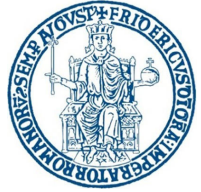




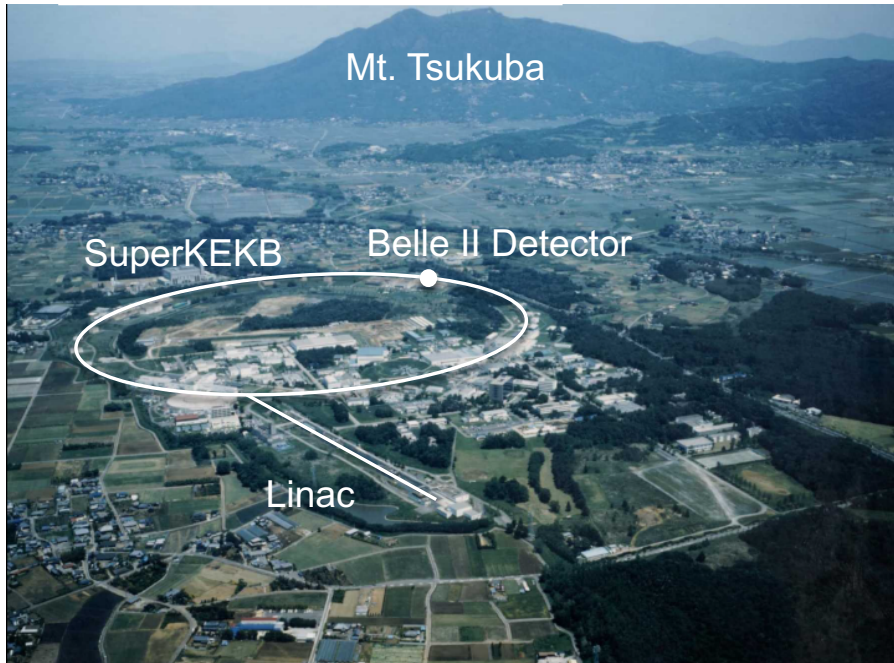
# LFV, lepton universality, and rare decay searches at $e^+e^-$ colliders



Mario Merola (Università di Napoli Federico II and INFN)

On behalf of the Belle II Collaboration

BLV2019, 21-24 October 2019, Madrid



**BL 2019** 2019 International Workshop on Baryon and Lepton Number Violation

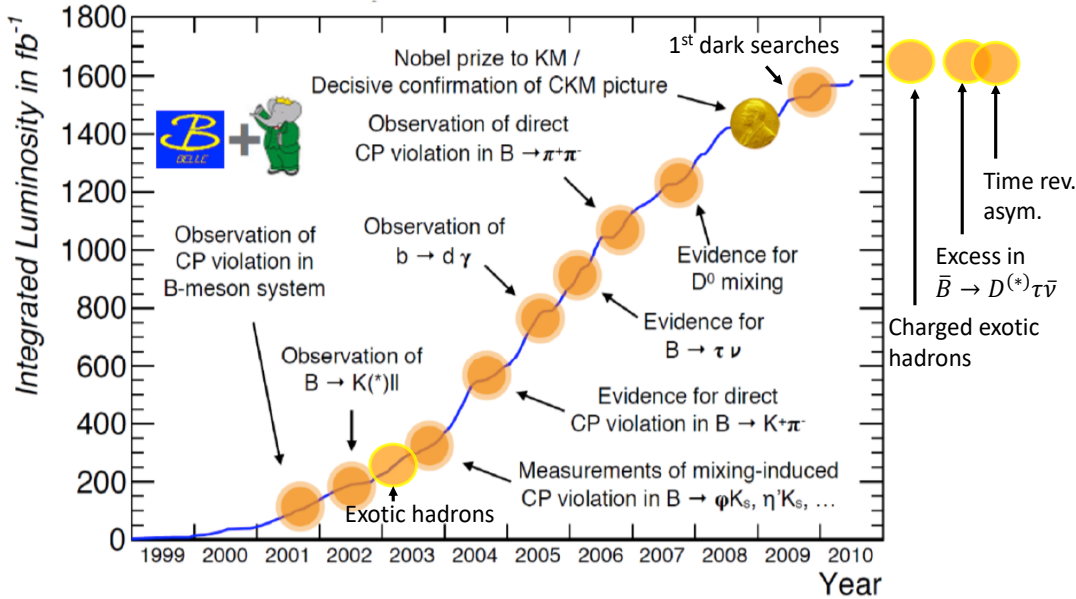
21-24 October 2019, Madrid, IFT

International Organizing Committee	Conveners	Junior Organizing Committee	Administrative support
A. Abada	K. Abazajian	J. Alonso	R. Belló
L. Baudis	S. Davidson	F. Arias	C. Rubiera
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E. Fernandez-Martinez	J. M. No	A. Tait	
F. Ferrer-Pérez (co-chair)	S. Pascoli	G. Tselika	
	N. Rius	Y. Wang	
		T. Lin	

**inVisiblesPlus** **elusiões**

\*Deceased. We are saddened by the tragic passing away of our colleagues and coorganizers.

<https://indico.cern.ch/event/754031>



To: PEP-II/BaBar  
and KEKB/Belle

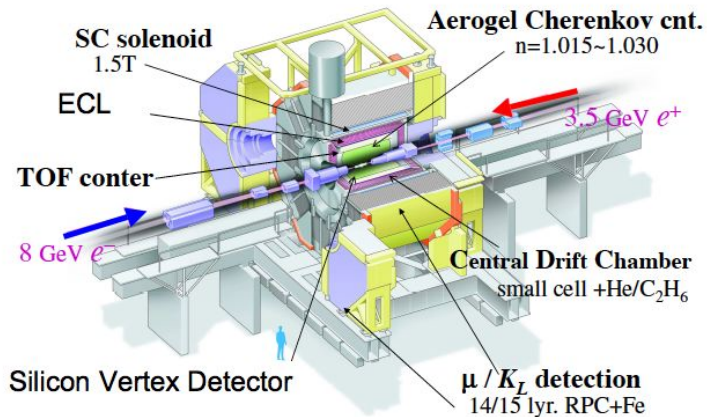
小林 尚  
益川 敏英

2008.10.25

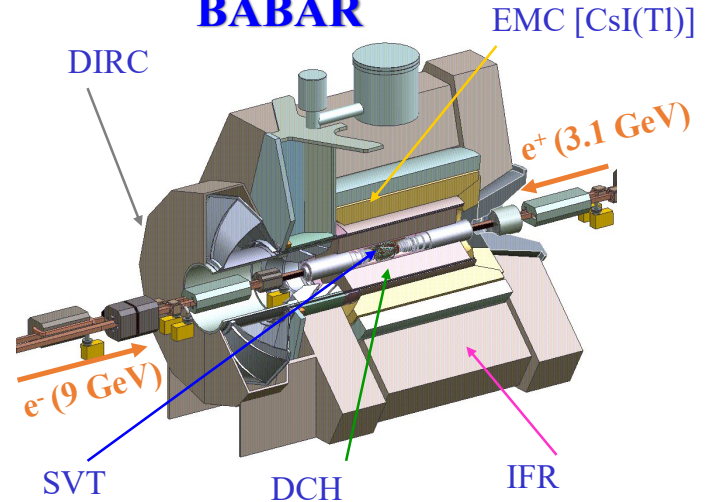


**Kobayashi, Maskawa  
nobel prize in 2008**

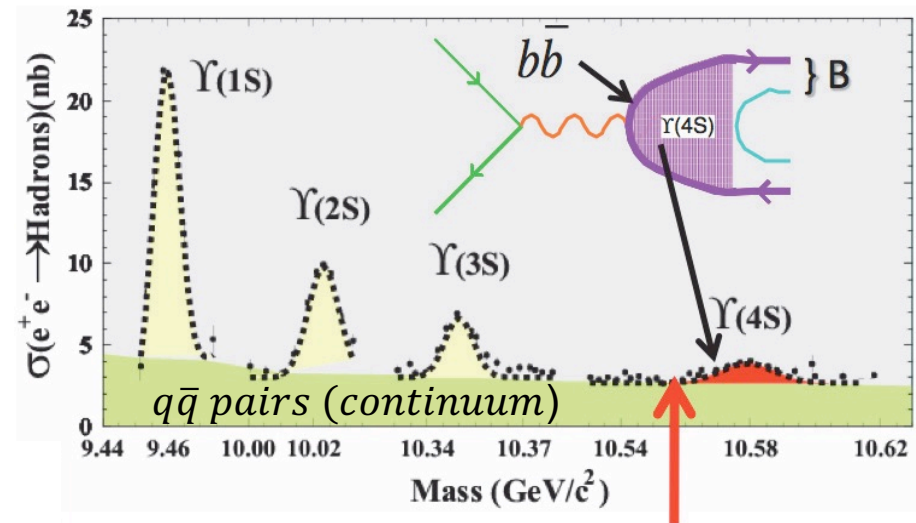
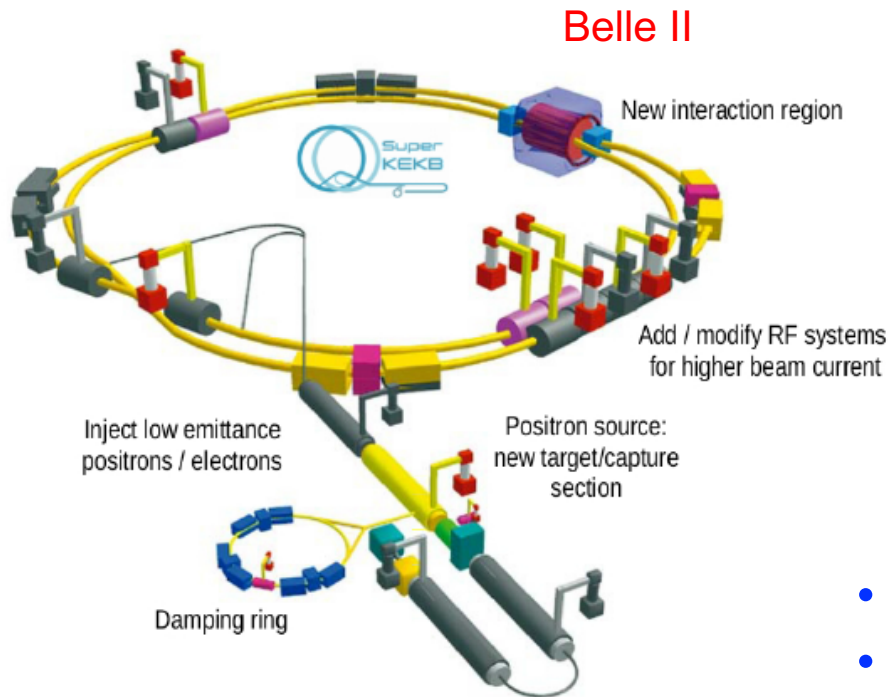
## Belle Detector



## BABAR

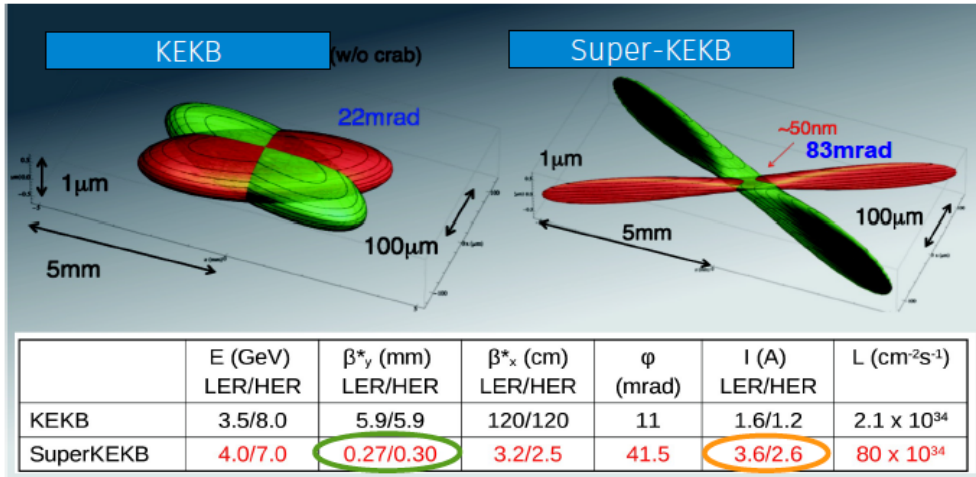


- **Electron-positron collider** situated at KEK (Tsukuba, Japan), upgrade of KEKB
- $e^+e^-$  (4 GeV + 7 GeV)  $\rightarrow$   $B\bar{B}$  mainly at  $\sqrt{s_{cm}}=10.58$  GeV (peak of  $\Upsilon(4S)$  resonance)



- **B-factory** ( $10^9$  pairs per  $ab^{-1}$ )
- **tau and charm factory** ( $10^9$  pairs per  $ab^{-1}$ )

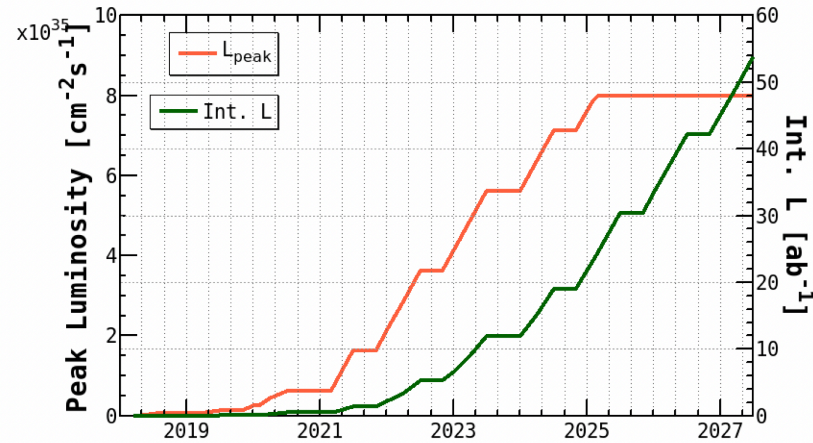
Nano-beam scheme firstly proposed by P. Raimondi for SuperB



factor 20

factor 2-3

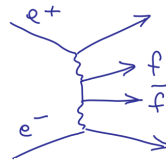
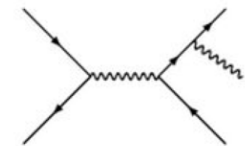
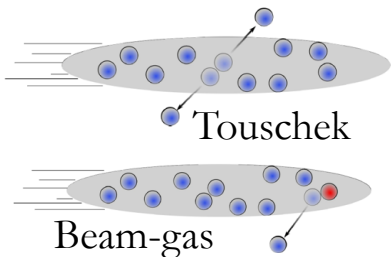
Factor ~ 40-50 in the luminosity



$$L = \frac{\gamma_{\pm}}{2 e r_e} \left( 1 + \frac{\sigma_y^*}{\sigma_x^*} \right) \frac{I_{\pm} \xi_{y\pm}}{\beta_{y\pm}} \frac{R_L}{R_{\xi_y}}$$

