

Prospects for charm mixing at Belle II

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On behalf of the Belle II Collaboration



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Mixing in D^0 system

- Mass and weak eigenstates are expressed as

$$|D_{1,2}^0\rangle = \frac{1}{\sqrt{|p|^2 + |q|^2}} (p |D^0\rangle \pm q |\bar{D}^0\rangle) \quad \text{If } p \neq q, \text{ CP is violated}$$

- Mixing parameterized by mass/width splittings:

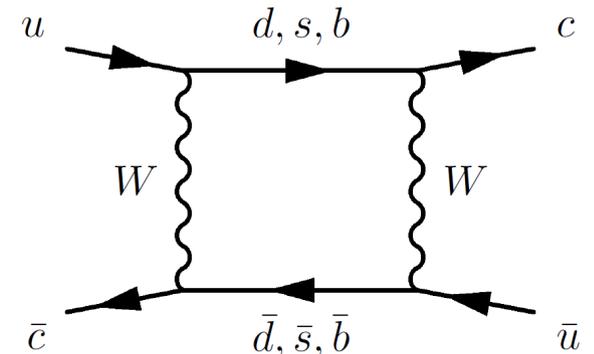
$$x = \frac{m_1 - m_2}{\Gamma}, \quad y = \frac{\Gamma_1 - \Gamma_2}{2\Gamma}$$

- In SM, D-mixing is heavily suppressed
 - CKM suppressed
 - GIM suppressed

- SM expectation: $|x|, |y| \sim O(10^{-3} - 10^{-2})$.

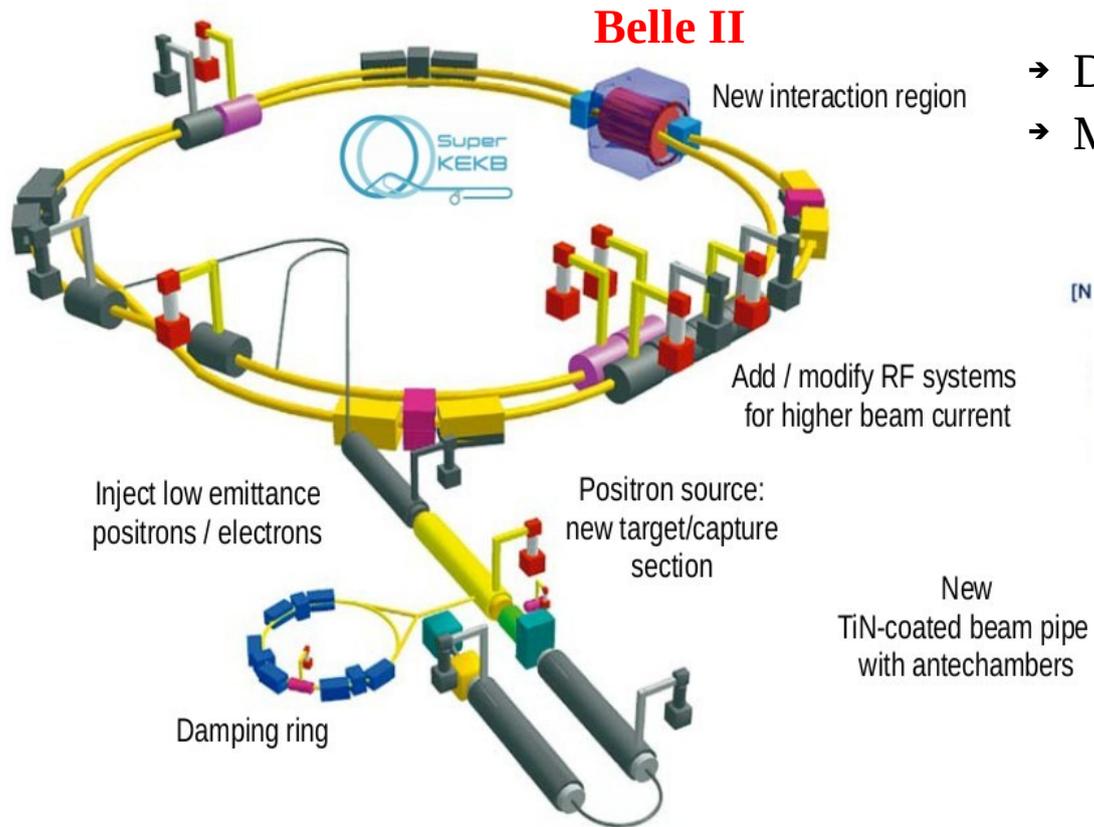
- Non-SM particles contributing to the box diagram (NP) could significantly affect the measured values

- Precision measures need huge statistics (KEKB \rightarrow SuperKEKB) and clean, accurate signals (Belle \rightarrow Belle II)



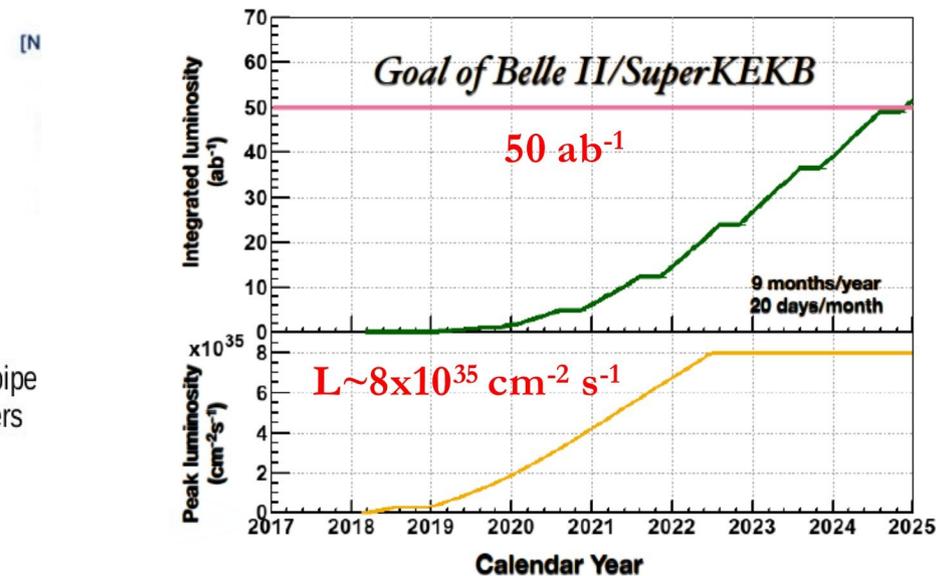
SuperKEKB (High luminosity frontier machine!)

