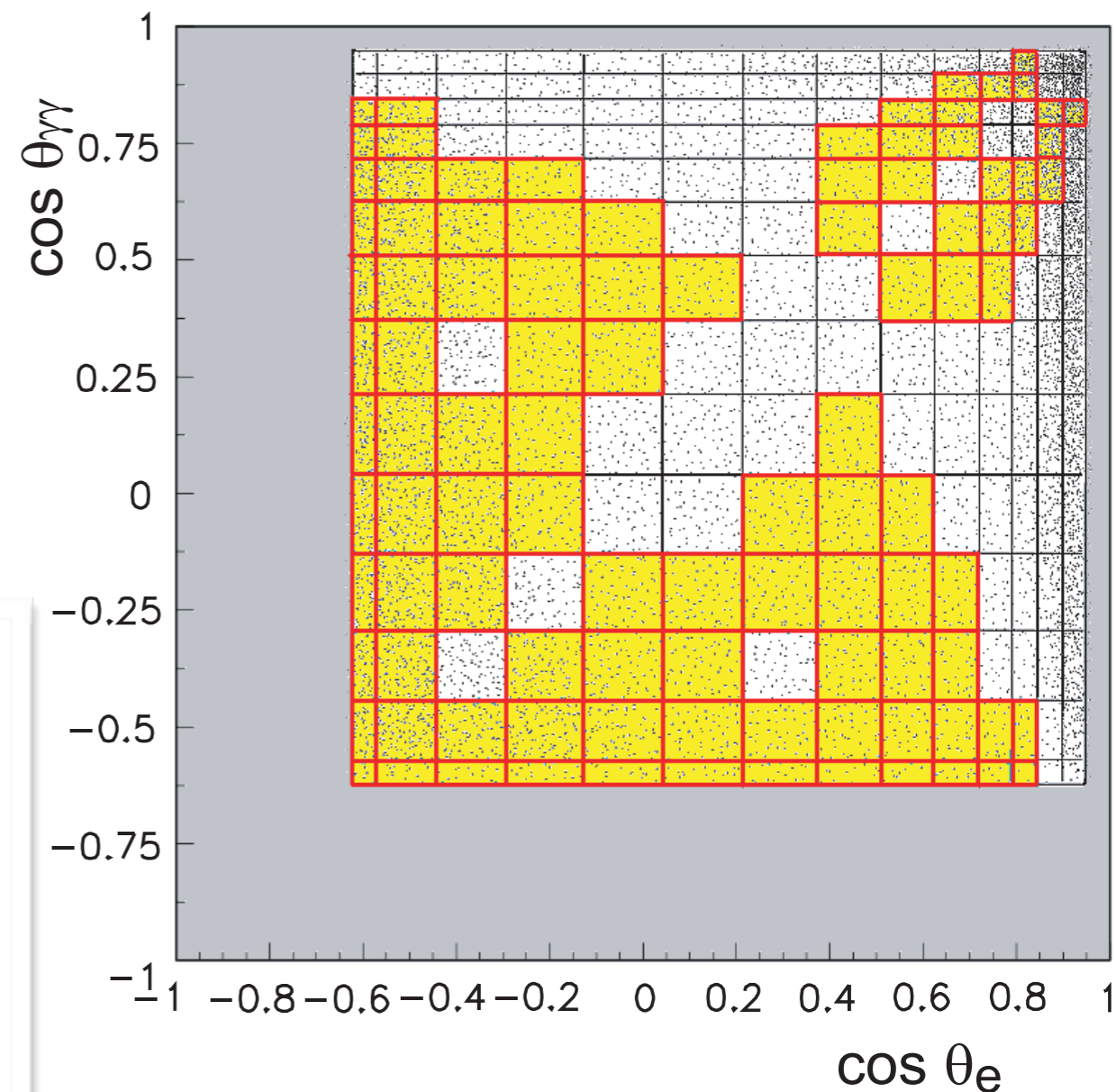
- cluster position on ECL:  $\vec{R} = (x, y) = (R, \theta)$   
(Cluster position is with 15cm depth to the inner surface.)
- Deposit Energy



- Solve the expect hit position for a track on ECL:

- $\vec{R}' = (x', y') = (R, \theta')$ ,  
where  $\theta' = \cos^{-1}(R/2r) + \phi$  or  $\phi - \cos^{-1}(R/2r)$

