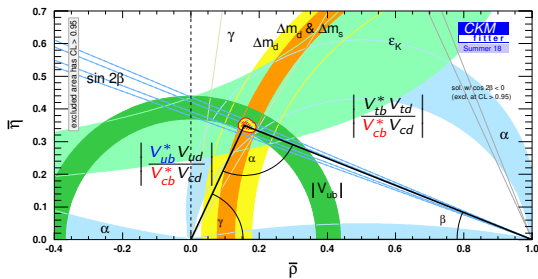


The Prospects for $|V_{ub}|$ and $|V_{cb}|$ at Belle II

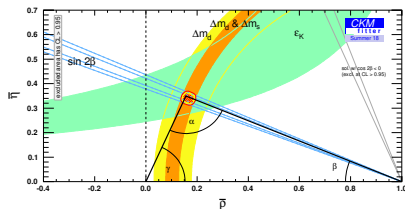
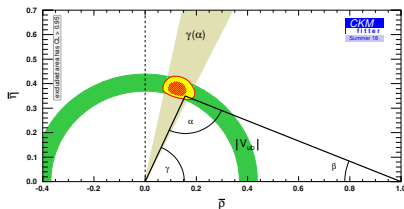


Why are $|V_{ub}|$ and $|V_{cb}|$ important?

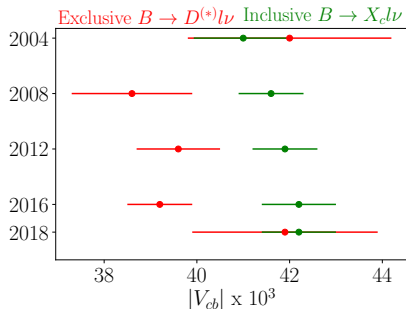
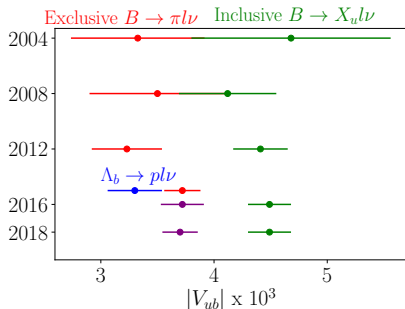
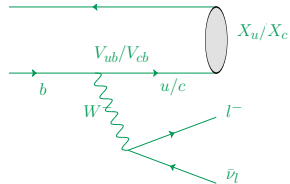
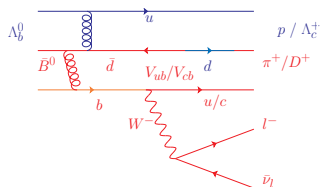


Trees

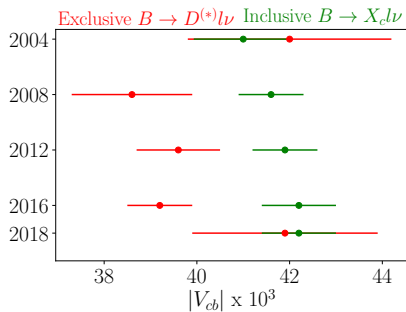
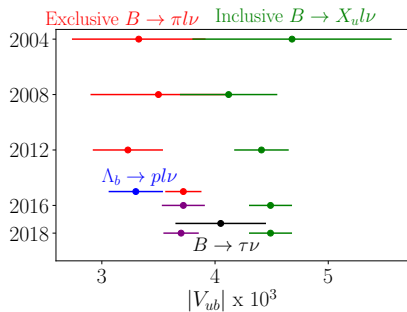
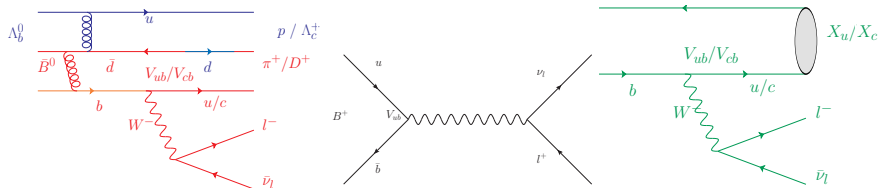
Loops



Status of $|V_{ub}|$ and $|V_{cb}|$

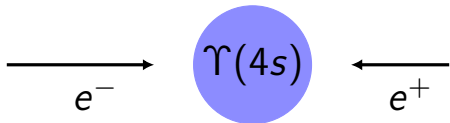


Status of $|V_{ub}|$ and $|V_{cb}|$



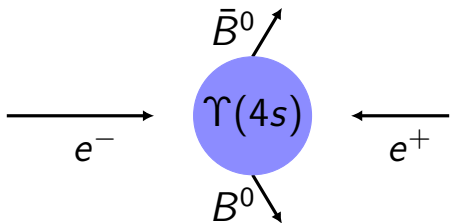
Semileptonic B reconstruction

- Collide e^+ and e^- at the energy to make $\Upsilon(4S)$ particles



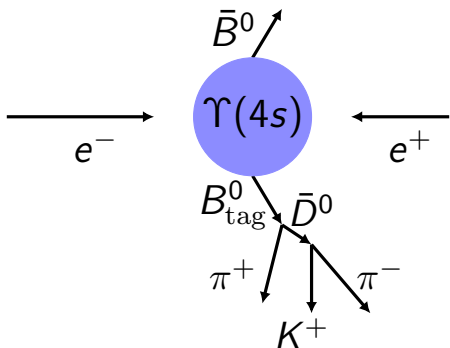
Semileptonic B reconstruction

- Collide e^+ and e^- at the energy to make $\Upsilon(4S)$ particles
- $\Upsilon(4S)$ decays to B^+B^- and $B^0\bar{B}^0 > 96\%$ of the time.



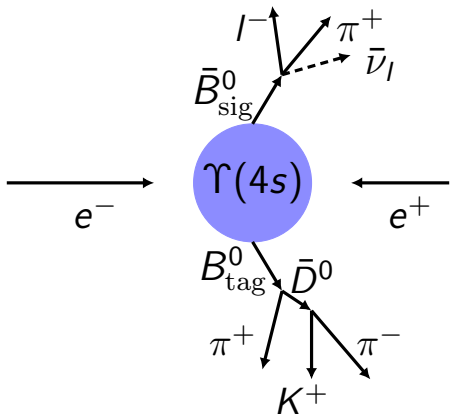
Semileptonic B reconstruction

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- $\Upsilon(4S)$ decays to B^+B^- and $B^0\bar{B}^0 > 96\%$ of the time.
- Tagged approach:
 - ▶ Reconstruct one B meson as tag-side (B_{tag}) hadronic or SL



