



Studies of the X(3872) at Belle and Belle II: measurements and perspectives

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Workshop on Hadron Spectroscopy: The Next Big Steps

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Outline

- Absolute branching fraction
- Decays to χ_{c1}
- Searches for partner states
- Production mechanism
($B \rightarrow K\pi X$ and $\gamma\gamma$)
- Width measurement (3-dim fit)
- Width measurement (small Q value)
- Production mechanism
(B^+ vs. B^0)
- Search for molecule partner X(4014)

Belle

Belle II

ABSOLUTE BRANCHING FRACTION

PDG 2020

$\chi_{c1}(3872)$

$$I^G(J^{PC}) = 0^+(1^{++})$$

also known as $X(3872)$

$$\text{Mass } m = 3871.69 \pm 0.17 \text{ MeV}$$

$$m_{\chi_{c1}(3872)} - m_{J/\psi} = 775 \pm 4 \text{ MeV}$$

$$\text{Full width } \Gamma < 1.2 \text{ MeV, CL} = 90\%$$

$\chi_{c1}(3872)$ DECAY MODES

Fraction (Γ_i/Γ)

p (MeV/c)

$\pi^+ \pi^- J/\psi(1S)$	> 3.2 %	650
$\omega J/\psi(1S)$	> 2.3 %	†
$D^0 \bar{D}^0 \pi^0$	> 40 %	117
$\bar{D}^{*0} D^0$	> 30 %	4
$\pi^0 \chi_{c1}$	> 2.8 %	319
$\gamma J/\psi$	> 7×10^{-3}	697
$\gamma \psi(2S)$	> 4 %	181
$\pi^+ \pi^- \eta_c(1S)$	not seen	745
$\pi^+ \pi^- \chi_{c1}$	not seen	218
$p \bar{p}$	not seen	1693

100% ?

PDG 2021

$\chi_{c1}(3872)$

$$I^G(J^{PC}) = 0^+(1^{++})$$

also known as $X(3872)$

$$\text{Mass } m = 3871.65 \pm 0.06 \text{ MeV}$$

$$m_{\chi_{c1}(3872)} - m_{J/\psi} = 775 \pm 4 \text{ MeV}$$

$$\text{Full width } \Gamma = 1.19 \pm 0.21 \text{ MeV } (S = 1.1)$$

$\chi_{c1}(3872)$ DECAY MODES

Fraction (Γ_i/Γ)

Confidence level

p
(MeV/c)

$e^+ e^-$	< 2.8×10^{-6}	90%	1936
$\pi^+ \pi^- J/\psi(1S)$	(3.8 ± 1.2) %		650
$\pi^+ \pi^- \pi^0 J/\psi(1S)$	not seen		588
$\omega \eta_c(1S)$	< 33 %	90%	368
$\omega J/\psi(1S)$	(4.3 ± 2.1) %		†
$\phi \phi$	not seen		1646
$D^0 \bar{D}^0 \pi^0$	(49^{+18}_{-20}) %		116
$\bar{D}^{*0} D^0$	(37 ± 9) %		†
$\gamma \gamma$	< 11 %	90%	1936
$D^0 \bar{D}^0$	< 29 %	90%	519
$D^+ D^-$	< 19 %	90%	502
$\pi^0 \chi_{c2}$	< 4 %	90%	273
$\pi^0 \chi_{c1}$	(3.4 ± 1.6) %		319
$\pi^0 \chi_{c0}$	< 70 %	90%	–
$\pi^+ \pi^- \eta_c(1S)$	< 14 %	90%	745
$\pi^+ \pi^- \chi_{c1}$	< 7×10^{-3}	90%	218
$p \bar{p}$	< 2.4×10^{-5}	95%	1693

Radiative decays

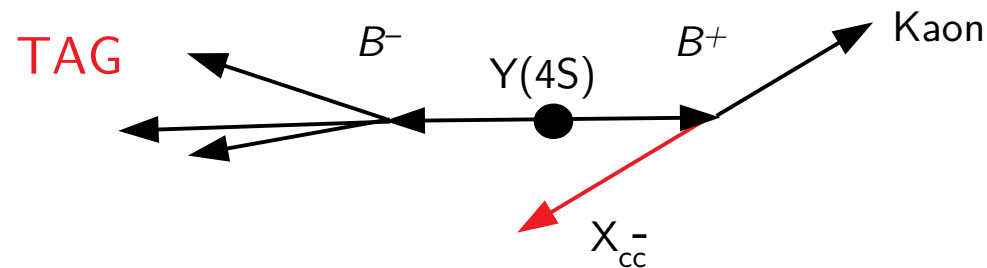
$\gamma D^+ D^-$	< 4 %	90%	502
$\gamma \bar{D}^0 D^0$	< 6 %	90%	519
$\gamma J/\psi$	(8 ± 4) $\times 10^{-3}$		697
$\gamma \chi_{c1}$	< 9×10^{-3}	90%	344
$\gamma \chi_{c2}$	< 3.2 %	90%	303
$\gamma \psi(2S)$	(4.5 ± 2.0) %		181

C-violating decays

$\eta J/\psi$	< 1.8 %	90%	491
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$$B^+ \rightarrow K^+ X_{c\bar{c}}$$

Particular situation at $\Upsilon(4S)$: $m(\Upsilon(4S)) = m_B + m_{\bar{B}}$
 $\rightarrow B$ mesons at rest in cms system



Hierarchical full reconstruction of 1104 hadronic decays

NeuroBayes neural-network package

M. Feindt, F. Keller, M. Krepes, T. Kuhr, S. Neubauer, D. Zander, A. Zupanc

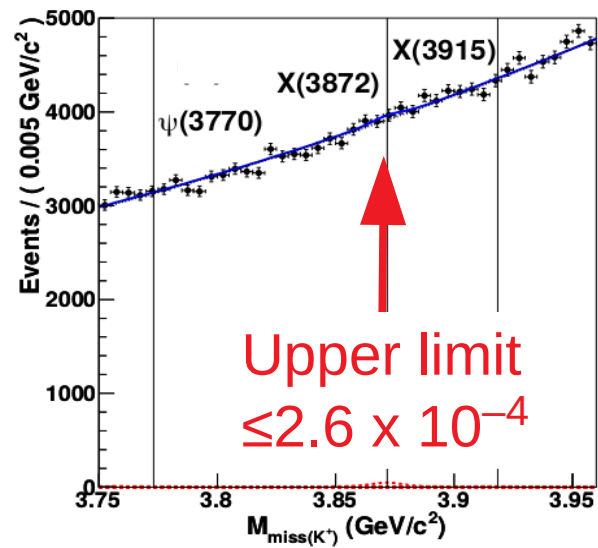
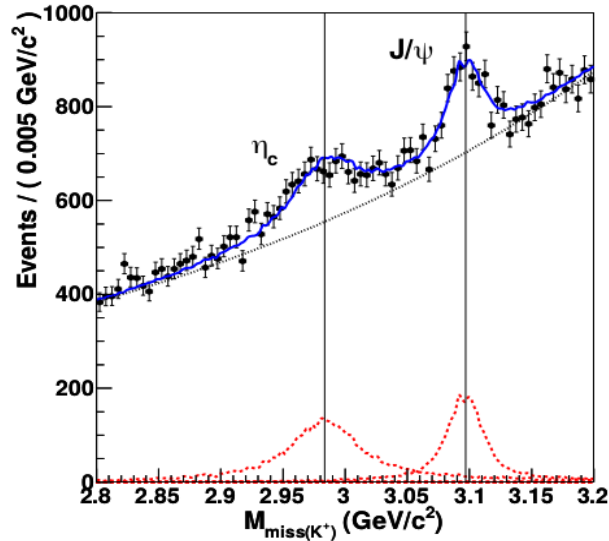
Nucl. Instrum. Meth. A654 (2011) 432

