

# Lepton flavor universality at Belle and Belle II

**Seema Choudhury**

on behalf of the Belle & Belle II collaborations

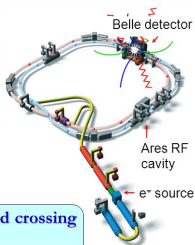


8<sup>th</sup> International Symposium on Symmetries in Subatomic Physics  
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Vienna, Austria





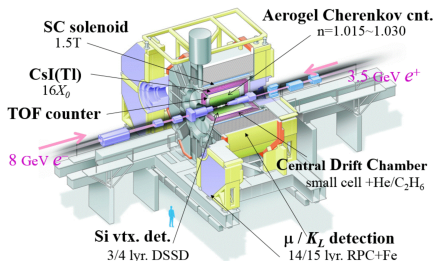
## KEKB Accelerator



8 GeV  $e^-$  x 3.5 GeV  $e^+$ ; 22mrad crossing

$L_{\text{peak}} = 2.11 \times 10^{34} / \text{cm}^2 \text{s}$

Integ. Lum.  $\sim 1040 \text{ fb}^{-1}$

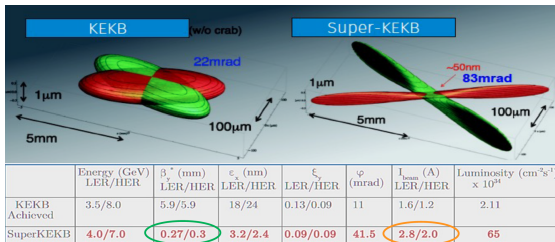
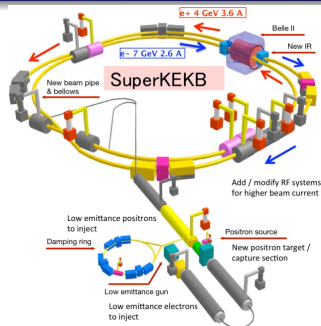


- Belle experiment is located at the KEKB accelerator in Tsukuba, Japan.
- Asymmetric  $e^+e^-$  collider with center-of-mass (CM) energy at  $B\bar{B}$  threshold, 10.58 GeV.
- Data taking from 1999 to 2010.
- Data collected:  $711 \text{ fb}^{-1} = 772 \text{ million } B\bar{B} \text{ pairs}$ .

$$e^+e^- \rightarrow \Upsilon(4S) \rightarrow B\bar{B}$$

# SuperKEKB Accelerator

- Located at Tsukuba, Japan.
- Asymmetric  $e^+$  (4 GeV) -  $e^-$  (7 GeV) collider with CM energy at  $B\bar{B}$  threshold, 10.58 GeV.
- Aims to collect  $50 \text{ ab}^{-1}$  ( $50 \times$  Belle) of data sample.
- Plan to deliver collision at a peak luminosity of  $6.5 \times 10^{35} \text{ cm}^{-2}\text{s}^{-1}$  (30 times that of KEKB) by;
  - reducing beam size by 20 times.
  - increasing beam current by 1.5 times.



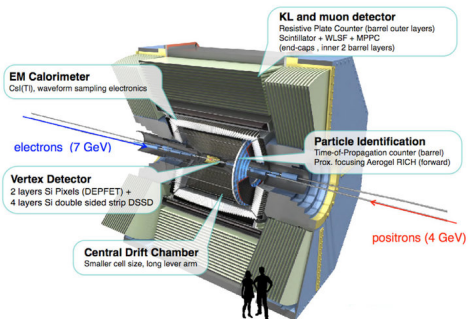
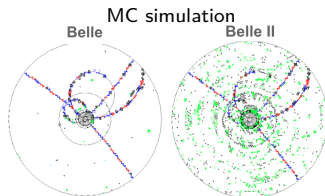
factor 20

factor 1.5

Factor ~30 in the luminosity

# Belle II detector

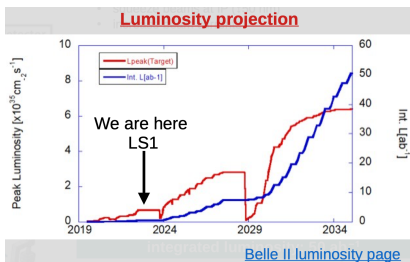
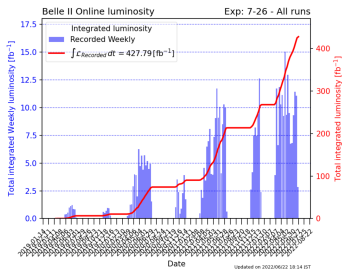
- Designed to operate with a performance similar or better than Belle.
- New detector (only the structure, the superconducting magnets, the crystals of the calorimeter, and KLM RPCs are re-utilized).
- Expect increased beam background ( $\times 10 - 20$ ) at design luminosity
  - Upgraded trigger system and sub-detectors.



