



Recent results from Belle II

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Collider

- The superKEKB collider
- The Belle II detector

Recent results from Belle II

- Physics program at Belle II
- A brief introduction to some physics areas
- Followed by recent results

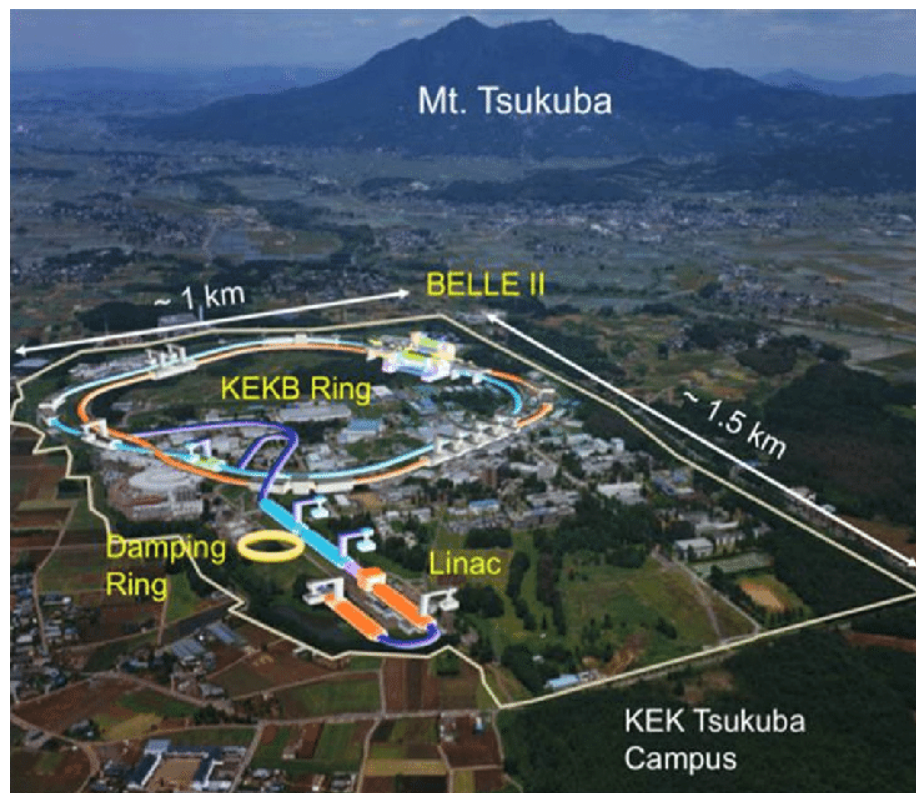
Summary and outlook

- Future prospects of Belle 2

Abbreviations

- Standard Model: SM
- New Physics: NP
- Interaction point: IP
- Electroweak: EW
- Quantum Chromodynamics: QCD
- Flavor Changing Neutral Current: FCNC
- Multivariate Analysis: MVA
- Boosted Decision Tree: BDT
- Full Event Interpretation: FEI
- Kernel Density Estimation: KDE
- Boyed-Grienstein-Lebed: BGL
- Caprini-Lellouch-Neubert: CLN
- Bourely-Caprini-Lellouch: BCL

The SuperKEKB collider (Luminosity frontier)



- Goal to achieve instantaneous luminosity (\mathcal{L}) of $6 \times 10^{35} \text{ cm}^{-2}\text{s}^{-1}$ and integrated \mathcal{L} of 50 ab^{-1} to meet various physics requirements

$$L = \frac{\gamma_{\pm}}{2e r_e} \left(1 + \frac{\sigma_y^*}{\sigma_x^*} \right) \left(\frac{I_{\pm}^{\xi} \beta_y^*}{R_{\xi y_{\pm}}} \right) \left(\frac{R_L}{R_{\xi y_{\pm}}} \right)$$

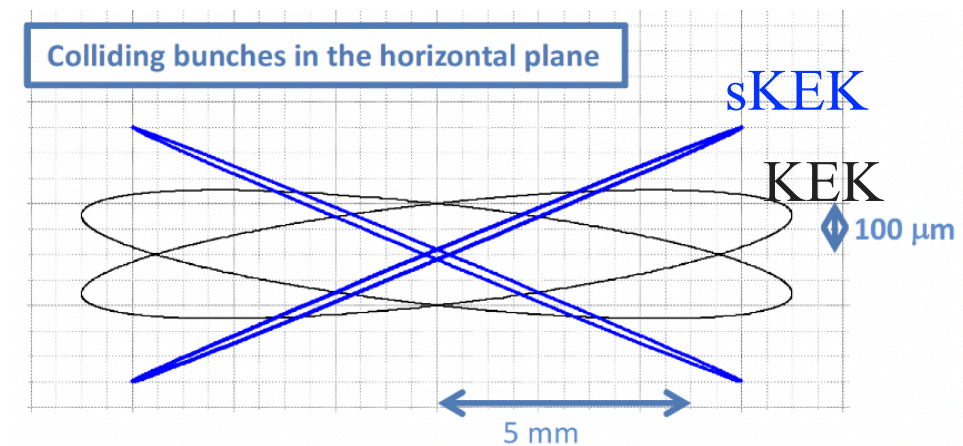
Lorentz factor $\rightarrow \gamma_{\pm}$
 Beam size at IP $\rightarrow \sigma_y^*$
 Beam current $\rightarrow I_{\pm}^{\xi}$
 Vertical beam-beam parameter at IP $\rightarrow R_{\xi y_{\pm}}$
 e^- radius $\rightarrow r_e$
 Vertical beta function at IP $\rightarrow \beta_y^*$
 Reduction factors $\rightarrow R_L, R_{\xi y_{\pm}}$

- β_y^* is a function related to the transverse beam size along the beam trajectory

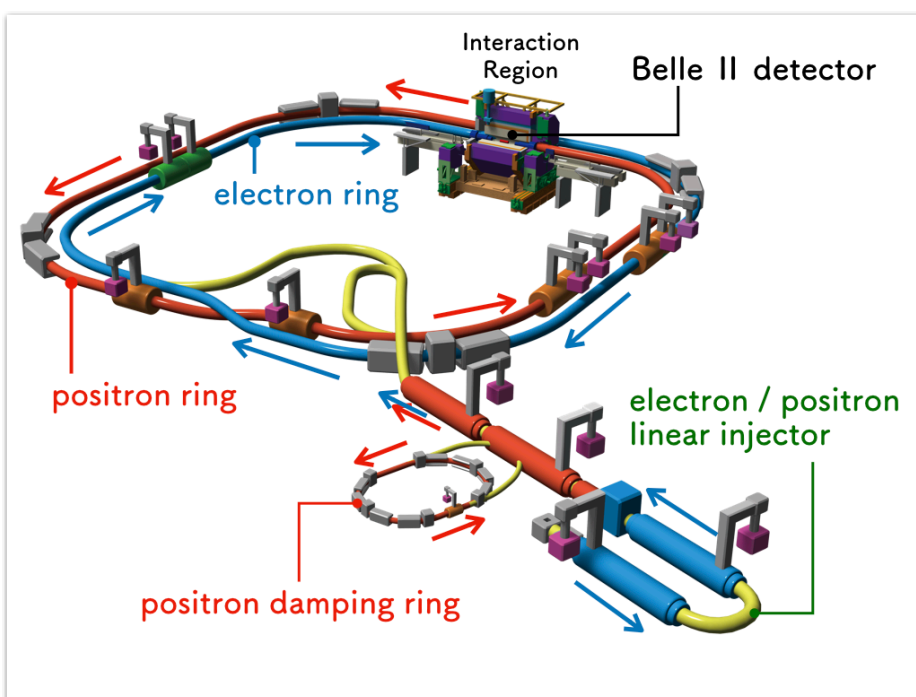
In comparison to KEKB

- β_y^* is reduced by 1/20
- Beam currents are doubled ($I_{e^-} = 2.60 \text{ A}$, $I_{e^+} = 3.60 \text{ A}$)
- Lesser asymmetry in beam energy is to reduce backgrounds ($E_{e^-} = 4.0 \text{ GeV}$, $E_{e^+} = 7.0 \text{ GeV}$)
- The crossing angle is quadrupled (83 mrad)

- Nano-beam scheme (Raimondi)



50 X more data than KEKB



The Belle II detector



- Belle II is a general purpose next generation 4π detector
- It is designed to withstand extreme luminosity
- Currently it is undergoing upgrade (LS1) to boost data-taking capability

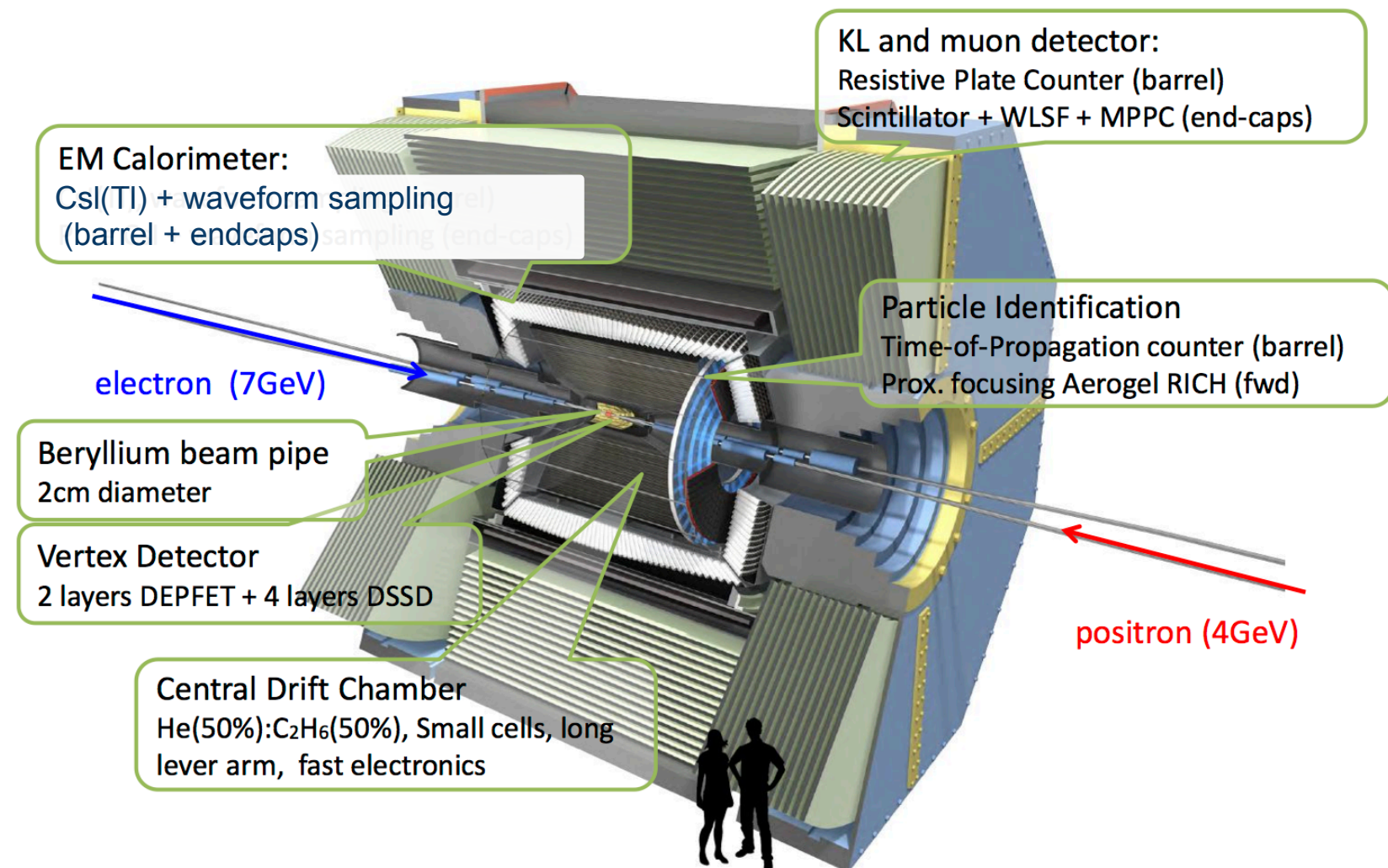
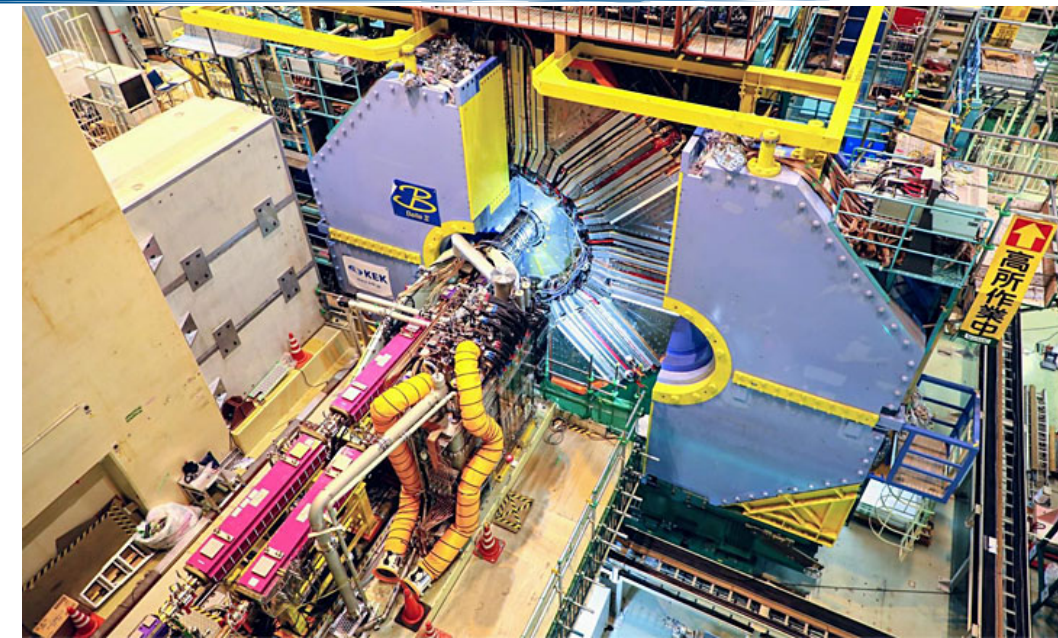
Belle II TDR (arXiv:1011.0352)

Improvements over Belle

- Addition of PXD to VXD with close proximity to IP improves vertex reconstruction
- Larger CDC with more sense wires
- Improvement in PID using Cherenkov imaging technique (TOP)
- Electronics improvement in the ECL
- Addition of inner layers to KLM

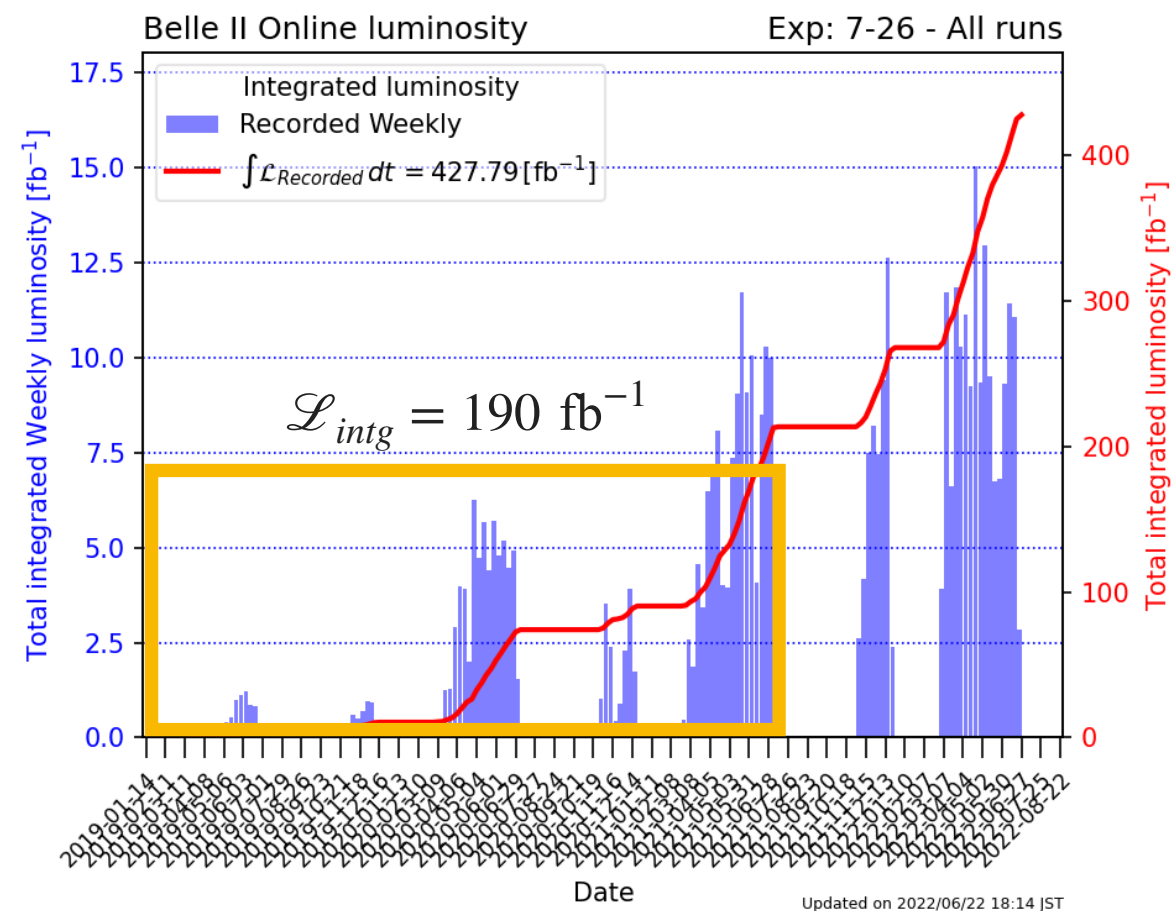
Other improvements

- New triggers introduced for dark matter searches
- Use of advanced analysis tools and techniques
- Optimal use of machine learning techniques

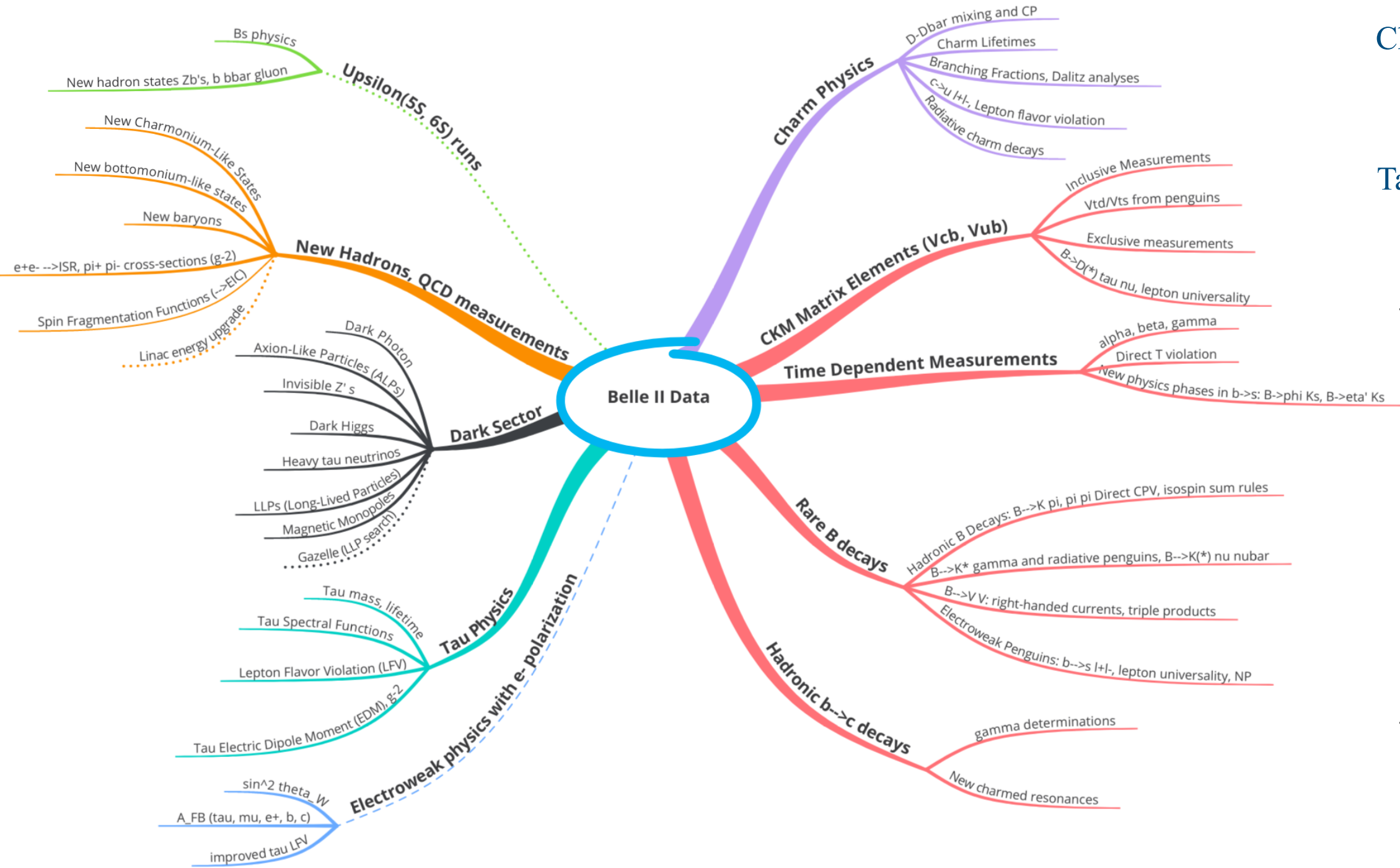


- Belle II collected data mainly at e^+e^- CM energy of 10.56 GeV
- This CM energy corresponds to the threshold production of $B\bar{B}$ events from $\Upsilon(4S)$ resonance

- Reached a world record of peak instantaneous luminosity of $4.71 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$
- Recorded total integrated luminosity of $\sim 424 \text{ fb}^{-1}$



Physics programs at Belle II



Charm lifetime measurements

Tagged and Untagged exclusive

$$|V_{cb}|, |V_{ub}|$$



- Isospin sum rule
- α/ϕ_2 measurement
- Three body TDCPV
- EW and Radiative
- LFU

Charm Lifetime measurements

Motivation to study charm

- Charm is the only up type quark whose hadronic weak decays can be analyzed, as the top quark decays much before it can hadronize
- Their lifetime (τ) measurements can be used to ‘test’ models explaining strong interactions in the charm sector.