beam current  
vertical beta function at IP

## Higher backgrounds

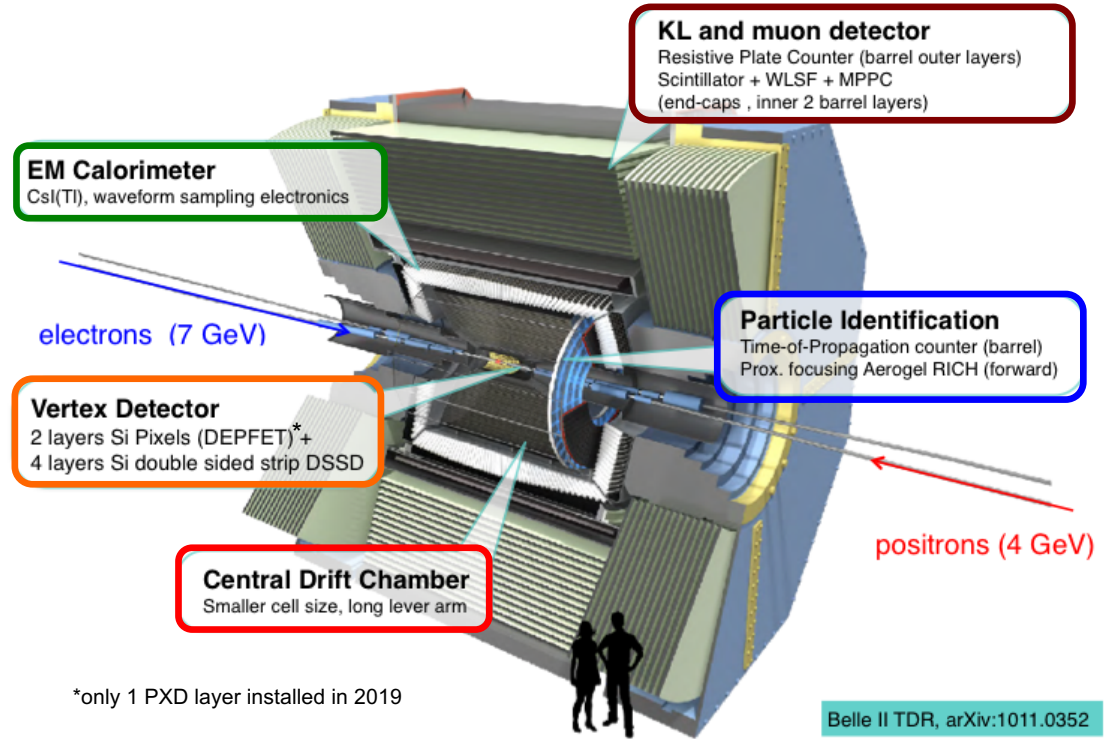
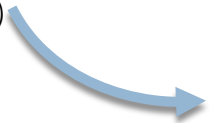


$e^+e^-$ :  
 $\sigma \sim O(10^7 \text{ nb})$

- Radiation damage
- Occupancy in inner detectors
- Fake hits and pile-up

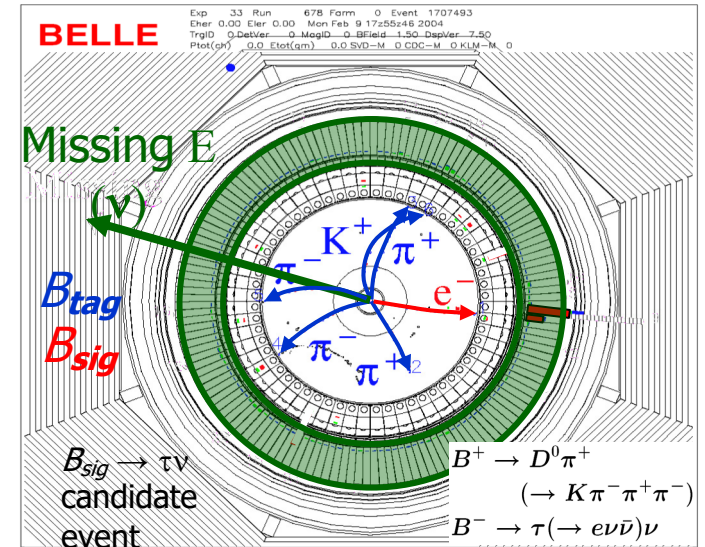
## Belle Upgrade:

- **Extended VXD region:** PXD and SVD (silicon pixel and strips detectors)
- **Extended Drift Chamber region**
- **ECL:** CsI(Tl) crystals. **New electronics** (waveform sampling and fitting)
- **TOP and ARICH detectors:** better hermeticity with new PID detector in the forward region
- **KLM detector:** **RPCs and scintillators** (some RPCs layers substituted with scintillators to resist neutron background)



- improved IP and secondary vertex resolution
- better K/ $\pi$  separation and flavor tagging
- robust against machine background
- higher  $K_S$ ,  $\pi^0$  and slow pions reconstruction efficiency

- **Beam energy constraint:** can be adjusted for different resonances  $\Upsilon(nS)$
- **Clean experimental environment:** high B, D, K,  $\tau$  lepton and neutral final states reconstruction efficiency.
- **BB produced in quantum correlated state:** high flavour tagging efficiencies (36% vs 3% @LHCb)

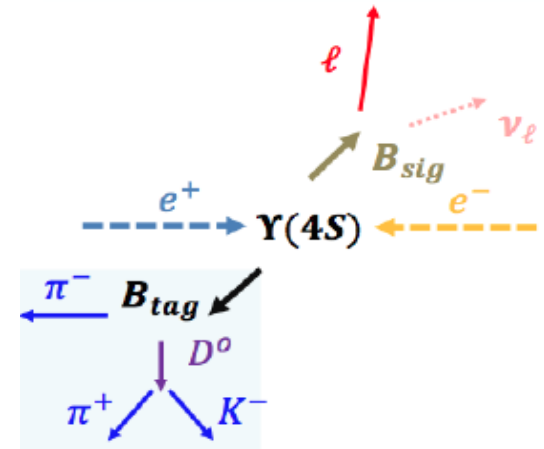


The **full reconstruction of one B ( $B_{tag}$ )** constraints the 4-momentum of the other ( $B_{sig}$ )



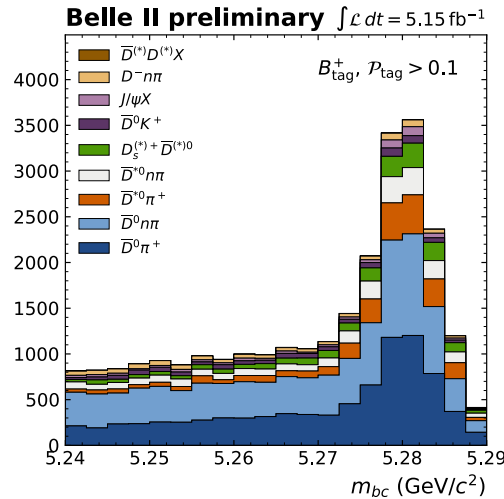
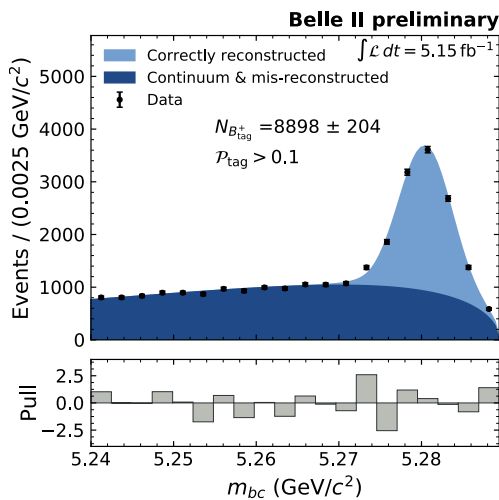
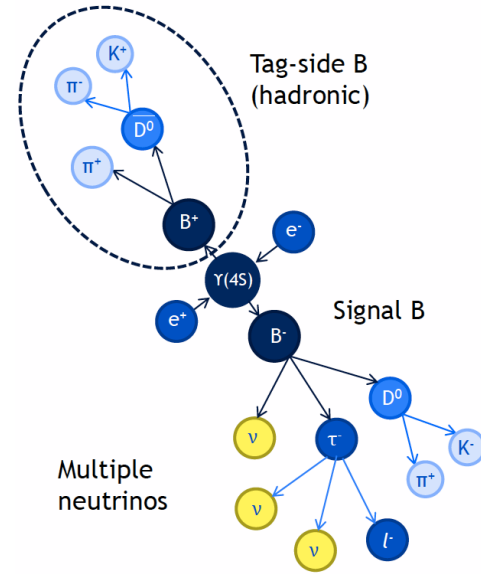
Reconstruction of **channels with missing energy**

$$p_\nu = p_{e^+e^-} - p_{B_{tag}} - p_{B_{sig}}$$



# Tag side reconstruction: Full Event Interpretation (FEI)

- It is a development of the Full Reconstruction (FR) used in Belle, and uses a **multivariate technique** to reconstruct the B-tag side (semileptonic or hadronic) through  $O(10^3)$  decay modes in a  $Y(4S)$  decay.
- Tested on Belle II early data



$$M_{bc} \equiv \sqrt{\frac{s}{4} - p_B^{*2}}$$

Tag algorithm	Efficiency $B^\pm/B^0$ (%)	Purity (%)
BaBar (SER)	0.4/0.2	30
Belle (FR)	0.28/0.18	10
Belle II (FEI)	0.76/0.46	10

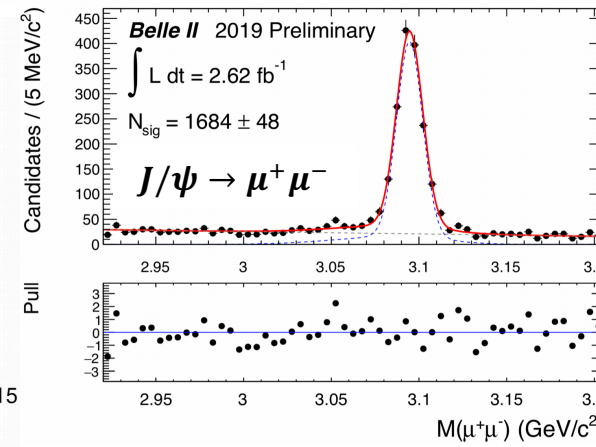
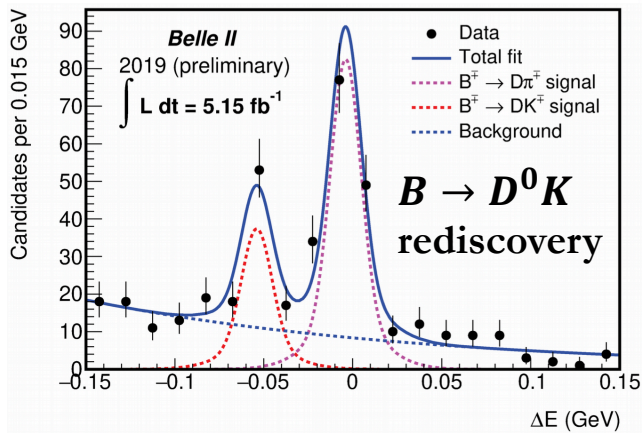
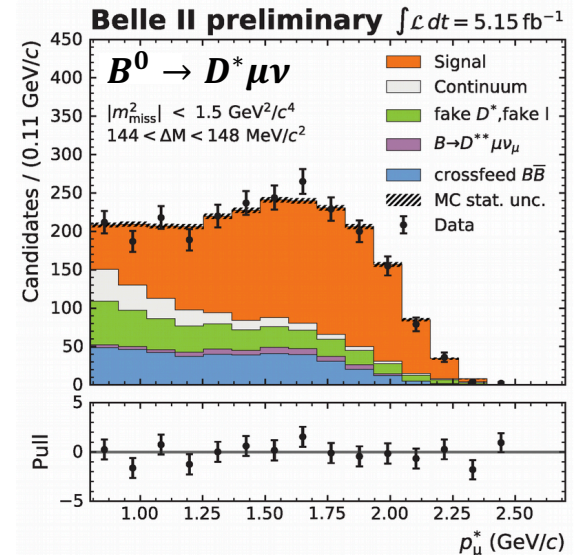
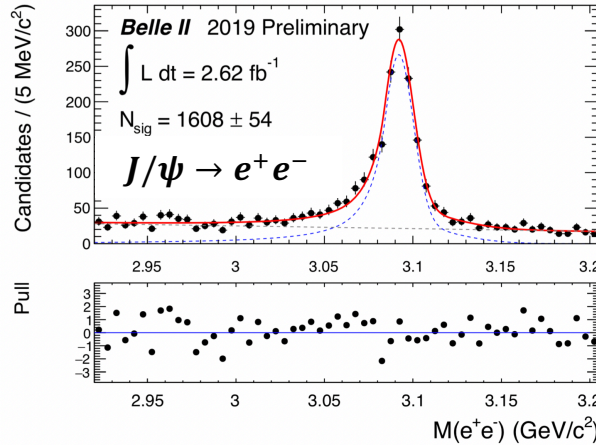
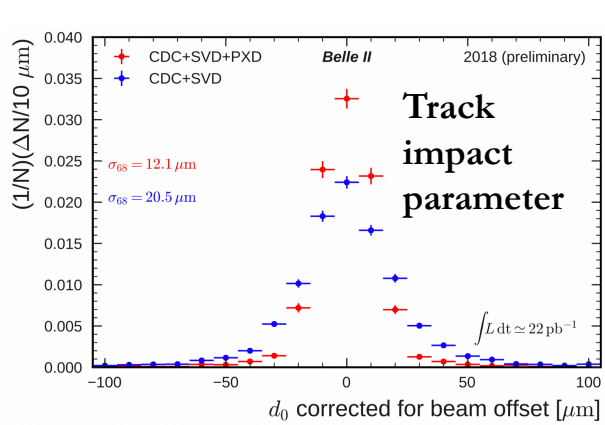
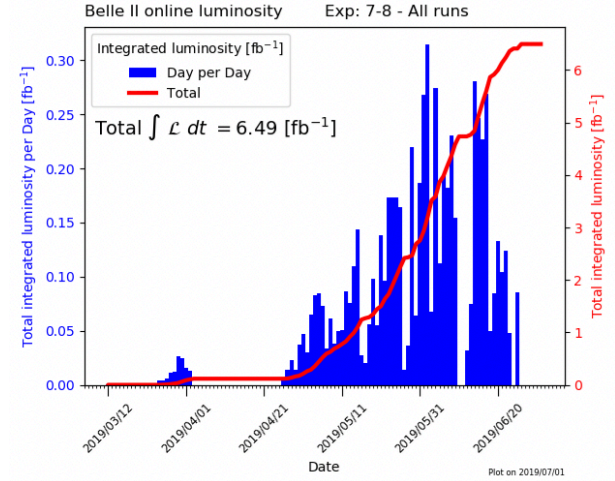
Performances with hadronic tag

**Belle FR:** NIM A 654, 432-440 (2011)

**Belle II FEI:** Keck, T., Abudinén, F., Bernlochner, F.U. et al. Comput Softw Big Sci (2019) 3: 6.

<https://doi.org/10.1007/s41781-019-0021-8>

- **Phase 1 (2016-2018):** no collisions, beam background studies
- **Phase 2 (2018):** collisions, no vertex detector, dark sector studies
- **Phase 3 (2019-2027):** full detector, superKEKB peak luminosity in 2019  $1.2 \times 10^{34} / (cm^2 \cdot s)$  (half of the KEKB peak)