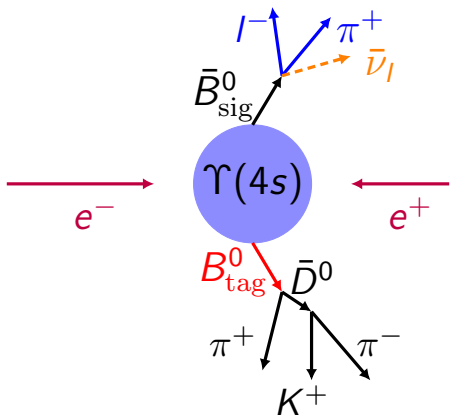
Semileptonic B reconstruction

- Collide e^+ and e^- at the energy to make $\Upsilon(4S)$ particles
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- Tagged approach:
 - ▶ Reconstruct one B meson as tag-side (B_{tag}) hadronic or SL
 - ▶ Study remaining B meson as signal (B_{sig})



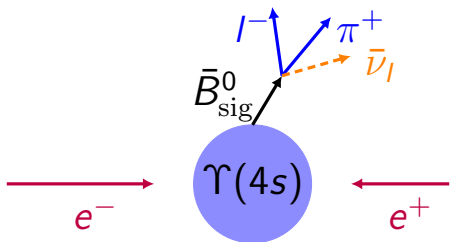
Semileptonic B reconstruction

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- $\Upsilon(4S)$ decays to B^+B^- and $B^0\bar{B}^0 > 96\%$ of the time.
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 - ▶ Reconstruct one B meson as tag-side (B_{tag}) hadronic or SL
 - ▶ Study remaining B meson as signal (B_{sig})
 - ▶ $p_\nu = p_{e^+e^-} - p_{\mu^-} - p_\pi - p_{B_{\text{tag}}}$



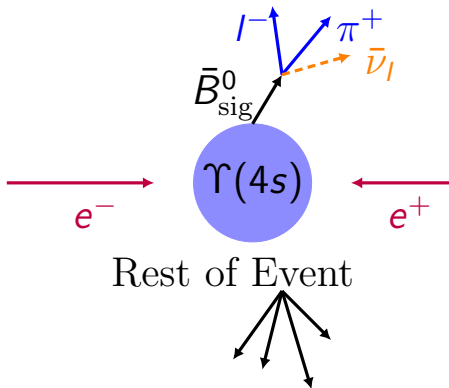
Semileptonic B reconstruction

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 - ▶ Study remaining B meson as signal (B_{sig})
 - ▶ $p_\nu = p_{e^+e^-} - p_{\mu^-} - p_\pi - p_{B_{\text{tag}}}$
- Untagged approach:
 - ▶ Reconstruct signal first.

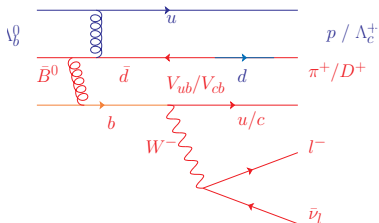


Semileptonic B reconstruction

- Collide e^+ and e^- at the energy to make $\Upsilon(4S)$ particles
- $\Upsilon(4S)$ decays to B^+B^- and $B^0\bar{B}^0 > 96\%$ of the time.
- Tagged approach:
 - ▶ Reconstruct one B meson as tag-side (B_{tag}) hadronic or SL
 - ▶ Study remaining B meson as signal (B_{sig})
 - ▶ $p_\nu = p_{e^+e^-} - p_{\mu^-} - p_\pi - p_{B_{\text{tag}}}$
- Untagged approach:
 - ▶ Reconstruct signal first.
 - ▶ Inclusively sum over all tracks and clusters in remaining event or only use signal information e.g $p_l, \cos\theta_{BHl}$

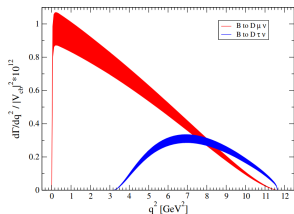
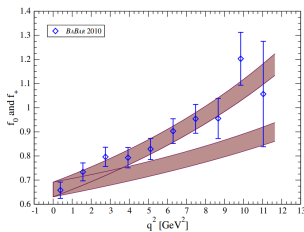


Exclusive theory



- Matrix element factorises

$$\mathcal{M} = -i \frac{G_F}{\sqrt{2}} V_{qb} H^\mu L_\mu$$
- $\mathcal{B} \propto \mathcal{M}^2 \propto |V_{qb}|^2$
- $H^\mu(f_i(q^2)) = \langle X | \bar{q} \gamma^\mu (1 - \gamma_5) b | B \rangle$
- **Form factors $f_i(q^2)$** computed with LCSR [see N. Gubernari] or LQCD [see A. Kronfeld]



H. Na et al. PRD 92 054510 (2015)

Exclusive $|V_{ub}|$ from untagged $\bar{B}^0 \rightarrow \pi^+ l^- \bar{\nu}_l$

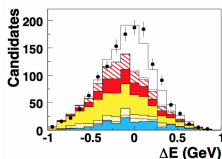
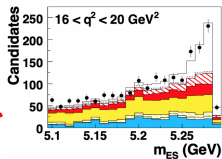
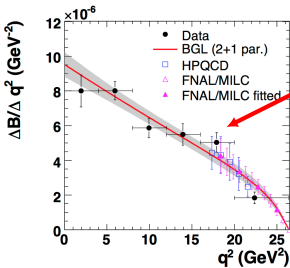
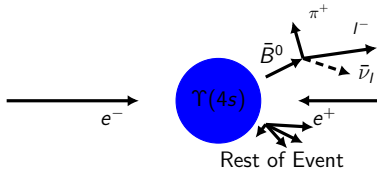
- Select good π and l candidates.

$$p_\nu = (E_{\text{miss}}, \mathbf{p}_{\text{miss}})$$

$$= p_{e^+e^-} - p_\pi - p_l - \sum p_{\text{tracks}} - \sum p_{\text{clusters}}$$

$$p_B = p_\pi + p_l + (P_{\text{miss}}, \mathbf{p}_{\text{miss}})$$

- Fit $M_{bc} = \sqrt{E_{\text{beam}}^{*2} - P_B^{*2}}$ and $\Delta E = E_B^* - E_{\text{beam}}^*$, ($*$ \Rightarrow CoM).