Disadvantage: reconstruction efficiency small (requires tag side)

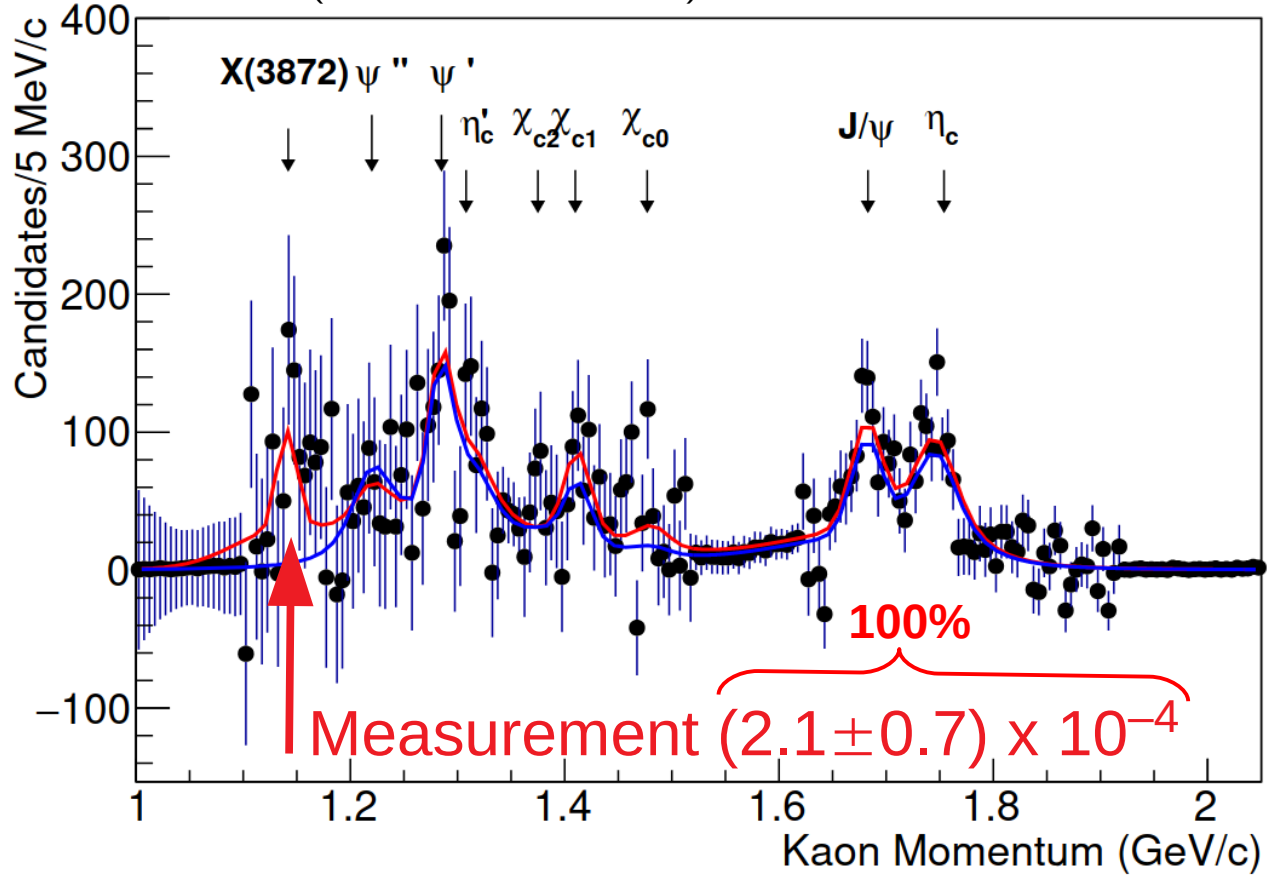
$$\varepsilon \leq 0.26 \%$$

$$B^+ \rightarrow K^+ X_{c\bar{c}}$$

Belle, Phys. Rev. D97 (2018) 012005
711 fb⁻¹ (full Belle data set)



BaBar, Phys.Rev.Lett. 124 (2020) 152001
424 fb⁻¹ (full BaBar data set)



$p(K^\pm)$ in the B meson rest frame

Belle II can improve error to ≤ 0.1 with 50 ab⁻¹

$$M_{\text{miss}(h)} = \sqrt{(p_{e^+e^-}^* - p_{\text{tag}}^* - p_h^*)^2 / c^2}$$

DECAYS

In the following, product branching fractions are given.

$$\underbrace{\mathcal{B}(B \rightarrow K X(3872))}_{\mathcal{B}_{absolute}} \times \mathcal{B}(X(3872) \rightarrow \dots)$$

Decays to χ_{c1}

- $X(3872) \rightarrow \chi_{c1} \pi^+ \pi^-$

Belle, Phys. Rev. D 93 (2016) 052016 (711 fb⁻¹)

upper limit $\mathcal{B} \leq 1.5 \times 10^{-6}$
(0.6% of all X(3872))

- $X(3872) \rightarrow \chi_{c1} \pi^0$

Belle, Phys. Rev. D 99 (2019) 111101 (711 fb⁻¹)

upper limit $\mathcal{B} \leq 8.1 \times 10^{-6}$
(3.2% of all X(3872))