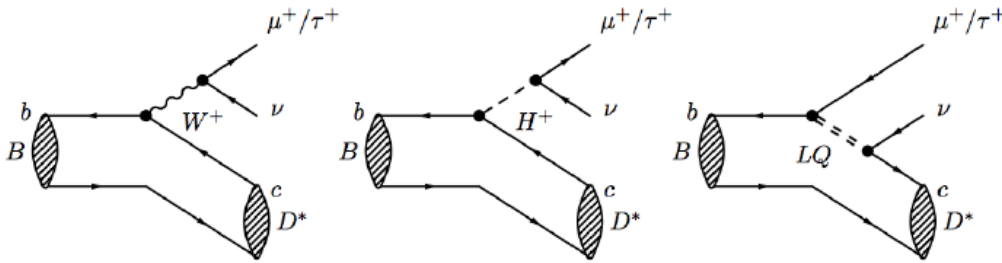
- **Semileptonic B decays with missing energy**
  - $B \rightarrow X\ell\nu$ , measurement of  $R(D), R(D^*)$
- **FCNC B decays with leptons in the final state**
  - $B \rightarrow X_s\ell^+\ell^-$ , measurement of  $R(K), R(K^*), P_5'$
- **Tau lepton decays**
  - $\tau \rightarrow 3\ell, \tau \rightarrow \ell\gamma, \tau \rightarrow \ell h$

Other channels as  $B \rightarrow K^{(*)}\nu\bar{\nu}, B \rightarrow \ell\nu (\gamma)$  in the backup slides

*Belle II physics reach projections summarized in the  
Belle II Physics Book*

*(<https://arxiv.org/abs/1808.10567>, soon available on PTEP)*

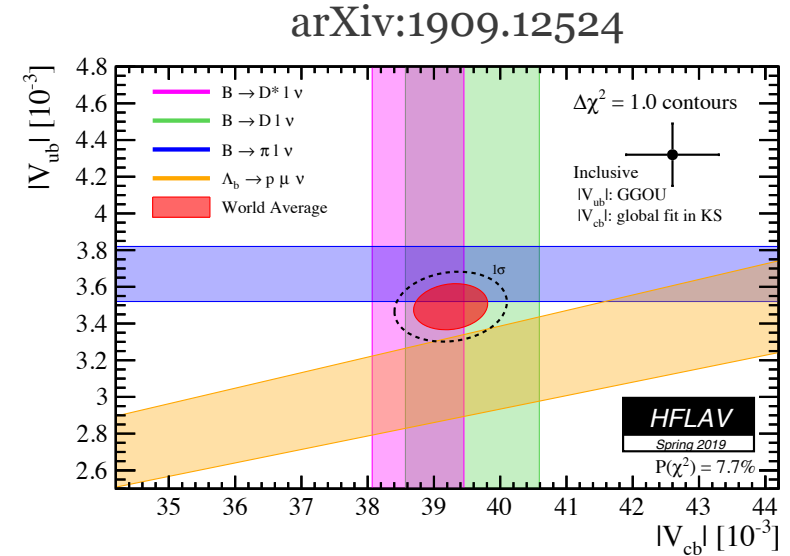
Clear test of the SM LFU: **NP** (charged Higgs in 2HDM models or Leptoquarks) **can affect the BR, the tau polarization  $P_\tau$  and  $|V_{cb}|$**



$$\mathcal{R}(D^{(*)}) = \frac{\mathcal{B}(\bar{B} \rightarrow D^{(*)}\tau^- \bar{\nu}_\tau)}{\mathcal{B}(\bar{B} \rightarrow D^{(*)}\ell^- \bar{\nu}_\ell)} \quad (\ell = e, \mu)$$

## Advantages of measuring $\mathcal{R}(D^{(*)})$ :

- **experimentally** we eliminate the uncertainties on the tagging efficiencies
- **theoretically** we eliminate the uncertainties on  $|V_{cb}|$  and on the semileptonic form factors  $\rightarrow$  **complementary to the inclusive / exclusive searches**

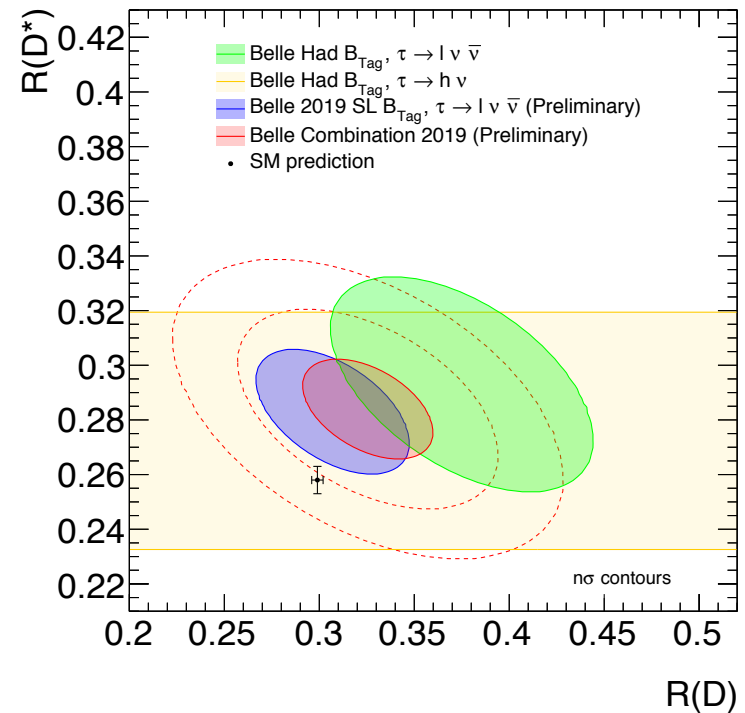
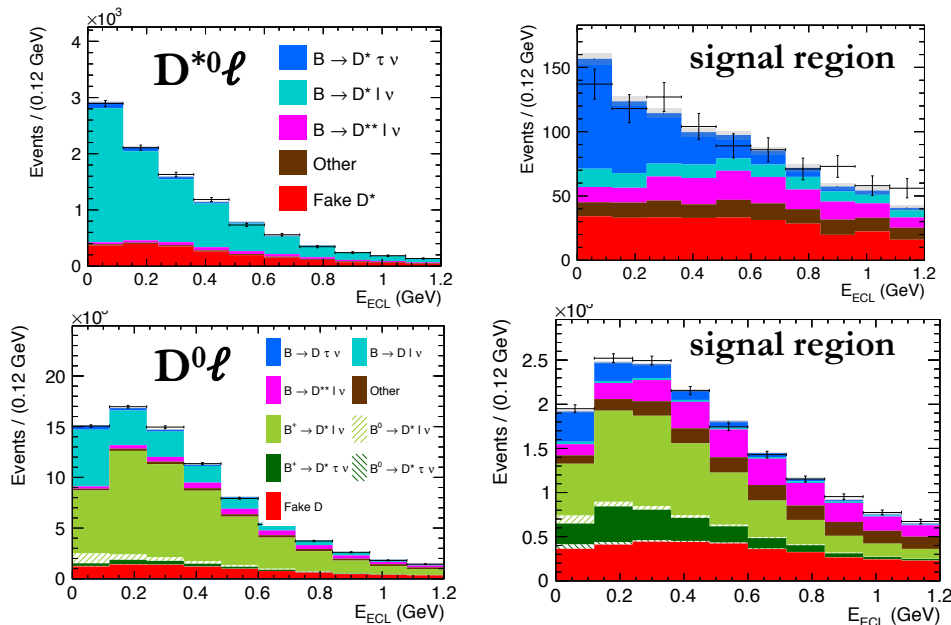


Inclusive vs exclusive tension

- Simultaneous fit to the  $E_{ECL}$  distribution of the signal ( $D^{(*)}\tau\nu$ ) and normalization modes ( $D^{(*)}\ell\nu$ )

[arXiv:1904.08794](https://arxiv.org/abs/1904.08794) (2019) **SL tag**

$E_{ECL}$  is the extra energy left in the calorimeter after the signal and tag B are reconstructed

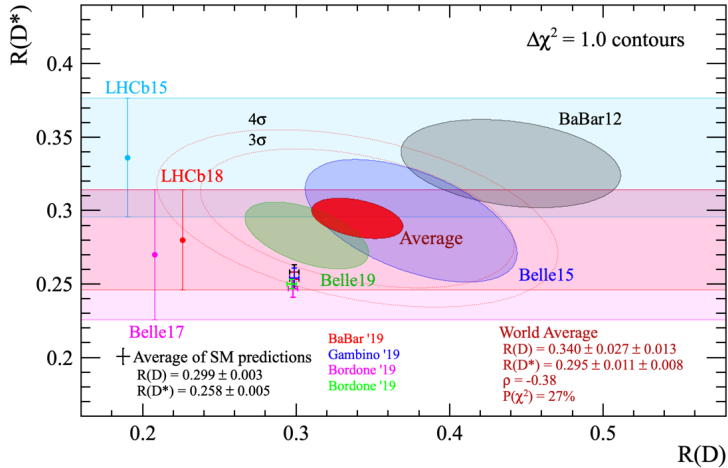


Signal and normalization separation is based mainly on the missing mass and the angle between B meson and  $D^{(*)}\ell$  system

New Belle combination is  $2\sigma$  from the SM

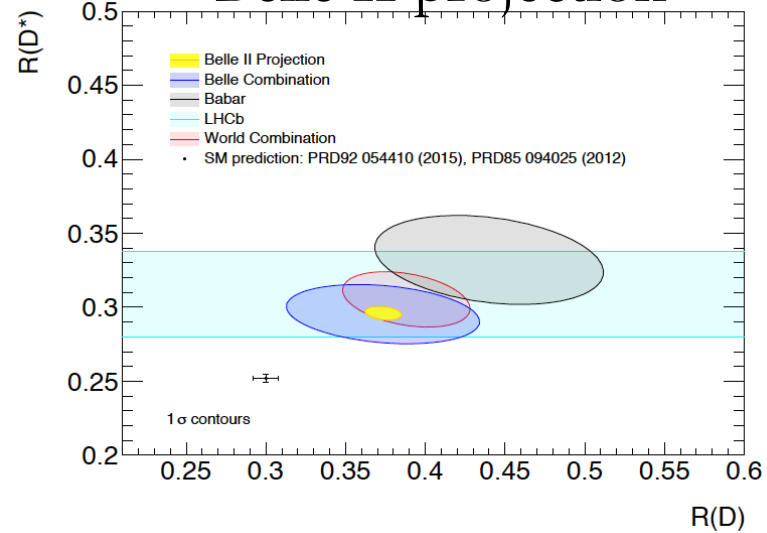
$$R(D^{*}) = \frac{1}{2\mathcal{B}(\tau^- \rightarrow \ell^- \bar{\nu}_\ell \nu_\tau)} \cdot \frac{\epsilon_{\text{norm}}}{\epsilon_{\text{sig}}} \cdot \frac{N_{\text{sig}}}{N_{\text{norm}}}$$

## World average



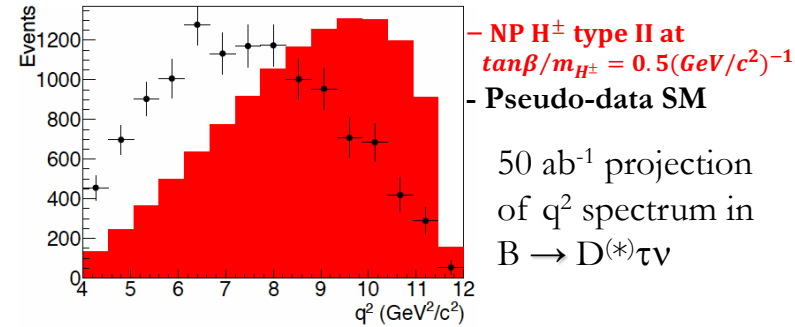
Current combination:  $3.1\sigma$  from the SM

## Belle II projection



	$\Delta R(D)$ [%]			$\Delta R(D^*)$ [%]		
	Stat	Sys	Total	Stat	Sys	Total
Belle 0.7 ab <sup>-1</sup>	14	6	16	6	3	7
Belle II 5 ab <sup>-1</sup>	5	3	6	2	2	3
Belle II 50 ab <sup>-1</sup>	2	3	3	1	2	2

Projections based on Belle SL tag measurement (before 2019)



Differential distributions can be measured to constrain NP

Main systematics: D<sup>\*\*</sup> modelling, soft pions, yield of fake D<sup>\*</sup> candidates. **Studies of B → D<sup>\*\*</sup>lv and B → D<sup>\*\*</sup>τv planned**

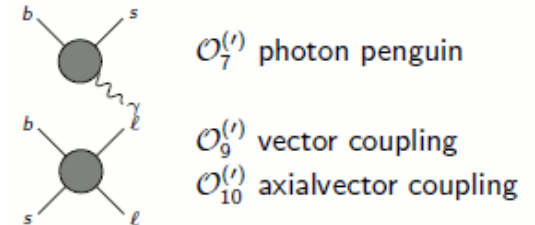
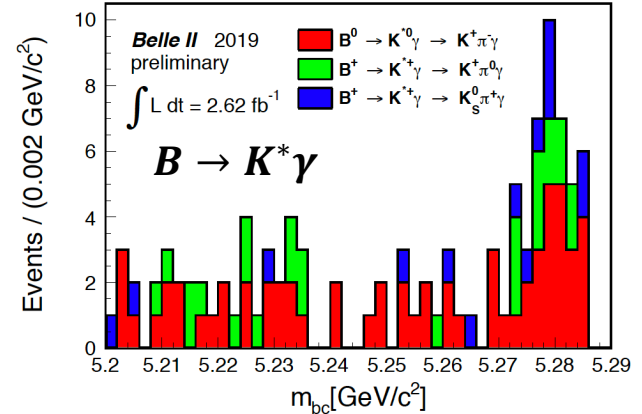
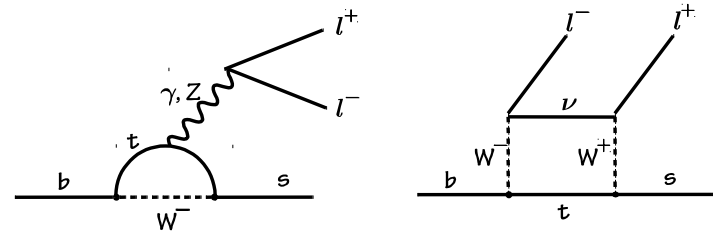
- **Very rare in the SM:**  $\mathfrak{B}(B \rightarrow K^{(*)} \ell \ell) \sim 10^{-(6-8)}$
- **Sensitive to NP** (supersymmetry, 2HDM models, fourth generation, extra dimensions...)
- Experimentally we measure the ratios:

$$R_K^{(*)} = \frac{\mathfrak{B}(B \rightarrow K^{(*)} \mu^+ \mu^-)}{\mathfrak{B}(B \rightarrow K^{(*)} e^+ e^-)}$$

- Effective, model independent, hamiltonian:

$$\mathcal{H}_{\text{eff}} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \sum_i C_i O_i$$