Measurement

BABAR (6 q^2 bins)

BABAR (12 q^2 bins)

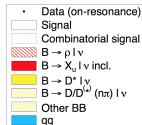
Belle (13 q^2 bins)

Reference

Phys. Rev. D83, 032007 (2011)

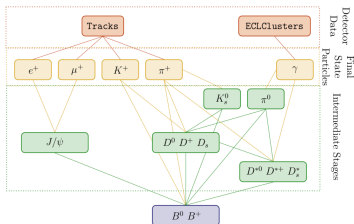
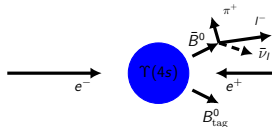
Phys. Rev. D86, 092004 (2012)

Phys. Rev. D83, 071101 (2011)



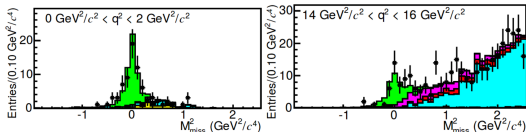
Exclusive $|V_{ub}|$ from tagged $\bar{B}^0 \rightarrow \pi^+ l^- \bar{\nu}_l$

- $p_\nu = p_{e^+e^-} - p_\pi - p_l - p_{B_{\text{tag}}}$
- Fit Missing Mass Squared (p_ν^2)

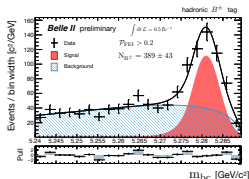
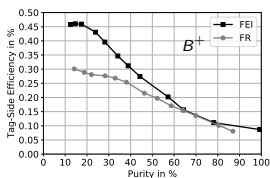


Measurement
Belle (13 q^2 bins)

Reference
Phys. Rev. D88, 032005 (2013)

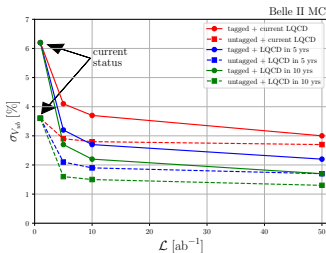
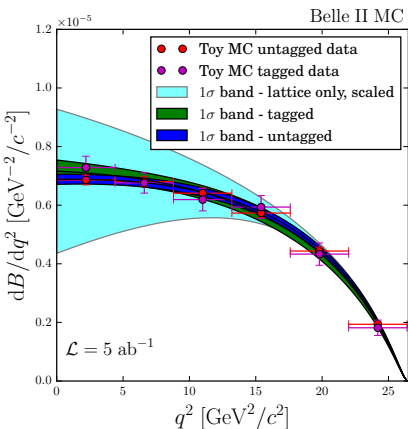


- Improved tag-side reconstruction algorithm: Full Event Interpretation
- Reconstructs O(5000) decay chains.
- Higher tag-side efficiency at lower purities.



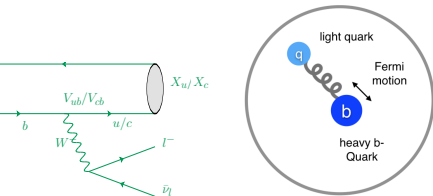
Projected $|V_{ub}|$ from $\bar{B}^0 \rightarrow \pi^+ l^- \bar{\nu}_l$ decays

- MC tagged and untagged analyses performed in the B2TIP report [[arXiv:1808.10567](https://arxiv.org/abs/1808.10567)]



Source	Error (Limit) [%]	
	Tagged [%]	Untagged
Tracking efficiency	0.4	2.0
Pion identification	–	1.3
Lepton identification	1.0	2.4
Kaon veto	0.9	–
Continuum description	1.0	1.8
Tag calibration and $N_{B\bar{B}}$	4.5 (2.0)	2.0 (1.0)
$X_U l \nu$ cross-feed	0.9	0.5 (0.5)
$X_C l \nu$ background	–	0.2 (0.2)
Form factor shapes	1.1	1.0 (1.0)
Form factor background	–	0.4 (0.4)
Total	5.0	4.5
(reducible, irreducible)	(4.6, 2.0)	(4.2, 1.6)

$|V_{ub}|$ from inclusive decays

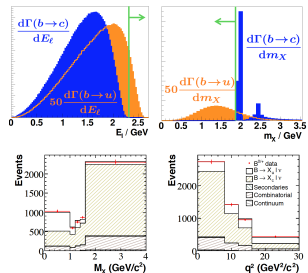
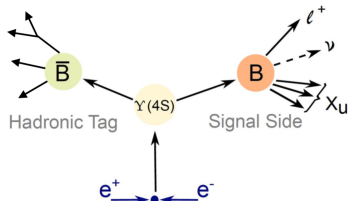


$$\frac{d^3\Gamma}{dp_X^+ dp_X^- dE_\ell} = \frac{G_F^2 |V_{ub}|^2}{192\pi^3} \int dk C(E_\ell, p_X^-, p_X^+, k) F(k) + O\left(\frac{\Lambda_{\text{QCD}}}{m_b}\right)$$

- Large background from $b \rightarrow c$
- Exploit $b \rightarrow c$ kinematic endpoints.
- $|V_{ub}| = \sqrt{\Delta\mathcal{B}/(\tau_B \Delta\Gamma)}$

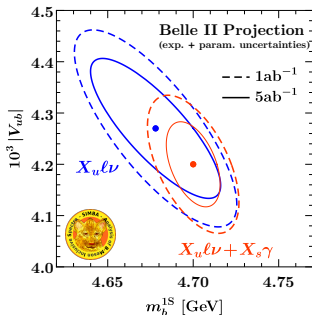
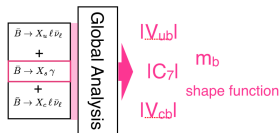
- $F(k)$ pdf of b quark momentum, k
- $C(E_\ell, p_X^-, p_X^+, k)$ computed perturbatively

Phys. Rev. Lett. 104, 021801



Future of inclusive $|V_{ub}|$

$$F(k) = \sum_n (c_n f_n(k))^2$$

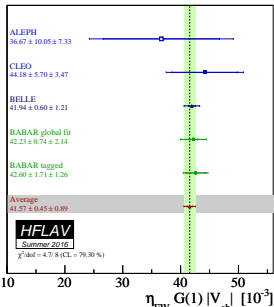
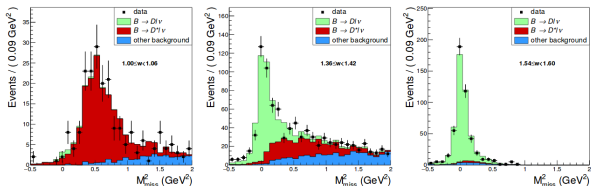


Source	Error on \mathcal{B} (irreducible limit)
$\mathcal{B}(D^{(*)}\ell\nu)$	1.2 (0.6)
Form factors ($D^{(*)}\ell\nu$)	1.2 (0.6)
Form factors & $\mathcal{B}(D^{**}\ell\nu)$	0.2
$B \rightarrow X_u \ell \nu$ (SF)	3.6 (1.8)
$B \rightarrow X_u \ell \nu (g \rightarrow s\bar{s})$	1.5
$\mathcal{B}(B \rightarrow \pi/\rho/\omega \ell \nu)$	2.3
$\mathcal{B}(B \rightarrow \eta^{(\prime)} \ell \nu)$	3.2
$\mathcal{B}(B \rightarrow X_u \ell \nu)$ unmeasured/fragmentation	2.9 (1.5)
Continuum & Combinatorial	1.8
Secondaries, Fakes & Fit	1.0
PID& Reconstruction	3.1
BDT/Normalisation	3.1 (2.0)
Total	8.1
(Total reducible)	7.4
(Total irreducible)	3.2