observed by BESIII,

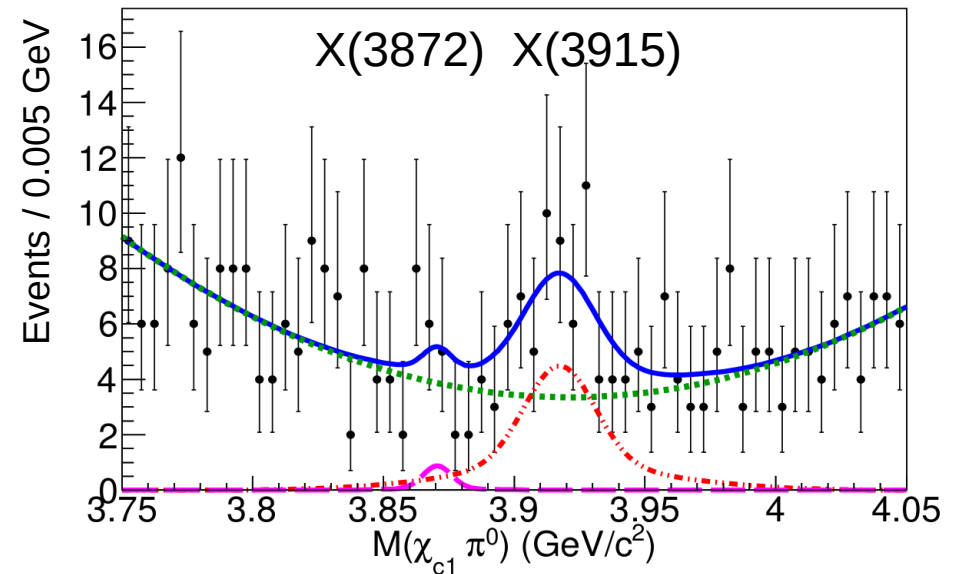
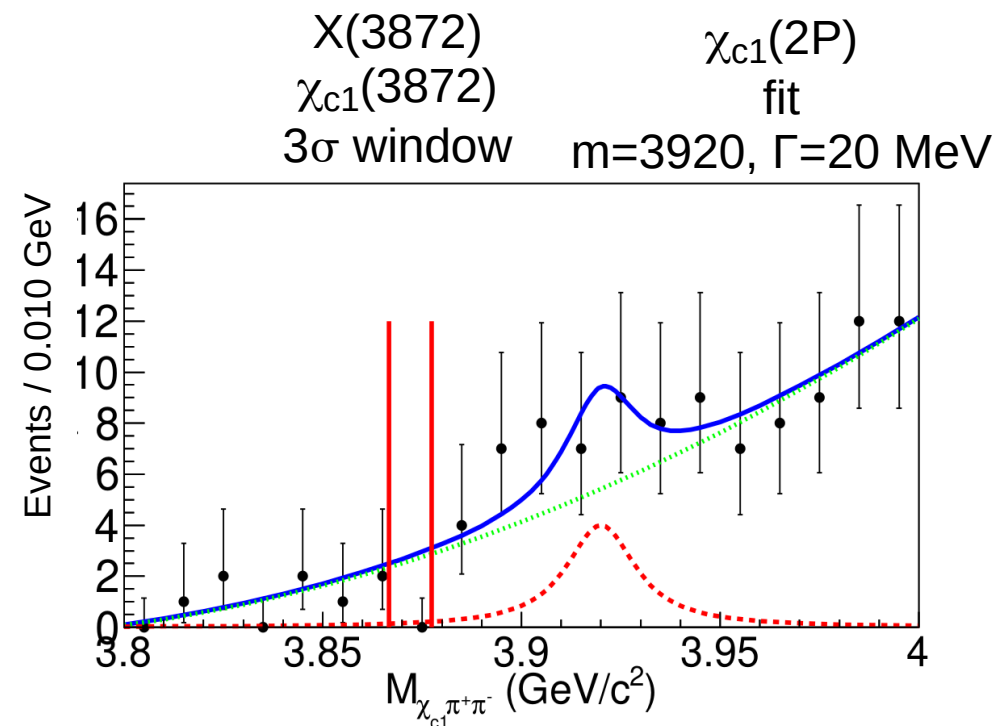
Phys. Rev. Lett. 122 (2019) 202001

$\mathcal{B} = 3.4 \pm 1.6 \%$

isospin violating decay

for charmonium small branching fraction

e.g. $\psi' \rightarrow J/\psi \pi^0$, $\mathcal{B} = (1.268 \pm 0.032) \times 10^{-3}$



Searches for partner states

- Charged partner (I_3 partner), $X^\pm \rightarrow J/\psi \rho^\pm$

PRD 84 (2011) 052004 (711 fb⁻¹)

upper limit $\mathcal{B} \leq 5.4 \times 10^{-6}$

(2.4% of all $X(3872)$, if $\mathcal{B}(X^\pm) = \mathcal{B}(X^0)$)

Reminder: $Z^{\pm,0}(3900)$ cannot be the isospin partner
(wrong G-parity)

- C=-1 partner*, $X^{C-odd} \rightarrow J/\psi \eta$

PTEP 2014 (2014) 4, 043C01 (711 fb⁻¹)

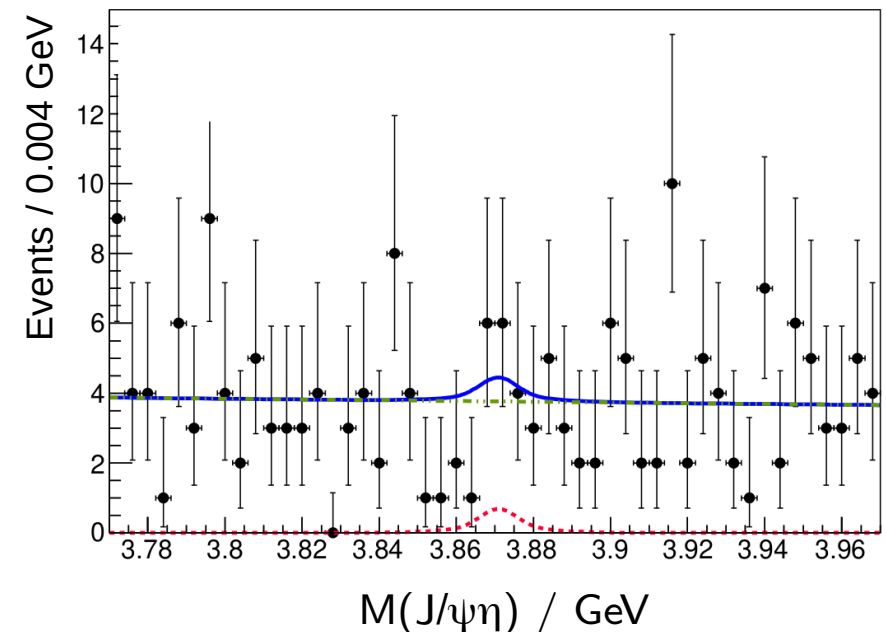
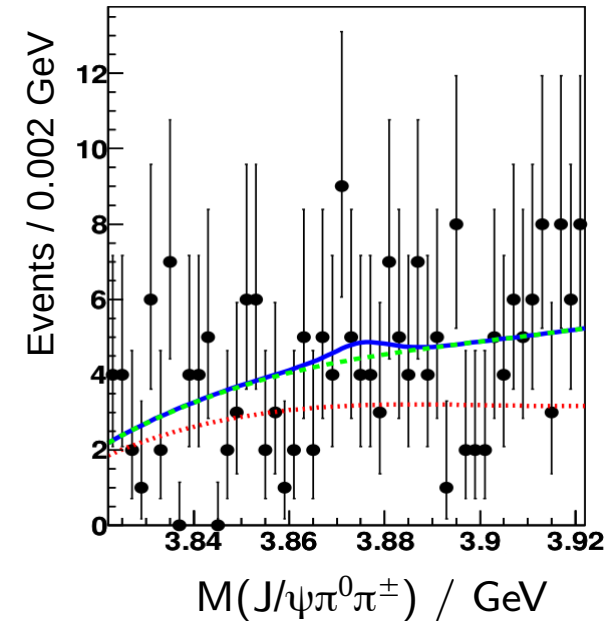
upper limit $\mathcal{B} \leq 3.8 \times 10^{-6}$

(1.7% all $X(3872)$, if $\mathcal{B}(X^{C-odd}) = \mathcal{B}(X^0)$)