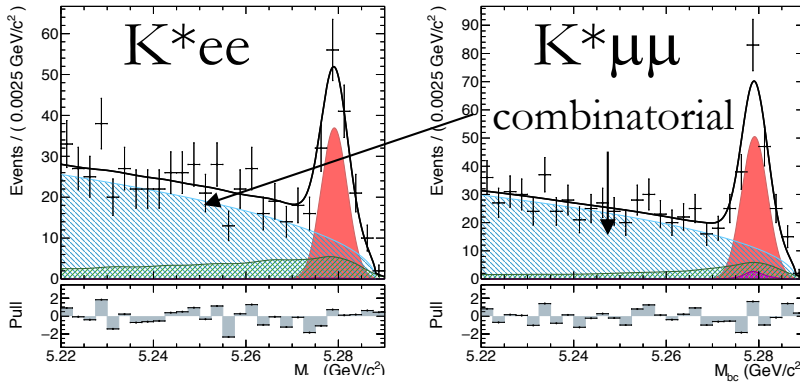
$C_i$ : Wilson coefficients, encode short distance physics  
 $O_i$ : Operators describing long-distance physics



- Measurement of parameters related to angular distributions of the decay products ( $P'_5, Q_5 = P'_5 e - P'_5 \mu$ ) (see Ben Grinstein's plenary talk for details)

•  $B \rightarrow K^{*} \ell \ell$

*arXiv:1904.02440 (Belle 2019)*

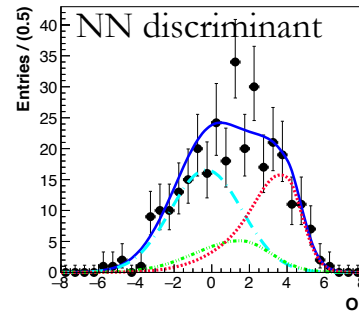
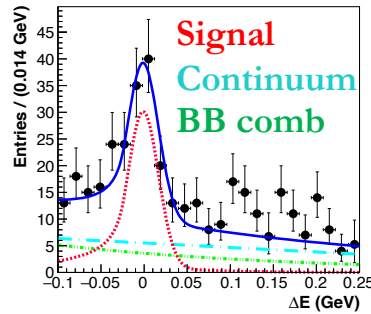
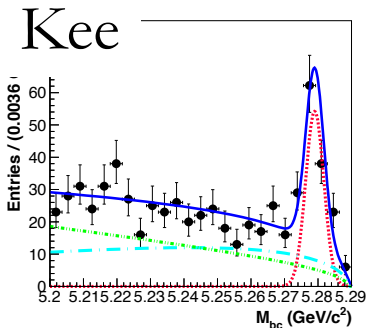


- Signal extraction with fit to  $M_{bc}$  distributions
- Dominant background: combinatorial
- Peaking background: charmonium  $J/\psi K^{*}$
- Main systematics: lepton efficiency and peaking background

$$M_{bc} \equiv \sqrt{\frac{s}{4} - p_B^{*2}}$$

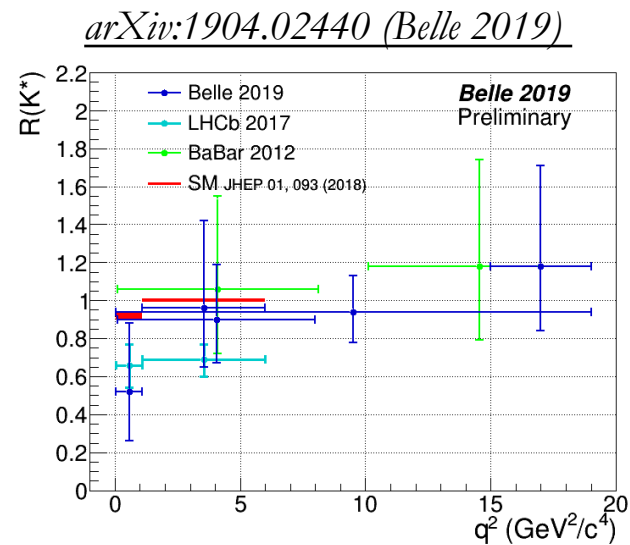
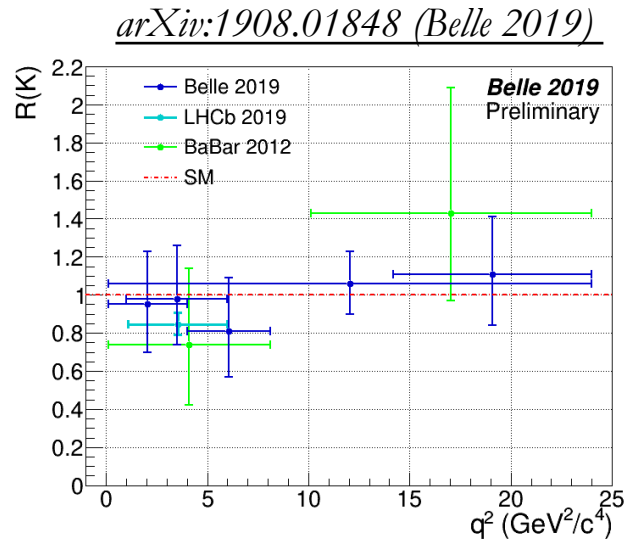
•  $B \rightarrow K \ell \ell$

*arXiv:1908.01848 (Belle 2019)*



- Signal extraction with 3D fit to  $M_{bc}$ ,  $\Delta E$ , NN discriminant
- NN discriminant built using kinematic and angular variables
- Main systematics: lepton identification, B counting, NN discriminant

$$\Delta E \equiv E_B^* - \sqrt{s}/2$$

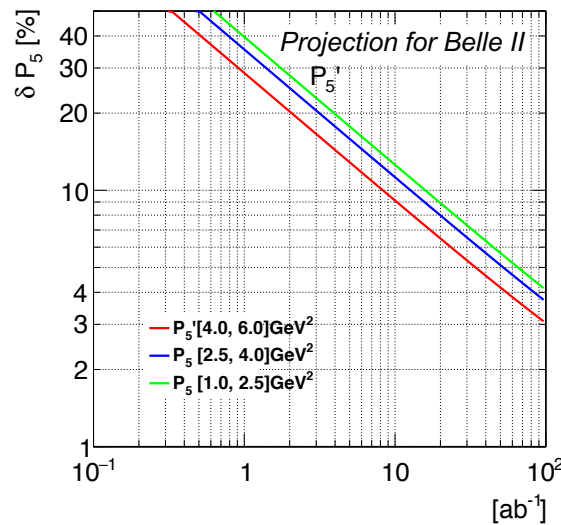
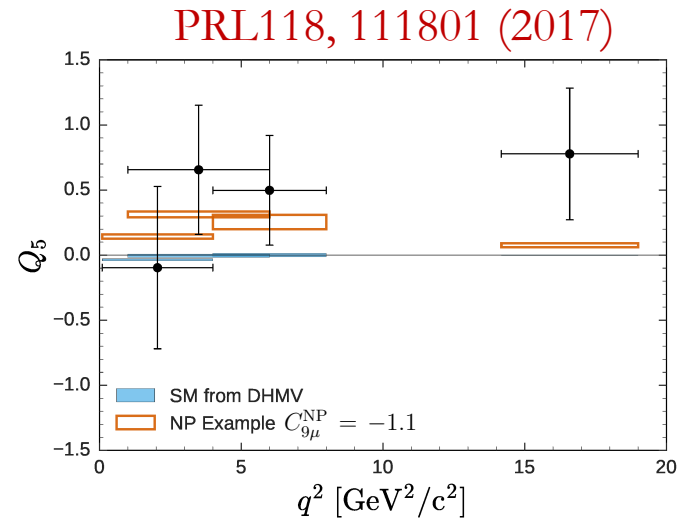
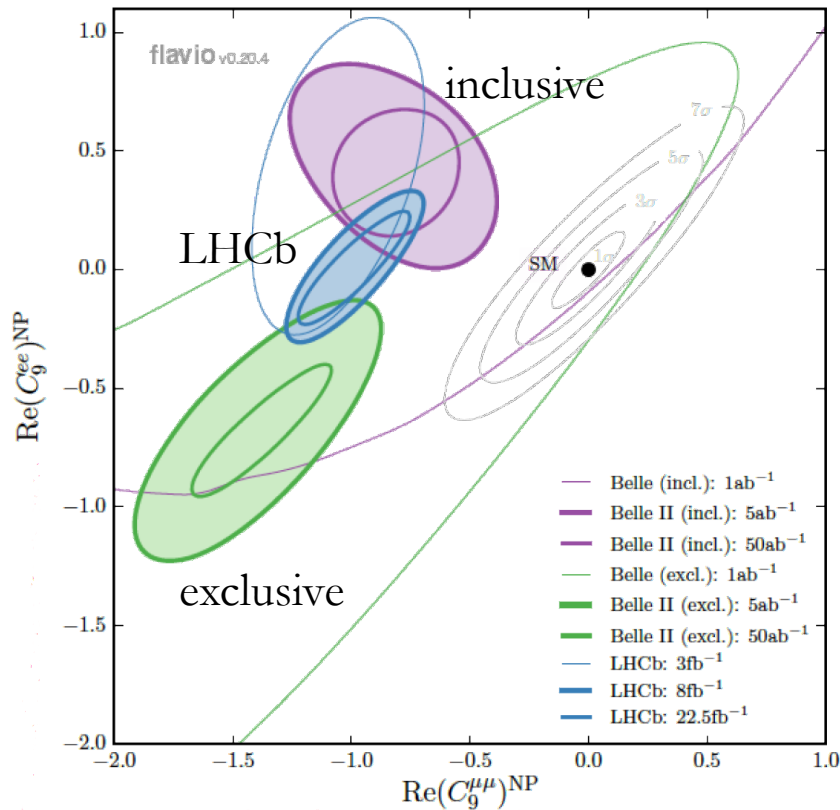


Observables	Belle $0.71 \text{ ab}^{-1}$	Belle II $5 \text{ ab}^{-1}$	Belle II $50 \text{ ab}^{-1}$
$R_K$ ( $[1.0, 6.0] \text{ GeV}^2$ )	28%	11%	3.6%
$R_K$ ( $> 14.4 \text{ GeV}^2$ )	30%	12%	3.6%
$R_{K^*}$ ( $[1.0, 6.0] \text{ GeV}^2$ )	26%	10%	3.2%
$R_{K^*}$ ( $> 14.4 \text{ GeV}^2$ )	24%	9.2%	2.8%
$R_{X_s}$ ( $[1.0, 6.0] \text{ GeV}^2$ )	32%	12%	4.0%
$R_{X_s}$ ( $> 14.4 \text{ GeV}^2$ )	28%	11%	3.4%

**Belle II  
projections**

- Differential distributions in  $q^2$  (dilepton invariant mass squared)
- Latest Belle result closer to the SM expectation ( $\sim 1$ )
- Measurements still dominated by statistical uncertainty
- Inclusive studies of  $B \rightarrow X_s \ell \ell$  possible: reduce hadronic uncertainties

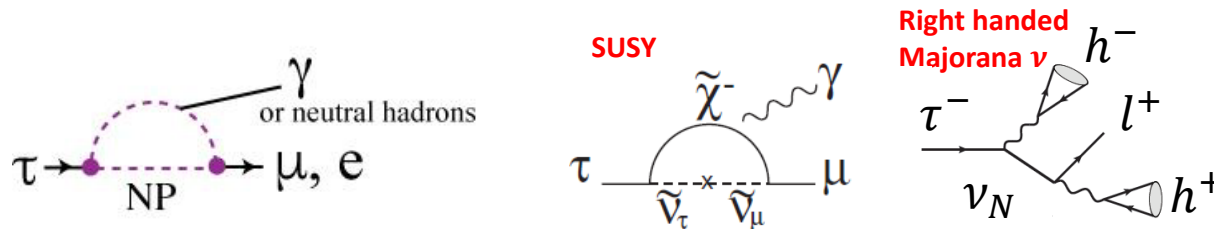
- Angular variables sensitive to NP
- LHCb measurement dominated by systematics
- Exploit Full Event Interpretation to perform fully inclusive searches



**5 $\sigma$  confirmation of NP possible with 20  $ab^{-1}$  at Belle II**



- LFV in tau decays is a **clear test of the SM**: expected **BR**  $\sim 10^{-45}$  (**NP predicts BR up to  $10^{-8}$** )