- SuperKEKB – major upgrade of the KEKB B factory at KEK
- e^+e^- (4 GeV + 7 GeV) → BB mainly at $\sqrt{s}_{\text{cm}}=10.58$ GeV (peak of Y(4S) resonance)



To obtain x40 higher instantaneous luminosity:

- Double beam current
- Major increase by small beam size “nano-beam” (vertical spot size $\sim 50\text{nm}$!!)

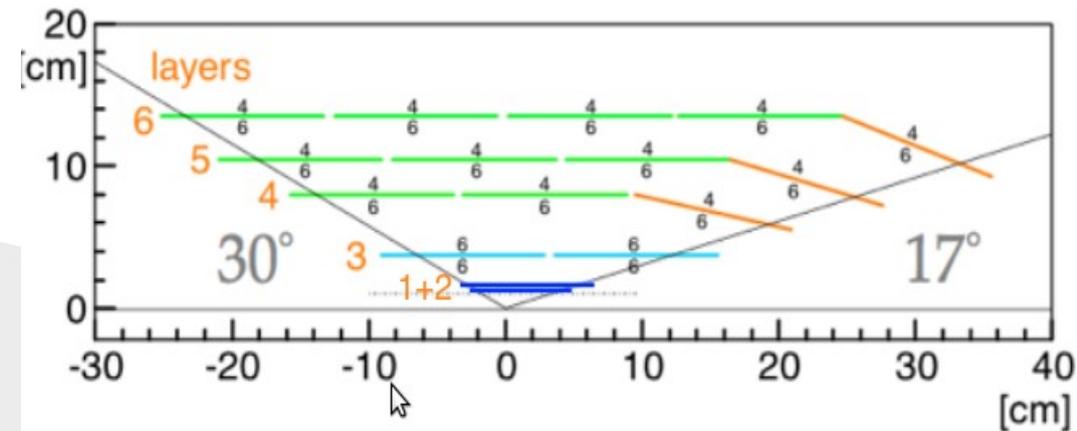
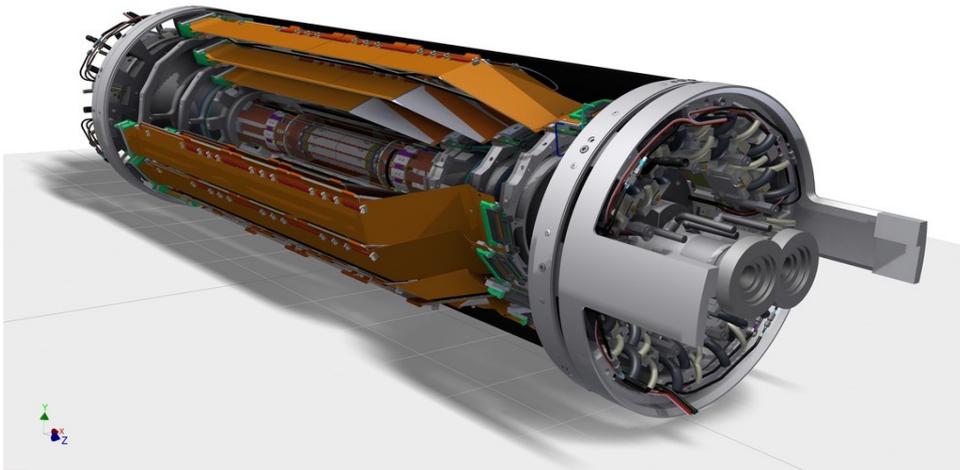


Covered by Alexei Sibidanov on Belle II readiness for Phase II collisions

Belle II Vertex detector (main player for D-mixing sensitivity measurement)

Belle II detector covered by Alexei

- VXD = silicon vertex detector (SVD) + pixel detector (PXD)
- Precise measurement of the primary and secondary vertices of short-lived particles



PXD:

- 2 layers of DEPFET pixels
- Very thin (50 μm) pixel sensor
- Inner most layer very close to IP ($r = 1.4\text{cm}$)
- Very low material budget
- Excellent spatial granularity ($\sigma \leq 15\mu\text{m}$)