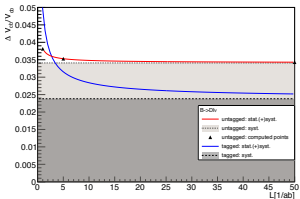
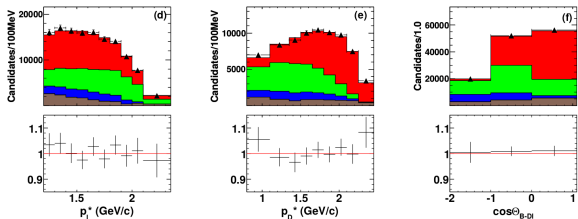
	Exp.	Theory	Total
605 fb^{-1}	6.0%	2.5-4.5%	6.5-7.5%
5 ab^{-1}	2.3%	2.5-4.5%	3.4-5.1%
50 ab^{-1}	1.7%	2.5-4.5%	3.0-4.8%

$|V_{cb}|$ from $B \rightarrow D l \nu$

- Tagged: fit M_{miss}^2 in bins of w [Phys. Rev. D93, 032006 (2016)] $w = (m_B^2 + m_{D^{(*)}}^2 - q^2)/(2m_B m_{D^{(*)}})$ Latest LQCD (2015) PRD 92 054510, PRD 92 034506

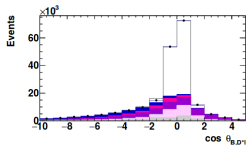
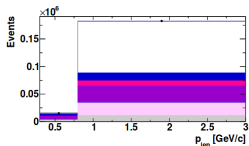
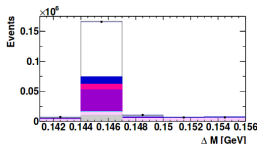


- Untagged fit of BaBar to p_D^* , p_l^* and $\cos\theta_{\text{BDI}}$

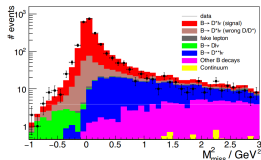


$|V_{cb}|$ from $B \rightarrow D^* l \nu$

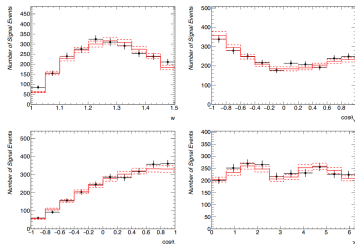
- Untagged: 3D fit ($\cos\theta_{BD^*l}$, p_l , ΔM) [Belle: PRD 82, 112007 (2010), arXiv:1809.03290]



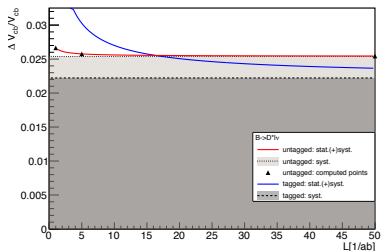
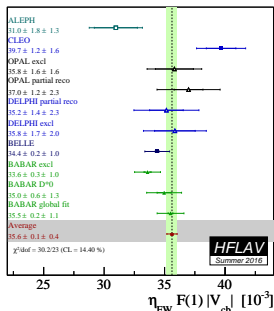
- Tagged fit to M_{miss}^2 [Belle: arXiv:1702.01521]



- Fits performed in 1D bins of angular variables and w .



$|V_{cb}|$ from $B \rightarrow D^* l \nu$



- Analysis of arXiv:1702.01521 by independent groups

[D. Bigi et al., PLB (2017) 441, B. Grinstein et al., PLB 771 (2017) 359]

BGL Fit:	Data + lattice	Data + lattice + LCSR	CLN Fit:	Data + lattice	Data + lattice + LCSR
χ^2/dof	27.9/32	31.4/35	χ^2/dof	34.3/36	34.8/39
$ V_{cb} $	$0.0417^{(+20)}_{(-21)}$	$0.0404^{(+16)}_{(-17)}$	$ V_{cb} $	$0.0382(15)$	$0.0382(14)$
a_0^f	$0.01223(18)$	$0.01224(18)$	$\rho_{D^*}^2$	$1.17^{(+15)}_{(-16)}$	$1.16(14)$
a_1^f	$-0.054^{(+58)}_{(-43)}$	$-0.052^{(+27)}_{(-15)}$	$R_1(1)$	$1.391^{(+92)}_{(-88)}$	$1.372(36)$
a_2^f	$0.2^{(+7)}_{(-12)}$	$1.0^{(+0)}_{(-5)}$	$R_2(1)$	$0.913^{(+73)}_{(-80)}$	$0.916^{(+65)}_{(-70)}$
$a_1^{f_1}$	$-0.0100^{(+61)}_{(-56)}$	$-0.0070^{(+54)}_{(-52)}$	$h_{A_1}(1)$	$0.906(13)$	$0.906(13)$
$a_2^{f_1}$	$0.12(10)$	$0.089^{(+96)}_{(-100)}$			
a_0^g	$0.012^{(+11)}_{(-8)}$	$0.0289^{(+57)}_{(-37)}$			
a_1^g	$0.7^{(+3)}_{(-4)}$	$0.08^{(+8)}_{(-22)}$			
a_2^g	$0.8^{(+2)}_{(-17)}$	$-1.0^{(+20)}_{(-0)}$			

- New LQCD at non-zero recoil imminent: arXiv1901.00216

$|V_{cb}|$ from inclusive $B \rightarrow X_c l \nu$ decays

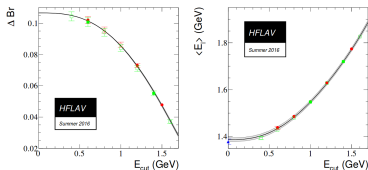
$$\Gamma = \frac{G_F^2 m_b^5}{192\pi^3} |V_{cb}|^2 \left(1 + \frac{c_5(\mu) O_5(\mu)}{m_b^2} + \frac{c_6(\mu) O_6(\mu)}{m_b^3} + \mathcal{O}\left(\frac{1}{m_b^4}\right) \right)$$

- Operator Product Expansion (OPE):

- ▶ O_i : hadronic matrix elements (non-perturbative)
- ▶ c_i : coefficients (perturbative)

Order	Kinetic	1S
$\mathcal{O}(1)$	m_b, m_c	m_b
$\mathcal{O}(1/m_b^2)$	μ_π^2, μ_G^2	λ_1, λ_2
$\mathcal{O}(1/m_b^3)$	ρ_D^3, ρ_{LS}^3	ρ_1, τ_{1-3}

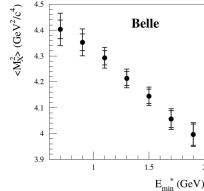
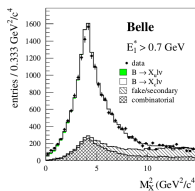
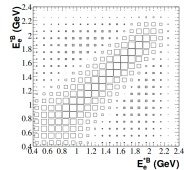
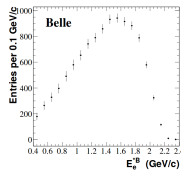
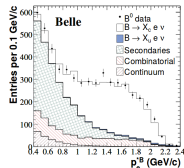
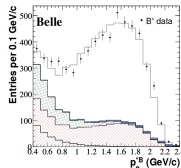
- Moments of E_l, M_X can be expressed with same OPE formulation.
- \implies Measure moments to constrain expansion parameters.