*In tetraquark models

$$\frac{1}{\sqrt{2}}(S\bar{A} \pm \bar{S}A)$$

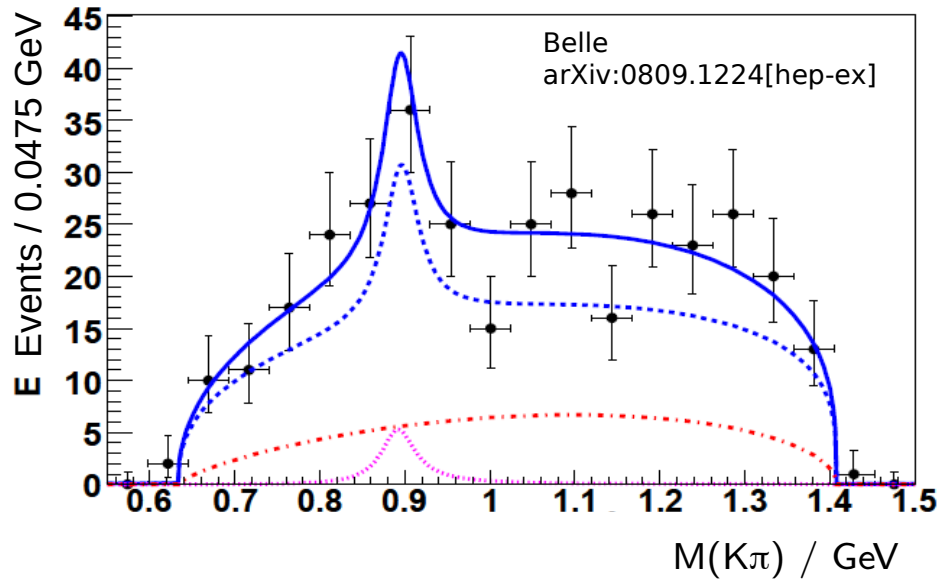
with S scalar diquark, A axialvector diquark



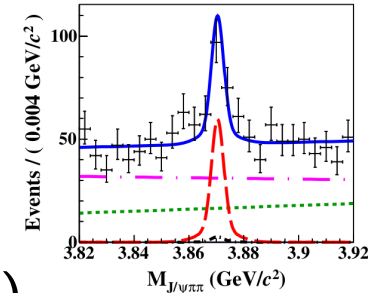
PRODUCTION MECHANISM

Production mechanism $B \rightarrow K \underline{\pi} X(3872)$

$K\pi X(3872)$

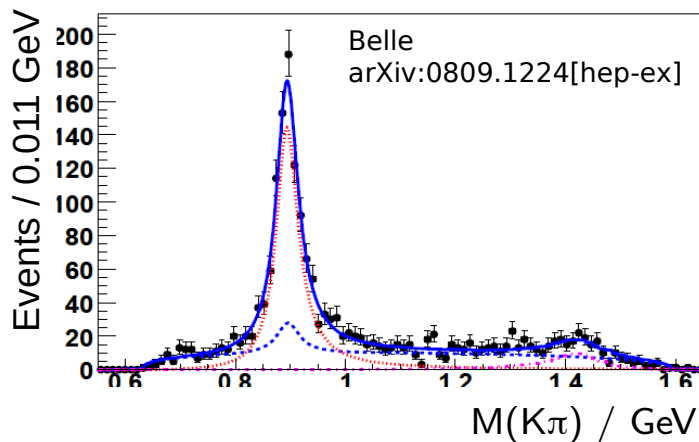


- $\mathcal{B} = 10.6 \times 10^{-6}$ for $B \rightarrow K\pi X$
same order of magnitude as
 $\mathcal{B} = 8.6 \times 10^{-6}$ for $B \rightarrow KX$
(although different phase space)
Phys. Rev. D 84 (2011) 052004 (711 fb⁻¹)
1st observation for B^0 , evidence for B^+

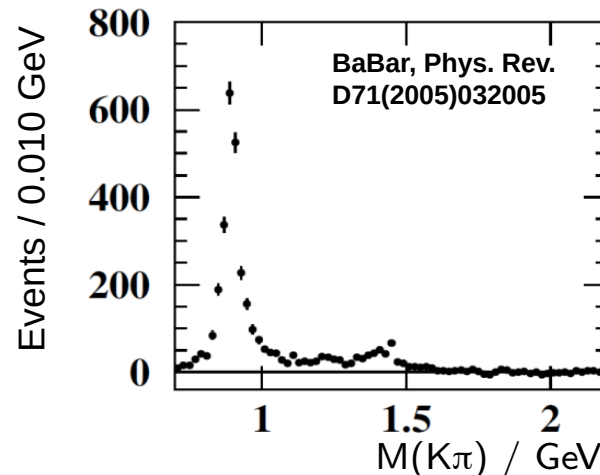


- Resonant K^* component is only 34%
(but 68% for $B \rightarrow K\pi\psi'$)

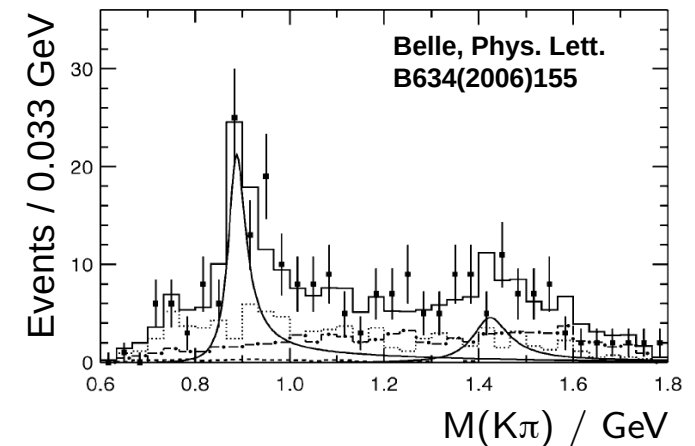
$K\pi\psi'$



$K\pi J/\psi$



$K\pi\chi_{c1}$



$B \rightarrow K\pi X(3872)$ is very different from $B \rightarrow K\pi [c\bar{c}]$

Evidence for $\gamma\gamma \rightarrow X(3872)$

- $X(3872)$ has $J^{PC} = 1^{++}$
Landau–Yang theorem:
coupling to two real photons is forbidden

- Here: at least one photon is virtual

$$\Gamma_{\gamma\gamma}^{X(3872)} \times \mathcal{B}(X(3872) \rightarrow J/\psi\pi^+\pi^-) = 5.5_{-3.8}^{+4.1} \pm 0.7 \text{ eV}$$

Belle, Phys. Rev. Lett. 126 (2021) 122001 (825 fb^{-1})