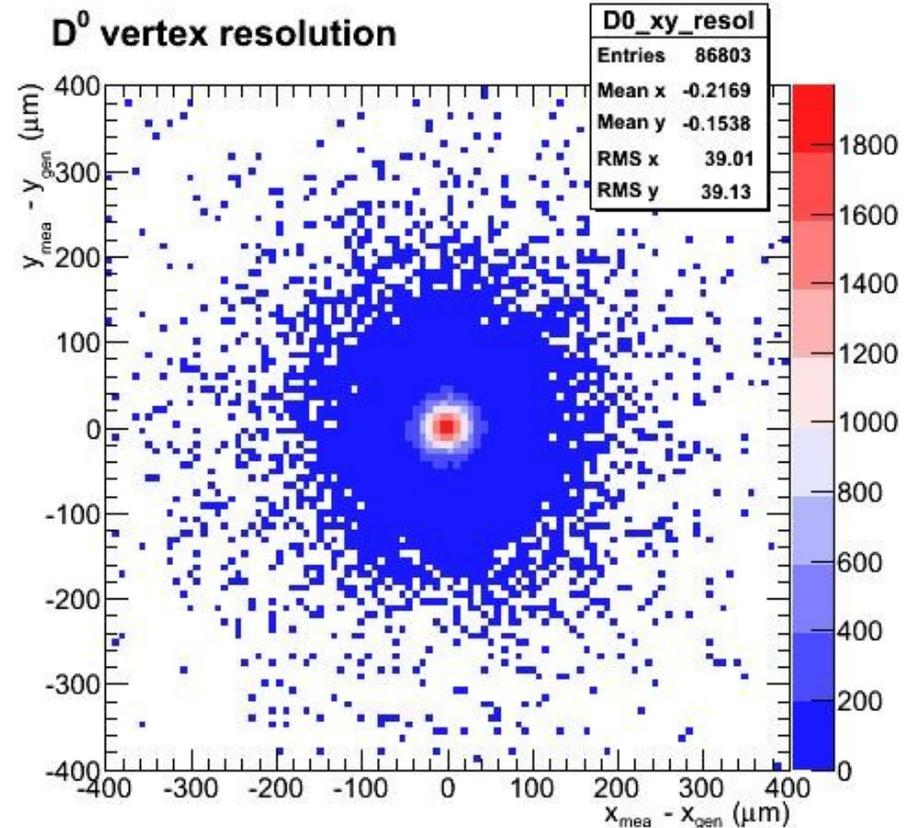
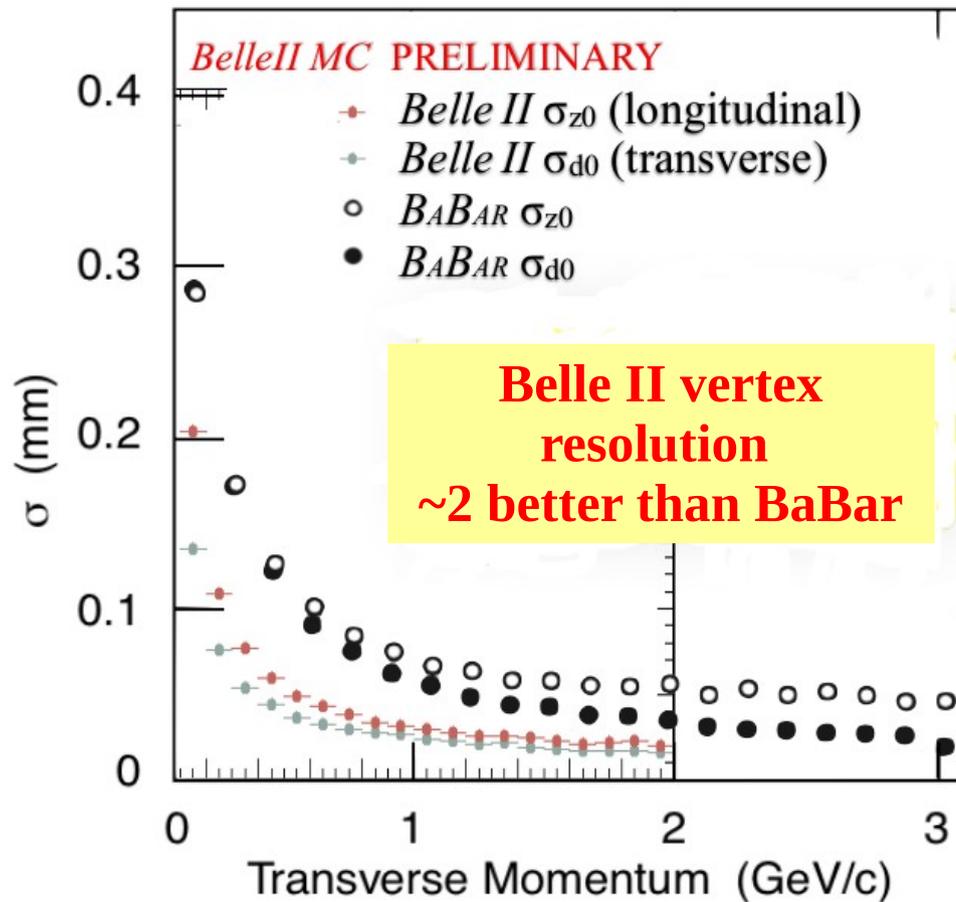
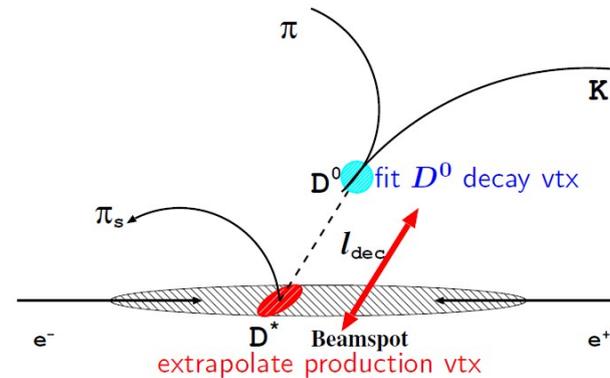
SVD:

- 4 layers of DSSD detectors
- Excellent timing resolution ($\sigma \sim 2\text{-}3\text{ ns}$)
- Low material budget
- Larger outer radius (6.05 cm \rightarrow 14 cm)
- Inner radius: 3.8cm
- covers the full Belle II angular acceptance of $17^\circ < \theta < 150^\circ$