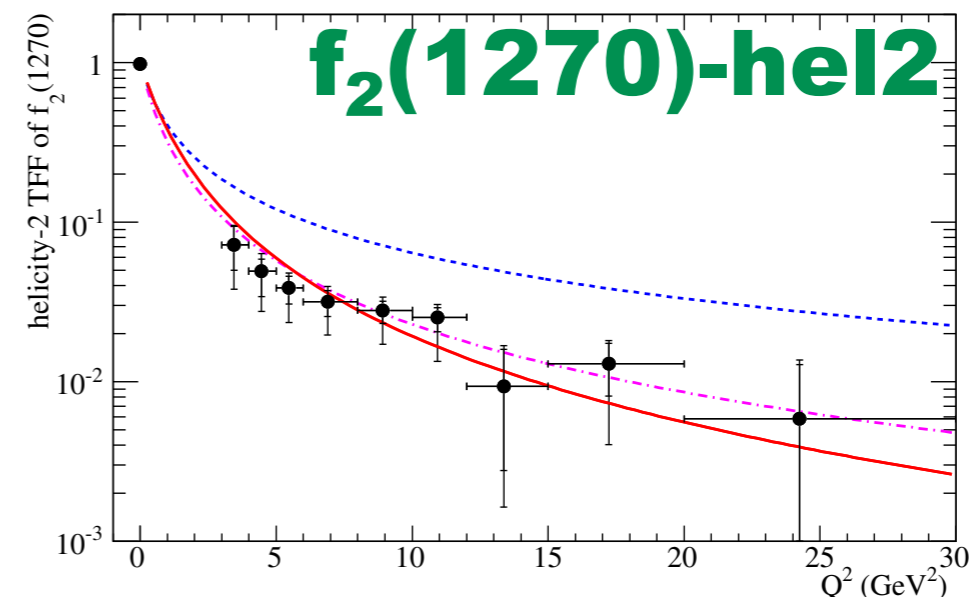
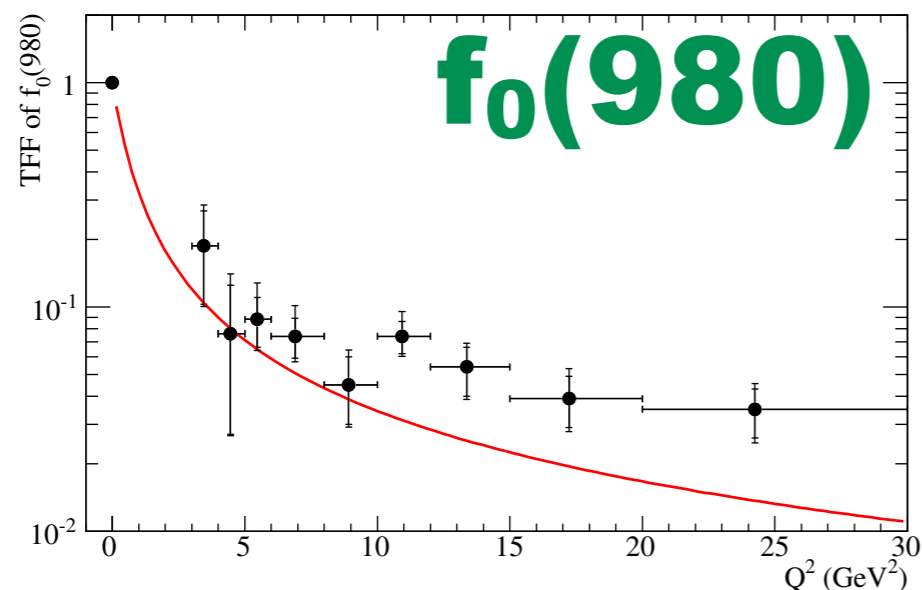
- $\Delta r \equiv |\vec{R} - \vec{R}'|$ : the deviation between cluster position and expected hit position.