$\approx 2.2 \text{ MeV}/c^2$ $\frac{2}{3}$ $\frac{1}{2}$ u up	$\approx 1.28 \text{ GeV}/c^2$ $\frac{2}{3}$ $\frac{1}{2}$ c charm	$\approx 173.1 \text{ GeV}/c^2$ $\frac{2}{3}$ $\frac{1}{2}$ t top
$\approx 4.7 \text{ MeV}/c^2$ $-\frac{1}{3}$ $\frac{1}{2}$ d down	$\approx 96 \text{ MeV}/c^2$ $-\frac{1}{3}$ $\frac{1}{2}$ s strange	$\approx 4.18 \text{ GeV}/c^2$ $-\frac{1}{3}$ $\frac{1}{2}$ b bottom

Spectator model term

Weak Annihilation, Pauli Interference term

$$\Gamma_{H_Q} = \Gamma_c \left[A_1 + \frac{A_2}{m_c^2} + \frac{A_3}{m_c^3} + \dots \right]$$

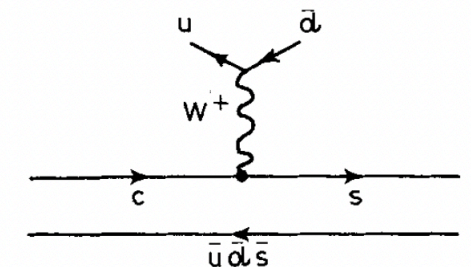
(Heavy Quark Expansion)

Lifetime differences among mesons and baryons

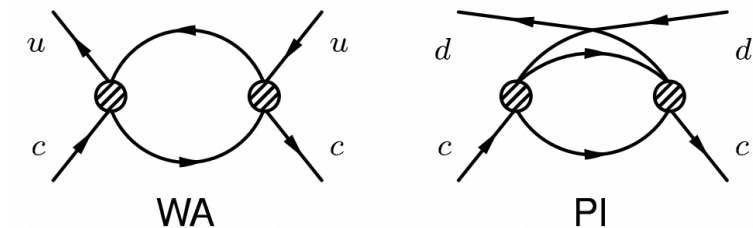
Take spectator quarks into account

$$\tau(D^+) > \tau(D_s^+) > \tau(\Xi_c^+) > \tau(D^0) > \tau(\Omega_c^0) > \tau(\Lambda_c^+) > \tau(\Xi_c^0)$$

$$(\tau = \hbar / \Gamma_{\text{total}})$$



- Precise τ measurements are used to calculate partial decay widths from experimentally measured decay fractions.
- Additionally, it can be used to extract Standard Model (SM) parameters ($|V_{cs}|, |V_{cd}|$)



Pre-Belle II status of charm lifetime measurements



Before 2000 (From theoretical predictions)

$$\tau(D^+) > \tau(D_s^+) > \tau(D^0) > \tau(\Xi_c^+) > \tau(\Lambda_c^+) > \tau(\Xi_c^0) > \tau(\Omega_c^0)$$

Before 2018 (From experimental measurements)

$$\tau(D^+) > \tau(D_s^+) > \tau(\Xi_c^+) > \tau(D^0) > \tau(\Lambda_c^+) > \tau(\Xi_c^0) > \tau(\Omega_c^0)$$

Hadron	Lifetimes (fs)	Experiment	Year
D^+	$1039.4 \pm 4.3 \pm 7.0$	FOCUS	2002
D_s^+	$506.4 \pm 3.0 \pm 1.7 \pm 1.7$	LHCb	2017
Ξ_c^+	$456.8 \pm 3.5 \pm 2.9 \pm 3.1$	LHCb	2019
D^0	$409.6 \pm 1.1 \pm 1.5$	FOCUS	2002
Ω_c^0	$268 \pm 24 \pm 10 \pm 2$	LHCb	2018
Λ_c^+	$203.5 \pm 1.0 \pm 1.3 \pm 1.4$	LHCb	2019
Ξ_c^0	$154.5 \pm 1.7 \pm 1.6 \pm 1.0$	LHCb	2019

After 2018 (From experimental measurements) (**Emerging**)

$$\tau(D^+) > \tau(D_s^+) > \tau(\Xi_c^+) > \tau(D^0) > \tau(\Omega_c^0) > \tau(\Lambda_c^+) > \tau(\Xi_c^0)$$

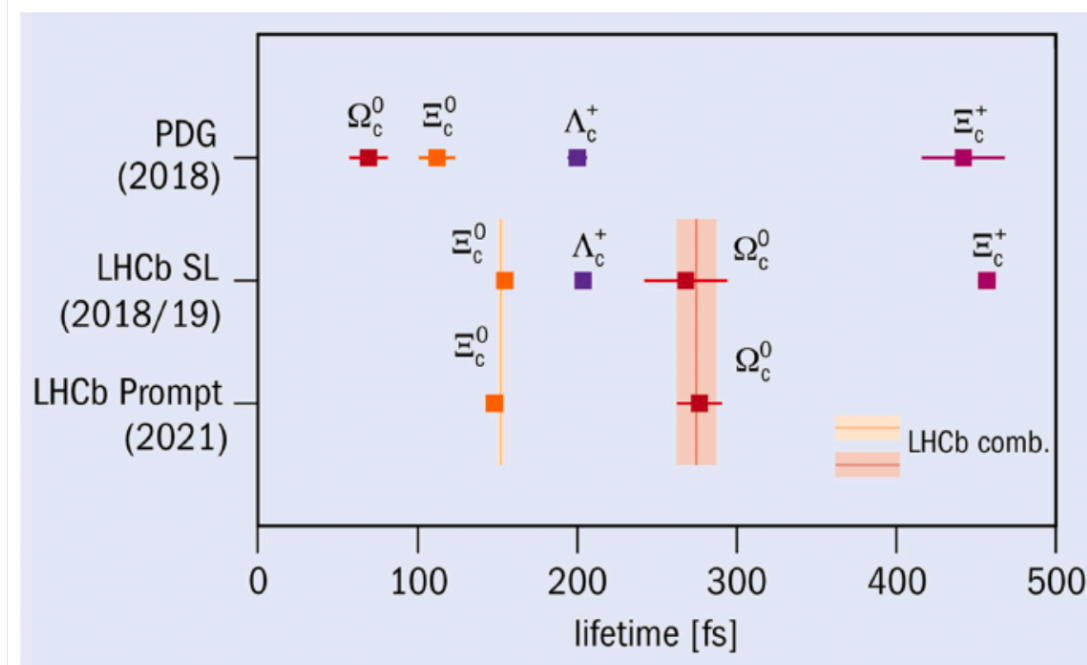
First uncertainty is stat., second is syst., third is due to $\tau(D^+)$

- D^0 and D^+ lifetime measurements are two decades old
- LHCb's measurements are relative and dominated by $\tau(D^+)$ uncertainties

Advantages at Belle II

- Large production cross-section of charm quarks, $\sigma_{c\bar{c}} \sim \sigma_{b\bar{b}}$
- Absolute measurement of lifetimes of all charm hadrons
- e^+e^- provides a 'clean' environment for reconstruction
- Better vertex resolution due to close proximity (1.4cm from IP) of the pixel detector in comparison to Babar and Belle

<https://cerncourier.com/a/new-charmed-baryon-lifetime-hierarchy-cast-in-stone>



Lifetime measurements of D^+ , D^0 , Λ_c^+ , Ω_c^0

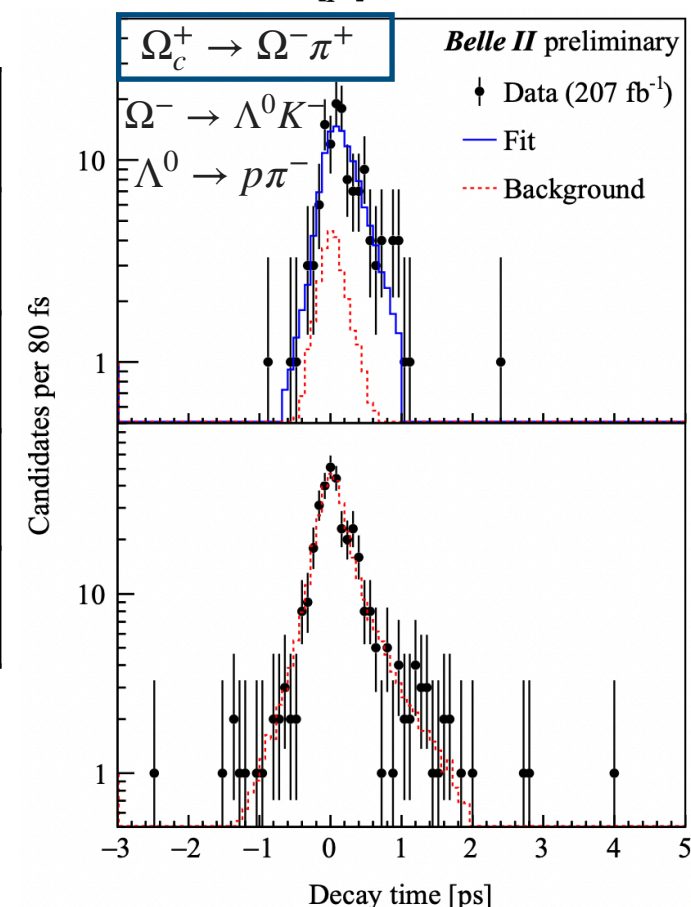
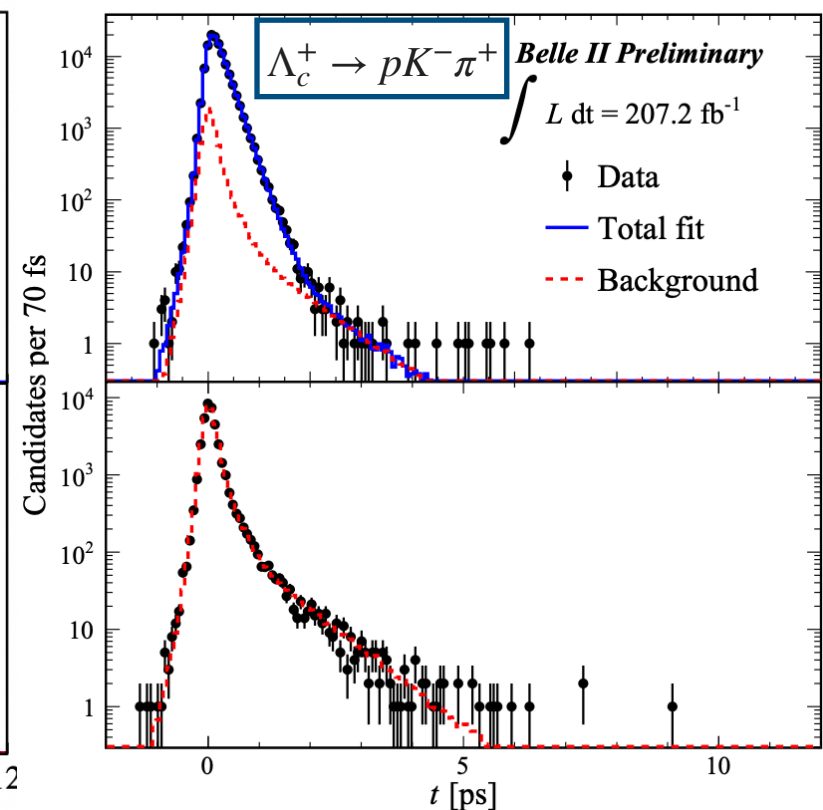
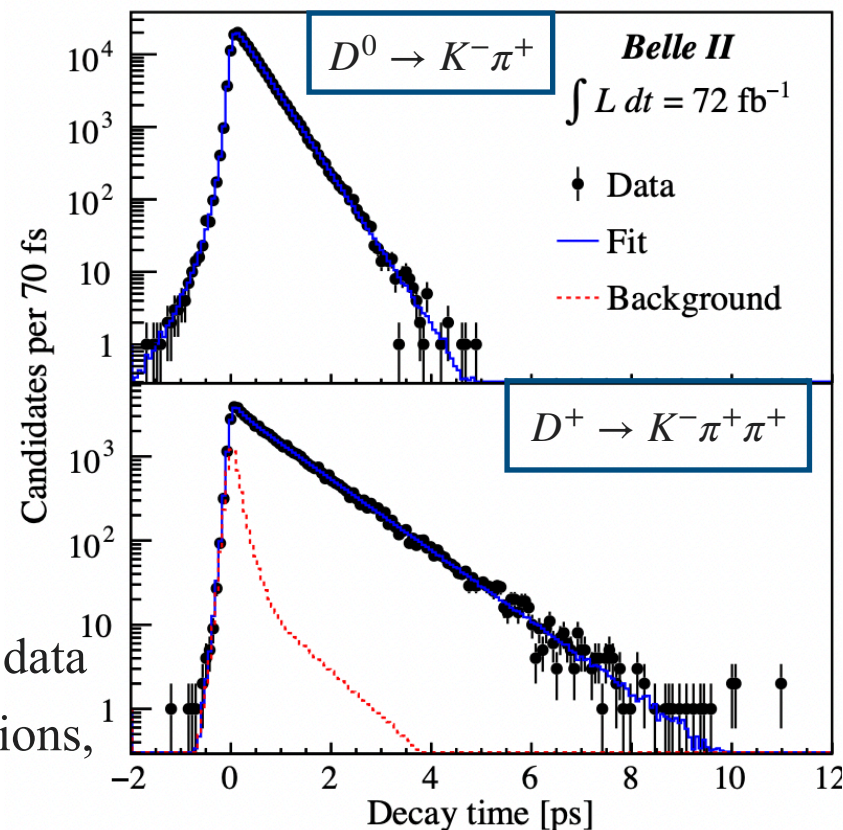


- The hadrons are considered from $e^+e^- \rightarrow c\bar{c}$ events produced near $\Upsilon(4S)$ resonance
- Lorentz boost provides the separation between the production and decay vertex (d)
- The decay time is calculated using,

$$t_H = \frac{m_H}{p^2} \vec{d} \cdot \vec{p}$$

mass
momentum

- Background shapes are determined using side-band data
- The lifetime is extracted from a fit to (t, σ_t) distributions, where σ_t is the uncertainty in t



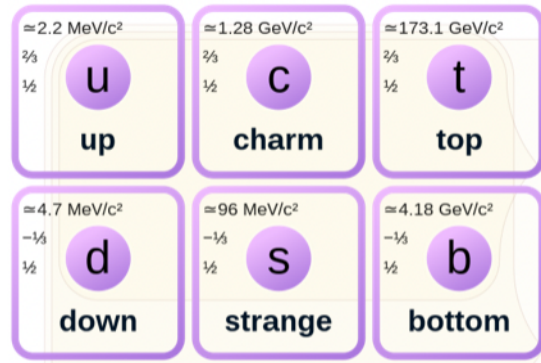
Hadron	Belle II (fs)	(fs)	References
D^+	$1030.4 \pm 4.7 \pm 3.1$	$1039.4 \pm 4.3 \pm 7.0$ (FOCUS)	PRL 127 211801 (2001)
D^0	$410.5 \pm 1.1 \pm 0.8$	$409.6 \pm 1.1 \pm 1.5$ (FOCUS)	“
Ω_c^0	$243 \pm 48 \pm 11$	$268 \pm 24 \pm 10 \pm 2$ (LHCb)	arXiv : 2208.08573v1 (PRD accepted)
Λ_c^+	$203.20 \pm 0.89 \pm 0.77$	$203.5 \pm 1.0 \pm 1.3 \pm 1.4$ (LHCb)	arXiv : 2206.15227v1 (PRL accepted)

World's precise measurement for D^+ , D^0 , Λ_c^+ lifetimes !

Confirms Ω_c^0 is not the shortest living charmed baryon !