- improved vertex resolution ( $2\times$  Belle) and  $K_S^0$  reconstruction efficiency
- enhanced  $K/\pi$  separation
- new trigger lines for dark sector searches
- more efficient reconstruction and analysis tools

# SuperKEKB: new intensity frontier machine

- Recorded integrated luminosity:  $424 \text{ fb}^{-1}$ , data taken between 2019–2022
  - $\sim 362 \text{ fb}^{-1}$  taken at a CM energy of 10.58 GeV, corresponding to the mass of the  $\Upsilon(4S)$
  - $\sim 42 \text{ fb}^{-1}$  taken 60 MeV below the  $\Upsilon(4S)$  peak, continuum background
  - $\sim 19 \text{ fb}^{-1}$  taken around 10.75 GeV for exotic hadron searches
- World record instantaneous luminosity of  $L = 4.71 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$  ( $> 2 \times$  KEKB record) on 22 June, 2022: Entering the regime of a “Super  $B$  factory”.



- Shutdown (LS1) from summer 2022 for 15 months: improvement of machine and detector (beam pipe, pixel vertex detector, Time-Of-Propagation PMT)

- Belle

- LFU in  $B^0 \rightarrow D^{*-} \ell^+ \nu_\ell$
- $\mathcal{R}(D)$  &  $\mathcal{R}(D^*)$
- $R_K$  &  $R_{K^*}$
- LFU in  $\Omega_c^0 \rightarrow \Omega^- \ell^+ \nu_\ell$

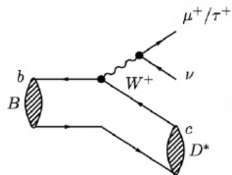
- Belle II

- Inclusive measurement of  $R(X_{e/\mu})$
- Measurement of  $\mathcal{B}(B \rightarrow K^* \ell \ell)$
- $R_K(J/\psi)$

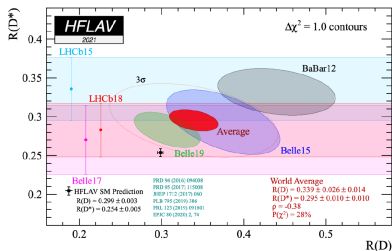
Results shown are with  $711 \text{ fb}^{-1}$  ( $920 \text{ fb}^{-1}$  for  $\Omega_c^0 \rightarrow \Omega^- \ell^+ \nu_\ell$ ) and  $190 \text{ fb}^{-1}$  data sample of Belle and Belle II, respectively.

- $B$  decays with  $b \rightarrow c$  tree-level transition (thus, assumed to be unaffected by NP) are an important probe to test LFU
- Ratio of exclusive decays with  $\tau$  lepton can be used to test SM

$$R_{D^{(*)}} = \frac{\mathcal{B}(B \rightarrow D^{(*)}\tau\nu)}{\mathcal{B}(B \rightarrow D^{(*)}\ell\nu)}$$



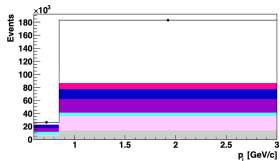
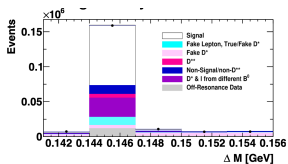
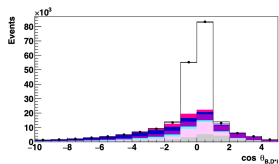
- Experimentally clean final state due to the entire decay chain being reconstructed



- Combined result from Belle [PRD 92, 072014 (2015), PRL 118, 211801 (2017), PRL 124 161803 (2020)], BaBar [PRD 88, 072012 (2013)], and LHCb [PRL 115, 111803 (2015), PRD 97, 072013 (2018)] has a tension of  $3.1\sigma$  with the SM
- Tension has decreased to  $3.1\sigma$  from  $3.8\sigma$  after recent measurement from Belle [PRL 124 161803 (2020)]

# Measurement of LFU in $B^0 \rightarrow D^{*-} \ell \nu_\ell$ at Belle [PRD 100, 052007 (2019)]

- Measurement of LFU using exclusive semileptonic  $B$  decay,  $B^0 \rightarrow D^{*-} (\bar{D}^0 (K^- \pi^+) \pi^-) \ell \nu_\ell$
- Untagged approach (high efficiency but sizable background)
- $D^*$  momentum in the CM frame ( $p^*(D^*) < 2.45$  GeV/ $c$ ) to suppress fake  $D^*$
- Signal yield is extracted with a 3-dimensional binned ML fit to  $\cos \theta_{B, D^* \ell}$  ( $\frac{2E_B^* E_{D^* \ell}^* - m_B^2 - m_{D^* \ell}^2}{2|p_B^*| |p_{D^* \ell}^*|}$ ),  $\Delta M = M(D^* - D^0)$ , and lepton momentum ( $p_\ell$ )