	$ V_{cb} [10^{-3}]$	$m_b^{\text{kin}} [\text{GeV}]$	$m_c^{\text{MS}} [\text{GeV}]$	$\mu_\pi^2 [\text{GeV}^2]$	$\rho_D^3 [\text{GeV}^3]$	$\mu_G^2 [\text{GeV}^2]$	$\rho_{LS}^3 [\text{GeV}^3]$
value	42.19	4.554	0.987	0.464	0.169	0.333	-0.153
error	0.78	0.018	0.015	0.076	0.043	0.053	0.096
$ V_{cb} $	1.000	-0.257	-0.078	0.354	0.289	-0.080	-0.051
m_b^{kin}		1.000	0.769	-0.054	0.097	0.360	-0.087
m_c^{MS}			1.000	-0.021	0.027	0.059	-0.013
μ_π^2				1.000	0.732	0.012	0.020
ρ_D^3					1.000	-0.173	-0.123
μ_G^2						1.000	0.066
ρ_{LS}^3							1.000

Inclusive $|V_{cb}|$ at Belle

- Analyses used 140 fb^{-1} and older tagging $\Rightarrow \times \mathcal{O}(10)$ statistics with Belle dataset.
- PRD 75, 032001 (2007):
 - Fit of p_l for $B \rightarrow X_c e \nu_e$ in B rest frame.
 - Unfolded E_e and determined its moments and a \mathcal{B}
- PRD 75, 032005 (2007):
 - Fit of M_X^2 for $B \rightarrow X_c l \nu_l$
 - Calculated moments of this distribution.
- Expect 1.2% uncertainty on inc. $|V_{cb}|$ from Belle II with 5 ab^{-1}

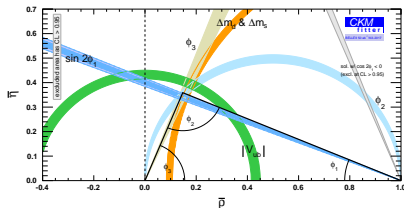
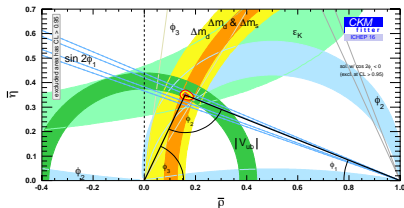
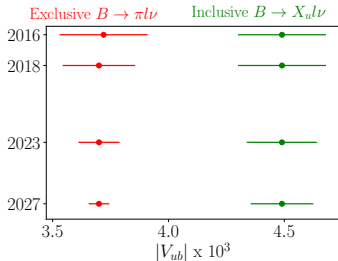
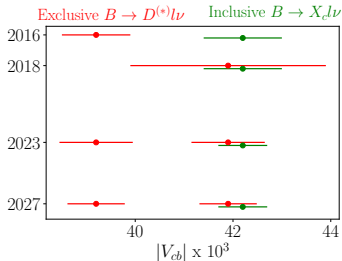


Summary of $|V_{ub}|$ projections

	Statistical	Systematic (reducible, irreducible)	Total Exp	Theory	Total
$ V_{ub} $ exclusive (had. tagged)					
711 fb ⁻¹	3.0	(2.3, 1.0)	3.8	7.0	8.0
5 ab ⁻¹	1.1	(0.9, 1.0)	1.8	1.7	3.2
50 ab ⁻¹	0.4	(0.3, 1.0)	1.2	0.9	1.7
$ V_{ub} $ exclusive (untagged)					
605 fb ⁻¹	1.4	(2.1, 0.8)	2.7	7.0	7.5
5 ab ⁻¹	1.0	(0.8, 0.8)	1.2	1.7	2.1
50 ab ⁻¹	0.3	(0.3, 0.8)	0.9	0.9	1.3
$ V_{ub} $ inclusive					
605 fb ⁻¹ (old B tag)	4.5	(3.7, 1.6)	6.0	2.5–4.5	6.5–7.5
5 ab ⁻¹	1.1	(1.3, 1.6)	2.3	2.5–4.5	3.4–5.1
50 ab ⁻¹	0.4	(0.4, 1.6)	1.7	2.5–4.5	3.0–4.8
$ V_{ub} B \rightarrow \tau\nu$ (had. tagged)					
711 fb ⁻¹	18.0	(7.1, 2.2)	19.5	2.5	19.6
5 ab ⁻¹	6.5	(2.7, 2.2)	7.3	1.5	7.5
50 ab ⁻¹	2.1	(0.8, 2.2)	3.1	1.0	3.2
$ V_{ub} B \rightarrow \tau\nu$ (SL tagged)					
711 fb ⁻¹	11.3	(10.4, 1.9)	15.4	2.5	15.6
5 ab ⁻¹	4.2	(4.4, 1.9)	6.1	1.5	6.3
50 ab ⁻¹	1.3	(2.3, 1.9)	2.6	1.0	2.8

Observables	Belle	Belle II	
	(2017)	5 ab ⁻¹	50 ab ⁻¹
$ V_{cb} $ incl.	$42.2 \cdot 10^{-3} \cdot (1 \pm 1.8\%)$	1.2%	–
$ V_{cb} $ excl.	$39.0 \cdot 10^{-3} \cdot (1 \pm 3.0\%_{\text{ex.}} \pm 1.4\%_{\text{th.}})$	1.8%	1.4%
$ V_{ub} $ incl.	$4.47 \cdot 10^{-3} \cdot (1 \pm 6.0\%_{\text{ex.}} \pm 2.5\%_{\text{th.}})$	3.4%	3.0%
$ V_{ub} $ excl. (WA)	$3.65 \cdot 10^{-3} \cdot (1 \pm 2.5\%_{\text{ex.}} \pm 3.0\%_{\text{th.}})$	2.4%	1.2%

The future of $|V_{ub}|$ and $|V_{cb}|$



Conclusion

- Exclusive determination of $|V_{ub}|$ from $B \rightarrow \pi/\nu$ decays will be most precise (1-2%)
- Exclusive and inclusive determinations of $|V_{cb}|$ will have a precision of 1 – 1.5%.
- Precision tree level determinations of $|V_{ub}|$ and γ will allow a stringent testing of any incompatibility with loop level CKM observables.