# transition form factors for $f_0(980)$ and $f_2(1270)$

## Single-tag measurement

- ★  $\gamma^* \gamma \rightarrow \pi^0 \pi^0$ , PWA with  $Q^2$
- ★ spin-1 particle, helicity-1 component allowed in single-tag
- ★  $f_2(1270)$  TFF for helicity-0, 1, 2 separately for the first time
  - ★ large helicity-0 and non-zero helicity-1 components seen
- ★ Spin-1 has not measured yet.  $\chi_{c1}$  TFF is useful to test LbL sum rules (1705.01179)





# Summary

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- ★ Belle has measured various two-photon processes
- ★ Mainly using no-tag method, a few with single-tag method
- ★ Light resonance,  $c\bar{c}$  and XYZ, and (p)QCD have been studied by the data
- ★ Challenges to go higher  $W$  and  $Q^2$  at Belle II

# QCD Calculation of Meson Pair Production

$W > 3$  GeV: Resonance effect is small

pQCD by BL (Brodsky and Lepage, PRD24, 1808)

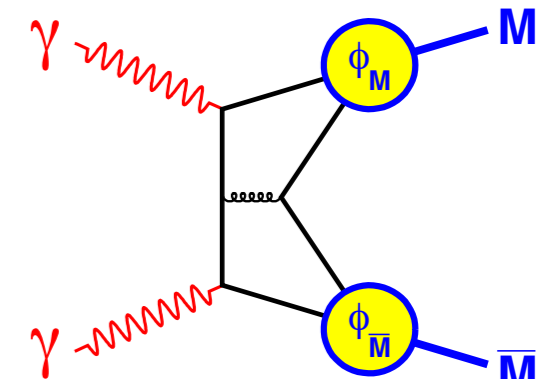
$$\mathcal{M}_{\lambda_1 \lambda_2}(W^2, \theta^*) = \int_0^1 \int_0^1 dx dy \phi_M(x, Q_x) \phi_{M'}(y, Q_y) T_{\lambda_1 \lambda_2}(x, y, \theta^*)$$

★ For charged pair,  $\sigma \sim f_M^4 / W^6 \sin^4 \theta^*$ ,  $d\sigma(K^+K^-) / d\sigma(\pi^+\pi^-) = 2.3$

Improved by BC (Benayoun and Chernyak, NPB329, 285 (1990))

★ SU(3) symmetry breaking  $d\sigma(K^+K^-) / d\sigma(\pi^+\pi^-) = 1.06$

★ For neutral pair,  $\sigma \sim 1/W^{10}$  Chernyak, 0912.0623



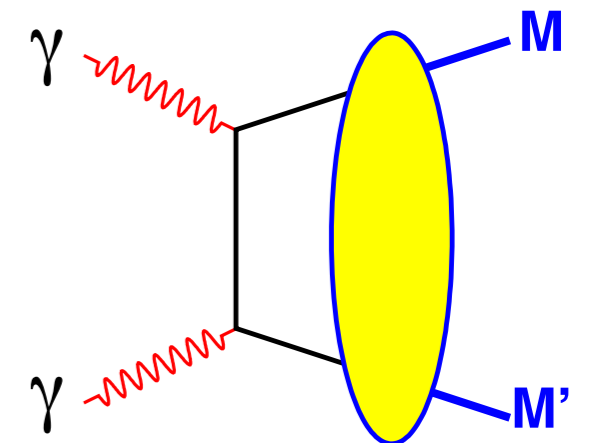
Handbag Model by DKV (Diehl, Kroll et.al. PLB532, 99 (2002))

$$\frac{d\sigma}{d|\cos \theta^*|}(\gamma\gamma \rightarrow MM') = \frac{8\pi\alpha^2}{W^2} \frac{1}{\sin^4 \theta^*} |R_{MM'}(W^2)|^2$$