Motivation to SuperKEKB and Belle II for charm mixing analysis

- Low backgrounds, high trigger efficiency, excellent γ and π^0 reconstruction, high flavor-tagging efficiency with low dilution
- Excellent Dalitz plot analysis with low background
- With Belle II VXD: D^0 decay vertex resolution precision of $\sim 40\mu\text{m}$, large improvement w.r.t B-Factories
- IP resolution improved by PXD being at radius of 1.4 cm
- Increased tracking volume in both SVD and CDC $\Rightarrow \sim 30\%$ higher K_s efficiency
- Improved PID with better K/π separation relative to Belle.
- Belle II by 2025: 50ab^{-1} data : $> 6 \times 10^{10}$ charm events (Belle had 10^9 charm events)

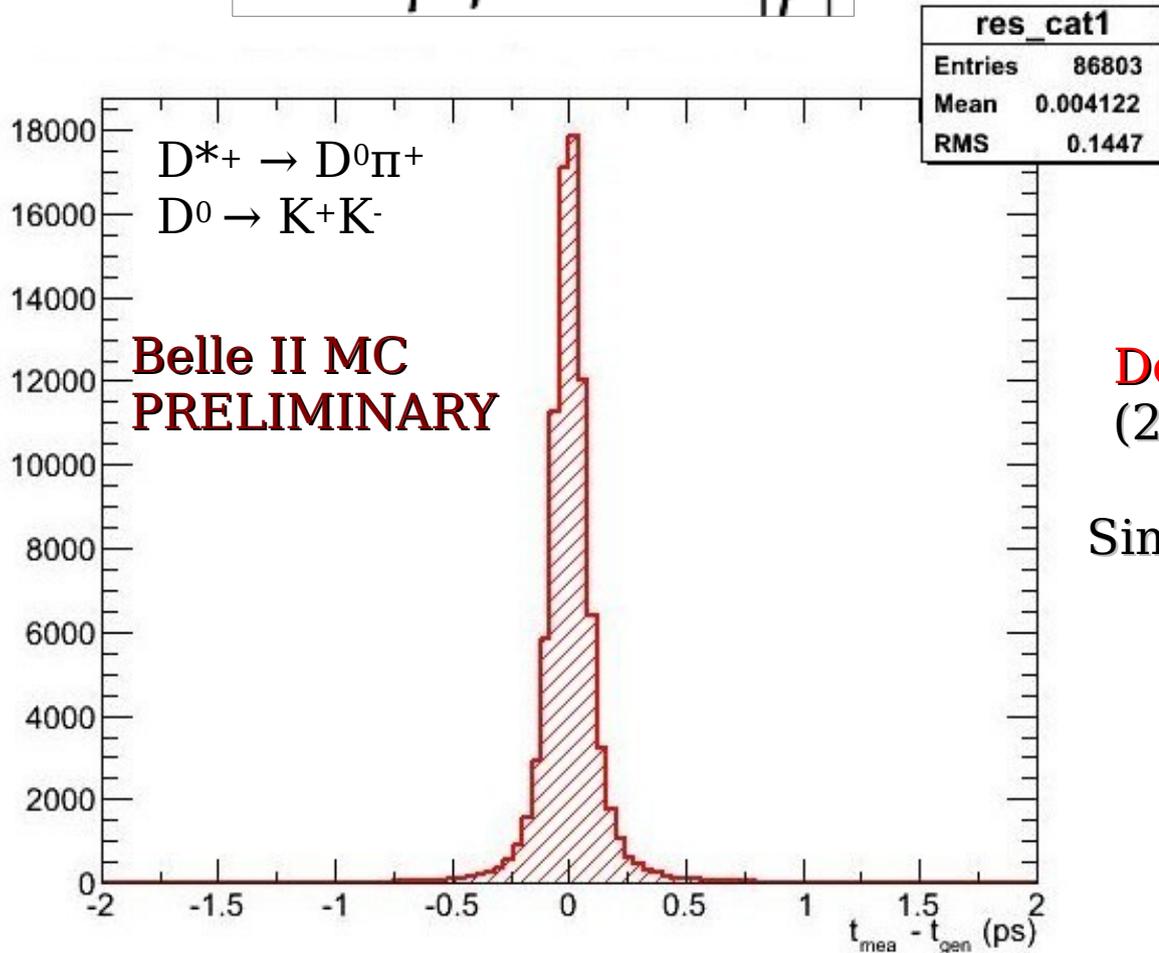
D0 decay vertex resolution



Belle II: $\sigma \approx 40 \mu\text{m}$

$D^0 \rightarrow h^+h^-$ decay time resolution (D^* tag)

$$t = \frac{\ell}{\beta\gamma c} = \frac{\ell m_D}{c |\vec{p}|}$$



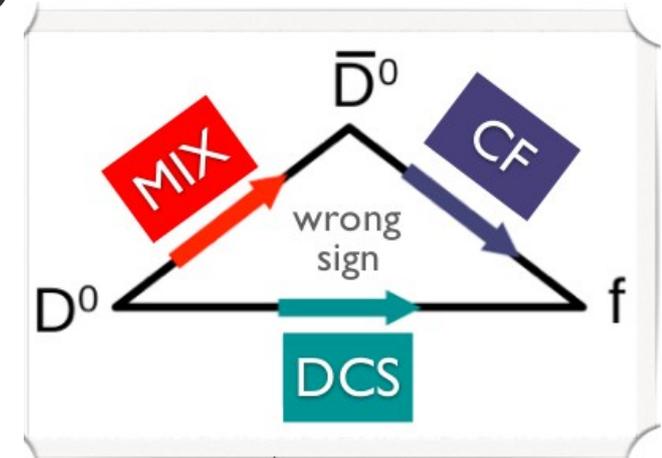
Decay time resolution of 0.14 ps
(2 x better than Belle and Babar)