$B \rightarrow D^{(*)} l \nu$ form factor parametrisations

$$\frac{d\Gamma}{dw}_{B \rightarrow D l \nu} = \frac{G_F^2 m_D^3}{48\pi^3} (m_B + m_D)^2 (w^2 - 1)^{3/2} \times \mathcal{G}^2(w) |V_{cb}|^2$$

$$w = (m_B^2 + m_{D^{(*)}}^2 - q^2) / (2m_B m_{D^{(*)}})$$

CLN [Nucl. Phys. B530, 153 (1998)]

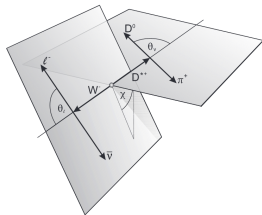
$$\mathcal{G}(z) = \mathcal{G}(1)(1 - 8\rho^2 z + (51\rho^2 - 10)z^2 - (252\rho^2 - 84)z^3)$$

$$z(w) = (\sqrt{w+1} - \sqrt{2}) / (\sqrt{w+1} + \sqrt{2})$$

BGL [Phys. Rev. Lett, 74,4603 (1995)]

$$f_i(z) = \frac{1}{P_i(z)\phi_i(z)} \sum_n a_{i,n} z^n$$

$$\frac{d\Gamma}{dw}_{B \rightarrow D^* l \nu} = \iiint \frac{d\Gamma}{dw d\theta_l d\theta_\nu d\chi} d\theta_l d\theta_\nu d\chi$$

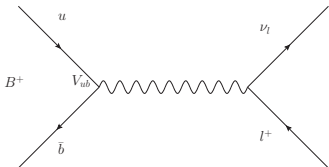


$$\frac{d\Gamma}{dq} = \frac{G_F^2 m_{D^*}^3}{48\pi^3} (m_B - m_{D^*})^2 (w^2 - 1)^{3/2} \times u(w) \mathcal{F}^2(w) |V_{cb}|^2$$

CLN pars $F(1)$, ρ^2 , $R_1(1)$ and $R_2(1)$

$|V_{ub}|$ from leptonic decays

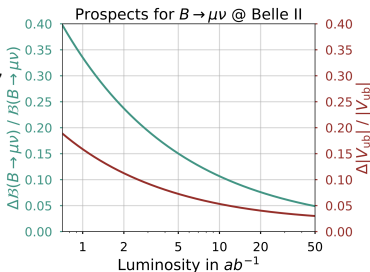
$$\mathcal{B}(B^- \rightarrow l^- \bar{\nu}_l) = \frac{G_F^2 m_B m_l^2}{8\pi} \left(1 - \frac{m_l^2}{m_B^2}\right) f_B^2 |V_{ub}|^2 \tau_B$$



- Expect 3% uncertainty on $|V_{ub}|$ from $B \rightarrow \tau\nu$ tagged and $B \rightarrow \mu\nu$ untagged.

	5 ab^{-1}	50 ab^{-1}
Had. tag	7.5	3.2
SL. tag	6.3	2.8

- \mathcal{B} s are hierarchical with lepton mass due to helicity suppression.
- $f_B = 187.1 \text{ MeV} (0.7\%)$
- 3 σ evidence for $B \rightarrow \mu\nu$ [see talk of M. Prim]

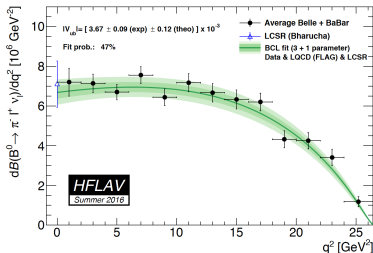
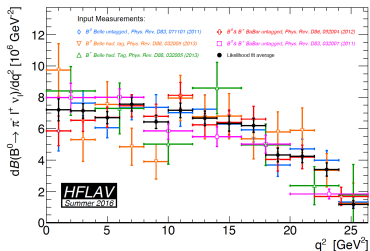


Global $|V_{ub}|$ determination from $\bar{B}^0 \rightarrow \pi^+ l^- \bar{\nu}_l$ decays

- Fit data and form factor, $f_+(q^2)$ under a BCL parametrisation.

$$f_+(q^2, \vec{b}) = \frac{1}{1 - q^2/m_{B^*}^2} \sum_{k=0}^{K-1} b_k \left[z^k - (-1)^{k-K} \frac{k}{K} z^K \right], \quad z = \frac{\sqrt{1 - q^2/t_+} - \sqrt{1 - t_0/t_+}}{\sqrt{1 - q^2/t_+} + \sqrt{1 - t_0/t_+}}$$

$$\chi^2 = (\Delta\vec{B} - \tau_B \Delta\vec{\Gamma}(\vec{b}, |V_{ub}|))^T C^{-1} (\Delta\vec{B} - \tau_B \Delta\vec{\Gamma}(\vec{b}, |V_{ub}|)) + (\vec{b} - \vec{b}_{LQCD})^T C_{LQCD}^{-1} (\vec{b} - \vec{b}_{LQCD})$$



$$|V_{ub}| = (3.70 \pm 0.10(exp.) \pm 0.12(th.)) \times 10^{-3} \quad (\text{data} + \text{LQCD}) \quad 4.2\%$$

$$|V_{ub}| = (3.67 \pm 0.09(exp.) \pm 0.12(th.)) \times 10^{-3} \quad (\text{data} + \text{LQCD} + \text{LCSR}) \quad 4\%$$

Previous Belle $\bar{B}^0 \rightarrow \pi^+ l^- \bar{\nu}_l$ systematics

Source	Error (Limit) [%]	
	Tagged [%]	Untagged
Tracking efficiency	0.4	2.0
Pion identification	–	1.3
Lepton identification	1.0	2.4
Kaon veto	0.9	–
Continuum description	1.0	1.8
Tag calibration and $N_{B\bar{B}}$	4.5 (2.0)	2.0 (1.0)
$\chi_{ul\nu}$ cross-feed	0.9	0.5 (0.5)
$\chi_{cl\nu}$ background	–	0.2 (0.2)
Form factor shapes	1.1	1.0 (1.0)
Form factor background	–	0.4 (0.4)
Total	5.0	4.5
(reducible, irreducible)	(4.6, 2.0)	(4.2, 1.6)