$|V_{cb}|$ and $|V_{ub}|$ measurements

Cabibbo-Kobayashi-Maskawa (CKM) matrix



$$V_{\text{CKM}} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

Connecting weak and mass eigenstates

$$\sim \begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + \mathcal{O}(\lambda^4)$$

CPV

Wolfenstein parametrization

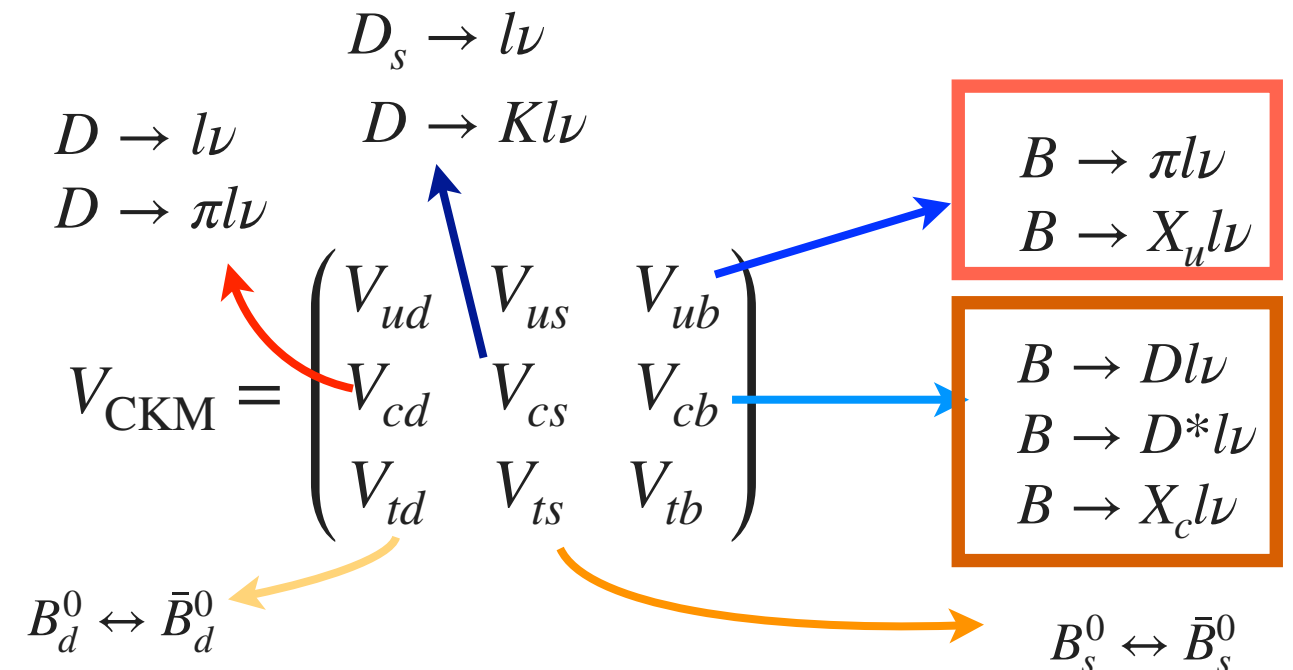
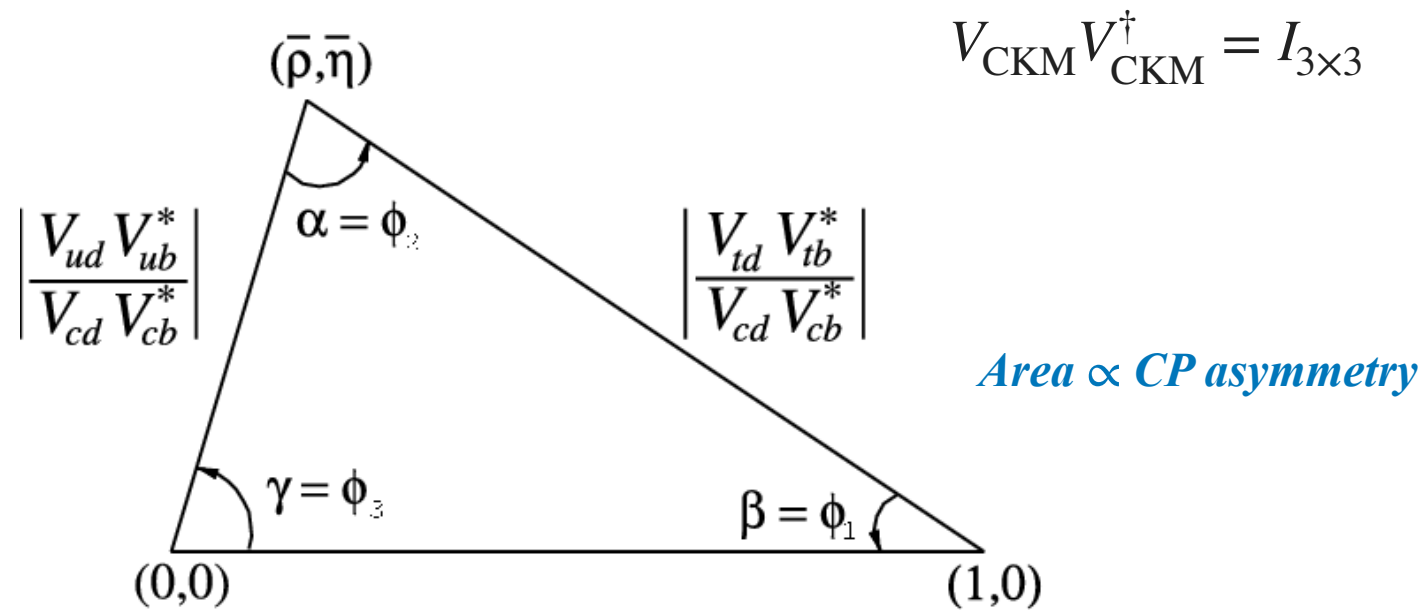
Quark transition	Physics	Experiments
$d \rightarrow u$	Nuclear β decay	PIBETA
$s \rightarrow u$	Kaon decays	KLOE, KTeV, NA62
$c \rightarrow d, s$	Charm decays	CLEO-c, Babar, Belle/Belle II, BESIII
$b \rightarrow u, c$	B decays	BaBar, Belle/Belle II, LHCb
$(t \rightarrow d, s)$		CDF, DØ
$t \rightarrow b$	Top decays	CDF, DØ, ATLAS, CMS

$$\lambda = |V_{us}| / \sqrt{|V_{ud}|^2 + |V_{us}|^2}$$

$$\bar{\rho} + i\bar{\eta} = -V_{ud}V_{ub}^*/V_{cd}V_{cb}^*$$

$$A\lambda^2 = \lambda |V_{cb}/V_{us}|$$

Measuring the sides of UT



Overconstrain the Unitarity Triangle by precisely measuring the sides and angles

Present status of $|V_{cb}|$ and $|V_{ub}|$ measurements



arXiv:2206.07501

Inclusive : Sum over all possible hadronic final states ($B \rightarrow X_{clu} l\nu$)

Exclusive : Consider a specific final state ($B \rightarrow (D/D^*/\pi) l\nu$)

These measurements are theoretically and experimentally independent !

Limitations

Knowledge of higher order perturbative and non-perturbative terms in HQE (Inclusive)

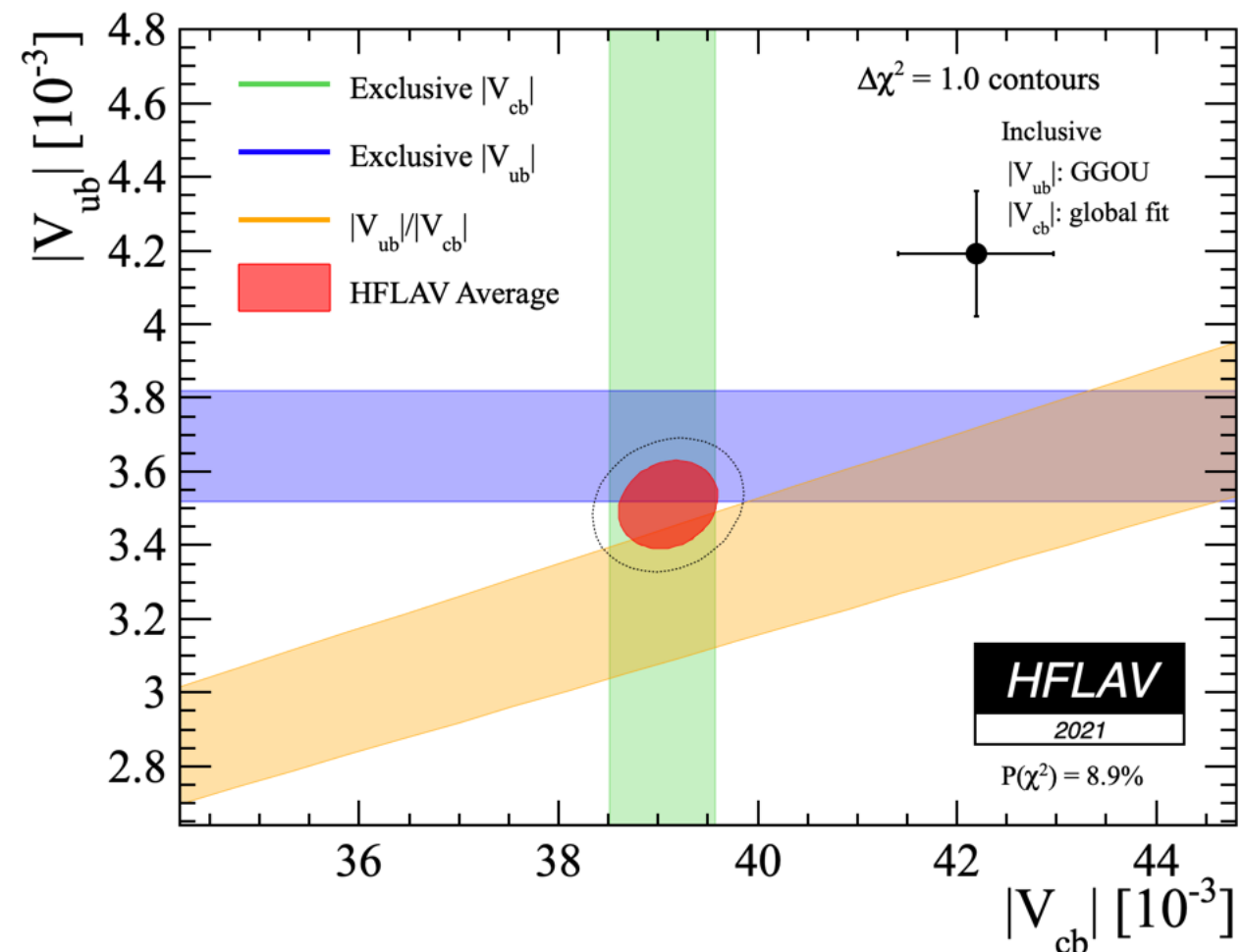
Knowledge of the hadronic form factors (Exclusive)

Complementary measurements are important !

Apart from, constraining the UT triangle,

- V_{cb} and V_{ub} values are determined from tree level processes, assuming no new physics (NP) contributions
- These values are then used to make SM predictions for loop level processes which are sensitive to new physics (NP)

Type	V_{cb}	V_{ub}
Inclusive	$(42.19 \pm 0.78) \times 10^{-3}$	$(4.19 \pm 0.17) \times 10^{-3}$
Exclusive	$(39.10 \pm 0.50) \times 10^{-3}$	$(3.51 \pm 0.12) \times 10^{-3}$
Deviation	3.3σ	3.3σ



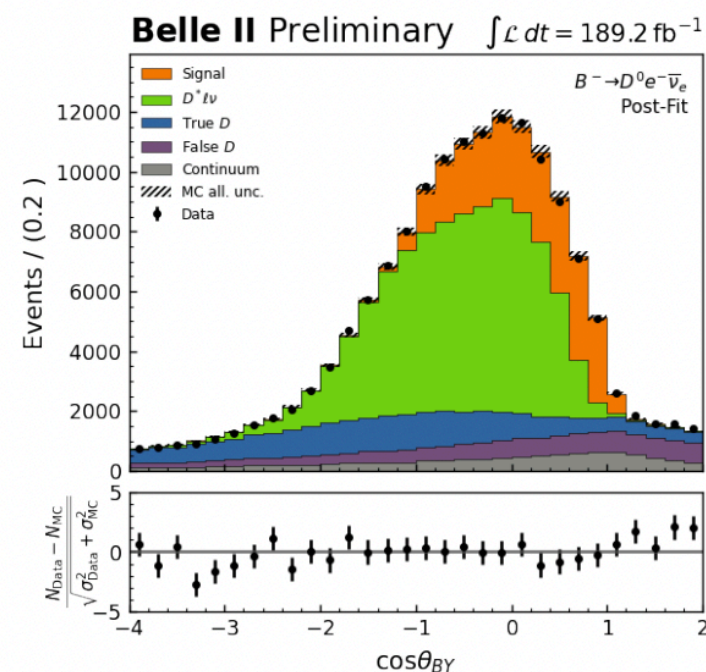
Untagged $|V_{cb}|$ measurement: $B \rightarrow Dl\nu$



Analysis strategy

- Signal: $B \rightarrow Dl\nu$ ($B^0 \rightarrow D^-l^+\nu, B^+ \rightarrow \bar{D}^0l^+\nu$)
- $D^- \rightarrow K^+\pi^-\pi^-, D^0 \rightarrow K^+\pi^-, l = e, \mu$
- Continuum is the dominant: Continuum Suppression
- Other backgrounds of concern are: other B decays, $B \rightarrow D^*l\nu$
- Use D^* veto to reject these backgrounds

Signal extraction: Angle between B and Dl ($\cos\theta_{BY}$)

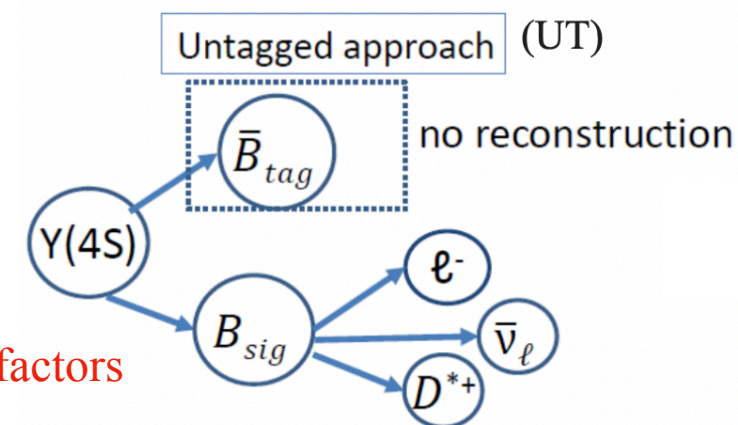


$$\frac{d\Gamma(B \rightarrow Dl\nu_\ell)}{dw} = \frac{G_F^2 m_D^3}{48\pi^3} (m_B + m_D)^2 (w^2 - 1)^{3/2} \eta_{EW}^2 \mathcal{G}^2(w) |V_{cb}|^2$$

product of 4-mom of B and D

Electroweak corrections

contain form factors



High efficiency/Low purity

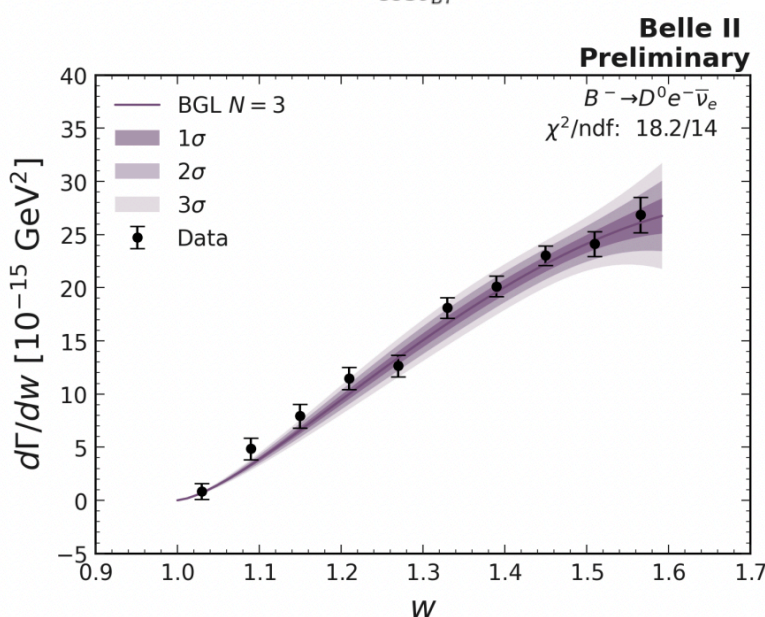
Extraction of $|V_{cb}|$

- The partial decay rates are extracted in bins of w by performing a combined fit to the BGL expression and QCD form factors

$$\eta_{EW} |V_{cb}| = (38.53 \pm 1.15) \times 10^{-3}$$

stat. + syst. + theoretical

Consistent with exclusive world average values !



Tagged $|V_{cb}|$ measurement: $B \rightarrow D^* l \nu$

- Signal: $B \rightarrow D^* l \nu$ ($B^0 \rightarrow D^{*-} l^+ \nu$)
- $D^{*-} \rightarrow \bar{D}^0 \pi^-, D^0 \rightarrow K^+ \pi^-, l = e, \mu$
- Reconstruction of low momentum pions from D^* is challenging
- FEI using HT algorithm to identify B_{tag} candidates

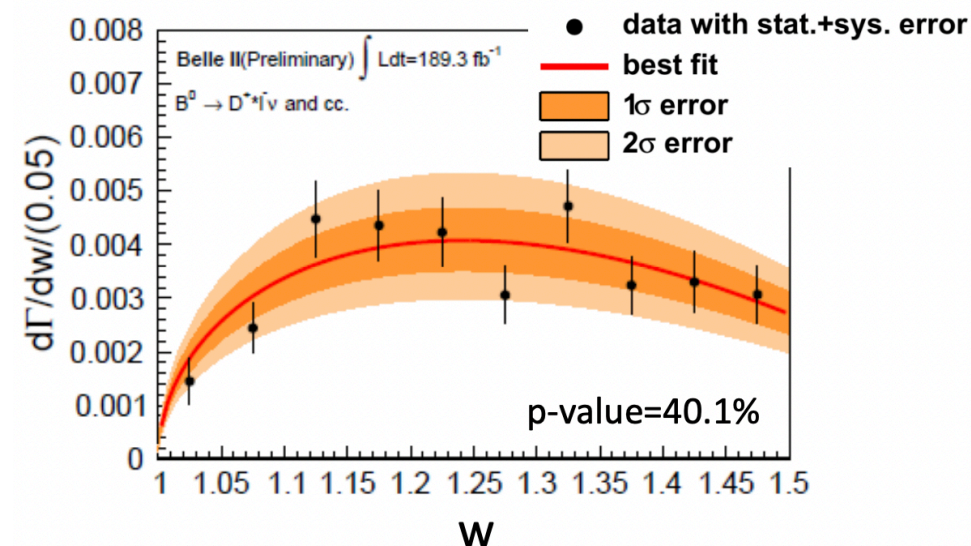
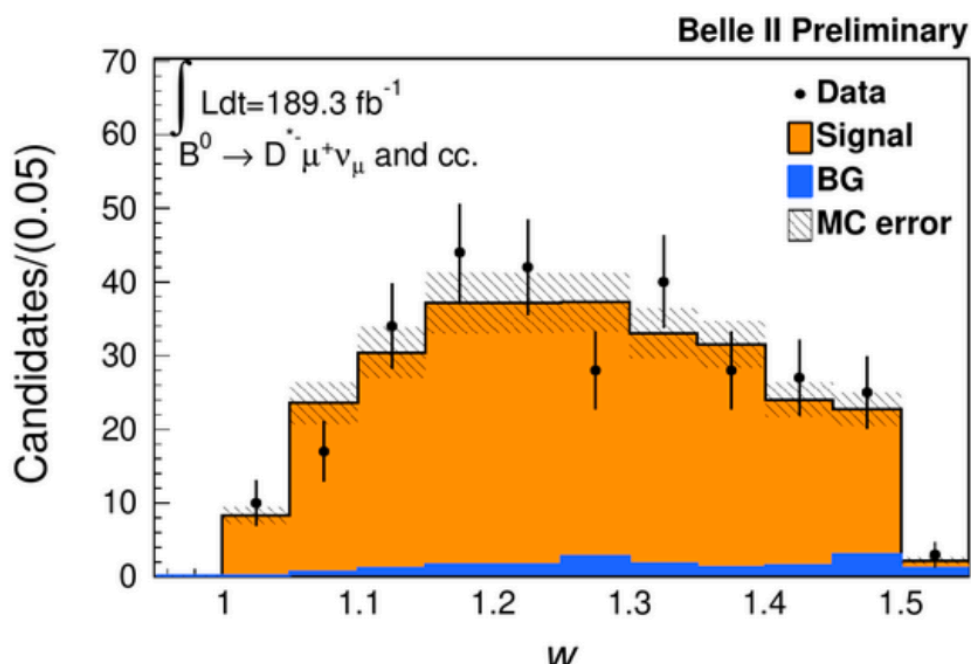
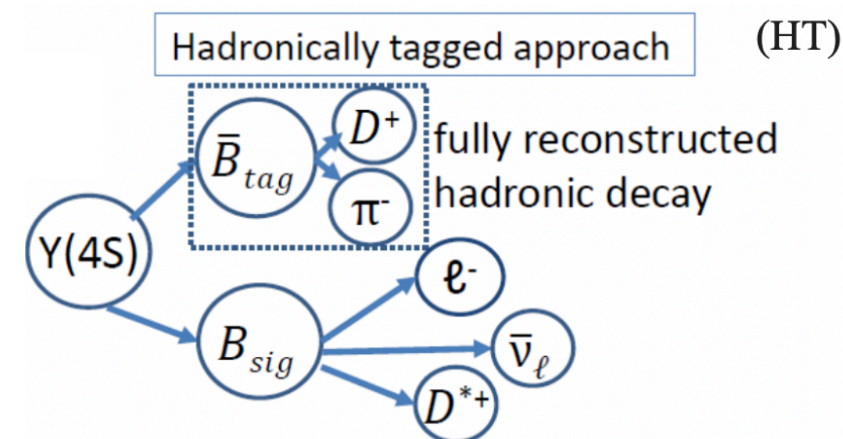
$$\frac{d\Gamma}{dw} = \frac{\eta_{EW}^2 G_F^2}{48\pi^3} m_{D^*}^3 (m_B - m_{D^*})^2 g(w) F^2(w) |V_{cb}|^2$$

product of 4-mom of B and D

Extraction of $|V_{cb}|$

- The partial decay rates are extracted in bins of w by performing a combined fit to the CLN expression and QCD form factors