★ Charge counting & flavor symmetry

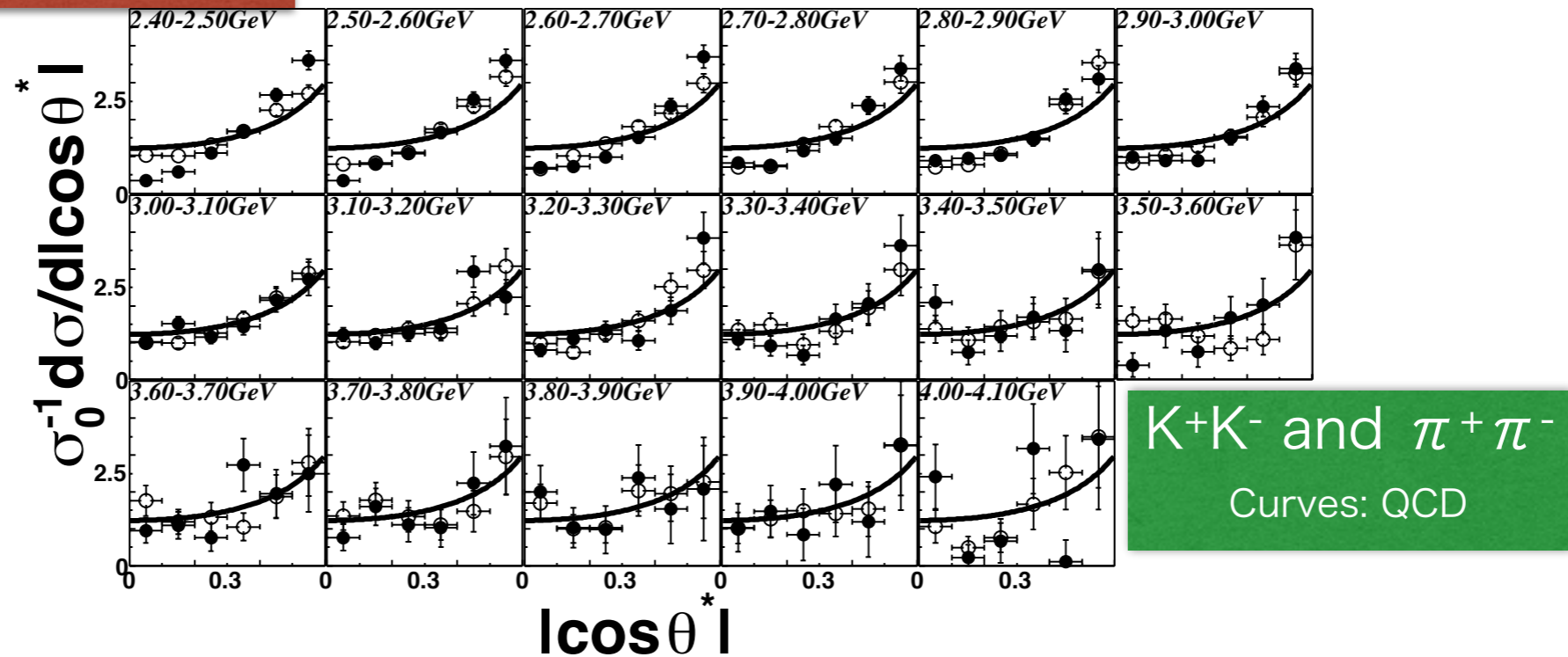
$$\sigma(K_S K_S) / \sigma(K^+ K^-) = 2/25$$

$$\sigma(\pi^0 \pi^0) / \sigma(\pi^+ \pi^-) = 0.5$$



# Angular Dependence

2.4 GeV →



mode	$1/\sin^4 \theta^*$	energy range	$ \cos \theta^* $ range
$\pi^+ \pi^-$	Match well.	3.0 - 4.1	$< 0.6$
$K^+ K^-$	Match well.	3.0 - 4.1	$< 0.6$
$K_S^0 K_S^0$	$\alpha$ varies from 4–8 for $1/\sin^\alpha \theta^*$	2.6 - 3.3	$< 0.8$
$\pi^0 \pi^0$	$1/\sin^4 \theta^* + b \cos \theta^*$ better. Approaches $1/\sin^4 \theta^*$ above 3.1 GeV.	2.4 - 4.1 <sup>†</sup>	$< 0.8$
$\eta \pi^0$	Good agreement above 2.7 GeV.	3.1 - 4.1	$< 0.8$
$\eta \eta$	Poor agreement. $1/\sin^6 \theta^*$ better above 3.0 GeV.	2.4 - 3.3	$< 0.9$

<sup>†</sup>  $\chi_{cJ}$  region, 3.3 - 3.6 GeV is excluded.