$|V_{ub}|$ from $\Lambda_b \rightarrow p\mu^-\bar{\nu}_\mu$ decays at LHCb

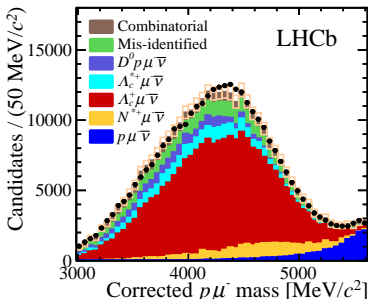
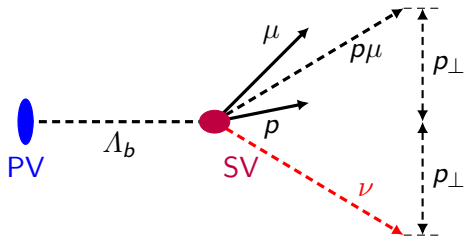
- Fit the corrected mass for $q^2 > 15 \text{ GeV}^2$:

$$M_{\text{corr}} = \sqrt{p_\perp^2 + M_{p\mu}^2} + p_\perp$$

$$\frac{|V_{ub}|^2}{|V_{cb}|^2} = \frac{\mathcal{B}(\Lambda_b \rightarrow p\mu^-\bar{\nu}_\mu)_{q^2 > 15 \text{ GeV}^2}}{\mathcal{B}(\Lambda_b \rightarrow \Lambda_c\mu^-\bar{\nu}_\mu)_{q^2 > 7 \text{ GeV}^2}} R_{FF}$$

- $|V_{ub}| = (3.27 \pm 0.23) \times 10^{-3}$

Nat. Phys. volume 11, (2015)



Prospects for $|V_{ub}|$ from $\Lambda_b \rightarrow p\mu^-\bar{\nu}_\mu$ decays

Table 1 | Summary of systematic uncertainties.

Source	Relative uncertainty (%)
$\mathcal{B}(\Lambda_c^+ \rightarrow pK^+\pi^-)$	+4.7 -5.3
Trigger	3.2
Tracking	3.0
Λ_c^+ selection efficiency	3.0
$\Lambda_b^0 \rightarrow N^*\mu^-\bar{\nu}_\mu$ shapes	2.3
Λ_b^0 lifetime	1.5
Isolation	1.4
Form factor	1.0
Λ_b^0 kinematics	0.5
q^2 migration	0.4
PID	0.2
Total	+7.8 -8.2

- $\mathcal{B}(\Lambda_c \rightarrow pK\pi)$ improves in line with Belle II data
- Account for increased luminosity, collision energy and trigger improvements.
- A differential q^2 measurement would reduce the theory uncertainty.

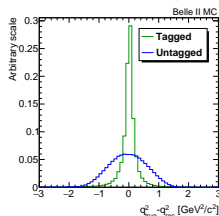
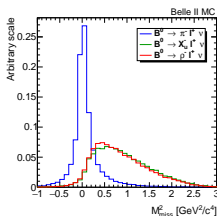
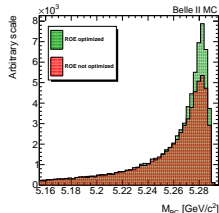
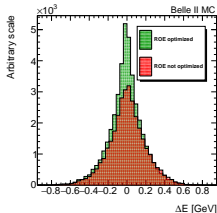
Albrecht et al. arXiv:1709.10308v5

	LHCb	8 fb ⁻¹	22 fb ⁻¹	50 fb ⁻¹
$ V_{ub}/V_{cb} $		3.4%	2.9%	2.1%
$ V_{ub} $		3.8%	3.3%	2.4%

$\bar{B}^0 \rightarrow \pi^+ l^- \bar{\nu}_l$ prospects

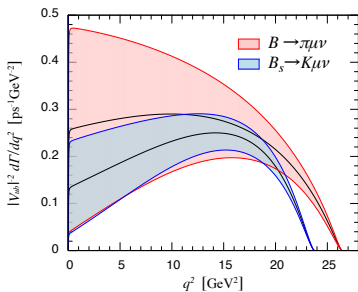
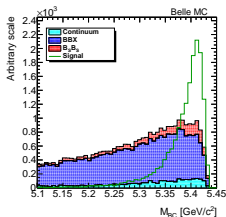
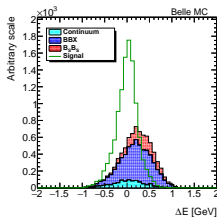
- Tagged and untagged analyses performed on Belle II MC.
- Untagged use optimised BDT selections for tracks and clusters in the Rest of the event.
- Tagged uses the Belle 2 tagging algorithm (FEI)

	Belle ϵ	Belle II ϵ
untagged	7.7-15%	20%
tagged	0.3%	0.55%



$\bar{B}_s^0 \rightarrow K^+ \mu^- \bar{\nu}_\mu$ Prospects

- Smaller theoretical uncertainty than $\bar{B}^0 \rightarrow \pi^+ l^- \bar{\nu}_l$
- LHCb measurement to come!



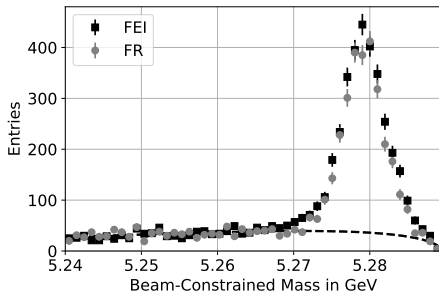
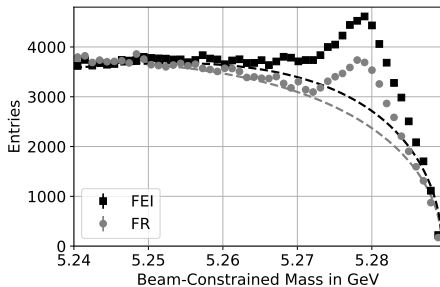
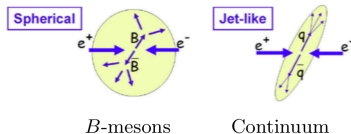
- At Belle II expect 60M $B_s^{(*)} \bar{B}_s^{(*)}$ pairs in 1ab^{-1}
- 5-10% precision on the decay rate with 1ab^{-1}

Tagging performance

$$m_{bc} = \sqrt{E_B^2 - p_B^2}$$

$$E_B = \sqrt{s}/2$$

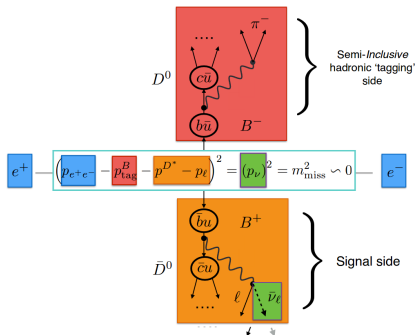
Different event topologies



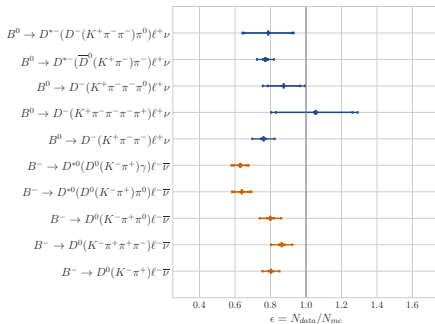
FR = Full Reconstruction

Calibration of hadronic tagging

- Use the FEI on Belle data to reconstruct several well known semileptonic decays.
- $\epsilon = N_{DATA}/N_{MC}$