Low efficiency/High purity



$$\eta_{EW} |V_{cb}| = (38.2 \pm 2.8) \times 10^{-3}$$

stat. + syst. + theoretical

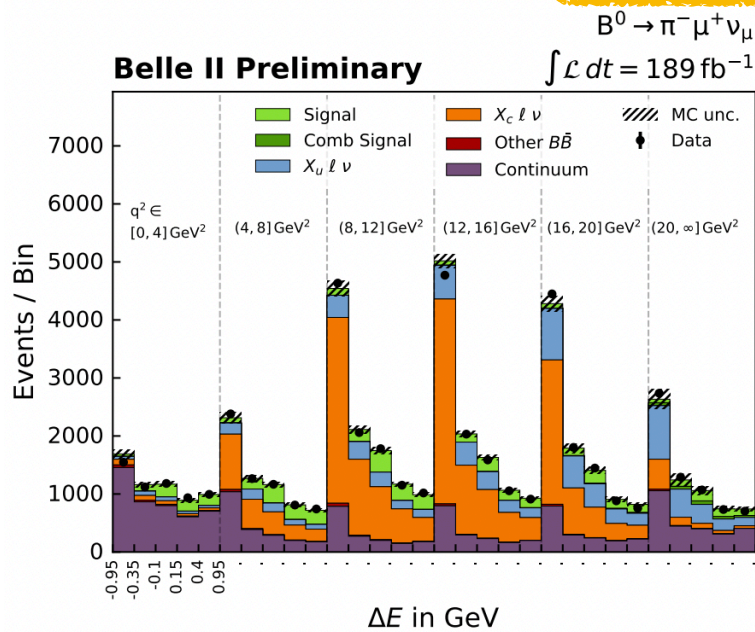
Consistent with exclusive world average values!

Untagged $|V_{ub}|$ measurement: $B \rightarrow \pi l \nu$



- Signal: $B \rightarrow \pi l \nu$ ($B^0 \rightarrow \pi^\pm l^\mp \nu$), $l = e, \mu$
- Everything else including the other B is included as the rest-of-events to determine p_ν
- Continuum is the dominant: Continuum Suppression (BDT)
- Other backgrounds of concern are: other B

Signal extraction: $M_{bc} = \sqrt{E_{\text{beam}}^{*2} - p_B^{*2}}$ and $\Delta E = E_B^* - E_{\text{beam}}^*$



$$\frac{d\Gamma(B \rightarrow \pi l \nu)}{dq^2} = \frac{G_F^2 |V_{ub}|^2}{24\pi^3} |p_\pi|^3 |f_+(q^2)|^2$$

$M(l\bar{l})$ form factor

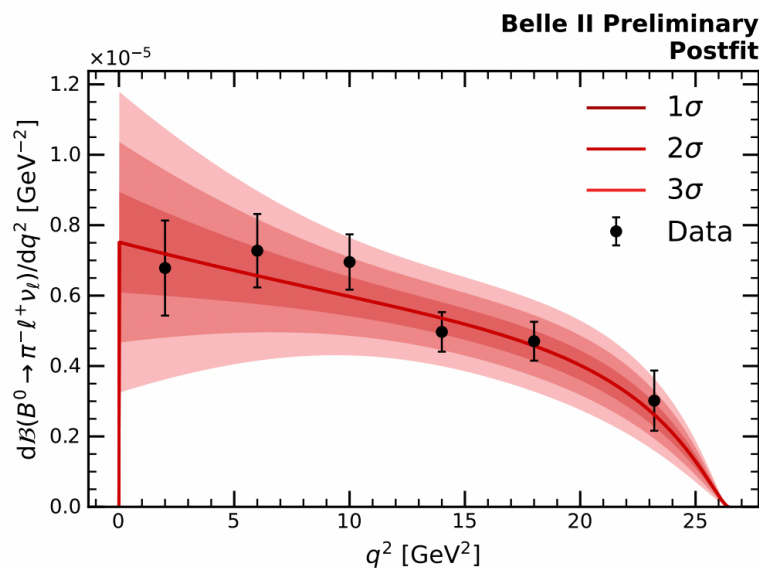
Extraction of $|V_{ub}|$

- The partial decay rates are extracted in bins of q^2 by performing a combined fit to the BCL expression and QCD form factor

ICHEP 2022

$$|V_{ub}|_{B^0 \rightarrow \pi^- l^+ \nu_l} = (3.54 \pm 0.12_{\text{stat.}} \pm 0.15_{\text{syst.}} \pm 0.16_{\text{theo.}}) \times 10^{-3}$$

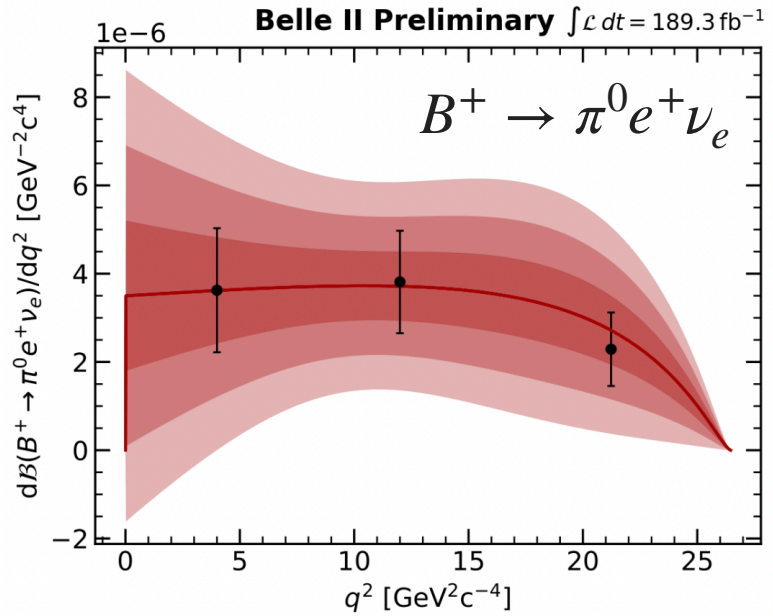
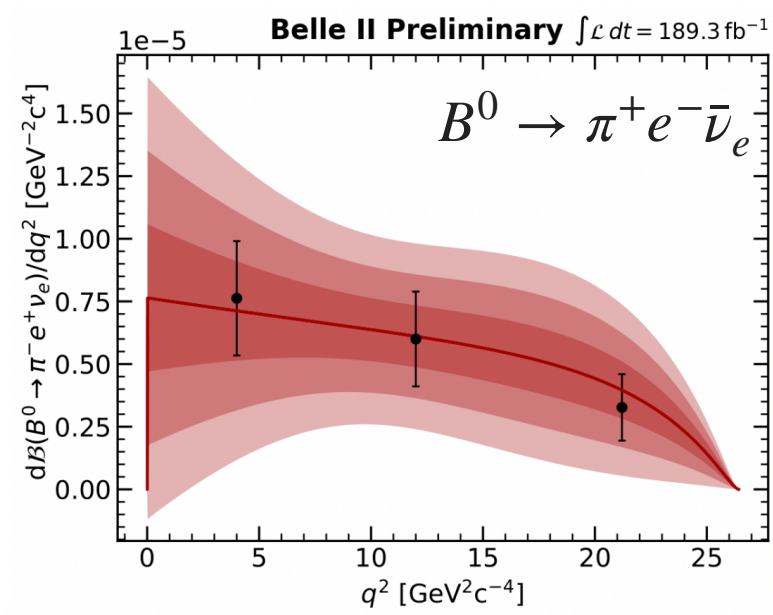
Consistent with exclusive world average values !



Tagged $|V_{ub}|$ measurement: $B \rightarrow \pi e \nu$



- Signal: $B \rightarrow \pi e \nu$ ($B^0 \rightarrow \pi^+ e^- \bar{\nu}_e, B^+ \rightarrow \pi^0 e^+ \nu_e$)
- FEI using HT algorithm to identify B_{tag} candidates
- MC simulations are considered for background studies
- Cross-feeds: $B^0 \rightarrow \rho^- l^+ \nu_l$
- Continuum backgrounds, generic $B\bar{B}$, and $B \rightarrow X_u l \nu$



Signal extraction: $M_{\text{miss}}^2 \equiv p_{\text{miss}}^2 = (p_{B_{\text{sig}}} - p_{e\pi})^2$

$$\frac{d\Gamma(B \rightarrow \pi l \nu)}{dq^2} = \frac{G_F^2 |V_{ub}|^2}{24\pi^3} |p_\pi|^3 |f_+(q^2)|^2$$

\swarrow $M(\bar{l})$ \searrow contain form factors

Extraction of $|V_{cb}|$

- The partial decay rates are extracted in bins of q^2 by performing a combined fit to the BCL expression and QCD form factors

arXiv:2206.08102

$|V_{ub}| = (3.88 \pm 0.45) \times 10^{-3}$

stat. + syst. + theoretical

Consistent with exclusive world average values !

u	c	t
d	s	b

$$b \not\rightarrow c$$

$$BF \leq (10^{-5})$$

Quark transition	Remarks
$b \rightarrow u$	Tree level (but suppressed) via u, c, t, X
$b \rightarrow d$	
$b \rightarrow s$	

Why go charmless ?

- Good place to look for non-SM physics (in general)
- Verify Isospin sum rule
- Determination of Φ_2 / α
- Measure CP asymmetry

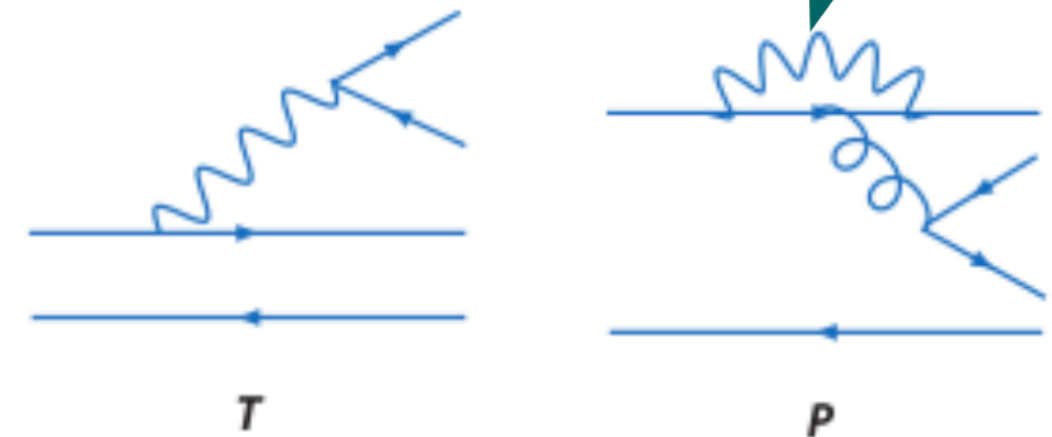


charmless Physics goals

Belle II can access all of these !

Ways of going charmless ?

- Two body decays ($B \rightarrow \pi\pi, B \rightarrow K\pi$)
- Quasi-two body decays ($B \rightarrow \rho\pi, B \rightarrow \rho\rho$)
- Multibody body decays ($B \rightarrow KKK$)



Two and three body B decay First reconstructions/ measurements at Belle II

Isospin sum rule in $K\pi$ decay channels

Assuming isospin symmetry in the dominant Feynman diagrams (QCD penguin),

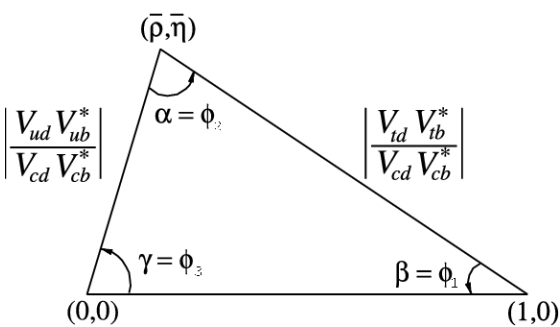
$$\Gamma(K^+\pi^-) \approx \Gamma(K^0\pi^+) \approx 2\Gamma(K^+\pi^0) \approx 2\Gamma(K^0\pi^0)$$

$$\mathcal{A}_{\text{CP}}(K^+\pi^-) + \mathcal{A}_{\text{CP}}(K^0\pi^+) \approx \mathcal{A}_{\text{CP}}(K^+\pi^0) + \mathcal{A}_{\text{CP}}(K^0\pi^0)$$

In SM, $I_{K\pi} = 0$

Isospin sum rule in terms of CP asymmetries

$$I_{K\pi} = \mathcal{A}_{K^+\pi^-} + \mathcal{A}_{K^0\pi^+} \frac{\mathcal{B}(K^0\pi^+)}{\mathcal{B}(K^+\pi^-)} \frac{\tau_{B^0}}{\tau_{B^+}} - 2\mathcal{A}_{K^+\pi^0} \frac{\mathcal{B}(K^+\pi^0)}{\mathcal{B}(K^+\pi^-)} \frac{\tau_{B^0}}{\tau_{B^+}} - 2\mathcal{A}_{K^0\pi^0} \frac{\mathcal{B}(K^0\pi^0)}{\mathcal{B}(K^+\pi^-)}$$



Determination of α/ϕ_2 using $\pi\pi$ decay channels

Extraction of α/ϕ_2 is complicated by the presence of tree and penguin diagrams.

- To disentangle them, an isospin analysis is necessary which requires precision measurement of the \mathcal{B} and CP asymmetry.

Direct CP asymmetry determination using three body decays

- Dalitz decays are useful to understand the relative contribution of tree and penguin amplitudes.
- Moreover, they are good places to look for direct CP asymmetries.

Belle II provides unique opportunity to measure all these decays consistently !

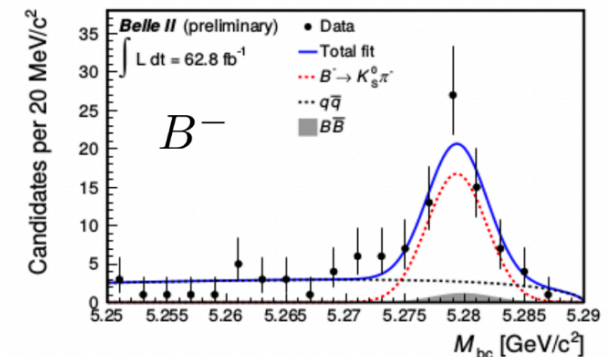
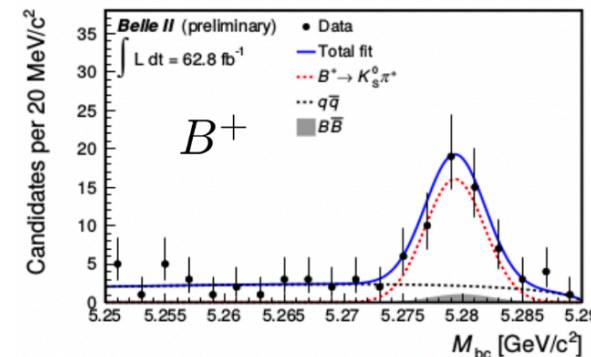
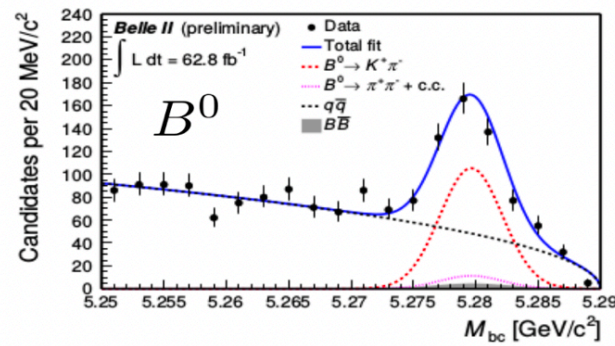
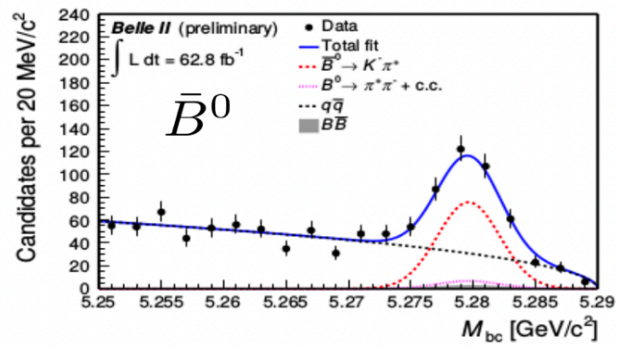
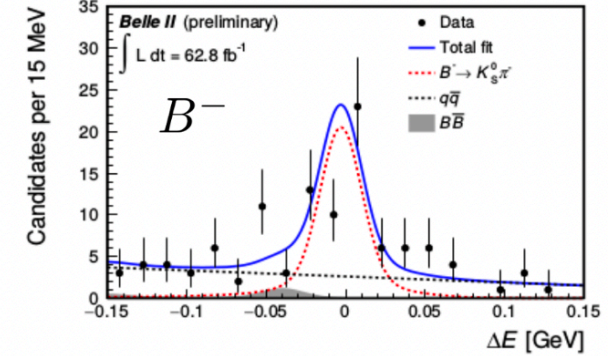
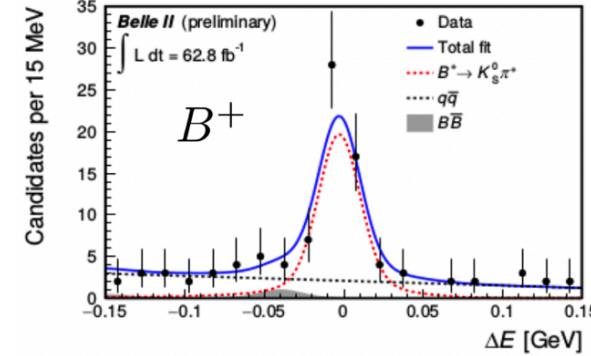
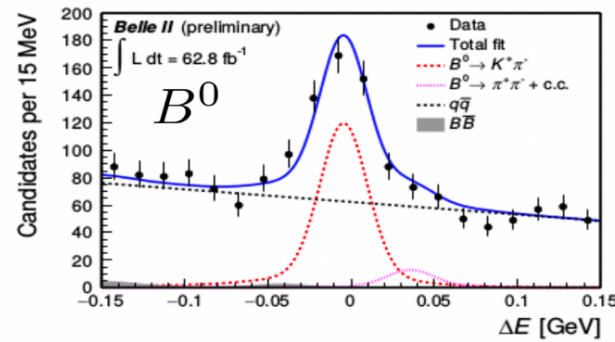
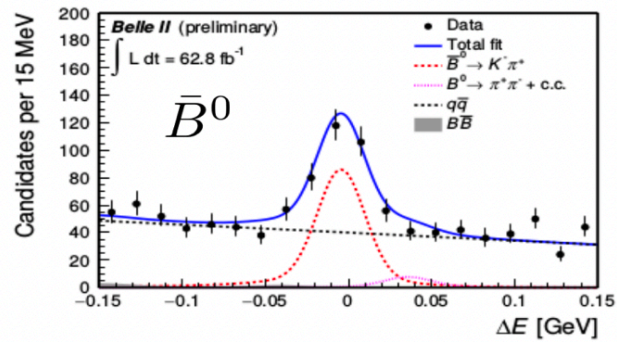
Isospin analysis