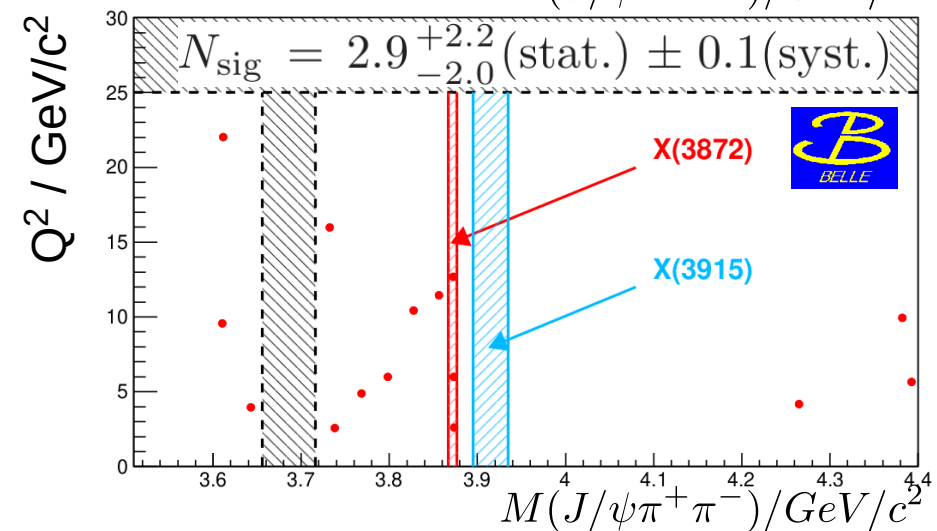
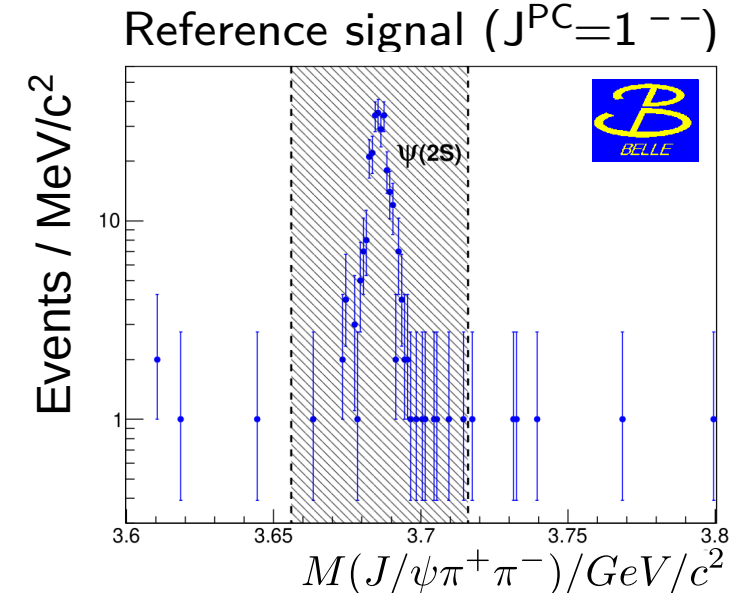
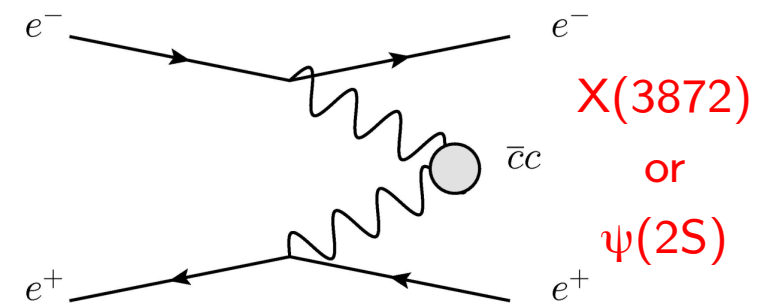
$$\underbrace{\Gamma_{ee}^{X(3872)} \times \mathcal{B}(X(3872) \rightarrow J/\psi\pi^+\pi^-)}_{<0.13 \text{ eV}} \cdot \underbrace{\frac{1}{4\pi\alpha_{em}}}_{\text{vertex}} \leq 1.4 \text{ eV}$$

BESIII, Phys. Lett. B749 (2015) 414

- compatible with prediction for charmonium
J. Kühn et al., Nucl. Phys. B 157 (1979) 125

Significance 3.2σ
(background
 0.11 ± 0.10 events)

Q^2 calculated from momentum of single tagging electron

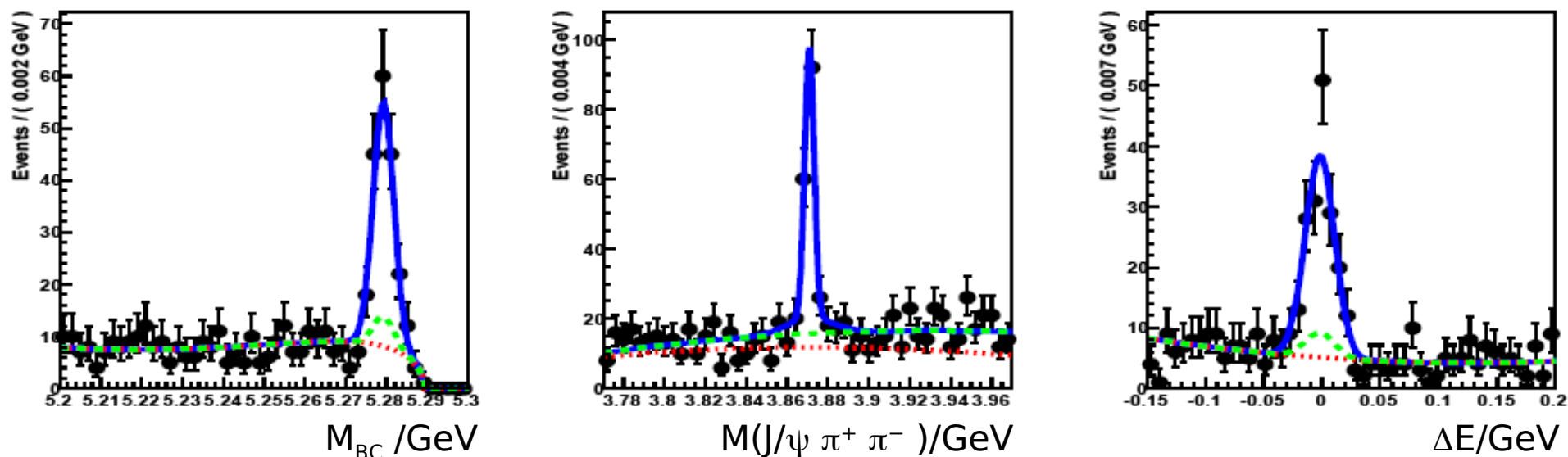


WIDTH

X(3872) width measurement at Belle

$$M_{bc} \equiv \sqrt{(E_{\text{beam}}^{\text{cms}})^2 - (p_B^{\text{cms}})^2}$$

$$\Delta E \equiv E_B^{\text{cms}} - E_{\text{beam}}^{\text{cms}}$$



- 3-dim fit for $X \rightarrow J/\psi \pi^+ \pi^- \rightarrow$ kinematical over-constraint
access to observables smaller than detector resolution
- Upper limit was determined, $\Gamma_X < 1.2 \text{ MeV}$ (90% C.L.)
Belle, Phys. Rev. D84 (2011) 052004
close to later world average ($1.19 \pm 0.21 \text{ MeV}$, Breit-Wigner fit, PDG 2021)
- Fit was validated with ψ' (as control signal), factor $\simeq 4$ narrower width
 $\Gamma_{\psi'} = 0.52 \pm 0.11 \text{ MeV}$ ($0.304 \pm 0.009 \text{ MeV}$, PDG 2011)
 \rightarrow offset bias 230 keV, systematic error 110 keV