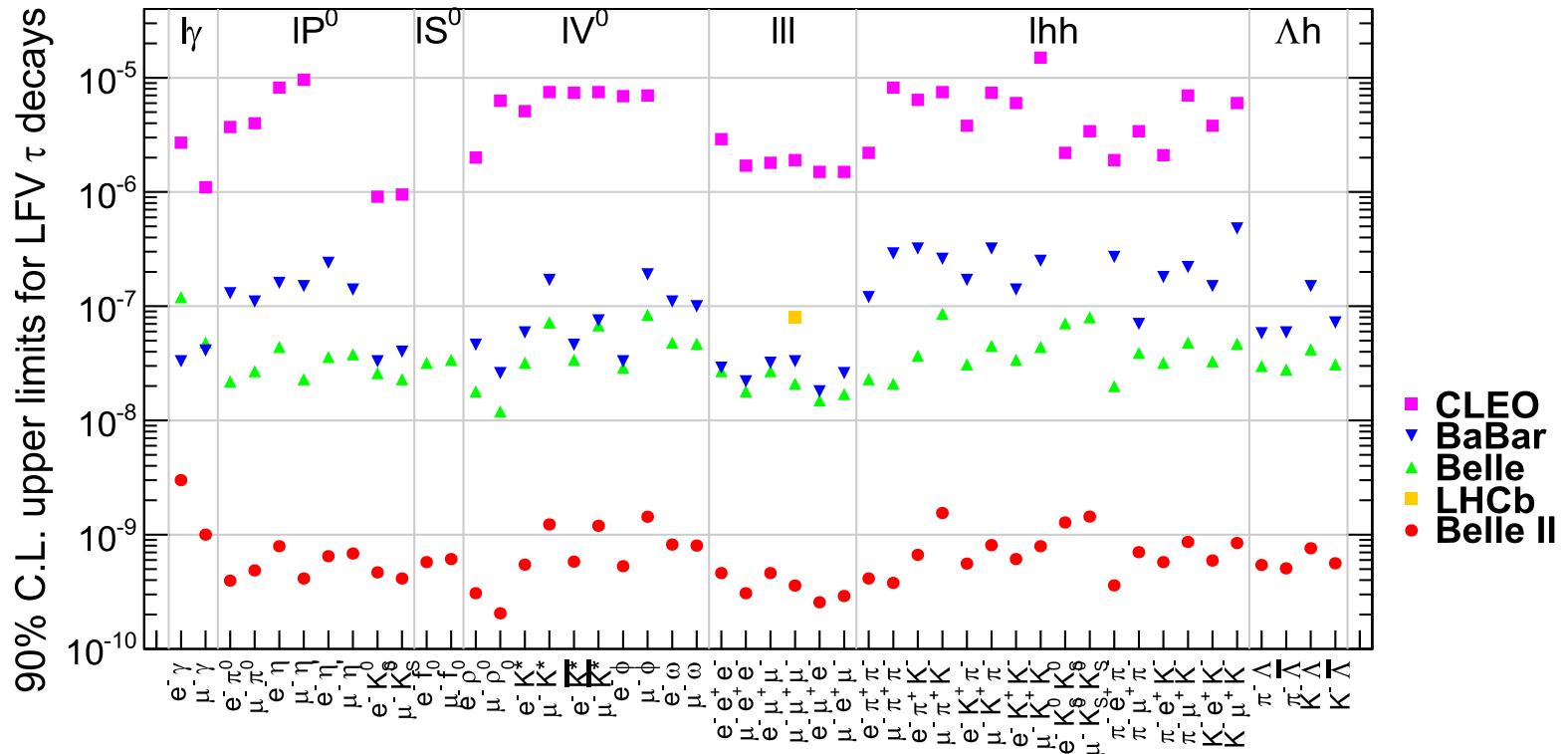


- Searches in different channels may provide discrimination among **NP models**

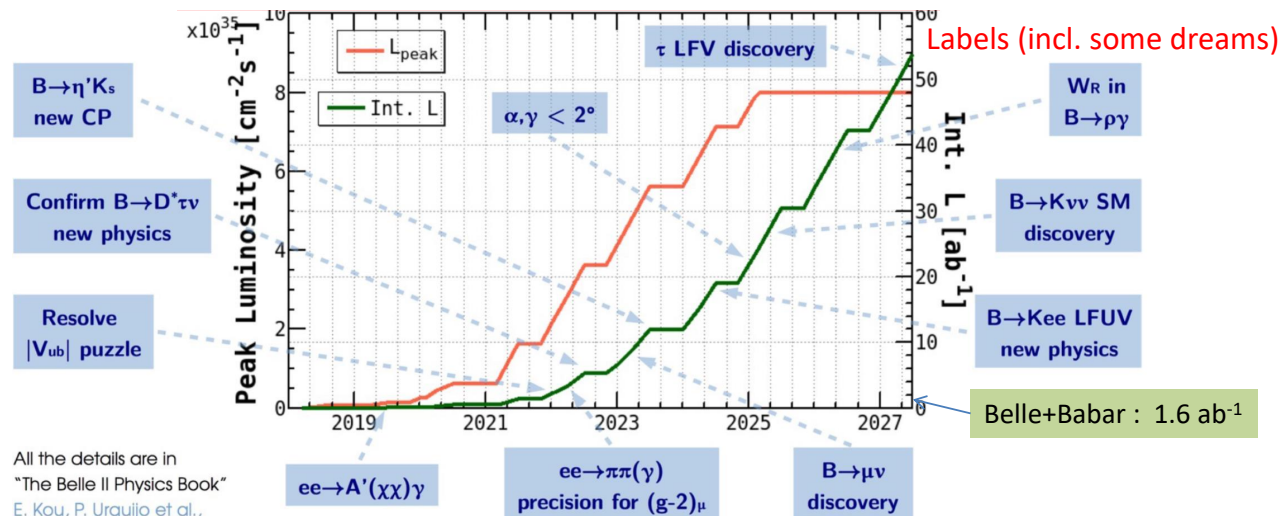
(M.Blanke, et al., JHEP 0705, 013(2007), C.Yue, et al.,PLB547, 252 (2002))

	SUSY+GUT (SUSY+Seesaw)	Higgs mediated	Little Higgs	non-universal Z' boson
$\left(\frac{\tau \rightarrow \mu\mu\mu}{\tau \rightarrow \mu\gamma}\right)$	$\sim 2 \times 10^{-3}$	0.06~0.1	0.4~2.3	$\sim 16$
$\left(\frac{\tau \rightarrow \mu ee}{\tau \rightarrow \mu\gamma}\right)$	$\sim 1 \times 10^{-2}$	$\sim 1 \times 10^{-2}$	0.3~1.6	$\sim 16$
Br ( $\tau \rightarrow \mu\gamma$ )	$< 10^{-7}$	$< 10^{-10}$	$< 10^{-10}$	$< 10^{-9}$

At Belle II an improvement of **2 orders of magnitude** is expected with full dataset

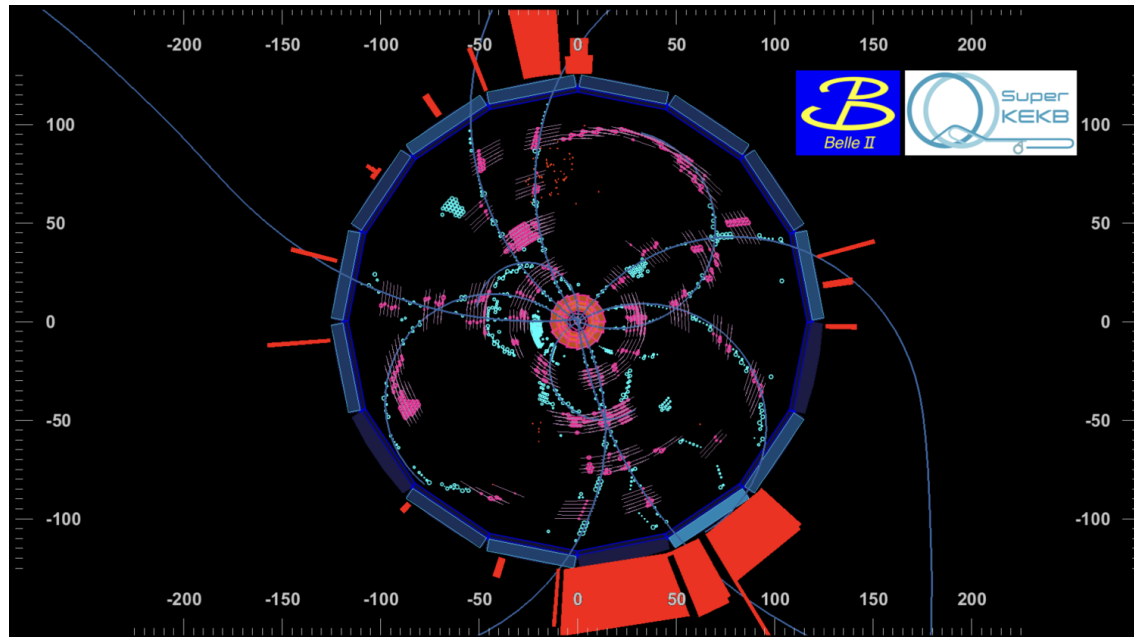


- Within the next **three-five years of data taking Belle II** will collect **5-20  $ab^{-1}$**  and will be able to address the Lepton Flavour Universality Violation by precisely measuring  **$R(D^{(*)}), R(K^{(*)}), P_5'$**
- With **full dataset** Belle II will also be able to potentially discover LFV in the tau lepton sector
- In addition Belle II will also have the sensitivity to shed light on anomalies in the  $B \rightarrow X_u \ell \nu$  decays and investigate other rare processes suppressed in the SM ( $B \rightarrow \ell \nu, B \rightarrow K^{(*)} \nu \bar{\nu}, B \rightarrow \nu \bar{\nu}$ , etc.)



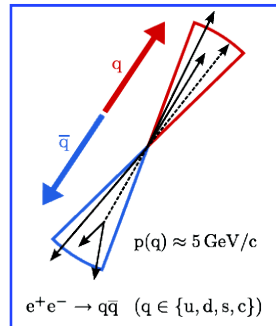
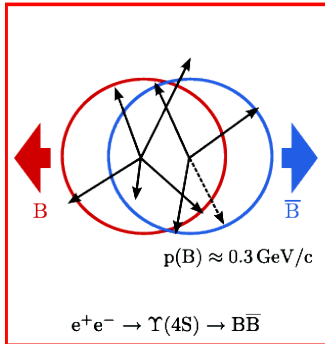
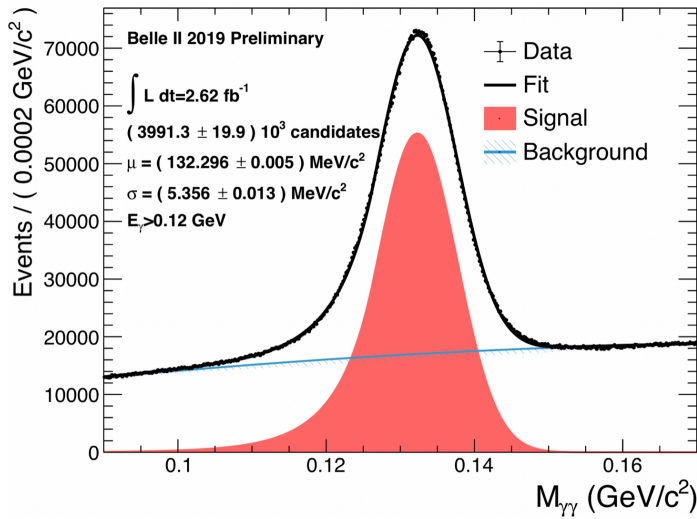
All the details are in  
 "The Belle II Physics Book"  
 E. Kou, P. Urquijo et al.,

# Thanks !



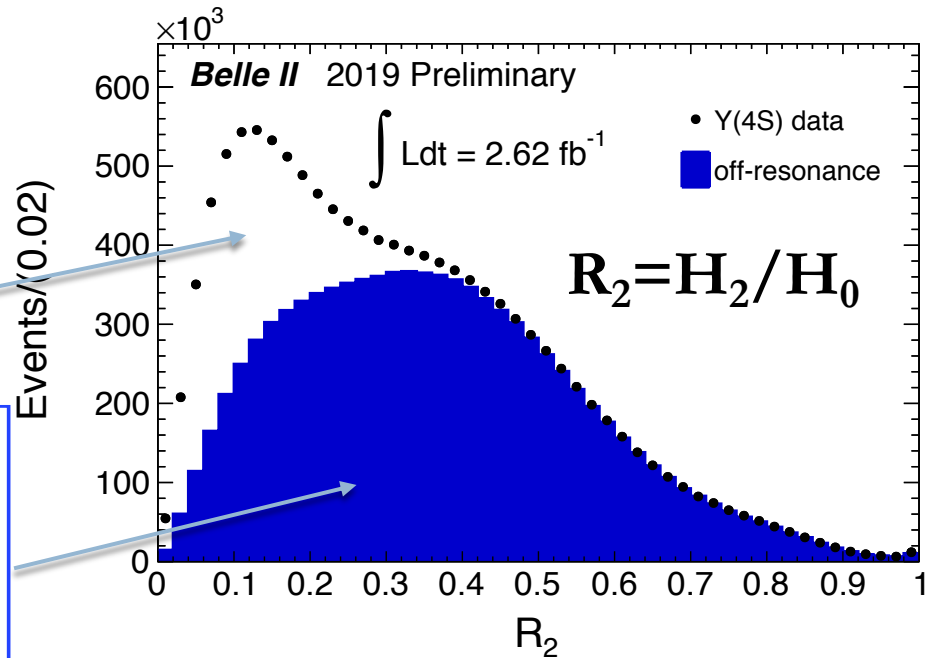
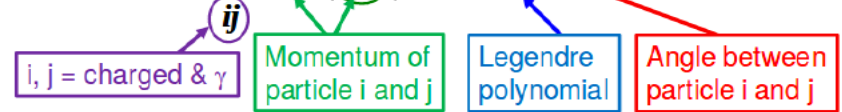
- Belle II first data (22-23)
- FEI Calibration (24)
- $B \rightarrow X_{u,c} l \nu$  decays (25-28)
- Leptonic B decays (29-32)
- $B \rightarrow K^* \nu \nu$  (33-35)
- $B \rightarrow s l l$  (36-39)

## $\pi^0$ invariant mass



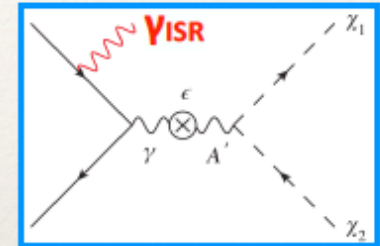
$R_2$  is the ratio between  $H_2$  and  $H_0$

$$H_l = \sum_{ij} |p_i| |p_j| P_l(\cos\theta_{ij})$$

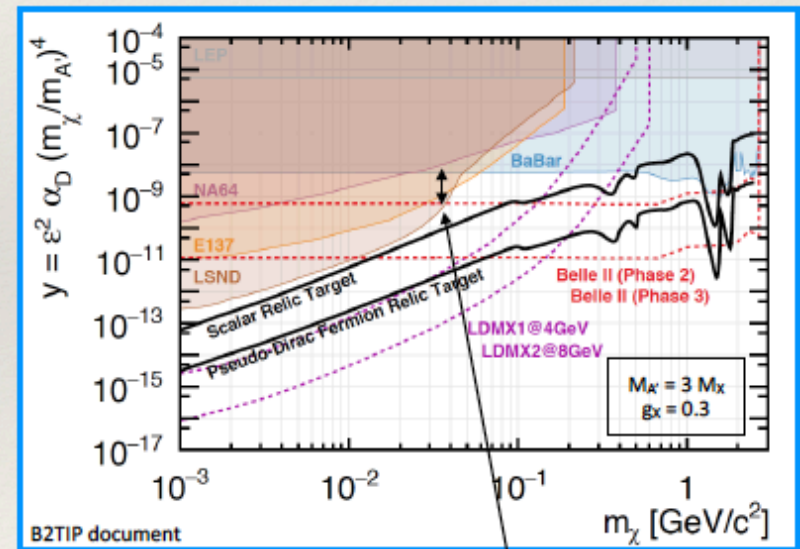
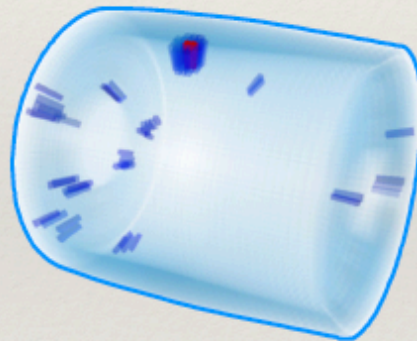
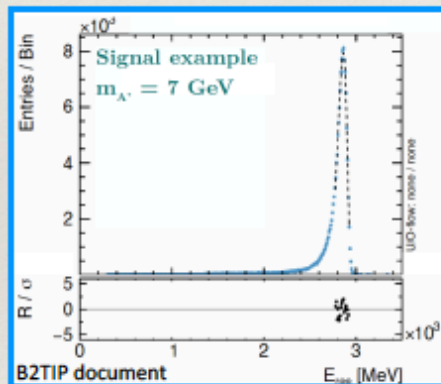


# Early physics: the dark sector

- Light dark matter and light mediator searches in Belle II:
  - Dark photons, dark higgs, axion-like particles (ALPs), mass scale  $\sim$ GeV or sub-GeV.
  - Production, e.g.:  $e^+e^- \rightarrow M+X$ ,  $e^+e^- \rightarrow Y(ns) \rightarrow M+X$ ,  $e^+e^- \rightarrow B+X \rightarrow K+M+X$ .



- Example: on-shell dark photon decaying to invisible DM:
  - Signal: single, mono-energetic, high-E photon & peak in recoil mass.
  - Single Photon trigger with 1 GeV threshold.



- Particularly relevant with Phase 2 data:
  - Low luminosity and lower beam background allow to **open up triggers**.
  - Small dataset can still give world best sensitivity.