Isospin sum rule : $B^0 \rightarrow K^+\pi^-$ and $B^+ \rightarrow K^0\pi^+$

62.8 fb⁻¹

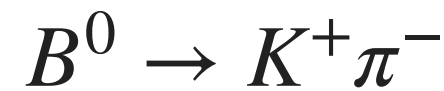


$$I_{K\pi} = \mathcal{A}_{K^+\pi^-} + \mathcal{A}_{K^0\pi^+} \frac{\mathcal{B}(K^0\pi^+)}{\mathcal{B}(K^+\pi^-)} \frac{\tau_{B^0}}{\tau_{B^+}} - 2\mathcal{A}_{K^+\pi^0} \frac{\mathcal{B}(K^+\pi^0)}{\mathcal{B}(K^+\pi^-)} \frac{\tau_{B^0}}{\tau_{B^+}} - 2\mathcal{A}_{K^0\pi^0} \frac{\mathcal{B}(K^0\pi^0)}{\mathcal{B}(K^+\pi^-)}$$



arXiv:2106.03766v1

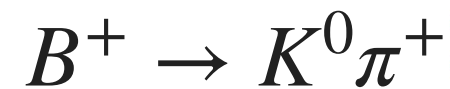
PRD 69, 111102 (2004)



Quantity	Belle II [69M $B\bar{B}$]	Belle [85M $B\bar{B}$]
\mathcal{B}	$(18.0 \pm 0.9(\text{stat.}) \pm 0.9(\text{syst.})) \times 10^{-6}$	$(18.5 \pm 1.0(\text{stat.}) \pm 0.7(\text{syst.})) \times 10^{-6}$
\mathcal{A}	$-0.16 \pm 0.05(\text{stat.}) \pm 0.01(\text{syst.})$	—

arXiv:2106.03766v1

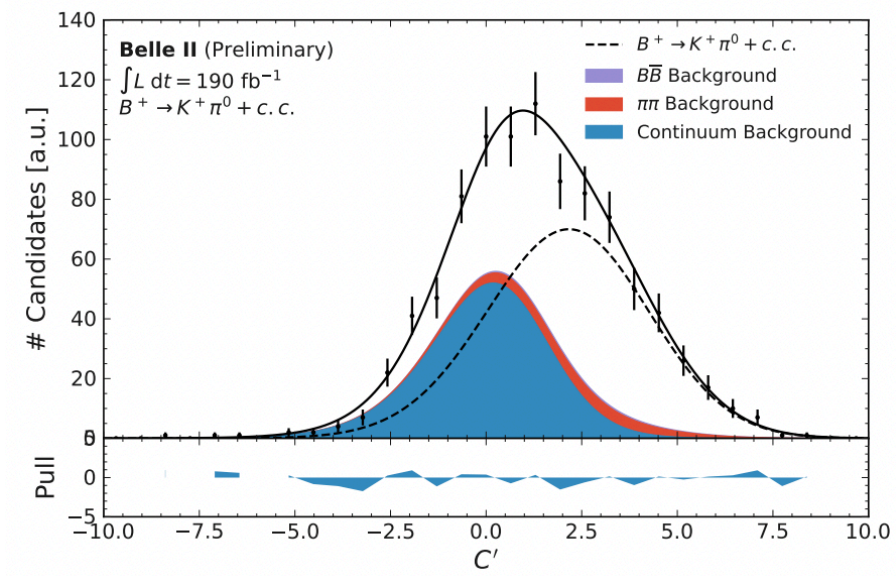
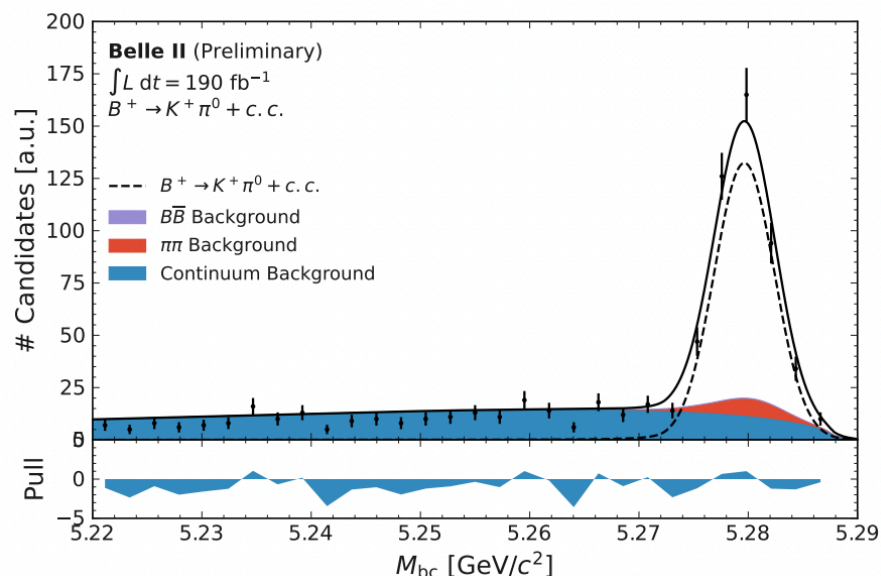
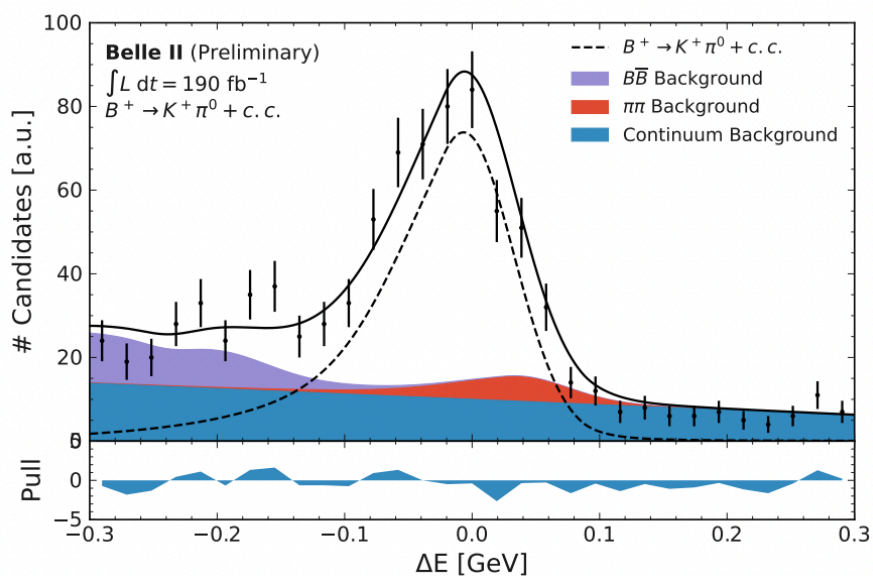
PRD 69, 111102 (2004)



Quantity	Belle II [69M $B\bar{B}$]	Belle [85M $B\bar{B}$]
\mathcal{B}	$(21.4^{+2.3}_{-2.2}(\text{stat.}) \pm 1.6(\text{syst.})) \times 10^{-6}$	$(22.0 \pm 1.9(\text{stat.}) \pm 1.1(\text{syst.})) \times 10^{-6}$
\mathcal{A}	$-0.01 \pm 0.08(\text{stat.}) \pm 0.05(\text{syst.})$	—

Consistent with previous Belle measurement

$$I_{K\pi} = \mathcal{A}_{K^+\pi^-} + \mathcal{A}_{K^0\pi^+} \frac{\mathcal{B}(K^0\pi^+) \tau_{B^0}}{\mathcal{B}(K^+\pi^-) \tau_{B^+}} - 2\mathcal{A}_{K^+\pi^0} \frac{\mathcal{B}(K^+\pi^0) \tau_{B^0}}{\mathcal{B}(K^+\pi^-) \tau_{B^+}} - 2\mathcal{A}_{K^0\pi^0} \frac{\mathcal{B}(K^0\pi^0)}{\mathcal{B}(K^+\pi^-)}$$



- An updated measurement with a better fit strategy : 3D fit
- Validation of analysis procedure: $B^0 \rightarrow \bar{D}(\rightarrow K^+\pi^-)\pi^0$
- Use of off-resonance data and control mode: shift and scaling parameter

$$\mathcal{A}_{CP} = \frac{N(B^+) - N(B^-)}{N(B^+) + N(B^-)}$$

arXiv:2209.05154

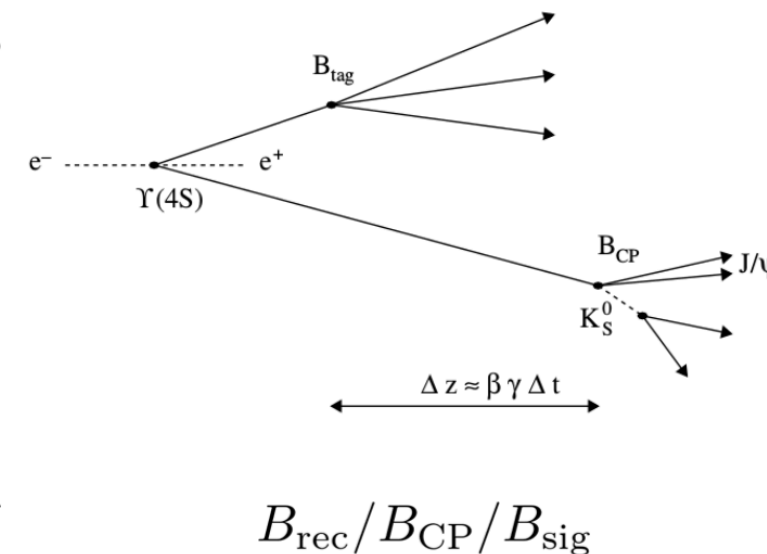
PRL 99 121601 (2007)

Parameter	Belle II (~197 M BB pairs)	Belle (449 M BB pairs)
$\mathcal{B}(B^+ \rightarrow K^+\pi^0)$	$(14.30 \pm 0.69 \pm 0.79) \times 10^{-6}$	$(12.4 \pm 0.5 \pm 0.6) \times 10^{-6}$
\mathcal{A}_{CP}	$0.014 \pm 0.047 \pm 0.010$	-

First uncertainty: stat.; second: syst.

Within 1.5σ of the previous Belle result even with 2.3 times less statistics

- B_{tag} is reconstructed from (after applying selection criteria in ROE events) inclusive B decays.
- They are so chosen that the flavor of the B_{tag} (B or \bar{B}) can be determined. Eg. $B^0 \rightarrow X^- l^+ \nu$
- They are not 100% efficient in correctly identifying the flavor of B_{tag} .
- Hence, dilution factors are introduced to quantify the mistag probability (w).

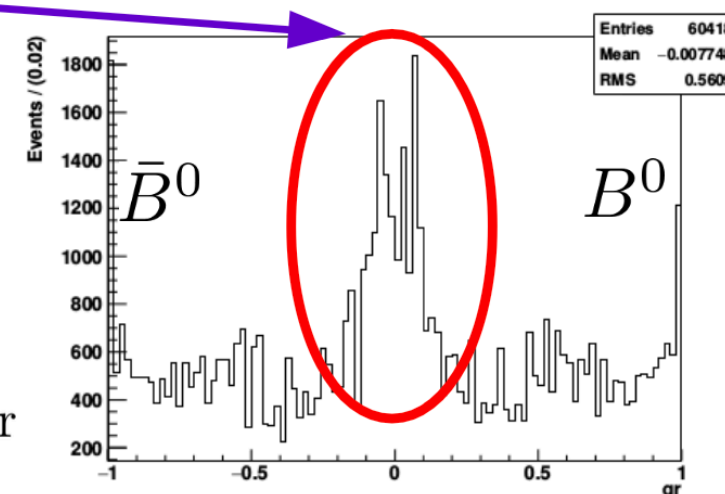


Output of the Flavor Tagger

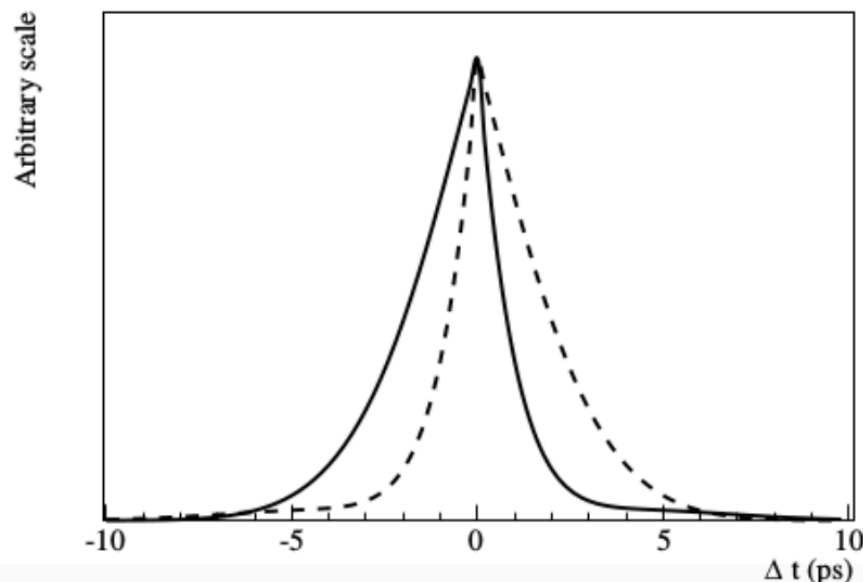
$$q \in [+1(B^0), -1(\bar{B}^0)]$$

$$r = (1 - 2w)$$

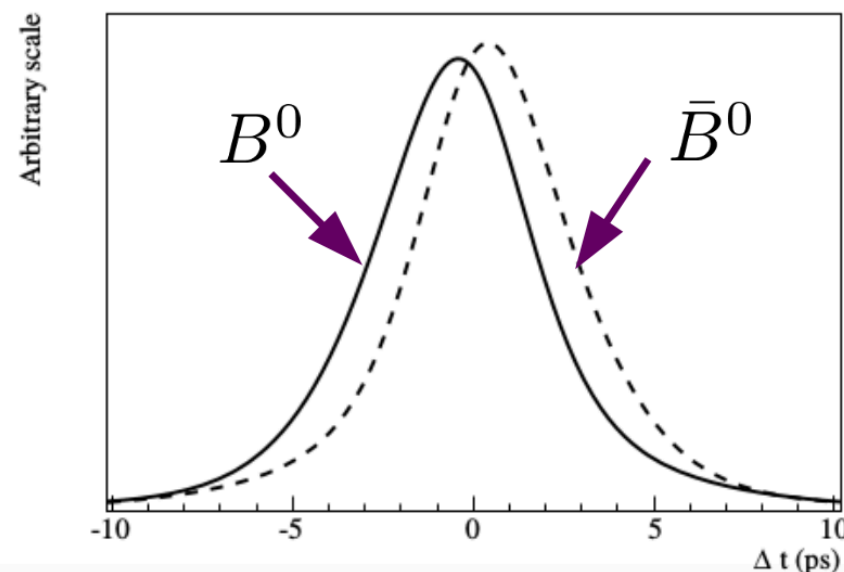
No flavor info.



Perfect reconstruction



Resolution effects + Dilution factor



EPJ C 82 4 (2007)

$$\epsilon_{\text{eff}} = (28.8 \pm 1.2 \text{ (stat.)} \pm 0.4 \text{ (syst.)}) \%$$

Isospin sum rule : $B^0 \rightarrow K^0 \pi^0$

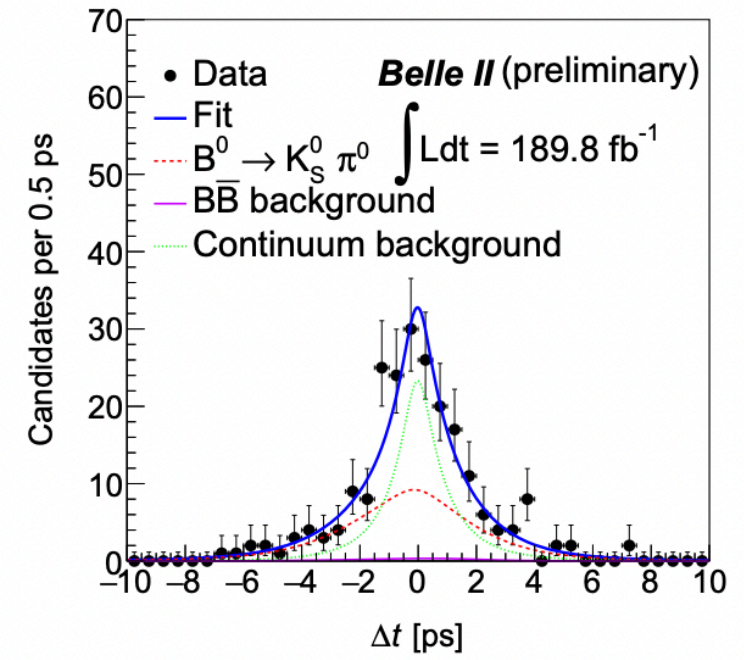
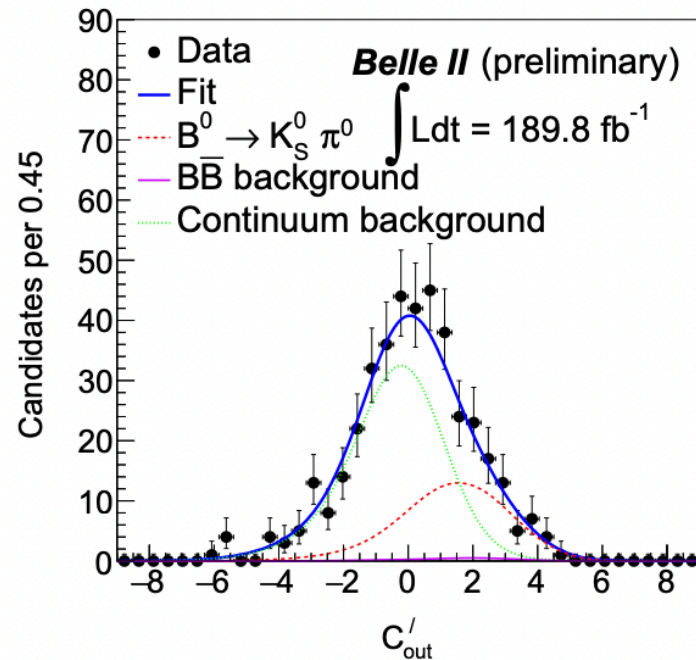
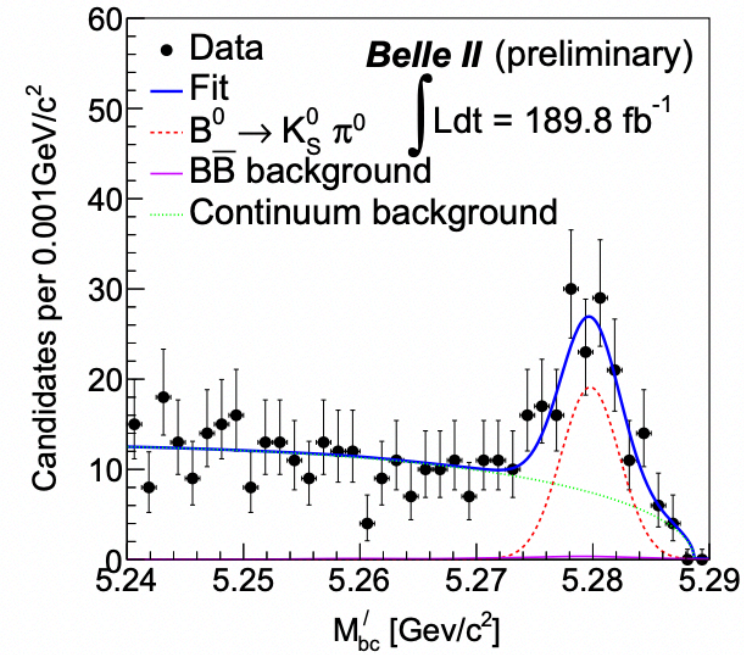
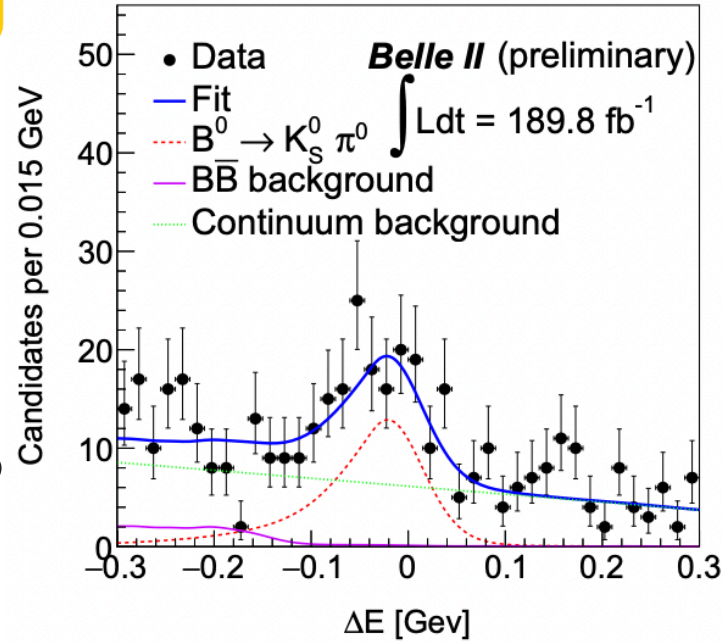
190 fb⁻¹