Similar result for $D^0 \rightarrow h^+h^-$ prompt
decay (0.15 ps)

Time dependent D^0 mixing studies

- Final state accessed both by D^0 or D^0 bar, the two paths interfere in the amplitude as:

$$|\mathcal{M}(\bar{f}, t)|^2 = e^{-\Gamma t} \left(|\mathcal{A}_{\bar{f}}|^2 + \frac{x^2 + y^2}{4} |\bar{\mathcal{A}}_{\bar{f}}|^2 (\Gamma t)^2 - \Re(\mathcal{A}_{\bar{f}} \bar{\mathcal{A}}_{\bar{f}}^*) \cdot y \Gamma t - \Im(\mathcal{A}_{\bar{f}} \bar{\mathcal{A}}_{\bar{f}}^*) \cdot x \Gamma t \right)$$



- Measuring the decay rate as a function of the D^0 proper time gives access to be sensitive to mixing
- With multibody final state, the Dalitz analysis allows to access to more than one channel at the same time

Belle II sensitivity extrapolation

$$\sigma_{\text{Belle II}} = \sqrt{(\sigma_{\text{stat}}^2 + \sigma_{\text{syst}}^2) \cdot \frac{\mathcal{L}_{\text{Belle}}}{50 \text{ ab}^{-1}} + \sigma_{\text{irred}}^2}$$

- Estimation for Belle II: scaling by the ratio of luminosities, and assuming the same reconstruction efficiency as Belle
- we assumed that most of the systematics scale with statistics
- irred. syst. those do not scale with luminosity. e.g. decay time resolution due to detector misalignment

Mixing precision for $D^0 \rightarrow K^+\pi^-$ decay

- Two body final state $D^0 \rightarrow K^+\pi^-$ is an ideal channel for mixing study, almost systematic free
- Belle measurement using full statistics:

$$x'^2 = (0.09 \pm 0.22) \times 10^{-3} \quad \text{and} \quad y' = (4.6 \pm 3.4) \times 10^{-3}$$

$$x' = x \cos \delta + y \sin \delta, \quad y' = y \cos \delta - x \sin \delta$$

PRL 112, 111801 (2014)

no CPV assumption:

fit decay time distribution for mixing parameters R_D, x'^2, y'

$$\frac{dN(D^0 \rightarrow f)}{dt} \propto e^{-\bar{\Gamma}t} \left\{ R_D + \sqrt{R_D} y' (\bar{\Gamma}t) + \frac{(x'^2 + y'^2)}{4} (\bar{\Gamma}t)^2 \right\}$$

with CPV assumption:

fit decay time distribution with additional parameters: $|q/p|, \phi$

$$D^0(t) = : e^{-\bar{\Gamma}t} \left\{ R_D + \left| \frac{q}{p} \right| \sqrt{R_D} (y' \cos \phi - x' \sin \phi) (\bar{\Gamma}t) + \left| \frac{q}{p} \right|^2 \frac{(x'^2 + y'^2)}{4} (\bar{\Gamma}t)^2 \right\}$$

$$\bar{D}^0(t) = : e^{-\bar{\Gamma}t} \left\{ \bar{R}_D + \left| \frac{p}{q} \right| \sqrt{\bar{R}_D} (y' \cos \phi + x' \sin \phi) (\bar{\Gamma}t) + \left| \frac{p}{q} \right|^2 \frac{(x'^2 + y'^2)}{4} (\bar{\Gamma}t)^2 \right\}$$

Estimated Mixing precision for $D^0 \rightarrow K^+\pi^-$ decay

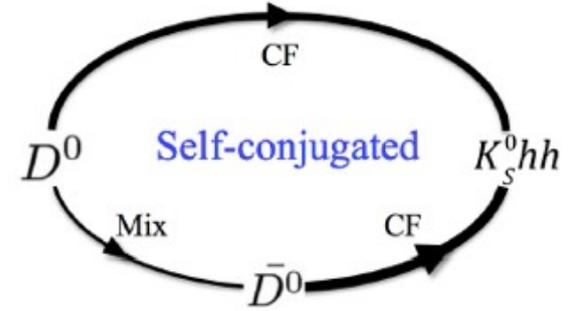
No CPV assumption

	976 fb ⁻¹ (Belle measurement)	5 ab ⁻¹	20 ab ⁻¹	50 ab ⁻¹
$\delta x'^2$ (x 10 ⁻⁵)	22	7.5	3.7	2.3
$\delta y'$ (%)	0.34	0.11	0.056	0.035

with CPV assumption

	5 ab ⁻¹	20 ab ⁻¹	50 ab ⁻¹
$\delta x'$ (%)	0.37	0.23	0.15
$\delta y'$ (%)	0.26	0.17	0.10
$\delta q/p $	0.197	0.089	0.051
$\delta\Phi$ (deg)	15.5	9.2	5.7

Mixing precision for $D^0 \rightarrow K_S \pi^+ \pi^-$ decay



- Belle II sensitivity to x, y from $D^0 \rightarrow K_S \pi^+ \pi^-$ decay is estimated by scaling from the Belle measurement

Peng et al., PRD 89, 091103(R) (2014)

- Using 0.921 ab^{-1} data, Belle measurements of x and y :

$$x = (0.56 \pm 0.19_{-0.09}^{+0.03} \text{ }_{-0.09}^{+0.06})\% \quad y = (0.30 \pm 0.15_{-0.05}^{+0.04} \text{ }_{-0.06}^{+0.03})\%$$

- Expected Belle II sensitivity:

Data	stat.	syst.		Total	stat.	syst.		Total
		red.	irred.			red.	irred.	
		$\sigma_x(\%)$				$\sigma_y(\%)$		
976 fb^{-1}	0.19	0.06	0.11	0.20	0.15	0.06	0.04	0.16
5 ab^{-1}	0.08	0.03	0.11	0.14	0.06	0.03	0.04	0.08
50 ab^{-1}	0.03	0.01	0.11	0.11	0.02	0.01	0.04	0.05

→ At high statistics, the irreducible uncertainty is due to the D^0 decay model. This will be improved with model independent approach

→ Improvement in decay time resolution is not included here.