Belle II calo more hermetic than BaBar

## FEI validated on Belle real data

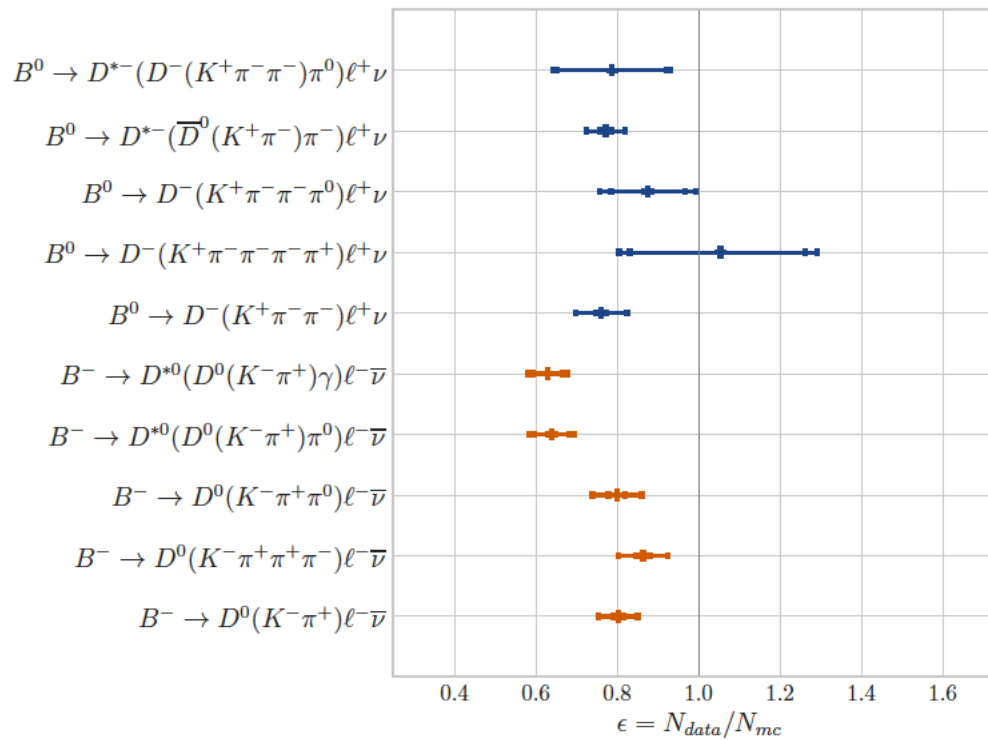
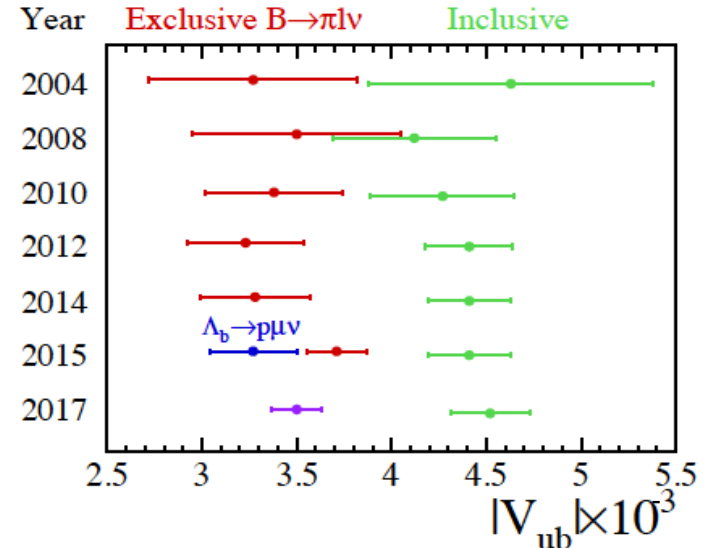
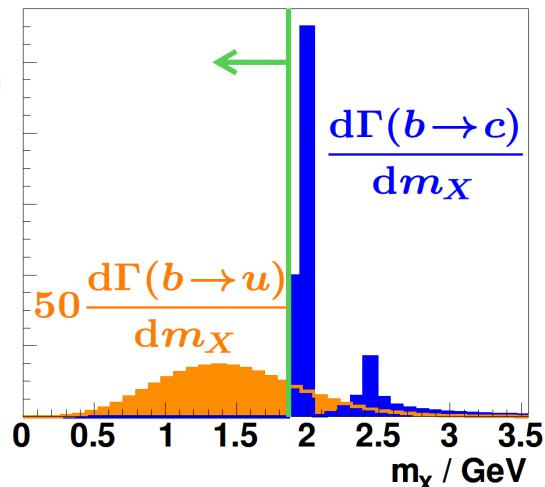


Figure 4.18.: The overall efficiency correction calculated by measuring the known branching fractions of 10 control channels on converted Belle data [76].



## Measurement of $|V_{ub}|$ from inclusive and exclusive B decays

- **Inclusive decays measurement**
  - Hadronic tag
  - Exploit kinematic endpoints to reduce  $B \rightarrow X_c l \nu$  bkg



Tension between inclusive and exclusive  $|V_{ub}|$  measurements

$$|V_{ub}|^2 = \frac{\Delta \mathcal{B}_{ul\nu}}{(\tau_B \Delta \mathcal{R})}$$

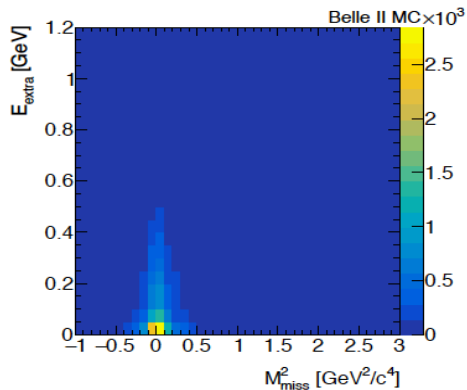
Measured BR in fiducial phase space region

B meson lifetime

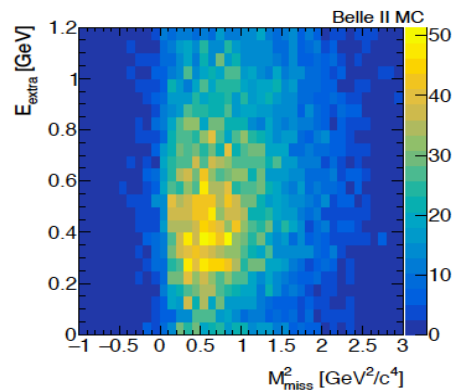
Predicted partial decay rate

*Belle II Full Simulation study*

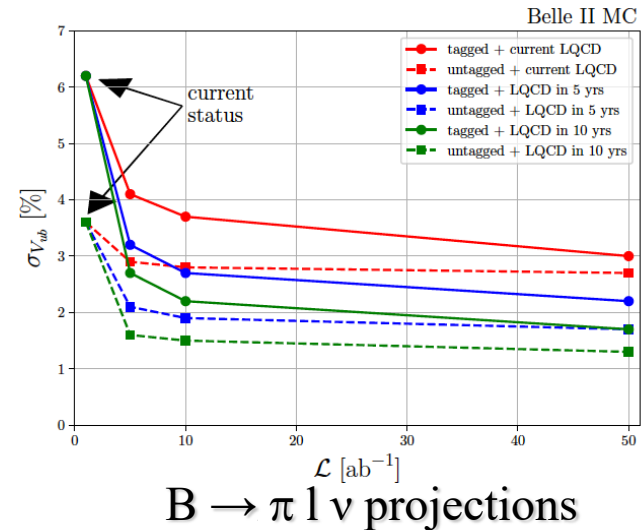
- $B^0 \rightarrow \pi l \nu$  decay
  - Untagged or tagged (with FEI)
  - Exploit missing mass and extra energy in the calorimeter
  - $\mathcal{B} \sim f_i |V_{ub}|^2$ ; form factors  $f_i$  computed with LQCD (PRD 91, 074510 (2015))



signal



background



$B \rightarrow \pi l \nu$  projections

Belle II @ 50  $ab^{-1}$ :  $\sim 3\%$  (inclusive) /  $\sim 2\%$  (exclusive  $\pi l \nu$ ) uncertainty

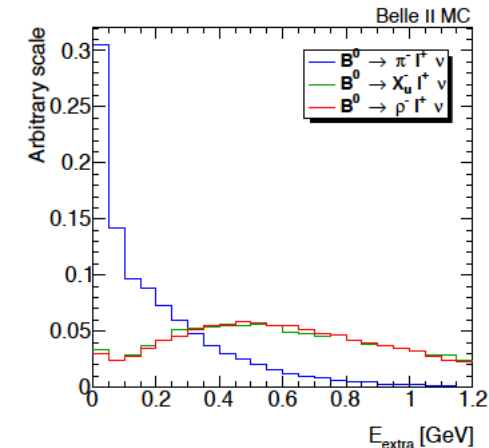
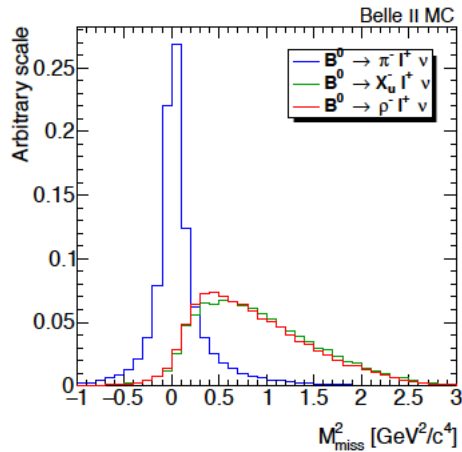


Table 54: Summary of systematic uncertainties on the branching fractions of  $B^0 \rightarrow \pi^- \ell^+ \nu_\ell$  decays in hadronic tagged and untagged Belle analyses with  $711 \text{ fb}^{-1}$  [271] and  $605 \text{ fb}^{-1}$  [269] data samples, respectively. The estimated precision limit for some sources of systematic uncertainties is given in brackets.

Source	Error (Limit) [%]	
	Tagged [%]	Untagged
Tracking efficiency	0.4	2.0
Pion identification	–	1.3
Lepton identification	1.0	2.4
Kaon veto	0.9	–
Continuum description	1.0	1.8
Tag calibration and $N_{B\bar{B}}$	4.5 (2.0)	2.0 (1.0)
$X_u \ell \nu$ cross-feed	0.9	0.5 (0.5)
$X_c \ell \nu$ background	–	0.2 (0.2)
Form factor shapes	1.1	1.0 (1.0)
Form factor background	–	0.4 (0.4)
Total	5.0	4.5
(reducible, irreducible)	(4.6, 2.0)	(4.2, 1.6)

LQCD: current is the world average by FLAG group

- 5 yr w/o EM<sup>19</sup>: We assume a factor of 2 reduction of the lattice QCD uncertainty in the next few years and that the uncertainty of the EM correction is negligible (e.g. for processes insensitive to the EM correction).

- 5 yr w/ EM<sup>19</sup>: The lattice QCD uncertainty is reduced by a factor of 2, but we add in quadrature 1% uncertainty from the EM correction<sup>19</sup>.

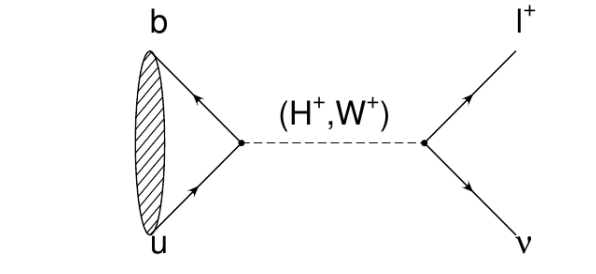
- 10 yr w/o EM<sup>19</sup>: We assume a factor of 5 reduction of the lattice QCD uncertainty in the next ten years. It is also assumed that the EM correction will be under control and its uncertainty is negligible.

- 10 yr w/ EM<sup>19</sup>: We assume lattice QCD uncertainties reduced by a factor of 5, but add in quadrature 1% uncertainty from the EM correction.

Source	$\Delta R(D)$ (%)	$\Delta R(D^*)$ (%)
$D^{**}$ composition	0.76	1.41
Fake $D^{(*)}$ calibration	0.19	0.11
$B_{\text{tag}}$ calibration	0.07	0.05
Feed-down factors	1.69	0.44
Efficiency factors	1.93	4.12
Lepton efficiency and fake rate	0.36	0.33
Slow pion efficiency	0.08	0.08
MC statistics	4.39	2.25
$B$ decay form factors	0.55	0.28
Luminosity	0.10	0.04
$\mathcal{B}(B \rightarrow D^{(*)} \ell \nu)$	0.05	0.02
$\mathcal{B}(D)$	0.35	0.13
$\mathcal{B}(D^*)$	0.04	0.02
$\mathcal{B}(\tau^- \rightarrow \ell^- \bar{\nu}_\ell \nu_\tau)$	0.15	0.14
Total	5.21	4.94

- Helicity suppressed decays

$$BR_{SM}(B \rightarrow \ell \nu) = \frac{G_F^2 m_B \tau_B}{8\pi} f_B^2 |V_{ub}|^2 m_\ell^2 \left[ 1 - \frac{m_\ell^2}{m_B^2} \right]^2$$



- Sensitive to NP contributions, e.g. type III Higgs doublet model [[PhysRevD.86.054014](#)]

SM Prediction	
$\mathcal{B}(B^+ \rightarrow e^+ \nu_e)$	$(1.09 \pm 0.21) \cdot 10^{-11}$
$\mathcal{B}(B^+ \rightarrow \mu^+ \nu_\mu)$	$(4.65 \pm 0.91) \cdot 10^{-7}$
$\mathcal{B}(B^+ \rightarrow \tau^+ \nu_\tau)$	$(1.03 \pm 0.2) \cdot 10^{-4}$

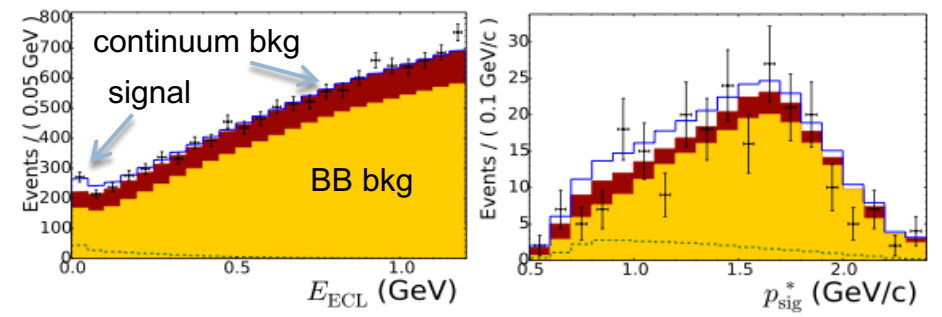
- Clean theoretically, hard experimentally: only  $B \rightarrow \tau \nu$  has been measured

Belle combination

$$\mathcal{B} = [0.91 \pm 0.19(\text{stat.}) \pm 0.11(\text{syst.})] \times 10^{-4}$$

(evidence at  $\sim 4.6 \sigma$  level)

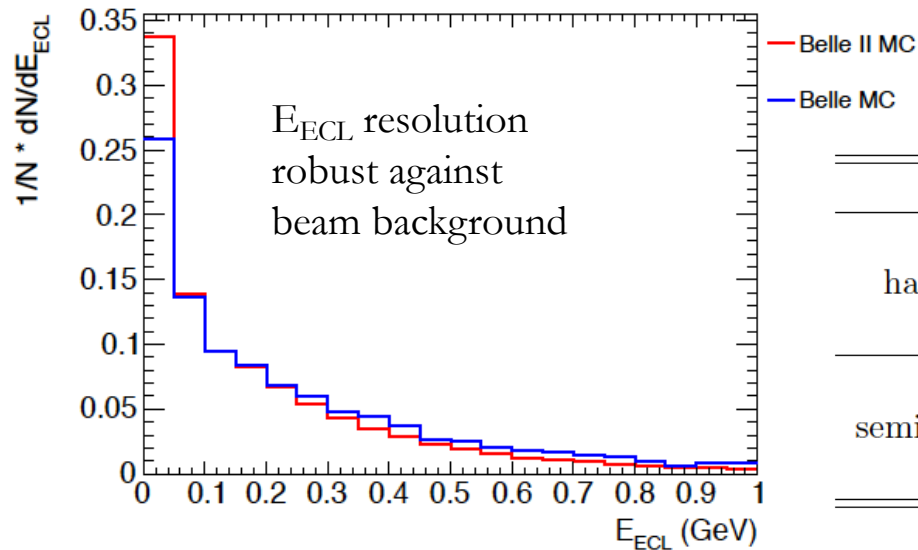
Belle PRD 92, 051102 (2015), SL tag



## Belle II full simulation study

- Hadronic tag with FEI
- 1-prong  $\tau$  decays ( $\mu\nu\nu$ ,  $e\nu\nu$ ,  $\pi\nu$ ,  $\rho\nu$ )
- Dedicated study on machine background impact
- ML fit to extra energy  $E_{\text{ECL}}$