- Ratio of the branching fractions of modes with electrons and muons provides a test of LFU

$$\frac{\mathcal{B}(B^0 \rightarrow D^{*-} e^+ \nu_e)}{\mathcal{B}(B^0 \rightarrow D^{*-} \mu^+ \nu_\mu)} = 1.01 \pm 0.01 \pm 0.03$$

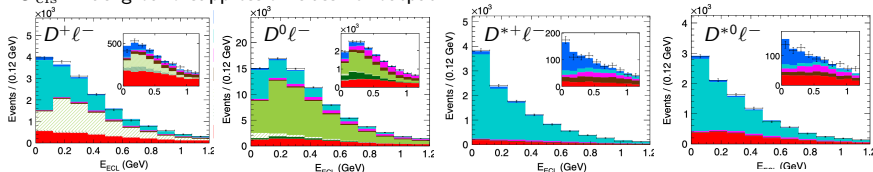
- Result is consistent with unity within the uncertainty
- Stringent test of LFU in  $B$  decays to date



- Simultaneous measurement of  $\mathcal{R}(D)$  &  $\mathcal{R}(D^*)$  at Belle with semileptonic tagging method
- Exclusive semileptonic  $B$  decay analysis  
tag-side:  $B^{0/\pm} \rightarrow D^{(*)}\ell^{-}\nu$   
signal side: signal channel  $B^{0/\pm} \rightarrow D^{(*)}\tau^{-}(\ell^{-}\bar{\nu}\nu)\nu$  and normalization channel  $B^{0/\pm} \rightarrow D^{(*)}\ell^{-}\nu$
- High signal purity at the cost of lower signal reconstruction efficiency.
- Signal is extracted by 2-dimensional binned extended ML fit to  $E_{\text{ECL}}$  and  $\mathcal{O}_{\text{cls}}$

$E_{\text{ECL}}$  : Sum of energies of neutral clusters in the ECL, not associated with any reconstructed particles

$\mathcal{O}_{\text{cls}}$  : Background suppression classifier output

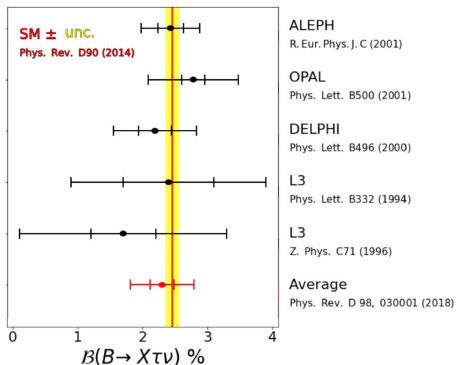
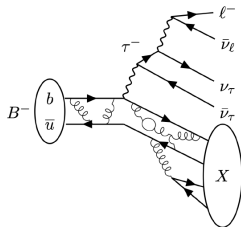


$$\mathcal{R}(D) = 0.307 \pm 0.037 \pm 0.016$$

$$\mathcal{R}(D^*) = 0.283 \pm 0.018 \pm 0.014$$

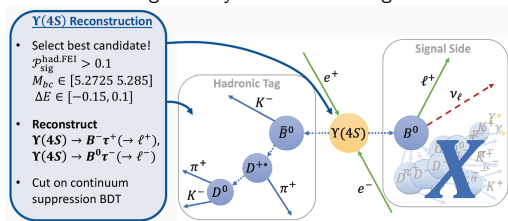
- Most precise measurements of  $\mathcal{R}(D)$  &  $\mathcal{R}(D^*)$
- Results are in agreement with the SM within  $0.2\sigma$  and  $1.1\sigma$  for  $\mathcal{R}(D)$  &  $\mathcal{R}(D^*)$
- Combination of  $\mathcal{R}(D)$  &  $\mathcal{R}(D^*)$  has a deviation of  $0.8\sigma$

- $R(X) = \frac{\mathcal{B}(B \rightarrow X\tau\nu)}{\mathcal{B}(B \rightarrow X\ell\nu)}$  is the complimentary measurement to the  $R_{D^{(*)}}$  via inclusive reconstruction for  $b \rightarrow c$  transition.
- In the SM,  $R(X) = 0.223 \pm 0.004$  [PRD 92, 054018 (2015)]
- More challenging due to larger background from less constrained X system