Expected y_{CP} precision for $D^0 \rightarrow K^+K^- / \pi^+\pi^-$ decay (CP even modes)

$$y_{CP} = \frac{1}{2} \left(\left| \frac{q}{p} \right| + \left| \frac{p}{q} \right| \right) y \cos \phi - \frac{1}{2} \left(\left| \frac{q}{p} \right| - \left| \frac{p}{q} \right| \right) x \sin \phi$$

$$\approx y \cos \phi - A_M x \sin \phi .$$

- Belle: $y_{CP} = (1.11 \pm 0.22 \pm 0.09)\%$ (M. Staric et al., Phys. Lett. B 753, 412 (2016).)
- BaBar: $y_{CP} = (0.72 \pm 0.18 \pm 0.12)\%$ (B. Aubert et al., Phys. Rev. D87, 012004 (2013).)

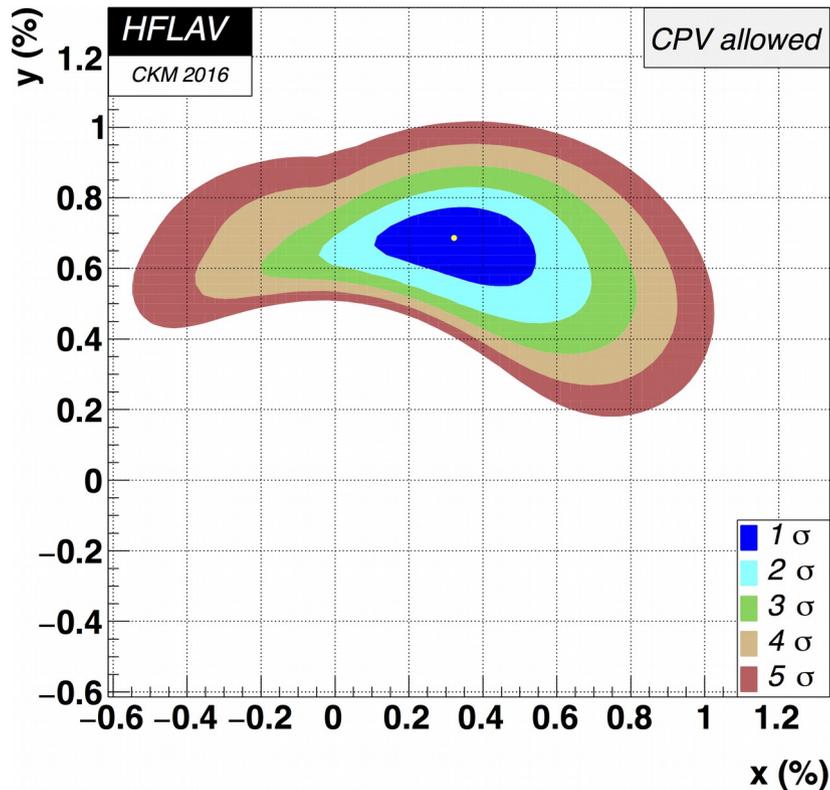
Expected Belle II sensitivity

Observable	Statistical	Systematic		Total
		red.	irred.	
$y_{CP}(\%)$				
976 fb ⁻¹	0.22	0.07	0.07	0.24
5 ab ⁻¹	0.10	0.03-0.04	0.07-0.04	0.11-0.12
50 ab ⁻¹	0.03	0.01	0.07-0.04	0.05-0.08

Using full Belle data

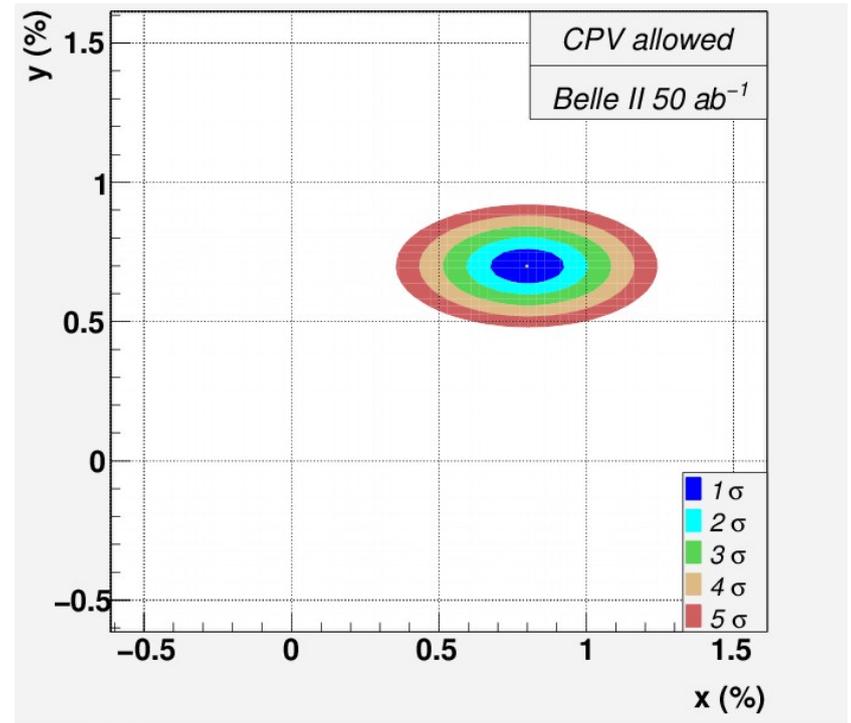
Source	$\Delta y_{CP} [10^{-2}]$
acceptance	0.050
SVD misalignments	0.060
mass window position	0.007
background	0.059
resolution function	0.030
binning	0.021
total syst. error	0.105
stat. error	0.220