Extra energy in the calorimeter



Main **systematic uncertainties**:

background  $E_{\text{Extra}}$  PDF, branching fractions of the peaking backgrounds, tagging efficiency, and  $K^0_L$  veto efficiency

	Integrated Luminosity ( $\text{ab}^{-1}$ )	1	5	50
hadronic tag	statistical uncertainty (%)	29.2	13.0	4.1
	systematic uncertainty (%)	12.6	6.8	4.6
	total uncertainty (%)	31.6	14.7	6.2
semileptonic tag	statistical uncertainty (%)	19.0	8.5	2.7
	systematic uncertainty (%)	17.9	8.7	4.5
	total uncertainty (%)	26.1	12.2	5.3

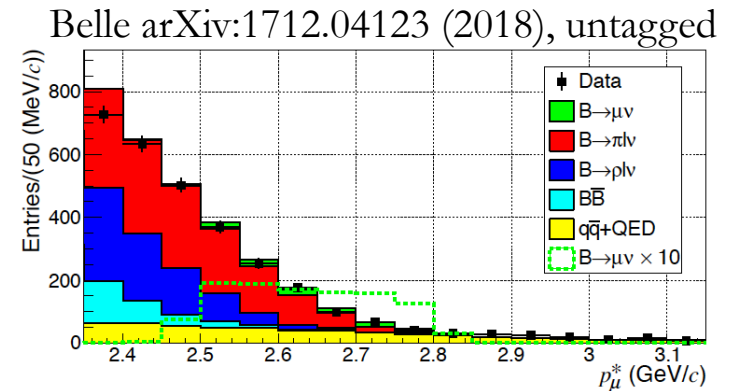
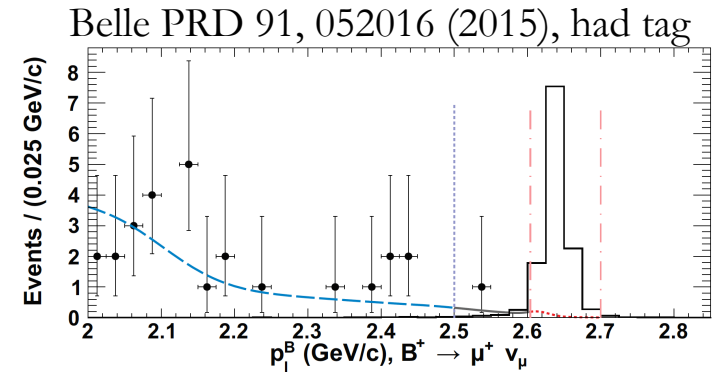
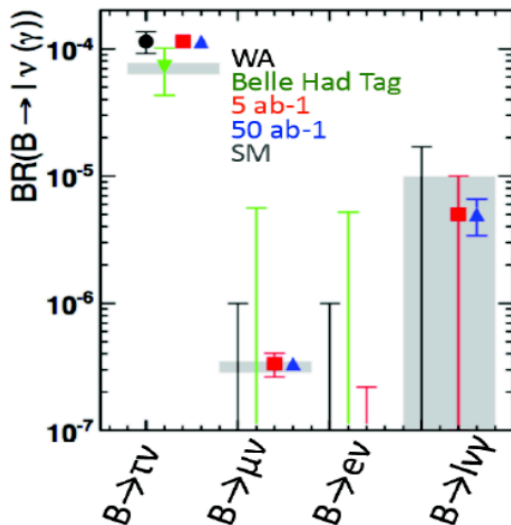
Observation at  $\sim 3 \text{ ab}^{-1}$

## $B \rightarrow \mu\nu$ and radiative $B \rightarrow l\nu\gamma$

31

### $B \rightarrow \mu\nu$

- Two body decay:  $p_\mu^* = m_B/2$  in B rest frame
- Tagging  $\rightarrow$  better  $p_\mu^*$  resolution but small statistics
- $\sim 2.4\sigma$  measurement



### $B \rightarrow l\nu\gamma$

- Radiative decay lifts the helicity suppression
- Allows a measurement of  $\lambda_B \rightarrow$  crucial input to QCD factorization predictions of charmless hadronic B decays

$$\Gamma = \frac{d\Gamma}{dE_\gamma} = \frac{\alpha_{em} G_F^2 m_B^4 |V_{ub}|^2}{48\pi^2} x_\gamma^3 (1 - x_\gamma) [F_A^2 + F_V^2].$$

$$F_V(E_\gamma) = \frac{Q_u m_B f_B}{2E_\gamma \lambda_B} R(E_\gamma, \mu) + \left[ \xi(E_\gamma) + \frac{Q_b m_B f_B}{2E_\gamma m_b} + \frac{Q_u m_B f_B}{(2E_\gamma)^2} \right],$$

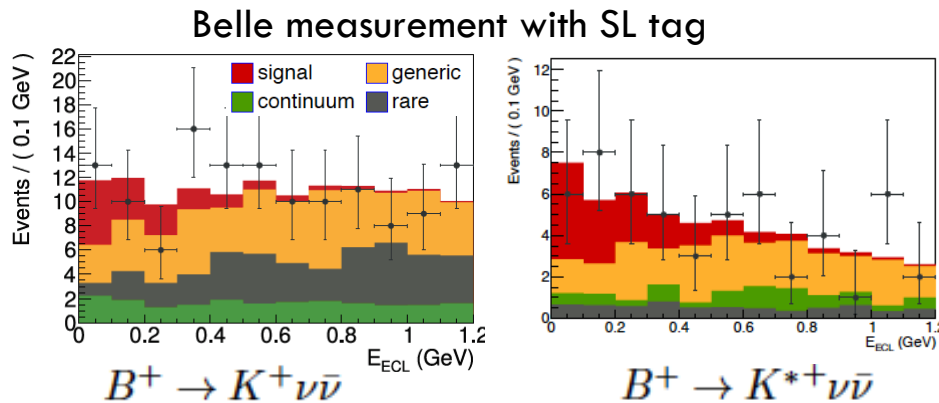
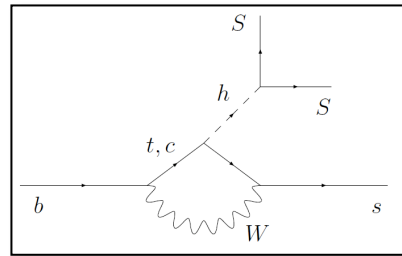
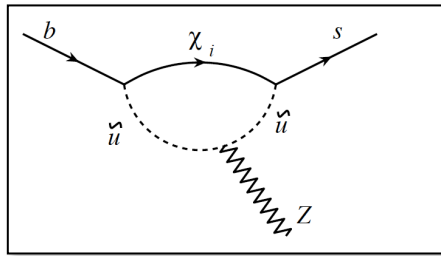
$$F_A(E_\gamma) = \frac{Q_u m_B f_B}{2E_\gamma \lambda_B} R(E_\gamma, \mu) + \left[ \xi(E_\gamma) - \frac{Q_b m_B f_B}{2E_\gamma m_b} - \frac{Q_u m_B f_B}{(2E_\gamma)^2} + \frac{Q_\ell f_B}{E_\gamma} \right],$$

Beneke and Rohrwild, 2011, <https://doi.org/10.1140/epjc/s10052-011-1818-8>

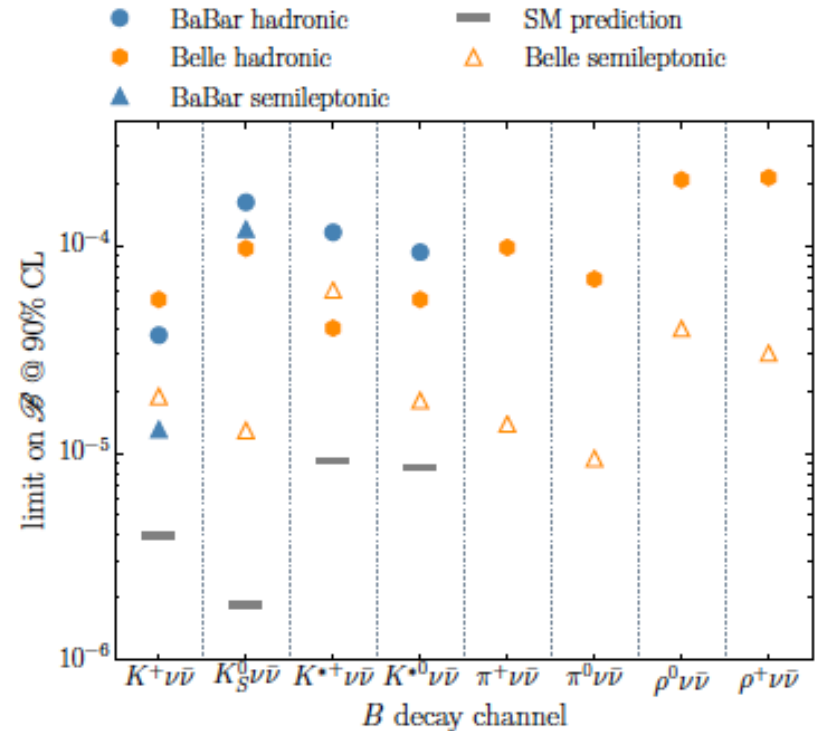


$$B \rightarrow K^{(*)} \nu \bar{\nu}$$

- Prohibited in the SM at tree level: **penguin + box diagrams**
- $BR \sim 10^{-5} \div 10^{-6}$ ; **NP contribution** can increase the BR by factor 50
  - non standard Z-couplings (SUSY)
  - New missing energy sources (DM, extra dim.)



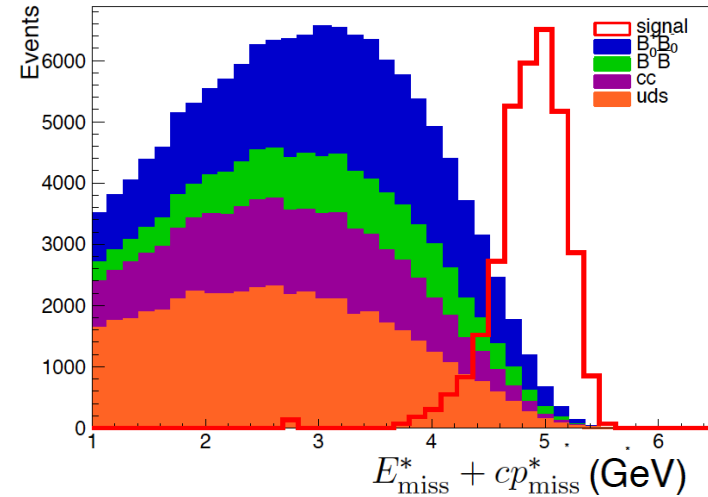
**Belle PRD(R) 96, 091101 (2017)**



$$B \rightarrow K^{(*)} \nu \bar{\nu}$$

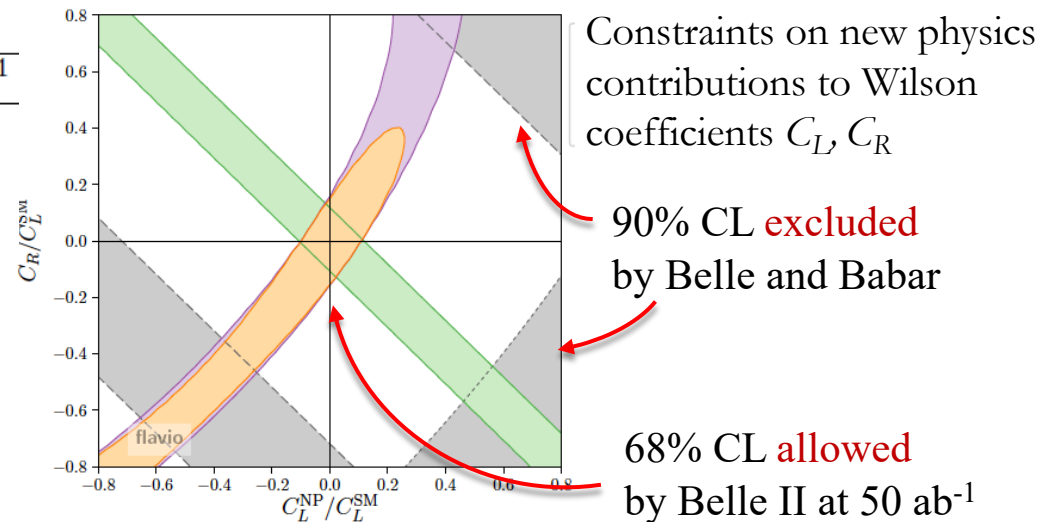
## Belle II full simulation study

- Hadronic tag with FEI
- $K^* \rightarrow K\pi^0$
- Powerful discriminating variable  $E_{miss}^* + cp_{miss}^*$
- Projections performed with a cut and count analysis in extra energy signal window



Observables	Belle II 5 $ab^{-1}$	Belle II 50 $ab^{-1}$
$Br(B^+ \rightarrow K^+ \nu \bar{\nu})$	30%	11%
$Br(B^0 \rightarrow K^{*0} \nu \bar{\nu})$	26%	9.6%
$Br(B^+ \rightarrow K^{*+} \nu \bar{\nu})$	25%	9.3%