From Belle to Belle II

Width of the X(3872) at Belle II, plan

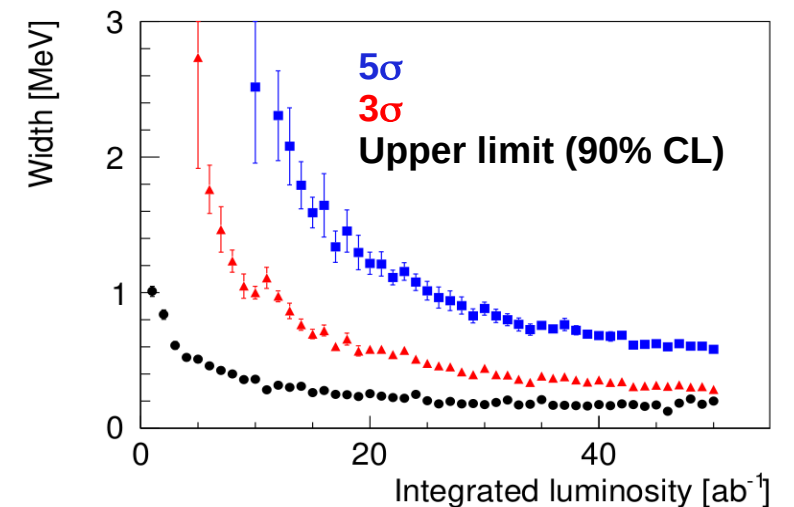
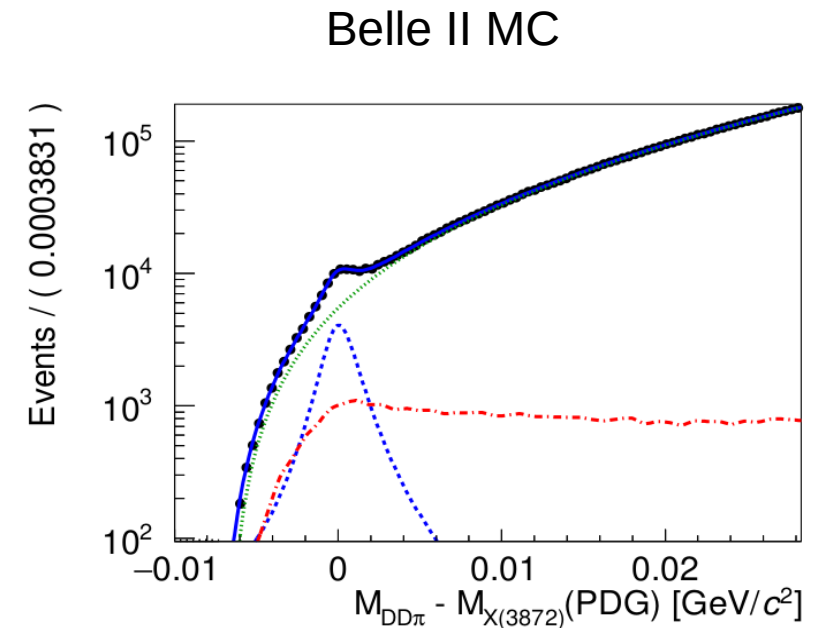
- New approach: use $X(3872) \rightarrow D^0 \bar{D}^0 \pi^0$ decay only seen at BaBar and Belle
small Q value of 7 MeV
(469 MeV for $J/\psi\pi\pi$)
- mass resolution 684 ± 8 keV
(1.93 ± 0.04 MeV for $J/\psi\pi\pi$)
- width can be measured down to 280 keV
(3σ significance for 50 ab^{-1})

Reminder: Flatté fit

$$220^{+70+110}_{-60-130} \text{ keV (FWHM)}$$

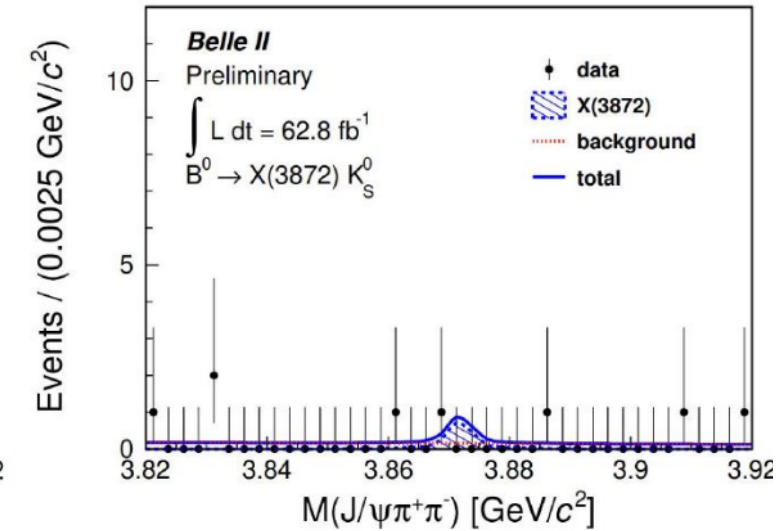
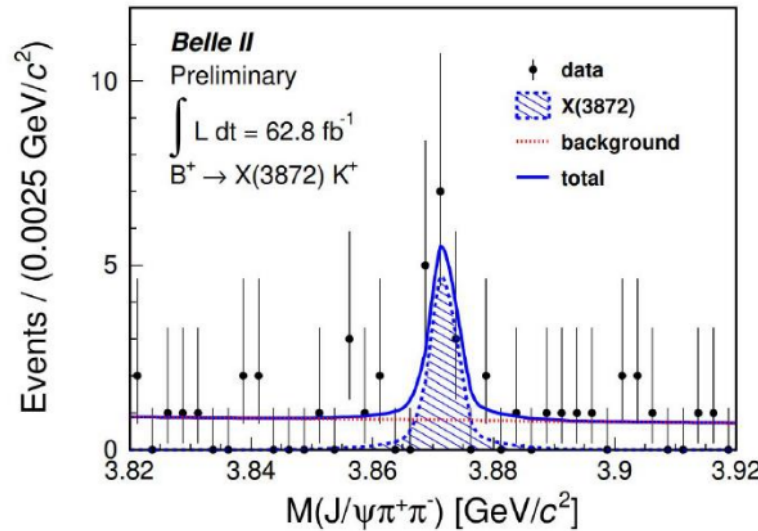
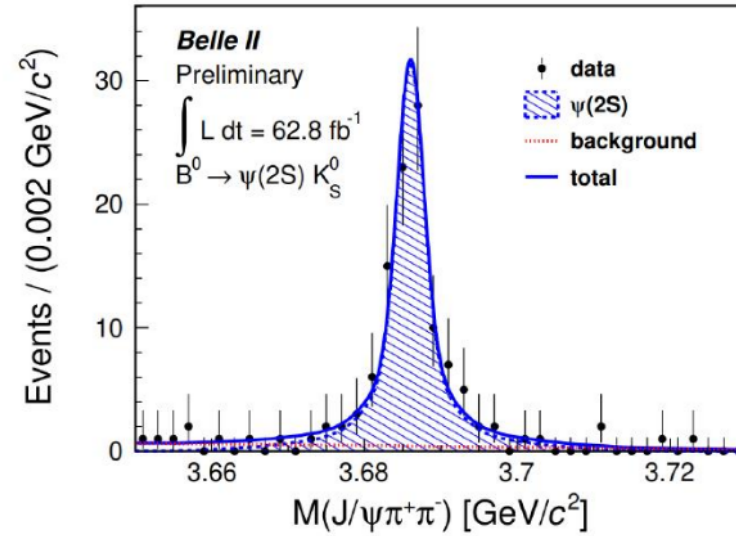
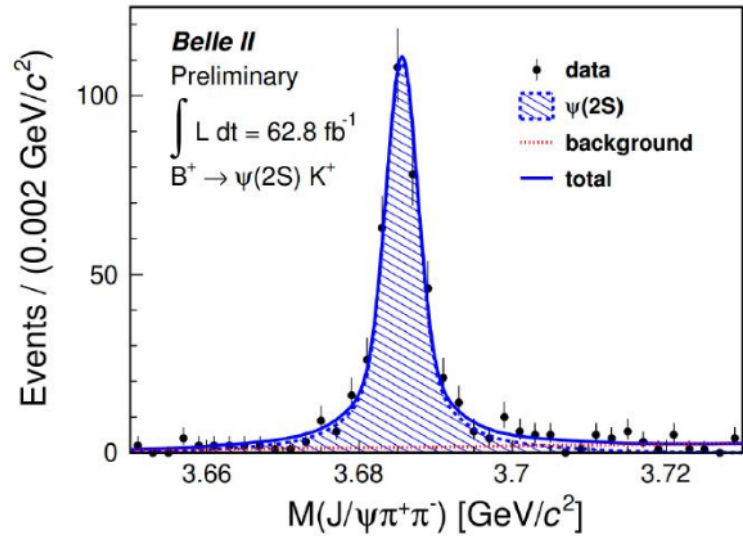
LHCb, Phys. Rev. D102 (2020) 092005