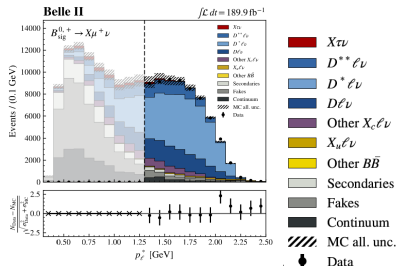


- Inclusive decay with  $\tau$  lepton is challenging
- World average from LEP experiments,  $\mathcal{B}(B \rightarrow X\tau\nu) = (2.41 \pm 0.23)\%$  is consistent with the SM  $(2.45 \pm 0.10)\%$
- LFU can also be tested using light leptons
 
$$R(X_{e/\mu}) = \frac{\mathcal{B}(B \rightarrow Xe\nu)}{\mathcal{B}(B \rightarrow X\mu\nu)}$$
- $R(X_{e/\mu})$  (SM) =  $1.006 \pm 0.001$  [arXiv:2207.03432]

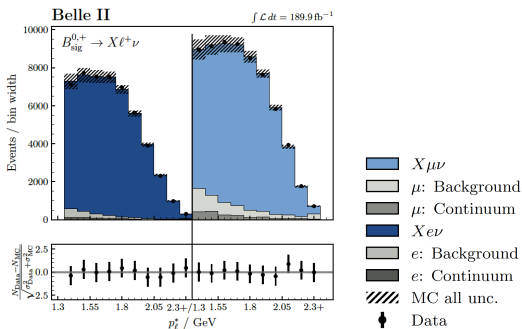
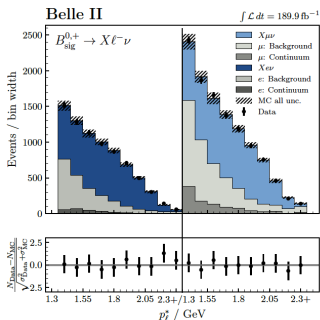
- Test LFU with inclusive measurement of  $R(X_{e/\mu})$
- Analysis is performed on Belle II data sample of 189/fb with hadronic- $B$  tagging (FEI)
- Constrain flavor and kinematics of the signal  $B$  meson by tagging the other  $B$  in its fully hadronic decays, *i.e.*, good purity at the cost of lower signal reconstruction efficiency.
- $X$  system in signal side contains a large variety of different charged and neutral final-state particles



- lepton momentum in the CM frame of the signal  $B$  meson,  $p_{\ell}^*$  is used to extract signal yield
- Require lepton to have high probability to be an electron or muon and  $p_{\ell}^* > 1.3 \text{ GeV}/c$  to suppress backgrounds from hadron faking leptons and secondary leptons from  $b \rightarrow c \rightarrow (\ell, s)$  cascades and  $B \rightarrow X\tau\nu$



- Signal yields for  $B \rightarrow X\mu\nu$  and  $B \rightarrow Xe\nu$  are extracted in 10 bins of  $p_\ell^*$
- Simultaneous fit for  $\mu$  and  $e$  channel: one-dimensional binned ML fit



- $48034 \pm 286$  and  $58569 \pm 429$  signal events for  $B \rightarrow Xe\nu$  and  $B \rightarrow X\mu\nu$  channels.

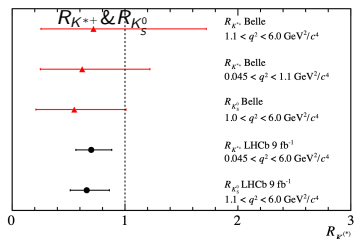
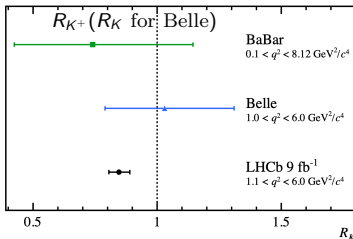
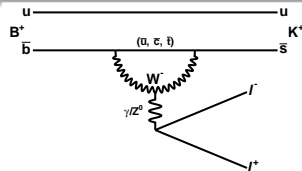
$$R(X_{e/\mu}) = 1.033 \pm 0.010 \pm 0.020 \text{ for } p_\ell^* > 1.3 \text{ GeV}/c$$

- First inclusive test of  $(e, \mu)$  lepton flavor universality in semileptonic  $B \rightarrow X\ell\nu$  decays
- Measurement in agreement with unity within  $1.5\sigma$
- World leading precision (2.2% combined uncertainty)
- Paved the path for inclusive  $R(X_{\tau/\ell}) = R(X)$  measurement

- $B$  decays with rare  $b \rightarrow s$  loop-level transitions are an important probe to test LFU
- LFU ratio is named as  $R_K$  and  $R_{K^*}$  for  $B \rightarrow K\ell\ell$  and  $B \rightarrow K^*\ell\ell$

$$R_{K^{(*)}} = \frac{\mathcal{B}(B \rightarrow K^{(*)}\mu\mu)}{\mathcal{B}(B \rightarrow K^{(*)}ee)}$$

- According to SM this ratio should be 1 [EPJC 76, 440 (2016)], as the coupling of lepton to gauge boson is independent of flavor.