D⁰ Mixing Parameters - World Average and Expected Belle II precision



World average (mixing):

$$\mathbf{x} = (0.32 \pm 0.14)\%, \mathbf{y} = (0.69^{+0.06}_{-0.07})\%$$



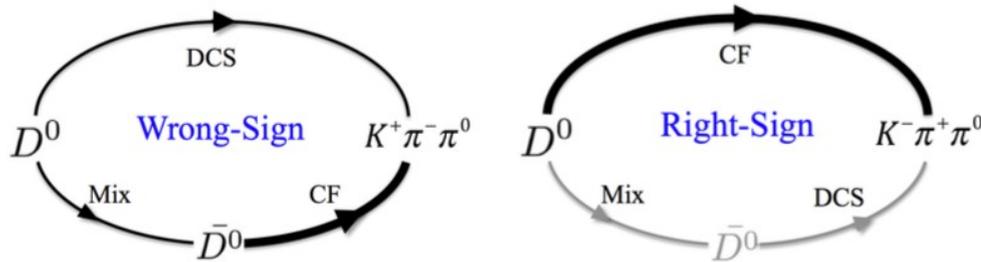
Belle II (50 ab⁻¹)

$$\mathbf{x} = 0.8 \pm 0.09\%, \mathbf{y} = 0.7 \pm 0.04\%$$

(result is conservative, does not include modes: $K^+\pi^-\pi^0$, $K_s K^+ K^-$ etc.)

- The experimental data consistently indicate that the D⁰ and D⁰bar do mix.
- Current measurement provides constraints on many NP models like fourth generation, extra gauge bosons, left right symmetric models...

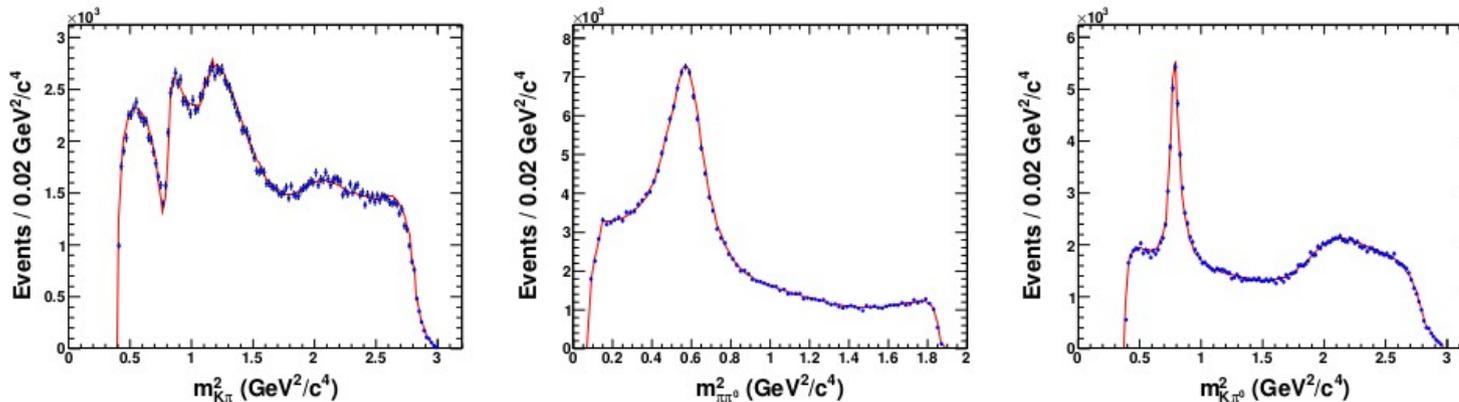
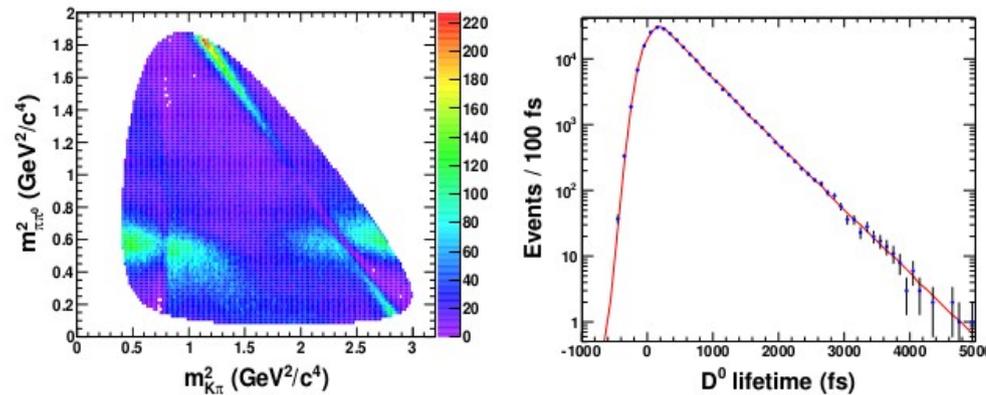
Time dependent Dalitz analysis of $D^0 \rightarrow K\pi^+\pi^0$ to measure mixing



$$x'' = x \cdot \cos \delta_{K\pi\pi^0} + y \cdot \sin \delta_{K\pi\pi^0},$$

$$y'' = y \cdot \cos \delta_{K\pi\pi^0} - x \cdot \sin \delta_{K\pi\pi^0}$$

time-dependent fit to the $(m_{K^+\pi^-}^2, m_{K^+\pi^0}^2)$ Dalitz plot to measure the effective mixing parameters