- systematics still to be evaluated
- Future option: combined fit of $D^0 \bar{D}^0 \pi^0$ and $J/\psi\pi\pi$



PRODUCTION MECHANISM

X(3872) at Belle II, data



Efficiency
22.9%

Efficiency
17.5%

Unbinned maximum likelihood fit with triple Gaussian and 1st order Chebyshev polynomial
By now, already factor 4 more data on tape (287.9 fb^{-1} , $\sim 1/4$ of Belle)

$X(3872)$ in neutral and charged B meson decays

- If $X(3872)$ is a $D\bar{D}^*$ molecule, ratio should be small (<0.1)

B^0, K^0 contain d quarks, B^+, K^+ contain u quarks

D^0, \bar{D}^{*0} contain u quarks

Braaten, Lu, Phys. Rev. D77 (2008) 014029

- If $X(3872)$ is charmonium, hybrid, glueball, ratio should be large ($=1$)
- Exotic nature of $X(3872)$ is already seen in present Belle II data but: simultaneous fit of B^0 and B^+ , and ratio was fixed

$$\frac{\mathcal{B}(B^0 \rightarrow K_s^0 \psi')}{\mathcal{B}(B^+ \rightarrow K^+ \psi')} = \frac{(5.8 \pm 0.5) \times 10^{-4}}{(6.24 \pm 0.20) \times 10^{-4}} \simeq 0.93$$

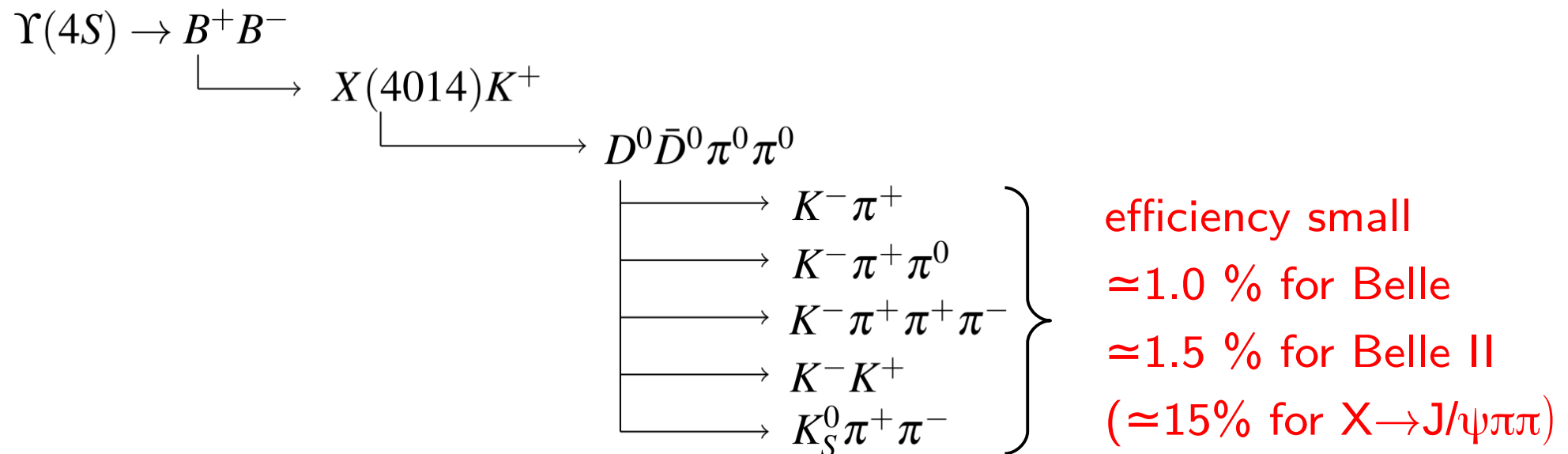
PDG 2021

$$\frac{\mathcal{B}(B^0 \rightarrow K_s^0 X(3872))}{\mathcal{B}(B^+ \rightarrow K^+ X(3872))} = \frac{(1.1 \pm 0.4) \times 10^{-4}}{(2.1 \pm 0.7) \times 10^{-4}} \simeq 0.52$$

X(4014)