- LHCb [arXiv:2103.11769]  $R_{K^+} = 0.846_{-0.041}^{+0.044}$  for  $1.1 < q^2 < 6.0 \text{ GeV}^2/c^4$  has a deviation of  $3.1\sigma$  from SM prediction with  $9 \text{ fb}^{-1}$  data sample, where  $q^2 = M_{\ell\ell}^2$ .
- $R_{K^{*+}}$  and  $R_{K_S^0}$  results from LHCb [PRL 128, 191802 (2022)] are individually consistent with the SM at the  $1.4\sigma$  and  $1.5\sigma$  level
- $B \rightarrow J/\psi K^{(*)}$  can be used to cross-check the ratio, which is compatible with the SM prediction of unity.

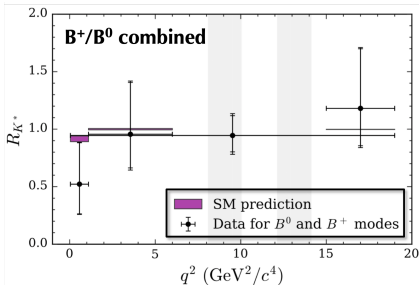
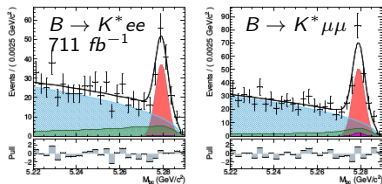
- $R_{K^*}$  tests the lepton-flavor-universality in  $B \rightarrow K^* \ell^+ \ell^-$ .
- Reconstructed 4 decay modes;  
 $B^+ \rightarrow K^{*+}(K^+ \pi^0, K_S^0 \pi^+) \ell^+ \ell^-$   
 $B^0 \rightarrow K^{*0}(K^+ \pi^-, K_S^0 \pi^0) \ell^+ \ell^-$ .
- Kinematic variables to distinguish signal from background;

$$M_{bc} = \sqrt{E_{beam}^2/c^4 - |p_B|^2/c^2}$$

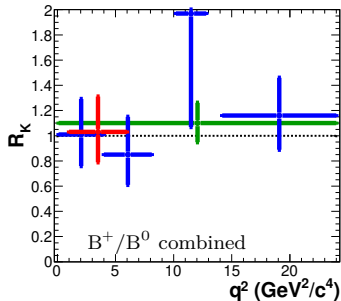
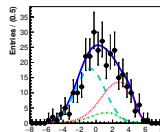
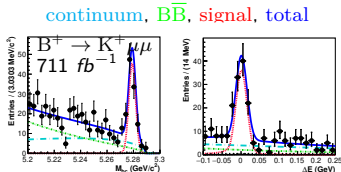
$$\Delta E = E_B - E_{beam}$$

- Continuum and  $B\bar{B}$  backgrounds are suppressed using Neural Networks.
- Performed 1D unbinned extended ML fit to extract the signal yield.
- $103^{+13.4}_{-12.7}$  and  $139.9^{+16.0}_{-15.4}$  events for electron and muon modes.
- $R_{K^{*+}}$ ,  $R_{K^{*0}}$  and  $R_{K^*}$  are measured for both low and high  $q^2$  bins.
- Results consistent with the SM predictions.
- First result for  $R_{K^{*+}}$  measurement.

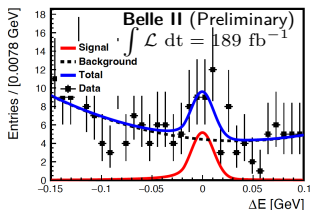
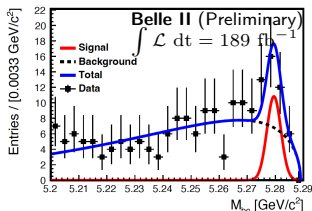
combinatorial, signal, charmonium, peaking, total