$$I_{K\pi} = \mathcal{A}_{K^+\pi^-} + \mathcal{A}_{K^0\pi^+} \frac{\mathcal{B}(K^0\pi^+) \tau_{B^0}}{\mathcal{B}(K^+\pi^-) \tau_{B^+}} - 2\mathcal{A}_{K^+\pi^0} \frac{\mathcal{B}(K^+\pi^0) \tau_{B^0}}{\mathcal{B}(K^+\pi^-) \tau_{B^+}} - 2\mathcal{A}_{K^0\pi^0} \frac{\mathcal{B}(K^0\pi^0)}{\mathcal{B}(K^+\pi^-)}$$

- Fit strategy: 4D fit
- Challenging $B^0 \rightarrow K_s^0 \pi^0$ decay vertex reconstruction
- Continuum is the dominant background
- Use of Belle II flavor tagging algorithm to measure Δt to enhance the sensitivity to \mathcal{A}_{CP}
- First measurement of \mathcal{A}_{CP} in $B^0 \rightarrow K_s^0 \pi^0$ to use time-dependent analysis.

arXiv: 2206.07453v1



Consistent with previous Belle measurement !

Experiment	Values
Belle II (197 M BB pairs)	$\mathcal{B} = (11.0 \pm 1.2 \pm 1.0) \times 10^{-6}$ $\mathcal{A}_{CP} = -0.41^{+0.30}_{-0.32} \pm 0.09$
Belle (449 M BB pairs)	$\mathcal{B} = (9.2 \pm 0.7 \pm 0.6) \times 10^{-6}$

First uncertainty: stat.; second: syst.

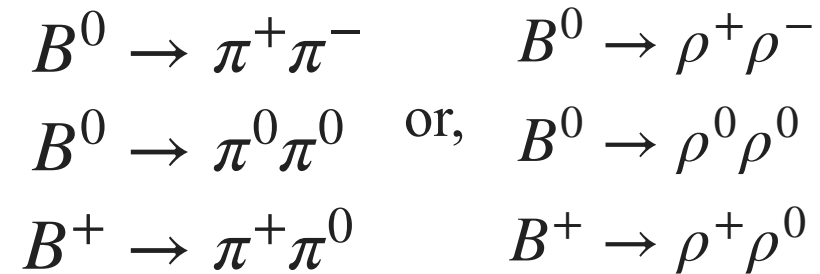
PRL 99 121601 (2007)

α/ϕ_2 determination

α/ϕ_2 determination: $B \rightarrow \pi\pi$ / $B \rightarrow \rho\rho$



- Target: Measurement of \mathcal{B} and \mathcal{A}_{CP}
- Process mediates via $b \rightarrow u$ diagrams
- Interference between ‘tree’ and ‘penguin’ diagrams



- Multivariate analysis to suppress continuum
- 3D signal extraction function
- Validation of analysis procedure: $B^+ \rightarrow \bar{D}(\rightarrow K^+\pi^-\pi^0)\pi^+$

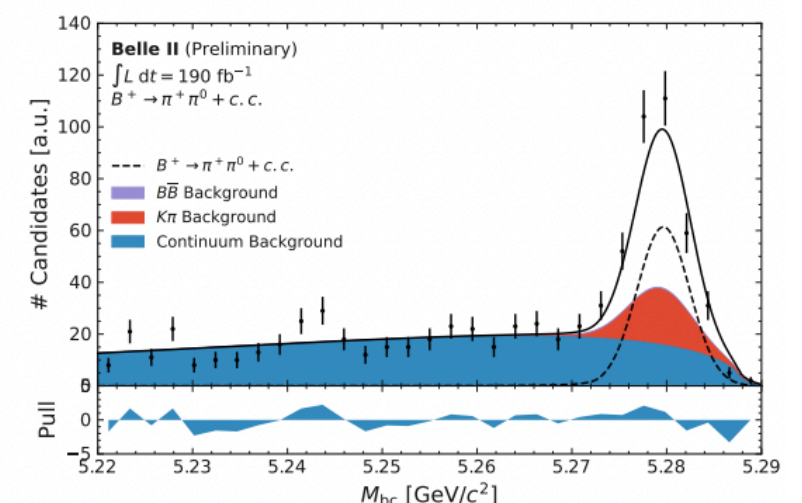
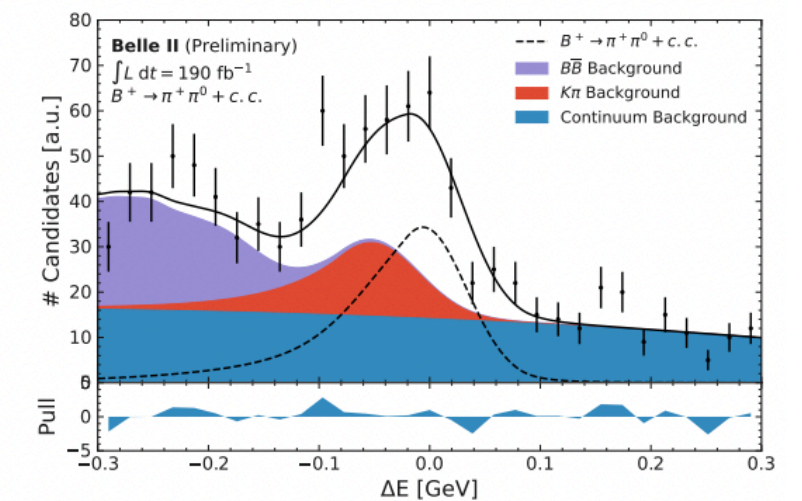
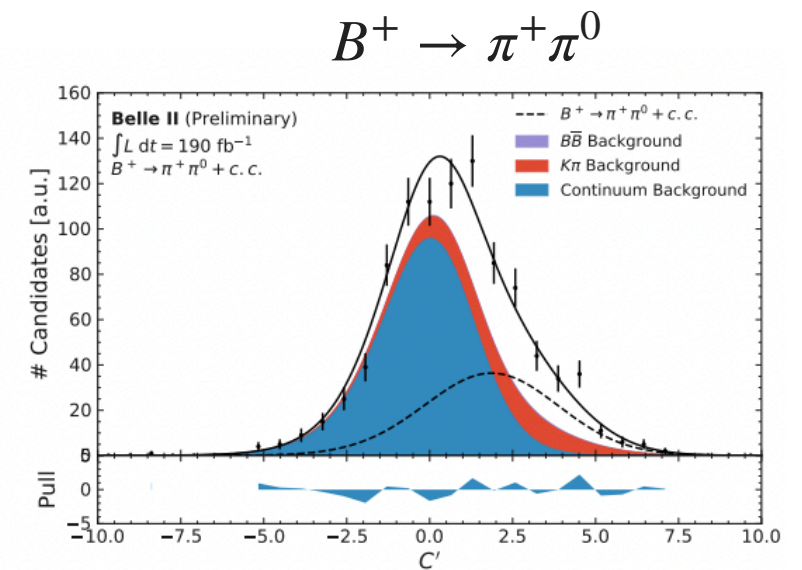
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PRL 99 121601 (2007)

Parameter	Belle II (~197 M BB pairs)	Belle (449 M BB pairs)
$\mathcal{B}(B^+ \rightarrow \pi^+\pi^0)$	$(6.12 \pm 0.53 \pm 0.53) \times 10^{-6}$	$(6.5 \pm 0.4 \pm 0.4) \times 10^{-6}$
\mathcal{A}_{CP}	$-0.085 \pm 0.085 \pm 0.019$	-

First uncertainty: stat.; second: syst.

Consistent with previous Belle measurement !



α/ϕ_2 determination: $B^0 \rightarrow \pi^0\pi^0$

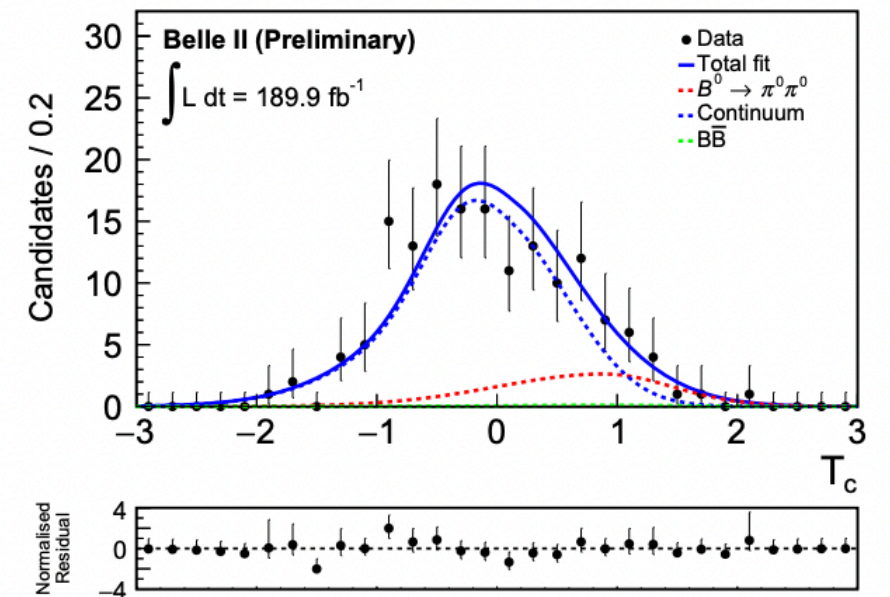
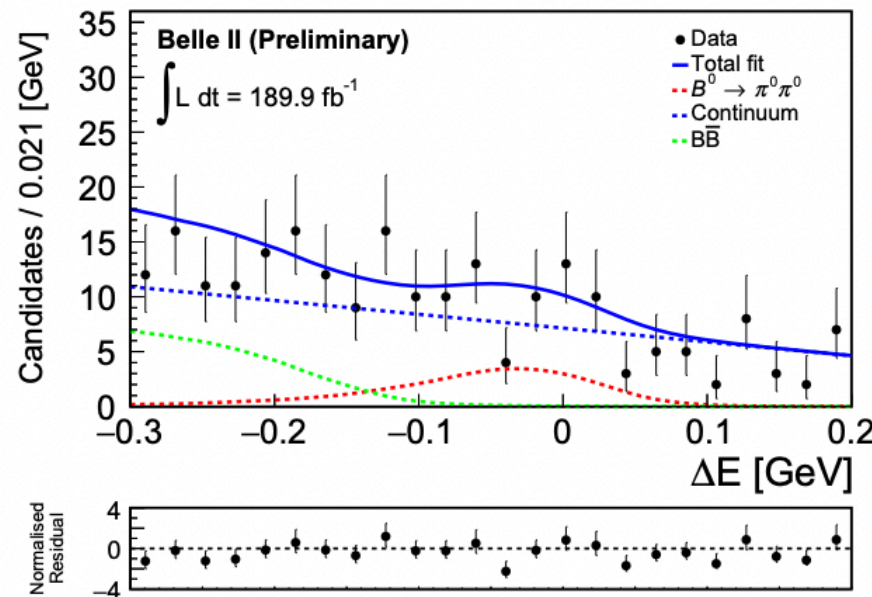
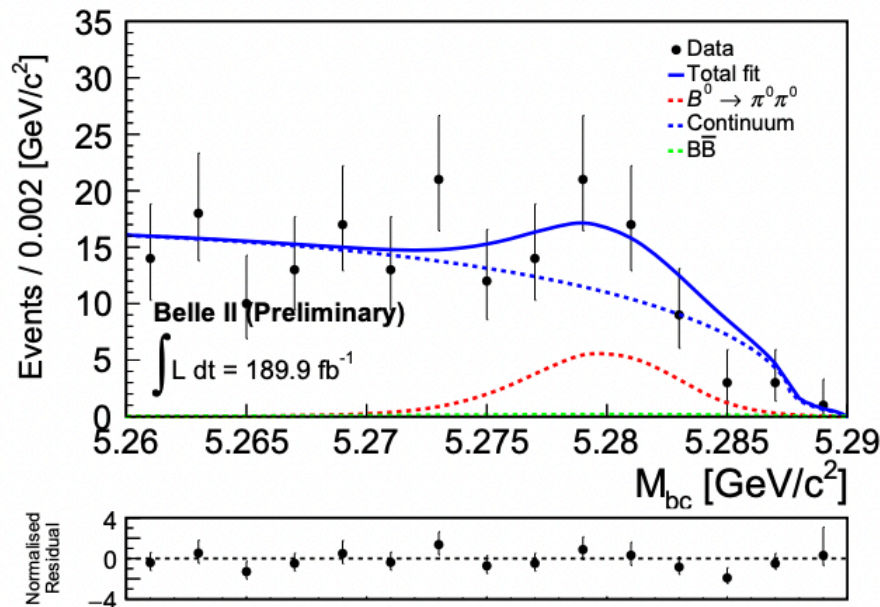


- Feasible only at e^+e^- colliders like Belle II
- Very challenging due to neutral final states

Analysis strategy

$$\mathcal{A}_{CP} = \frac{\Gamma(\bar{B} \rightarrow \pi^0\pi^0) - \Gamma(B \rightarrow \pi^0\pi^0)}{\Gamma(\bar{B} \rightarrow \pi^0\pi^0) + \Gamma(B \rightarrow \pi^0\pi^0)}$$

- Photons for signal reconstruction are selected via BDT
- 2D KDE function for signal extraction
- As is evident, continuum is the dominant background
- Use of data driven method for continuum suppression
- Use of Belle II flavor tagging algorithm
- Validation of analysis procedure: $B^0 \rightarrow D(\rightarrow K^+\pi^-\pi^0)\pi^0$



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PRD 96 032007 (2017)

Parameter	Belle II (~197 M BB pairs)	Belle (771 M BB pairs)
$\mathcal{B}(B^0 \rightarrow \pi^0\pi^0)$	$(1.32 \pm 0.25 \pm 0.18) \times 10^{-6}$	$(1.31 \pm 0.19 \pm 0.19) \times 10^{-6}$
\mathcal{A}_{CP}	$+0.14 \pm 0.46 \pm 0.07$	$+0.14 \pm 0.36 \pm 0.10$

First uncertainty: stat.; second: syst.

Comparable sensitivity with 1/4th of data!