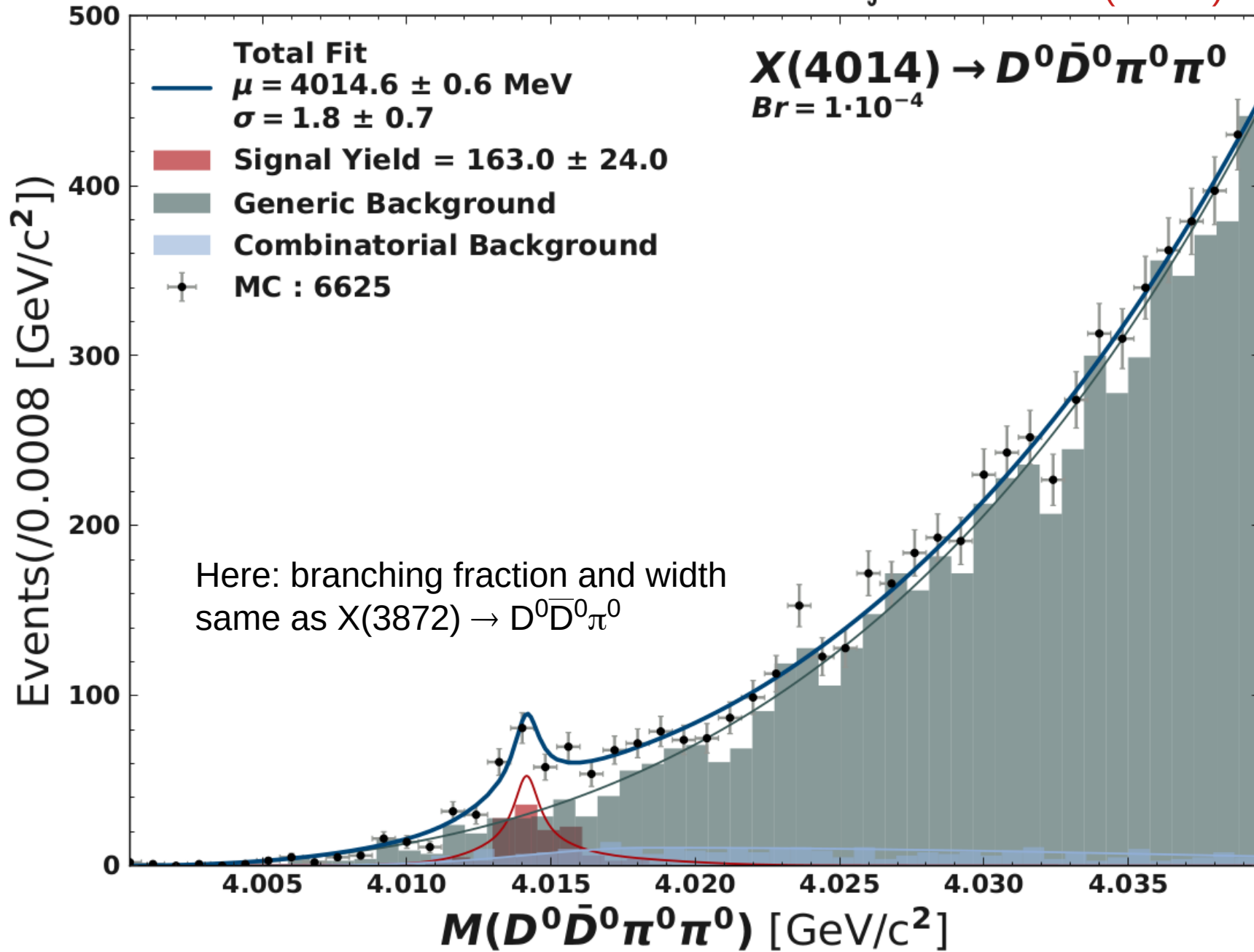
X(4014) at Belle II, plan

- $D^{*0}\bar{D}^{*0}$ molecule, predicted by Törnqvist, Phys. Rev. Lett. 67 (1991) 556
- $J^{PC} = 2^{++}$
pure (charmonium, tetraquark) or mixture (molecule)
- Mass prediction 4012 MeV (threshold 4017 MeV)
heavy quark spin symmetry to X(3872)
Guo, Hidalgo-Duque, Nieves, Valderrama,
Phys. Rev. D88 (2013) 054007
- D -wave decay to $D^0\bar{D}^0$ possible, implies $\Gamma \simeq 10$ MeV

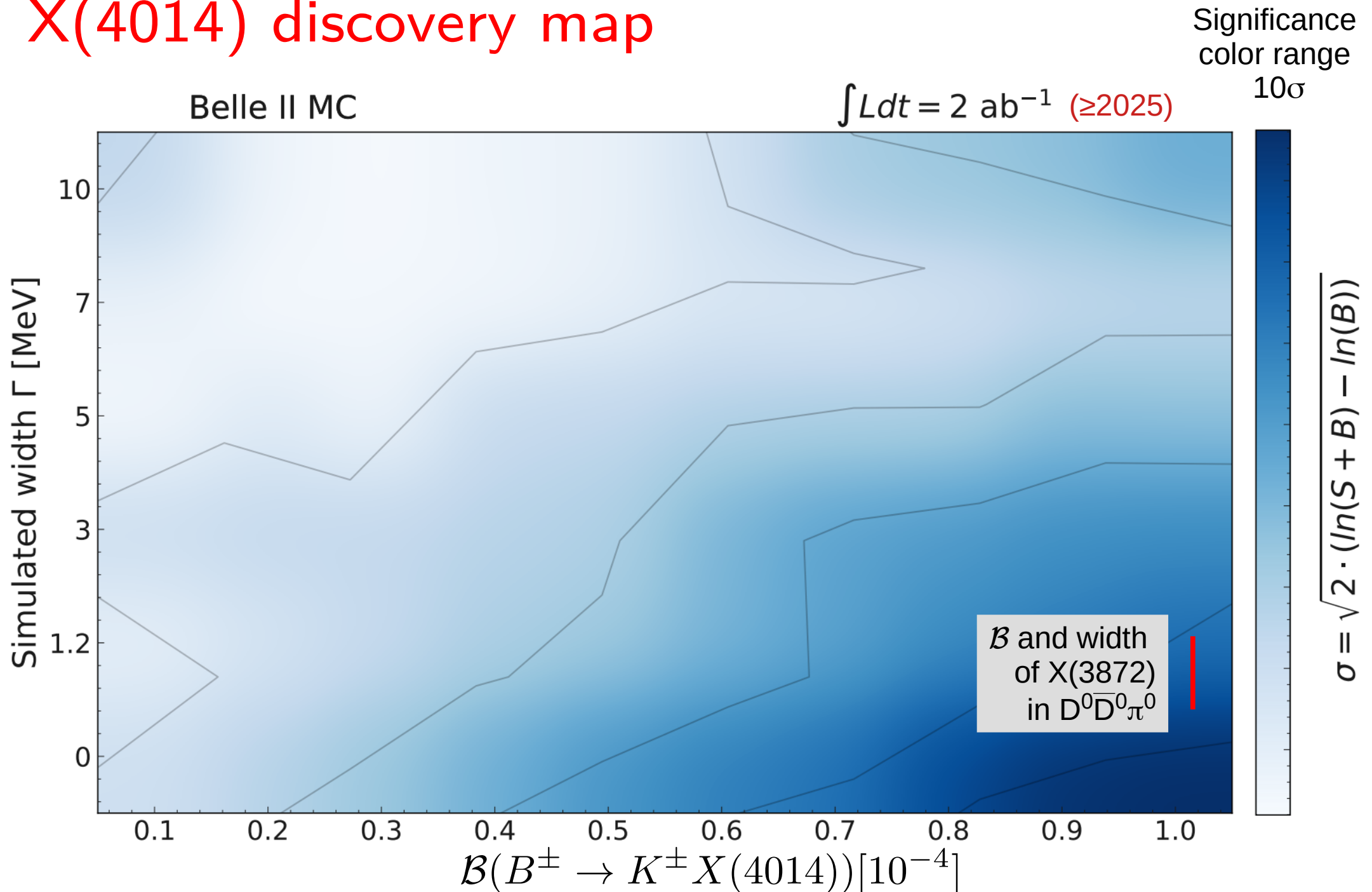


Belle II MC

$\int L dt = 2 \text{ ab}^{-1}$ (≥ 2025)



X(4014) discovery map



Conclusion

- Absolute branching fraction was measured
- Width measurements can reach sub-MeV sensitivity (3-dim fit, small Q value)
- Where are the partner states?