- $R_K$  tests the lepton-flavor-universality in  $B \rightarrow K \ell \ell$ .
- Decay modes reconstructed,  $B^+ \rightarrow K^+ \ell \ell$  and  $B^0 \rightarrow K_S^0 \ell \ell$ .
- Background from continuum and  $B\bar{B}$  are suppressed using a Neural Network having event shape, vertex quality, and kinematic variables.
- Performed 3D unbinned ML fit in  $M_{bc}$ ,  $\Delta E$ , and modified NN output ( $O'$ ) to extract the signal yield.
- Control mode is consistent with expectation;  $R_{K^+}(J/\psi) = 0.994 \pm 0.011 \pm 0.010$   
 $R_{K^0}(J/\psi) = 0.993 \pm 0.015 \pm 0.010$
- $137 \pm 14$ ,  $138 \pm 15$ ,  $27.3^{+6.6}_{-5.8}$ , and  $21.8^{+7.0}_{-6.1}$  signal events for  $B^+ \rightarrow K^+ \mu \mu$ ,  $B^+ \rightarrow K^+ e e$ ,  $B^0 \rightarrow K_S^0 \mu \mu$ , and  $B^0 \rightarrow K_S^0 e e$ .
- $R_{K^+}$ ,  $R_{K^0}$ ,  $R_K$  are measured in different  $q^2$  bins.  
 $q^2 \in [0.1, 4.0]$ ,  $[4.0, 8.12]$ ,  $[1.0, 6.0]$ ,  $[10.2, 12.8]$ ,  $> 14.18$ , and  $> 0.1 \text{ GeV}^2/c^4$
- $R_K$  values for various  $q^2$  bins agree with the SM prediction.



- Decay modes reconstructed:  $B^0 \rightarrow K^{*0}(K^+ \pi^-) \ell \ell$  and  $B^+ \rightarrow K^{*+}(K^+ \pi^0, K_S^0 \pi^+) \ell \ell$
- Background from continuum and  $B\bar{B}$  is suppressed using a BDT having event shape, vertex quality, and kinematic variables.
- Performed 2D unbinned ML fit in  $M_{bc}$  and  $\Delta E$  to extract the signal yield.



- Branching fraction are measured for the entire range of the dilepton mass, excluding the very low mass region to suppress the  $B \rightarrow K^* \gamma (\rightarrow e^+ e^-)$  background and regions compatible with decays of charmonium resonances

$$\mathcal{B}(B \rightarrow K^*(892) \mu^+ \mu^-) = (1.19 \pm 0.31^{+0.08}_{-0.07}) \times 10^{-6},$$

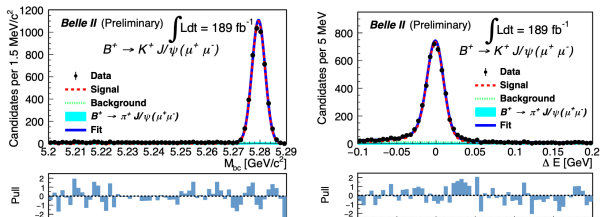
$$\mathcal{B}(B \rightarrow K^*(892) e^+ e^-) = (1.42 \pm 0.48 \pm 0.09) \times 10^{-6},$$

$$\mathcal{B}(B \rightarrow K^*(892) \ell^+ \ell^-) = (1.25 \pm 0.30^{+0.08}_{-0.07}) \times 10^{-6},$$

- Results are compatible with world averages within the uncertainties.
- Observation of these decays is the first step towards LFU test ( $R_{K^*}$ ).



- Decay channels:  $B^+ \rightarrow J/\psi(\ell\ell)K^+$  and  $B^0 \rightarrow J/\psi(\ell\ell)K^0$
- Important channels to test our analysis method
- Signal yield is extracted by a 2D unbinned ML fit in  $M_{bc}$  and  $\Delta E$ .



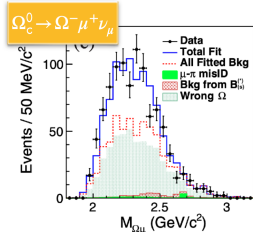
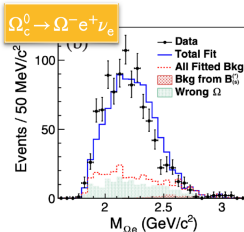
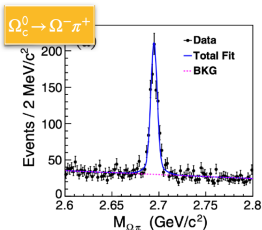
- Signal purity is 90 – 95%.

$$R_{K^+}(J/\psi) = 1.009 \pm 0.022 \pm 0.008$$

$$R_{K^0}(J/\psi) = 1.042 \pm 0.042 \pm 0.008$$

- Results are statistically dominated and in agreement with results from Belle and LHCb.
- Systematics uncertainties have been reduced compared to most precise measurements from Belle [JHEP 03, 105 (2021)].

- LFU in  $\Omega_c^0$  is probed for the first time with  $\Omega_c^0 \rightarrow \Omega^- \ell^+ \nu_\ell$
- $\Omega_c^0$  are reconstructed in the process;  $e^+e^- \rightarrow c\bar{c} \rightarrow \Omega_c^0 + \text{anything}$
- Used 89.5, 711, and 121.1  $\text{fb}^{-1}$  data collected at the CM energies of 10.52, 10.58, and 10.86 GeV.
- $\Omega_c^0$  signals are extracted by binned ML fits to the invariant mass ( $M_{\Omega\ell}$ ) spectra.