# Cross section and their ratio

Process	n of $\sigma \sim W^{-n}$	$W$ (GeV)	$ \cos \theta^* $	PRD24,1808	NPB329, 285	PLB532, 99
$\pi^+ \pi^-$	$7.9 \pm 0.4 \pm 1.5$	3.0 - 4.1	$< 0.6$	6	6	
$K^+ K^-$	$7.3 \pm 0.3 \pm 1.5$	3.0 - 4.1	$< 0.6$	6	6	
$K_S^0 K_S^0 \#$	$10.5 \pm 0.6 \pm 0.5$	2.4 - 4.0 <sup>†</sup>	$< 0.6$	-	10	
$K_S^0 K_S^0 \#\#$	$11.0 \pm 0.4 \pm 0.4$	2.6 - 4.0 <sup>†</sup>	$< 0.8$	-	10	
$\pi^0 \pi^0$	$8.0 \pm 0.5 \pm 0.4$	3.1 - 4.1 <sup>†</sup>	$< 0.8$	-	10	
$\eta \pi^0$	$10.5 \pm 1.2 \pm 0.5$	3.1 - 4.1	$< 0.8$	-	10	
$\eta \eta$	$7.8 \pm 0.6 \pm 0.4$	2.4 - 3.3	$< 0.8$	-	10	
Process	$\sigma_0$ ratio	$W$ (GeV)	$ \cos \theta^* $	PRD24,1808	NPB329, 285	PLB532, 99
$K^+ K^- / \pi^+ \pi^-$	$0.89 \pm 0.04 \pm 0.15$	3.0 - 4.1	$< 0.6$	2.3	1.06	
$K_S^0 K_S^0 / K^+ K^- \#$	$\sim 0.13$ to $\sim 0.01$	2.4 - 4.0	$< 0.6^\dagger$		0.005	2/25
$\pi^0 \pi^0 / \pi^+ \pi^-$	$0.32 \pm 0.03 \pm 0.06$	3.1 - 4.1	$< 0.6^\dagger$		0.04-0.07	0.5
$\eta \pi^0 / \pi^0 \pi^0$	$0.48 \pm 0.05 \pm 0.04$	3.1 - 4.0	$< 0.8^\dagger$	$0.24 R_f (0.46 R_f)^\ddagger$		
$\eta \eta / \pi^0 \pi^0$	$0.37 \pm 0.02 \pm 0.03$	2.4 - 3.3	$< 0.8$	$0.36 R_f^2 (0.62 R_f^2)^\ddagger$		

<sup>†</sup>  $\chi_{cJ}$  region, 3.3 - 3.6 GeV is excluded.