Observation at  $\sim 18 ab^{-1}$



$$B \rightarrow K^{(*)} \nu \bar{\nu}$$

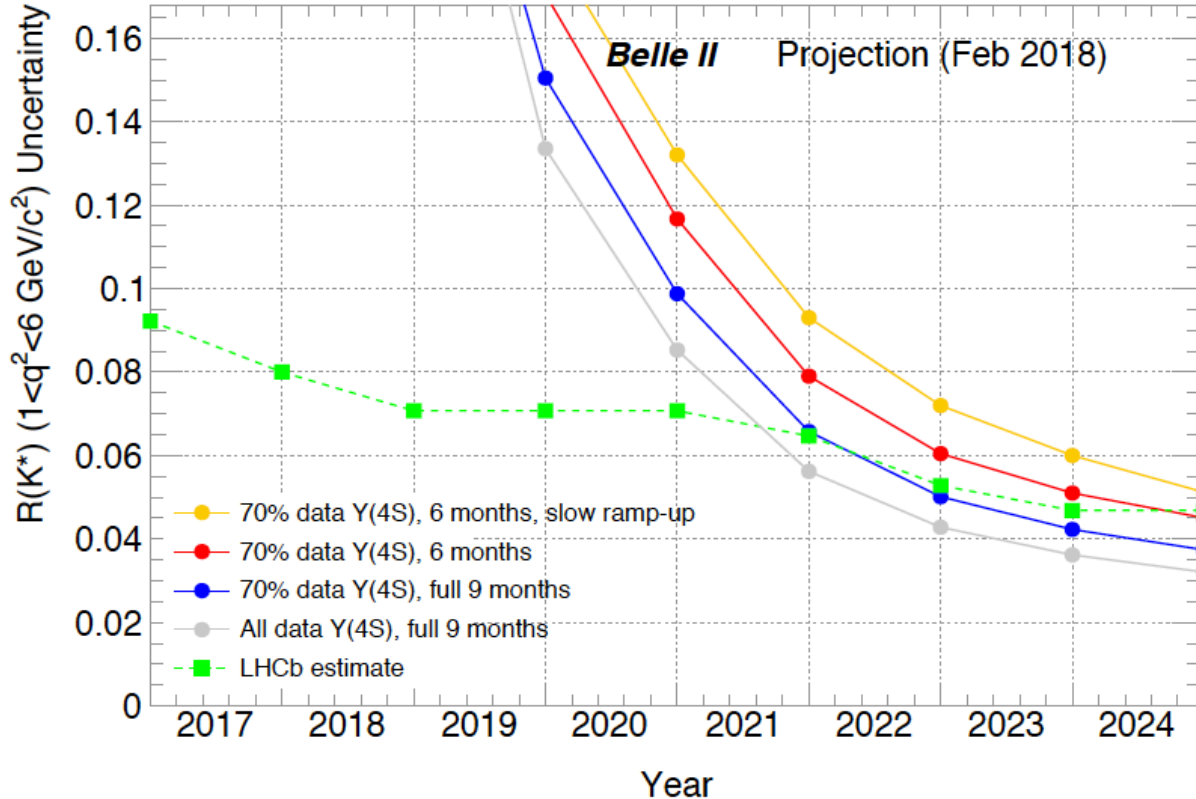
In BSM right handed operator for neutrinos  $Q_R^\ell = (\bar{s}_R \gamma_\mu b_R)(\bar{\nu}_{\ell L} \gamma^\mu \nu_{\ell L})$

$$\frac{\text{Br}(B \rightarrow K \nu \bar{\nu})}{\text{Br}(B \rightarrow K \nu \bar{\nu})_{\text{SM}}} = \frac{1}{3} \sum_{\ell} (1 - 2\eta_{\ell}) \epsilon_{\ell}^2,$$

$$\frac{\text{Br}(B \rightarrow K^* \nu \bar{\nu})}{\text{Br}(B \rightarrow K^* \nu \bar{\nu})_{\text{SM}}} = \frac{1}{3} \sum_{\ell} (1 + \kappa_{\eta} \eta_{\ell}) \epsilon_{\ell}^2,$$

$$\epsilon_{\ell} = \frac{\sqrt{|C_L^{\ell}|^2 + |C_R^{\ell}|^2}}{|C_L^{\text{SM}}|},$$

$$\eta_{\ell} = \frac{-\text{Re}(C_L^{\ell} C_R^{\ell*})}{|C_L^{\ell}|^2 + |C_R^{\ell}|^2}.$$



LHCb values based on naive run-1 extrapolation (not official)  
 Belle II scenarios due to operating conditions at KEK

\*\* Consider it as a sketch to show Belle II can provide confirmation of any persistent anomaly.

Observables	Belle $0.71 \text{ ab}^{-1}$	Belle II $5 \text{ ab}^{-1}$	Belle II $50 \text{ ab}^{-1}$
$\text{Br}(B \rightarrow X_s \ell^+ \ell^-) ([1.0, 3.5] \text{ GeV}^2)$	29%	13%	6.6%
$\text{Br}(B \rightarrow X_s \ell^+ \ell^-) ([3.5, 6.0] \text{ GeV}^2)$	24%	11%	6.4%
$\text{Br}(B \rightarrow X_s \ell^+ \ell^-) (> 14.4 \text{ GeV}^2)$	23%	10%	4.7%

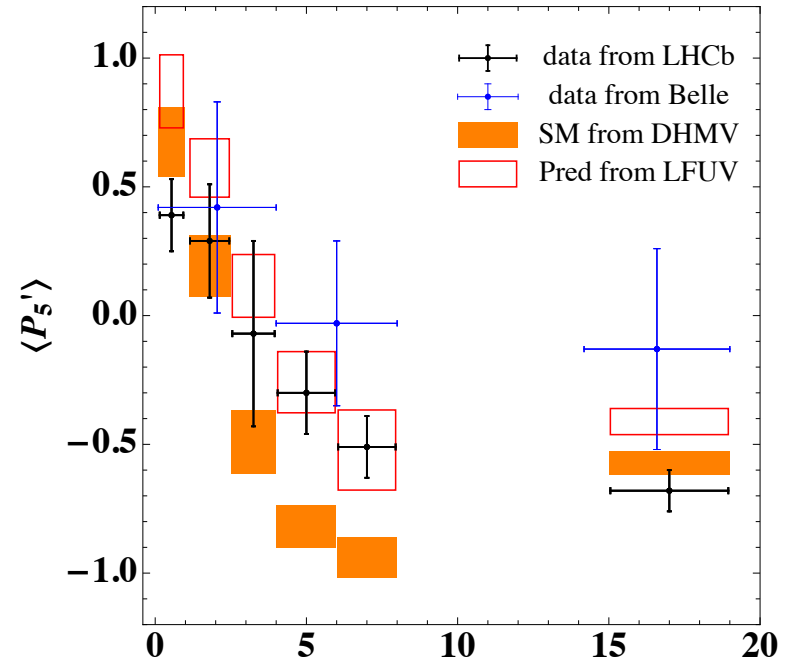
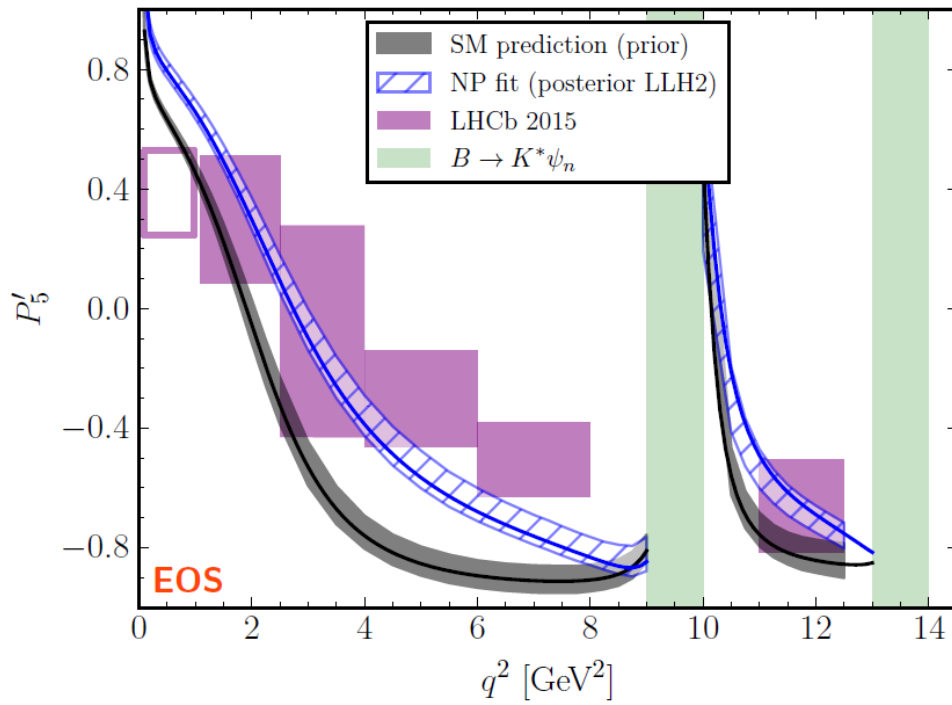
## Differential rate

$$\frac{1}{d\Gamma/dq^2} \frac{d^4\Gamma}{d \cos \theta_\ell d \cos \theta_K d\phi dq^2} = \frac{9}{32\pi} \left[ \frac{3}{4}(1 - F_L) \sin^2 \theta_K + F_L \cos^2 \theta_K + \frac{1}{4}(1 - F_L) \sin^2 \theta_K \cos 2\theta_\ell \right. \\ \left. - F_L \cos^2 \theta_K \cos 2\theta_\ell + S_3 \sin^2 \theta_K \sin^2 \theta_\ell \cos 2\phi + S_4 \sin 2\theta_K \sin 2\theta_\ell \cos \phi \right. \\ \left. + S_5 \sin 2\theta_K \sin \theta_\ell \cos \phi + S_6 \sin^2 \theta_K \cos \theta_\ell + S_7 \sin 2\theta_K \sin \theta_\ell \sin \phi \right. \\ \left. + S_8 \sin 2\theta_K \sin 2\theta_\ell \sin \phi + S_9 \sin^2 \theta_K \sin^2 \theta_\ell \sin 2\phi \right],$$

$$P'_{i=4,5,6,8} = \frac{S_{j=4,5,7,8}}{\sqrt{F_L(1 - F_L)}},$$

Observables	Belle II 5 ab <sup>-1</sup>	Belle II 50 ab <sup>-1</sup>
$\text{Br}(B^+ \rightarrow K^+ \tau^+ \tau^-) \cdot 10^5$	< 6.5	< 2.0
$\text{Br}(B^0 \rightarrow \tau^+ \tau^-) \cdot 10^5$	< 30	< 9.6
$\text{Br}(B_s^0 \rightarrow \tau^+ \tau^-) \cdot 10^4$	< 8.1	–
$\text{Br}(B^+ \rightarrow K^+ \tau^\pm e^\mp) \cdot 10^6$	–	< 2.1
$\text{Br}(B^+ \rightarrow K^+ \tau^\pm \mu^\mp) \cdot 10^6$	–	< 3.3
$\text{Br}(B^0 \rightarrow \tau^\pm e^\mp) \cdot 10^5$	–	< 1.6
$\text{Br}(B^0 \rightarrow \tau^\pm \mu^\mp) \cdot 10^5$	–	< 1.3

$B \rightarrow K^{(*)} \tau^+ \tau^-$  hard to measure even with 50 ab<sup>-1</sup> at Belle II (SM BR  $\sim 10^{-7}$ )



Observables	Expected th. accuracy	Expected exp. uncertainty	Facility (2025)
<b>UT angles &amp; sides</b>			
$\phi_1$ [°]	***	0.4	Belle II
$\phi_2$ [°]	**	1.0	Belle II
$\phi_3$ [°]	***	1.0	Belle II/LHCb
$ V_{cb} $ incl.	***	1%	Belle II
$ V_{cb} $ excl.	***	1.5%	Belle II
$ V_{ub} $ incl.	**	3%	Belle II
$ V_{ub} $ excl.	**	2%	Belle II/LHCb
<b>CPV</b>			
$S(B \rightarrow \phi K^0)$	***	0.02	Belle II
$S(B \rightarrow \eta' K^0)$	***	0.01	Belle II
$\mathcal{A}(B \rightarrow K^0 \pi^0) [10^{-2}]$	***	4	Belle II
$\mathcal{A}(B \rightarrow K^+ \pi^-) [10^{-2}]$	***	0.20	LHCb/Belle II
<b>(Semi-)leptonic</b>			
$\mathcal{B}(B \rightarrow \tau \nu) [10^{-6}]$	**	3%	Belle II
$\mathcal{B}(B \rightarrow \mu \nu) [10^{-6}]$	**	7%	Belle II
$R(B \rightarrow D \tau \nu)$	***	3%	Belle II
$R(B \rightarrow D^* \tau \nu)$	***	2%	Belle II/LHCb
<b>Radiative &amp; EW Penguins</b>			
$\mathcal{B}(B \rightarrow X_s \gamma)$	**	4%	Belle II
$A_{CP}(B \rightarrow X_{s,d} \gamma) [10^{-2}]$	***	0.005	Belle II
$S(B \rightarrow K_S^0 \pi^0 \gamma)$	***	0.03	Belle II
$S(B \rightarrow \rho \gamma)$	**	0.07	Belle II
$\mathcal{B}(B_s \rightarrow \gamma \gamma) [10^{-6}]$	**	0.3	Belle II
$\mathcal{B}(B \rightarrow K^* \nu \bar{\nu}) [10^{-6}]$	***	15%	Belle II
$\mathcal{B}(B \rightarrow K \nu \bar{\nu}) [10^{-6}]$	***	20%	Belle II
$R(B \rightarrow K^* \ell \ell)$	**	0.03	Belle II/LHCb

Observables	Belle or LHCb* (2014)	Belle II 50 ab <sup>-1</sup>	LHCb 2018 50 fb <sup>-1</sup>
<b>Charm Rare</b>			
$\mathcal{B}(D_s \rightarrow \mu \nu)$	$5.31 \cdot 10^{-3} (1 \pm 5.3\% \pm 3.8\%)$	2.9%	0.9%
$\mathcal{B}(D_s \rightarrow \tau \nu)$	$5.70 \cdot 10^{-3} (1 \pm 3.7\% \pm 5.4\%)$	3.5%	2.3%
$\mathcal{B}(D^0 \rightarrow \gamma \gamma) [10^{-6}]$	< 1.5	30%	25%
<b>Charm CP</b>			
$A_{CP}(D^0 \rightarrow K^+ K^-) [10^{-4}]$	$-32 \pm 21 \pm 9$	11	6
$\Delta A_{CP}(D^0 \rightarrow K^+ K^-) [10^{-3}]$	3.4*		0.5 0.1
$A_\Gamma [10^{-2}]$	0.22	0.1	0.03 0.02 0.005
$A_{CP}(D^0 \rightarrow \pi^0 \pi^0) [10^{-2}]$	$-0.03 \pm 0.64 \pm 0.10$	0.29	0.09
$A_{CP}(D^0 \rightarrow K_S^0 \pi^0) [10^{-2}]$	$-0.21 \pm 0.16 \pm 0.09$	0.08	0.03
<b>Charm Mixing</b>			
$x(D^0 \rightarrow K_S^0 \pi^+ \pi^-) [10^{-2}]$	$0.56 \pm 0.19 \pm_{0.13}^{0.07}$	0.14	0.11
$y(D^0 \rightarrow K_S^0 \pi^+ \pi^-) [10^{-2}]$	$0.30 \pm 0.15 \pm_{0.08}^{0.05}$	0.08	0.05
$ q/p (D^0 \rightarrow K_S^0 \pi^+ \pi^-)$	$0.90 \pm_{0.15}^{0.16} \pm_{0.06}^{0.08}$	0.10	0.07
$\phi(D^0 \rightarrow K_S^0 \pi^+ \pi^-) [^\circ]$	$-6 \pm 11 \pm_5^4$	6	4
<b>Tau</b>			
$\tau \rightarrow \mu \gamma [10^{-9}]$	< 45	< 14.7	< 4.7
$\tau \rightarrow e \gamma [10^{-9}]$	< 120	< 39	< 12
$\tau \rightarrow \mu \mu \mu [10^{-9}]$	< 21.0	< 3.0	< 0.3



- B2TiP Report (600p)
  - <https://confluence.desy.de/display/BI/B2TiP+ReportStatus>
- To be published in PTEP / Oxford University Press & printed.
  - Belle II Detector, Simulation, Reconstruction, Analysis tools
  - Physics working groups
  - New physics prospects and global fit code

**PTEP** Prog. Theor. Exp. Phys. 2015, 00000 (319 pages)  
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## The Belle II Physics Book

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The report of the Belle II Theory Interface Platform is presented in this document.

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