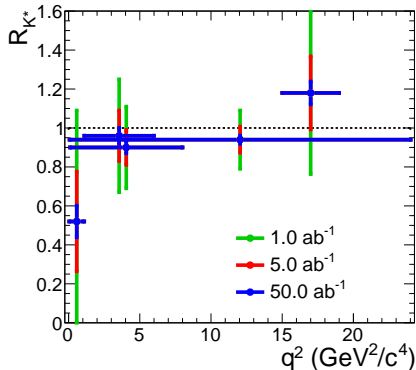
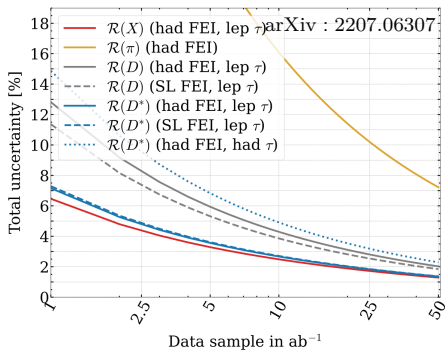


- Significances of the  $\Omega_c^0 \rightarrow \Omega^- \ell^+ \nu_\ell$  are both larger than  $10\sigma$ ,  $\Omega_c^0 \rightarrow \Omega^- \mu^+ \nu_\mu$  decay is seen for first time in Belle.
- $865.3 \pm 35.3$ ,  $707.6 \pm 37.7$ , and  $367.9 \pm 31.4$  signal events for  $\Omega_c^0 \rightarrow \Omega^- \pi^+$ ,  $\Omega_c^0 \rightarrow \Omega^- e^+ \nu_e$ ,  $\Omega_c^0 \rightarrow \Omega^- \mu^+ \nu_\mu$
- $\Omega_c^0$  semileptonic decay branching fraction ratio;

$$R(\Omega) = \frac{\mathcal{B}(\Omega_c^0 \rightarrow \Omega^- e^+ \nu_e)}{\mathcal{B}(\Omega_c^0 \rightarrow \Omega^- \mu^+ \nu_\mu)} = 1.02 \pm 0.10 \pm 0.02$$

- $\mathcal{B}(\Omega_c^0 \rightarrow \Omega^- e^+ \nu_e) / \mathcal{B}(\Omega_c^0 \rightarrow \Omega^- \mu^+ \nu_\mu)$  agrees with the expected LFU value  $1.03 \pm 0.06$  [arXiv:2108.06110].

# some LFU prospects at Belle II



- $R(X)$  (and in general inclusive processes) is unique to Belle II
- Currently estimated precision on  $R(X)$  to be  $\sim 17\%$  (stat+syst)
- Few  $\text{ab}^{-1}$  of data will be sufficient to clarify whether the anomaly on  $\mathcal{R}(D) - \mathcal{R}(D^*)$  has a statistical or systematic origin

- Belle II can perform  $R_K$  and  $R_{K^*}$  measurements for low as well as high  $q^2$  bins.
- Belle II will provide an independent measurement to confirm the tension with few  $\text{ab}^{-1}$  of data
- $R_{K^+}$  and  $R_{K^*}$  statistical sensitivity will be  $< 2\%$  for entire  $q^2$  region and  $\sim 3\%$  for  $q^2 \in [1 - 6] \text{ GeV}^2/c^4$

- Belle II has now collected  $\sim 424 \text{ fb}^{-1}$  of data sample (comparable to size of that of BaBar) and can be combined with that of Belle ( $711 \text{ fb}^{-1}$ )
- Flavor physics in  $e^+e^-$  collisions offers an extremely rich physics program with many opportunities to probe New Physics
- Access to charged and neutral  $B$  with equal efficiency
- Equal sensitivity for muon and electron channels
- Access to inclusive decay modes in addition to exclusive modes
- Untagged (high statistics) vs tagged (high purity) analysis
- Long way to go! A beginning has been made!

**No sign of LFU violation so far from Belle or Belle II**  
**An exciting era of discoveries and precision measurements !!!**

TABLE I. Systematic uncertainties contributing to the  $\mathcal{R}(D^{(*)})$  results, together with their correlation.