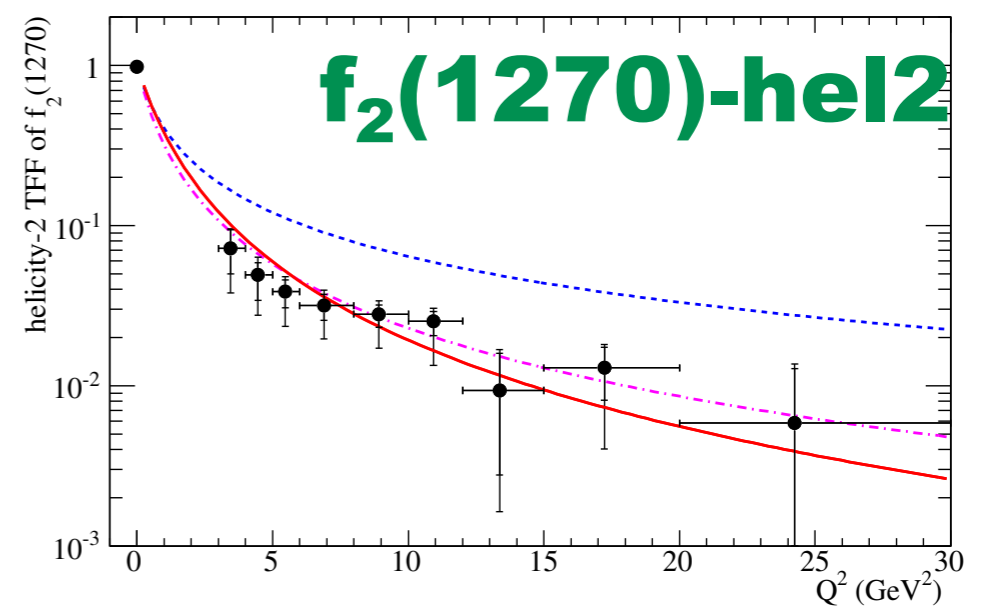
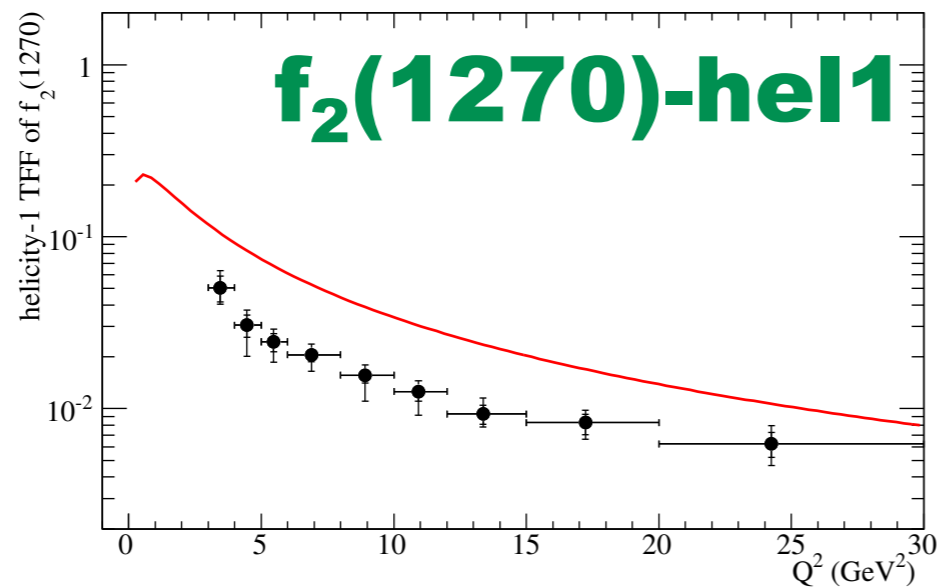
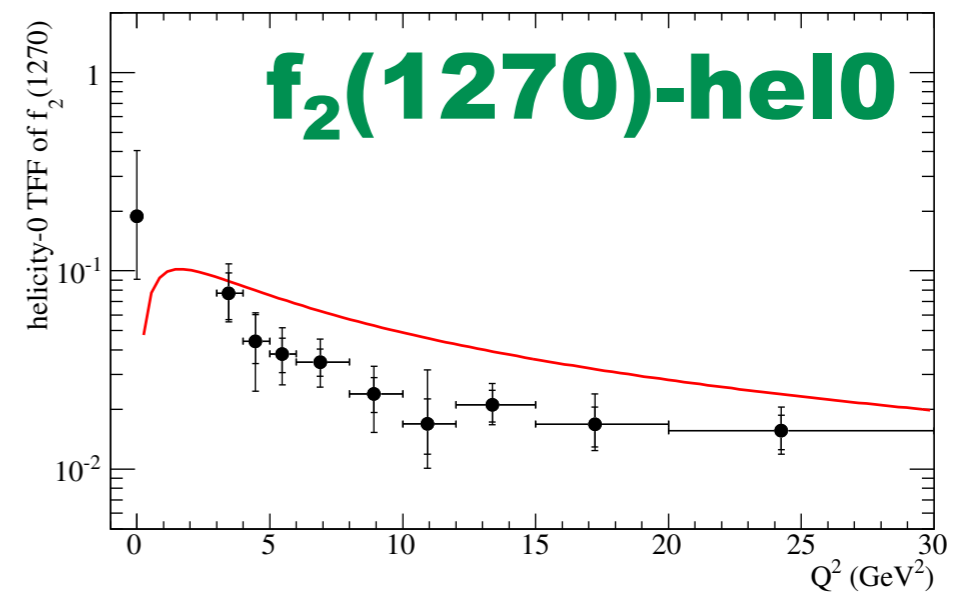
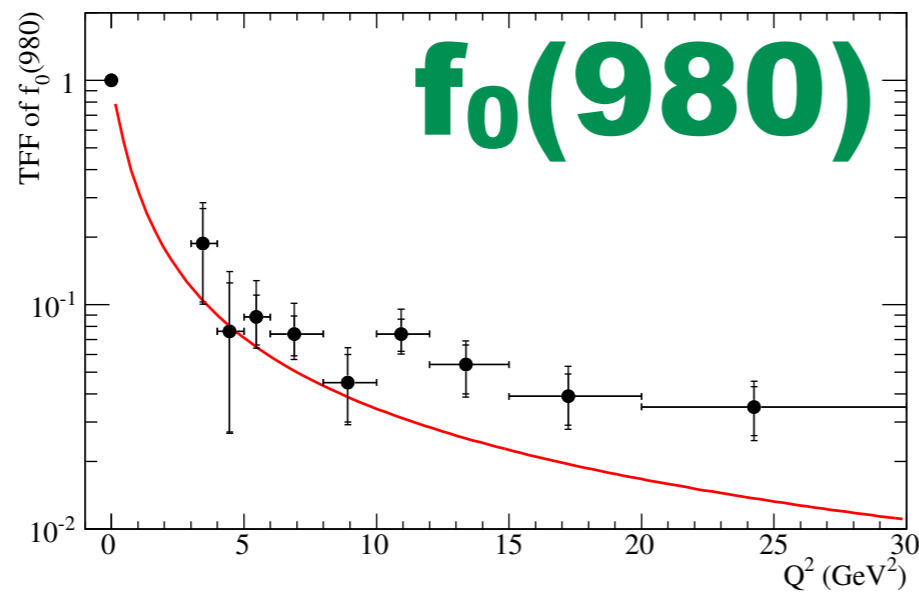
<sup>‡</sup>  $\eta$  meson as a pure  $SU(3)$  octet (mixture of octet and singlet with  $\theta_p = -18^\circ$ ),  $R_f = f_\eta^2 / f_{\pi^0}^2$ .