α/ϕ_2 determination: $B^0 \rightarrow \rho^+\rho^-$



- ‘Golden’ channel for ϕ_2 measurement: small contribution from ‘penguin’ diagram
- Relies on the excellent neutral performance of the Belle II detector
- Target: \mathcal{B} and polarization

Analysis strategy

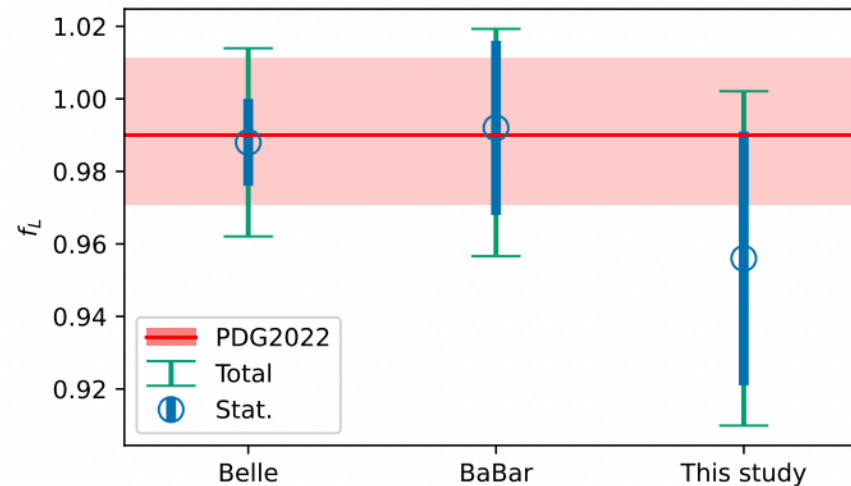
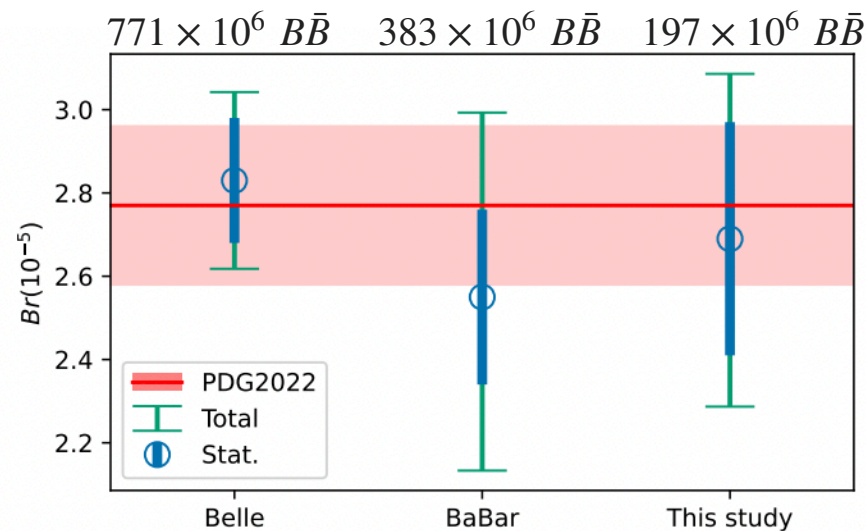
- 6D fit is performed to extract the yields
- Continuum and peaking background (with similar final state) complicates the analysis
- Validation: analysis procedure and continuum suppression inputs

arXiv: 2208.03554v1

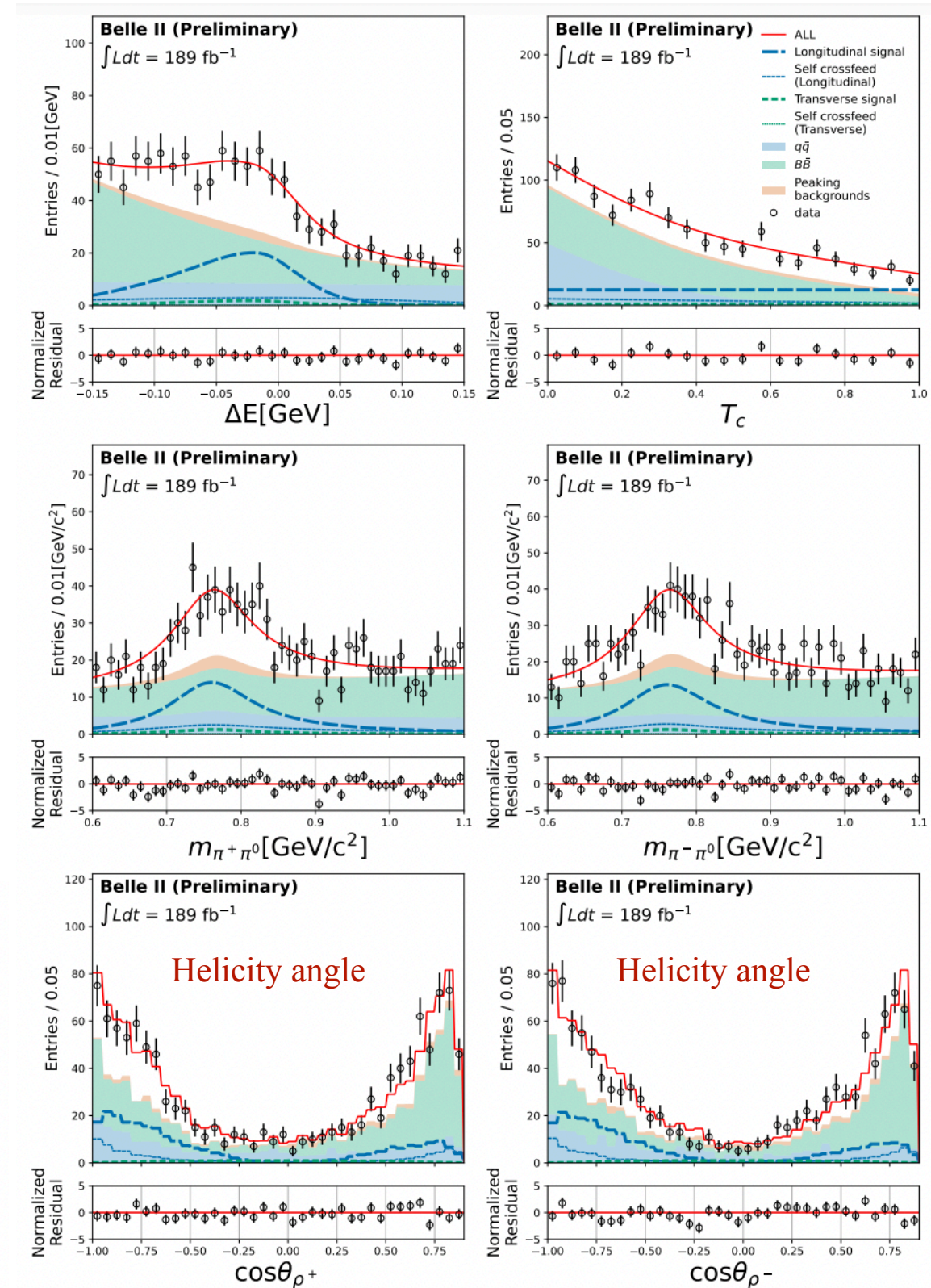
$$\mathcal{B} = (2.67 \pm 0.28 \pm 0.28) \times 10^{-5}$$

$$f_L = 0.956 \pm 0.035 \pm 0.033$$

First uncertainty: stat.; second: syst.



Consistent with previous measurements



α/ϕ_2 determination: $B^+ \rightarrow \rho^+ \rho^0$



- Relies on the excellent neutral performance of the Belle II detector
- Target: \mathcal{B} , \mathcal{A}_{CP} , and polarization

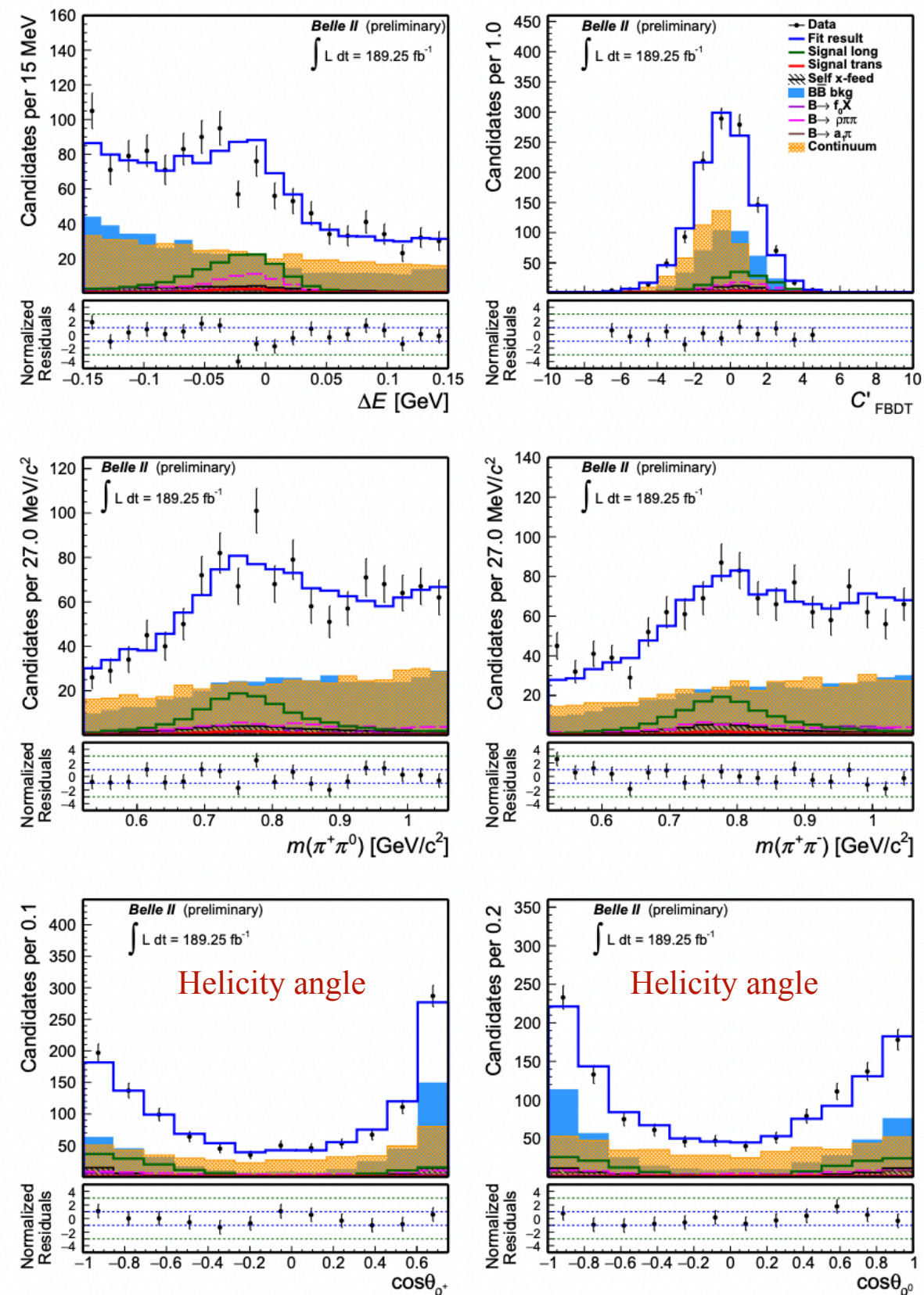
Analysis strategy

- 6D fit is performed to extract the yields
- Continuum and peaking background (with similar final state) complicates the analysis
- Validation: analysis procedure and continuum suppression inputs

Experiment	Values
Belle II (197 M BB pairs) arXiv: 2206.12362	$\mathcal{B} = (23.2^{+2.2}_{-2.1} \pm 2.7) \times 10^{-6}$ $f_L = 0.943^{+0.035}_{-0.033} \pm 0.027$ $\mathcal{A}_{CP} = -0.069 \pm 0.068 \pm 0.060$
BaBar (465 M BB pairs) PRL 102 141802 (2009)	$\mathcal{B} = (23.7 \pm 1.4 \pm 1.4) \times 10^{-6}$ $f_L = 0.950 \pm 0.015 \pm 0.006$ $\mathcal{A}_{CP} = -0.054 \pm 0.055 \pm 0.010$

First uncertainty: stat.; second: syst.

Consistent with previous measurements, however, dominated by systematic uncertainties

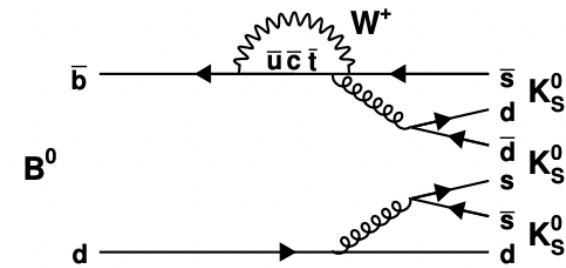


Time-dependent CPV measurement

3 body decays: Time dependent CPV analysis: $B^0 \rightarrow K_S^0 K_S^0 K_S^0$



- Target: \mathcal{B} and CP asymmetry
- Process mediates via $b \rightarrow sq\bar{q}$ transition
- It is sensitive to non-SM effects
- Important for understanding the CP asymmetry



$$\mathcal{P}(\Delta t) = \frac{e^{-|\Delta t|/\tau_{B^0}}}{4\tau_{B^0}} (1 + q[\mathcal{S} \sin(\Delta m_d \Delta t) + \mathcal{A} \cos(\Delta m_d \Delta t)])$$

Mixing induced CPV

Direct CPV

$$\begin{aligned} \mathcal{S} &= -\sin 2\phi_1 \\ &= -0.83 \pm 0.17 \end{aligned}$$

SM prediction
World average

$$\begin{aligned} \mathcal{A} &= 0 \\ &= 0.15 \pm 0.12 \end{aligned}$$

Any significant deviation of \mathcal{A}_{CP} and \mathcal{S}_{CP} from prediction of SM may be a hint of NP !

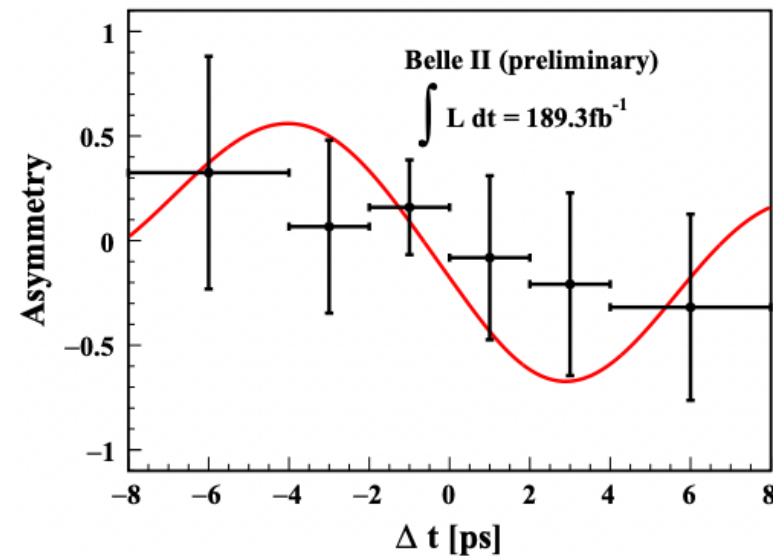
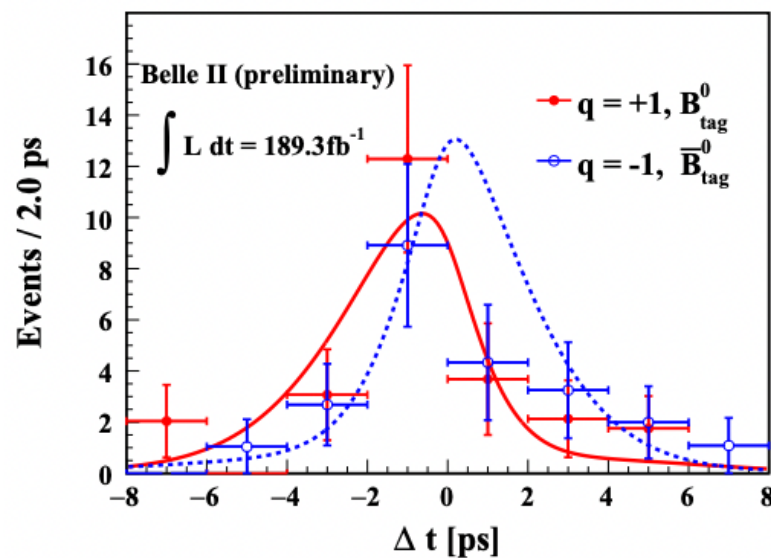
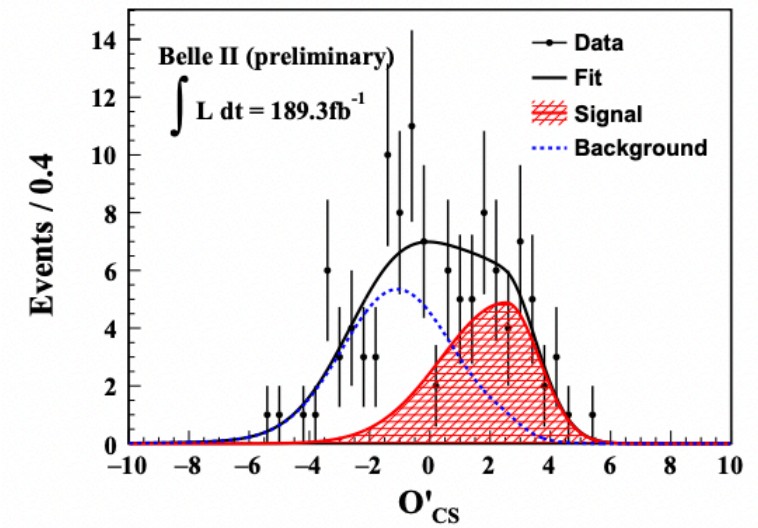
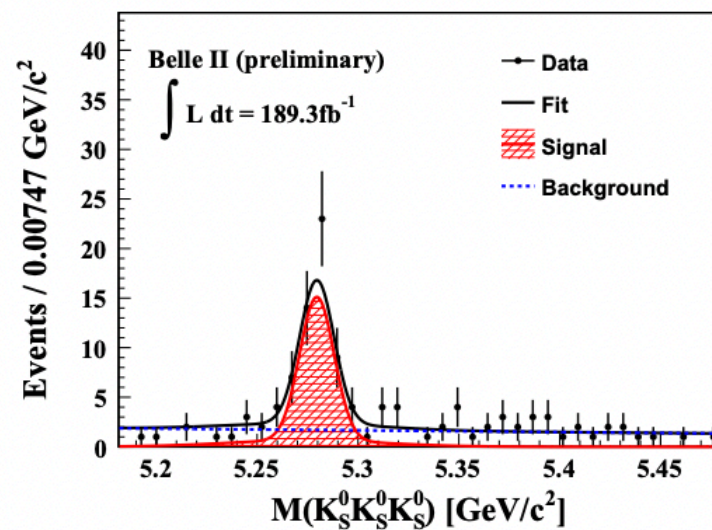
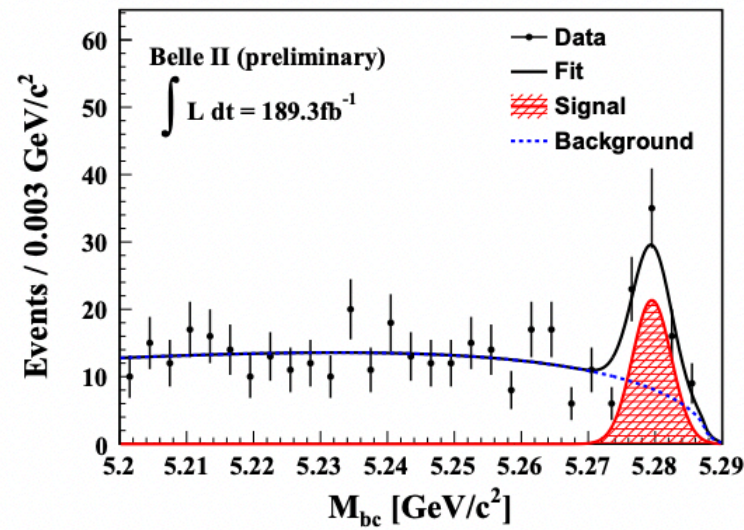
Analysis strategy

- Signal extraction using a 3D fit function comprising of: M_{bc} , $M(K_S^0 K_S^0 K_S^0)$, \mathcal{O}'_{CS}
- Continuum events pose as dominant background: BDT classifiers for suppression
- Additional backgrounds from, $B^0 \rightarrow X(\rightarrow K_S^0 K_S^0)K_S^0$ due to $b \rightarrow c$ transitions
- Veto $b \rightarrow c$ transitions through invariant mass, $M(K_S^0 K_S^0)$ selection criterion
- For CPV studies, Belle II flavor tagger algorithm is used to identify B_{tag} flavor
- Challenge is to correctly reconstruct K_S^0 vertex

Time dependent CPV: $B^0 \rightarrow K_S^0 K_S^0 K_S^0$



Signal yield = 53 ± 8



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World Average value

$$\mathcal{S} = (-1.86^{+0.91}_{-0.46} \pm 0.09)$$

$$\mathcal{A} = -0.22^{+0.30}_{-0.27} \pm 0.04$$

$$\mathcal{S} = -0.83 \pm 0.17$$

$$\mathcal{A} = 0.15 \pm 0.12$$

First uncertainty: stat.; second: syst.