Source	$\Delta\mathcal{R}(D)(\%)$	$\Delta\mathcal{R}(D^*)(\%)$	Correlation
$D^{**}$ composition	0.76	1.41	-0.41
PDF shapes	4.39	2.25	-0.55
Feed-down factors	1.69	0.44	0.53
Efficiency factors	1.93	4.12	-0.57
Fake $D^{(*)}$ calibration	0.19	0.11	-0.76
$B_{\text{tag}}$ calibration	0.07	0.05	-0.76
Lepton efficiency and fake rate	0.36	0.33	-0.83
Slow pion efficiency	0.08	0.08	-0.98
$B$ decay form factors	0.55	0.28	-0.60
Luminosity, $f^{+-}$ , $f^{00}$ , and $\mathcal{B}(\Upsilon(4S))$	0.10	0.04	-0.58
$\mathcal{B}(B \rightarrow D^{(*)}\ell\nu)$	0.05	0.02	-0.69
$\mathcal{B}(D)$	0.35	0.13	-0.65
$\mathcal{B}(D^*)$	0.04	0.02	-0.51
$\mathcal{B}(\tau^- \rightarrow \ell^- \bar{\nu}_\ell \nu_\tau)$	0.15	0.14	-0.11
Total	5.21	4.94	-0.52

Sources	$B^+ \rightarrow J/\psi K^+$	$B^0 \rightarrow J/\psi K_S^0$	$R_{K^+}(J/\psi)$	$R_{K^0}(J/\psi)$
Lepton identification	$\pm 0.68$	$\pm 0.68$	$\pm 0.97$	$\pm 0.97$
Kaon identification	$\pm 0.80$	–	–	–
$K_S^0$ identification	–	$\pm 1.57$	–	–
Track reconstruction	$\pm 1.05$	$\pm 1.40$	–	–
Efficiency calculation	$\pm 0.14$	$\pm 0.18$	$\pm 0.20$	$\pm 0.25$
Number of $B\bar{B}$ pairs	$\pm 1.40$	$\pm 1.40$	–	–
$f^{+- (00)}$	$\pm 1.20$	$\pm 1.20$	–	–
$\mathcal{O}_{\min}$	$\pm 0.16$	$\pm 0.28$	$\pm 0.24$	$\pm 0.39$
PDF shape parameters	$+0.15$ $-0.20$	$+0.05$ $-0.10$	$+0.22$ $-0.31$	$+0.10$ $-0.20$
Total	$\pm 2.38$	$\pm 2.90$	$+1.05$ $-1.07$	$+1.08$ $-1.09$

Source	$\mathcal{B}(B \rightarrow KJ/\psi)$				$R_K$	
	$K^+$	$K^+$	$K_S^0$	$K_S^0$	$K^+$	$K^0$
	$e^+e^-$	$\mu^+\mu^-$	$e^+e^-$	$\mu^+\mu^-$		
Number of $B\bar{B}$ events	1.5	1.5	1.5	1.5	–	–
PDF shape	0.2	0.2	0.2	0.2	0.2	0.2
Electron identification	0.6	–	0.6	–	0.6	0.6
Muon identification	–	0.4	–	0.4	0.4	0.4
Kaon identification	0.2	0.2	–	–	–	–
$K_S^0$ reconstruction	–	–	3.0	3.0	–	–
Tracking efficiency	0.9	0.9	1.2	1.2	–	–
Simulation sample size	0.1	0.1	0.1	0.1	0.1	0.1
$\Upsilon(4S)$ branching fraction	2.6	2.6	2.6	2.6	–	–
$(\tau_{B^+}/\tau_{B^0})$	–	–	–	–	–	–
Total	3.2	3.2	4.4	4.4	0.8	0.8

	$e$ channel	$\mu$ channel	Combination
$M_X$ scaling	7.8 % (21.2 %)	12.5 % (20.5 %)	8.7 % (26.8 %)
PID	1.8 % (1.2 %)	7.1 % (6.6 %)	2.1 % (1.6 %)
Tracking eff.	2.9 % (2.8 %)	5.1 % (3.4 %)	3.4 % (4.0 %)
$X_c \ell \nu$ BRs	6.6 % (15.2 %)	11.1 % (15.9 %)	7.5 % (19.9 %)
$X_c \ell \nu$ FFs	4.5 % (7.1 %)	7.2 % (6.8 %)	5.0 % (8.9 %)
Statistical	10.8 % (40.3 %)	19.4 % (48.9 %)	9.4 % (31.3 %)
Total	17.0 % (100 %)	27.7 % (100 %)	16.8 % (100 %)

- Dominate systematic comes from  $X_c \ell \nu$  BRs because of discrepancy between the inclusive semileptonic  $B$  meson width and sum of exclusively measured BRs. This difference is usually filled by  $D^* \pi \pi$  and  $D^* \eta$  modes and are scaled to inclusive  $B$  meson width. As this is speculative, they are assigned with 100% uncertainty, this become one of the leading systematic uncertainty.