# PLB651, 15

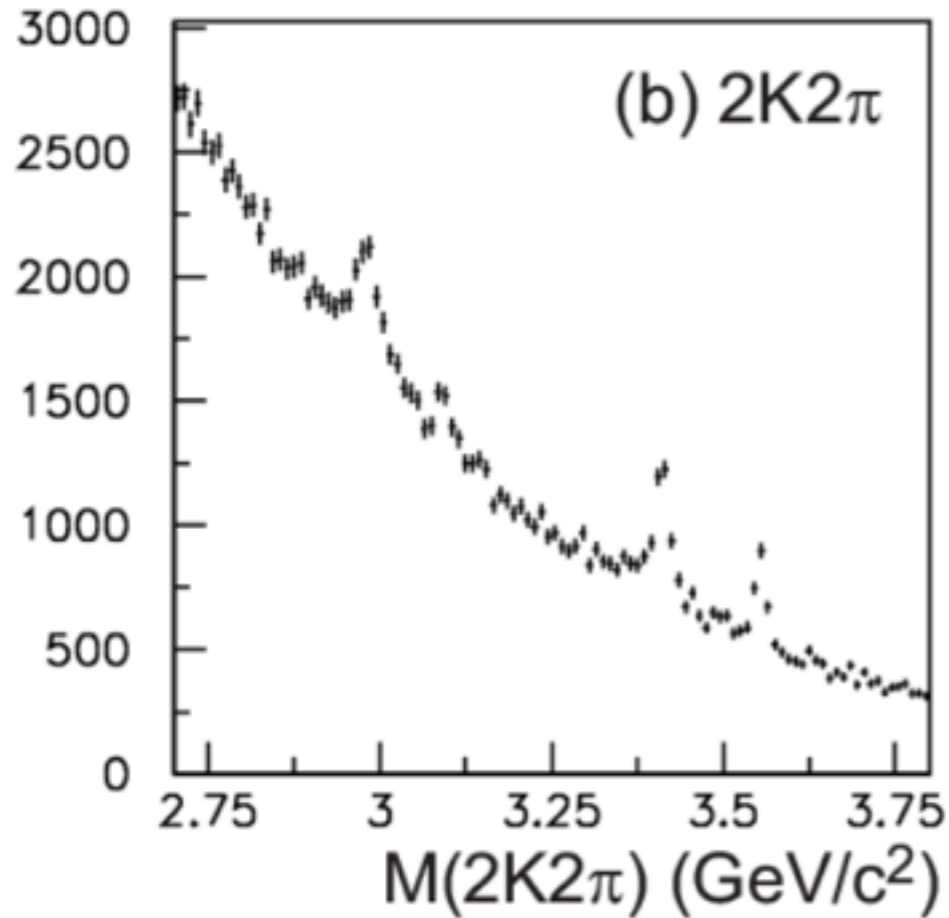
## PTEP2013, 123C01

# transition form factors for $f_0(980)$ and $f_2(1270)$

## Single-tag measurement



# charmonia and XYZ



$\gamma\gamma \rightarrow K_s K \pi$  (PHOTON2007)