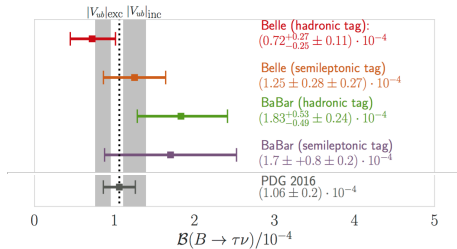
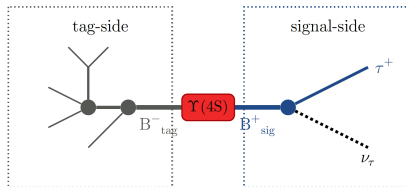
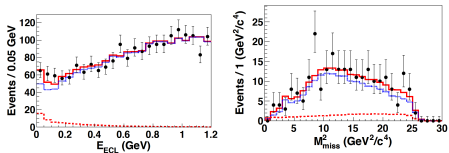
$$\epsilon_{\text{charged}} = 0.74 \pm 0.05$$



$$\epsilon_{\text{neutral}} = 0.86 \pm 0.07$$

$B^- \rightarrow \tau^- \bar{\nu}_\tau$ status

- Reconstruct B_{tag} hadronically or semileptonic.
- τ reconstructed in $e^- \nu_\tau \bar{\nu}_e$, $\mu^- \nu_\tau \bar{\nu}_\mu$, $\pi^- \bar{\nu}_\tau$, $\rho^- \bar{\nu}_\tau$,
- Fit sum of remaining energy in the EM calorimeter (E_{ECL})



Projecting $|V_{ub}|$ from $B^- \rightarrow \tau^- \bar{\nu}_\tau$

Belle Hadronic

Source	B syst. error (%)
Signal PDF	4.2
Background PDF	8.8
Peaking background	3.8
B_{tag} efficiency	7.1
Particle identification	1.0
π^0 efficiency	0.5
Tracking efficiency	0.3
τ branching fraction	0.6
MC efficiency statistics	0.4
K_L^0 efficiency	7.3
$N_{B^+B^-}$	1.3
Total	14.7

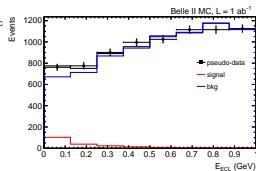
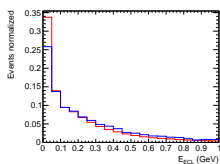
Belle Semileptonic

TABLE III. List of systematic uncertainties.

Source	Relative uncertainty (%)
Continuum description	14.1
Signal reconstruction efficiency	0.6
Background branching fractions	3.1
Efficiency calibration	12.6
τ decay branching fractions	0.2
Histogram PDF shapes	8.5
Best candidate selection	0.4
Charged track reconstruction	0.4
π^0 reconstruction	1.1
Particle identification	0.5
Charged track veto	1.9
Number of $B\bar{B}$ pairs	1.4
Total	21.2

- Pseudo analysis performed on Belle 2 MC

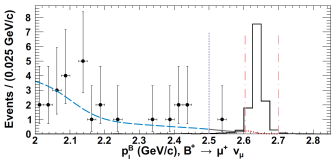
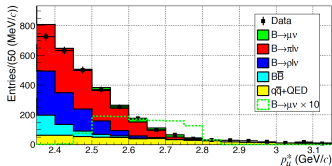
	$\int \mathcal{L} \text{ (ab}^{-1}\text{)}$	1	5	50
Had. tag	stat. uncertainty (%)	29.2	13.0	4.1
	syst. uncertainty (%)	12.6	6.8	4.6
	total uncertainty (%)	31.6	14.7	6.2
SL. tag	stat. uncertainty (%)	19.0	8.5	2.7
	syst. uncertainty (%)	17.9	8.7	4.5
	total uncertainty (%)	26.1	12.2	5.3



$ V_{ub} B \rightarrow \tau \nu$ (had. tagged)					
711 fb $^{-1}$	18.0	(7.1, 2.2)	19.5	2.5	19.6
5 ab $^{-1}$	6.5	(2.7, 2.2)	7.3	1.5	7.5
50 ab $^{-1}$	2.1	(0.8, 2.2)	3.1	1.0	3.2
$ V_{ub} B \rightarrow \tau \nu$ (SL tagged)					
711 fb $^{-1}$	11.3	(10.4, 1.9)	15.4	2.5	15.6
5 ab $^{-1}$	4.2	(4.4, 1.9)	6.1	1.5	6.3
50 ab $^{-1}$	1.3	(2.3, 1.9)	2.6	1.0	2.8

$|V_{ub}|$ from $B^- \rightarrow \mu^- \bar{\nu}_\mu$ decays

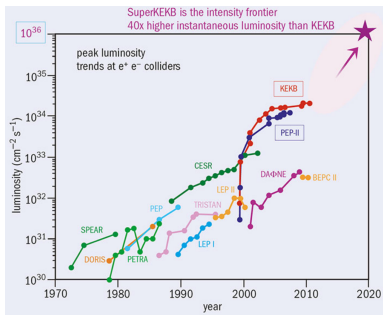
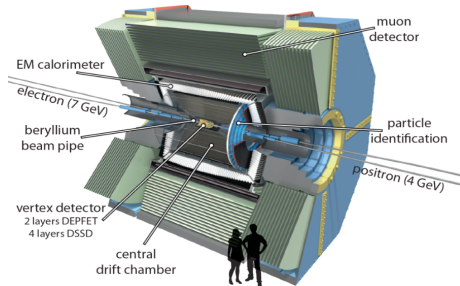
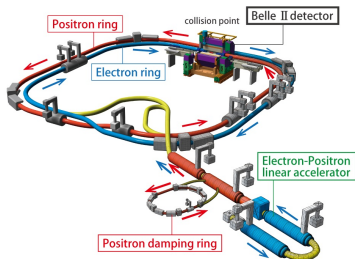
Experiment	Upper limit @ 90% C.L.	Comment
Belle	2.7×10^{-6}	Fully reconstructed hadronic tag, 711 fb^{-1}
Belle	1.7×10^{-6}	Untagged analysis, 253 fb^{-1}
BaBar	1.0×10^{-6}	Untagged analysis, $468 \times 10^6 B\bar{B}$ pairs
Belle	2.9×10^{-7}	Untagged analysis, 711 fb^{-1}



- Untagged using CoM p_μ^*
- Tagged use $p_\mu^B = m_B/2 \implies$ high resolution but smaller statistics.

	50 ab^{-1}	$\mathcal{B}\text{Stat.}$	$\mathcal{B}\text{Syst.}$	$ V_{ub} $
Belle II Untagged		$\sim 5\%$	$\sim 5\%$	3-4%
Belle II tagged		$\sim 13\%$	-	-

The Belle II Experiment



See P. Urquijo's talk