Precision results for $D^0 \rightarrow \bar{K}\pi^+\pi^0$ mixing

- Simulation study using an ensemble of 10 experiments of 225,000 WS events (estimated signal yield at 50 ab^{-1} of data) with decay time resolution = 140 fs
- The mixing parameters used for event generation are $x'' = 2.58\%$, $y'' = 0.39\%$

The expected precision of Belle II for these parameters:

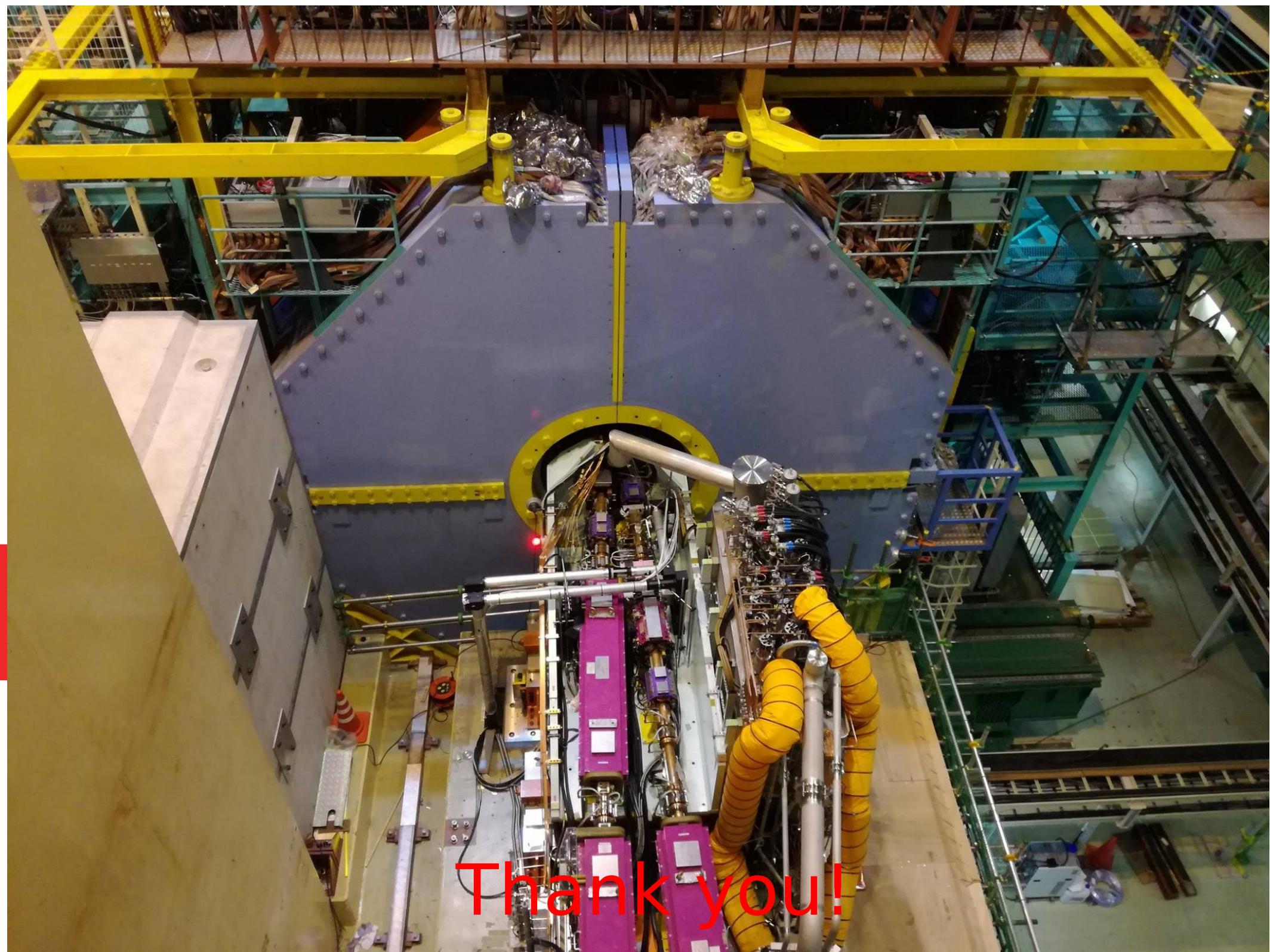
$$\sigma_{x''} = 0.057\%$$

$$\sigma_{y''} = 0.049\%$$

- an order of magnitude better than BaBar ([Phys. Rev. Lett. 103, 211801 \(2009\)](#)), if no background
- Estimation of background effects from Belle analysis: increase of stat error by 40%.
- conservative, as backgrounds smaller at Belle II than at Belle due to improved vertex resolution, mass resolution, particle identification.
- 20% estimated reduction of systematics at 50ab^{-1}

Summary

- B factories have proven to be an excellent tool for charm mixing study
- Super B factory will provide $L = 40 \times \text{Belle} \Rightarrow 50 \text{ ab}^{-1}$ (by 2025)
- Due to upgraded vertex detector, D^0 decay time resolution will improve twice than Belle/Babar which subsequently improves the precision of mixing/CPV parameters.
- Belle D-mixing measurements extrapolated at 50 ab^{-1} show expected precision $\leq 0.1\%$ on mixing parameters x and y .
- Phase 2 without vertex detector will be commissioned in few days, and phase 3 with full Belle II detector early next year.
- Era of precision measurements is approaching. Stay tuned!



Thank you!

Belle → Belle II

- High luminosity → higher event rate and radiation damage to detectors from **machine background processes**
- Upgrade Belle to have better performances in higher radiation environment

Covered by Alexei Sibidanov on Belle II readiness for Phase II collisions