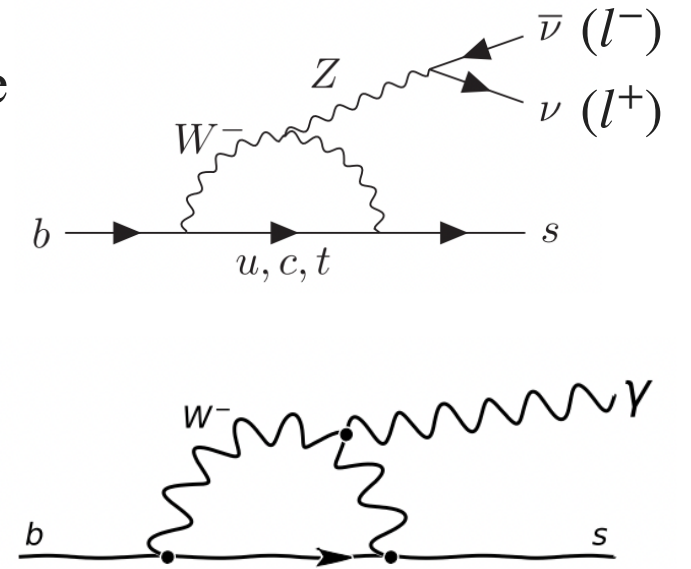


Electroweak and radiative penguin decays

Electroweak and radiative ‘penguins’: $b \rightarrow s$



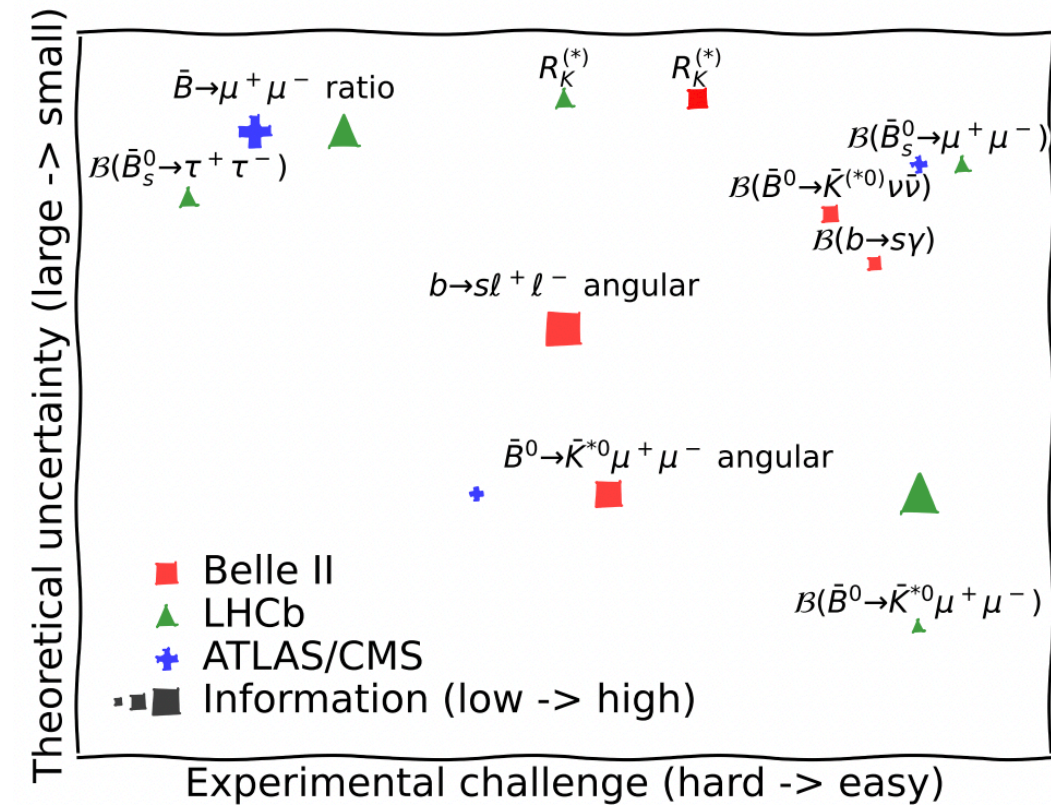
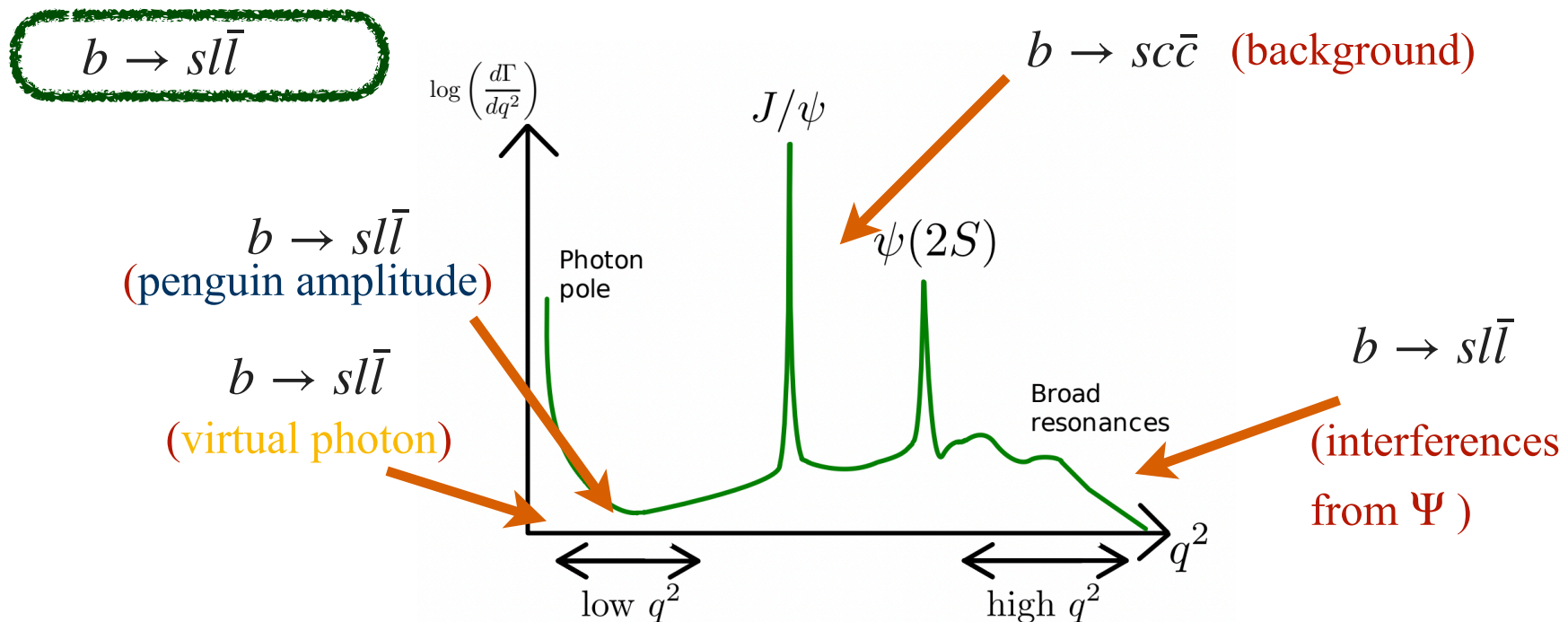
- A b quark decaying to an s/d quark requires the presence of a neutral vector boson at the vertex and a change of flavor (*Flavor changing neutral current*: FCNC)
- These, $b \rightarrow s$ FCNC processes are suppressed at ‘tree’ level within SM due to GIM
- However, can occur through loop-level within the SM
- New particles can couple to the SM particles and can influence its predictions, thereby making FCNC decays potent probe for NP searches



Theoretical Challenges

- Need to consider different kinematic regions to probe the complete q^2 spectrum
- Affected by form factor uncertainties

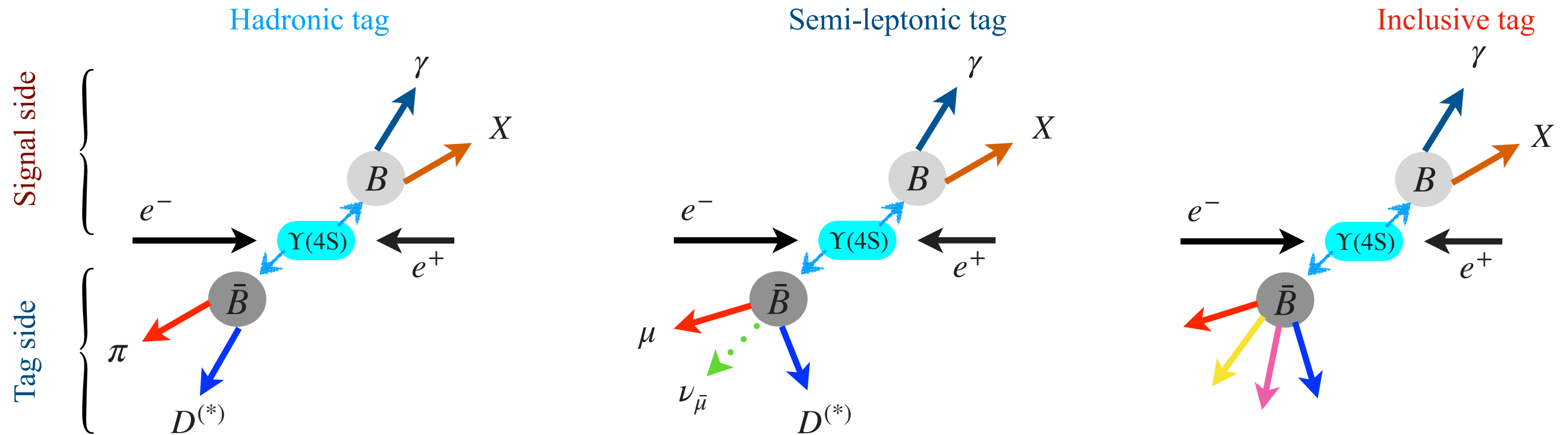
arXiv: 2205.05222v1



A single measurement is not sufficient!

Experimental challenges: missing particles / inclusive measurements

- Missing final state particles or inclusive measurements are experimentally very challenging
- e^+e^- colliders such as Belle II are best suited for such kind of measurements because of 4π coverage
- These measurements are performed using the **principle of conservation of momentum** and **identifying the conjugate B -meson very precisely** (the tagging approach)
- Three types of tagging: Exclusive (hadronic), Semi-exclusive (semi-leptonic), and inclusive tagging



Tagging reconstruction efficiency, backgrounds increases

Purity, physics constraints increases

Search for $B^+ \rightarrow K^+ \nu \bar{\nu}$ using inclusive tagging method



PRL 127 181802 (2021)

- Vary challenging due to missing particles in the signal-side B meson
- *An inclusive tag approach adopted for the first time at Belle II*

Analysis strategy

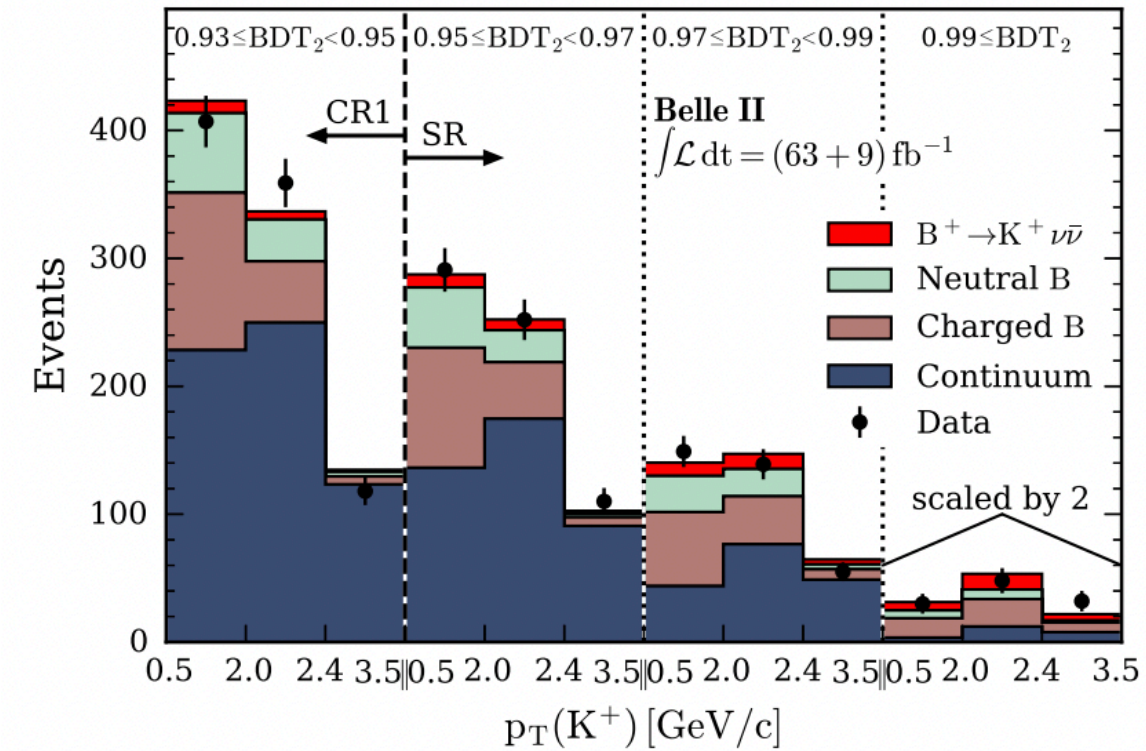
- Charged tracks and neutral clusters are identified with preliminary selection criteria to remove backgrounds
- Multivariate analysis techniques: 2 BDT classifiers used in cascade to separate signal from background, additional binary classifier to correct for mismodelling of qqbar events

Signal yield = $4.2^{+3.4}_{-3.2}$

$$\mathcal{B}(B^+ \rightarrow K^+ \nu \bar{\nu}) = (1.9^{+1.3}_{-1.3} \quad ^{+0.8}_{-0.7}) \times 10^{-5}$$

First uncertainty: stat.; second: syst.

UL on the $\mathcal{B}(B^+ \rightarrow K^+ \nu \bar{\nu})$ at 90% CL $< 2.3 \times 10^{-5}$

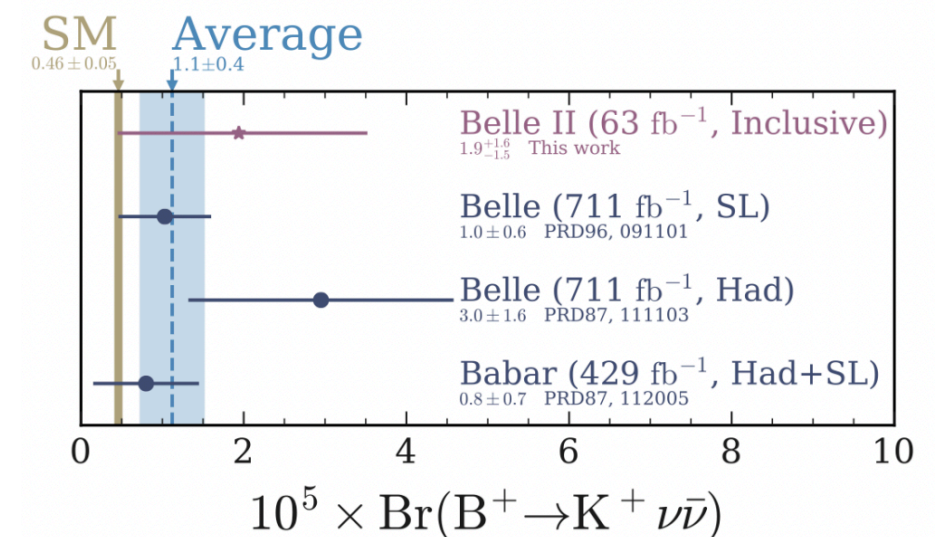


Signal efficiency

$$\epsilon^{incl} = 4\% \quad (\text{Belle II, } 63 \text{ fb}^{-1})$$

$$\epsilon^{sl} = 0.2\% \quad (\text{Belle, } 711 \text{ fb}^{-1})$$

$$\epsilon^{had} = 0.06\% \quad (\text{Belle, } 711 \text{ fb}^{-1})$$



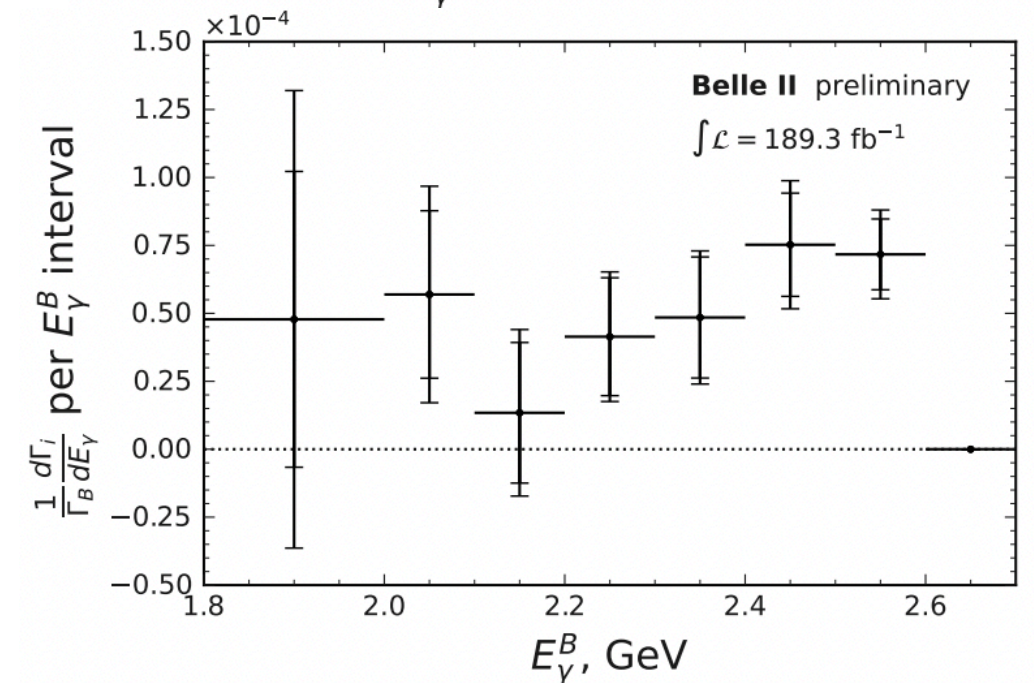
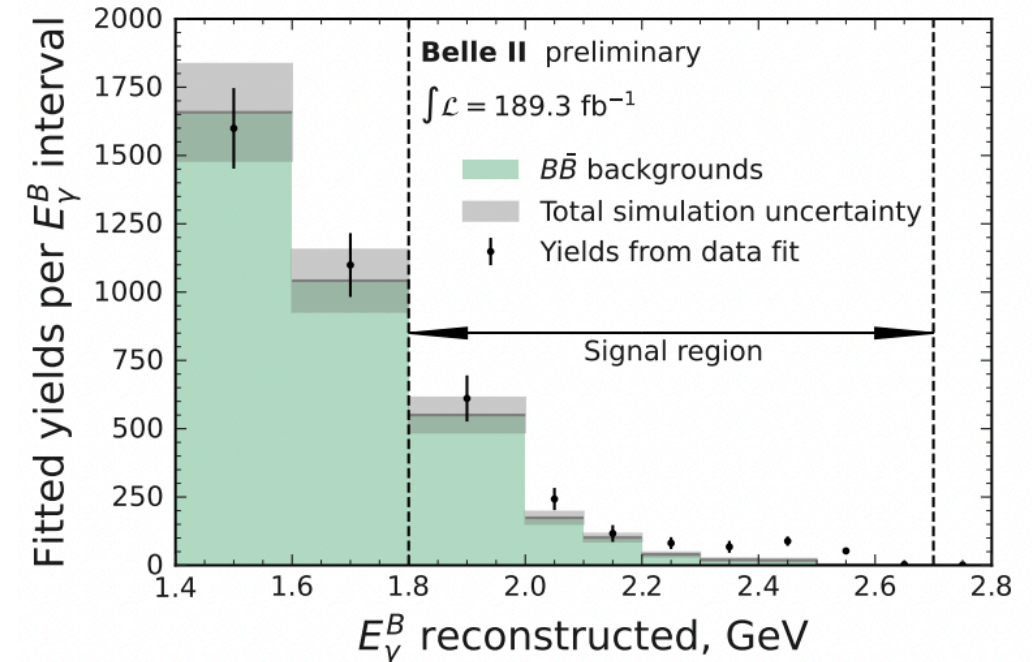
Radiative decay $B \rightarrow X_s \gamma$



- Target: Measurement of inclusive \mathcal{B} for different E_γ^B threshold
- Experimentally challenging

Analysis strategy

- No kinematic selection criteria applied to select X_s
- The tag side is reconstructed using hadronic decay channels
- Signal region is identified to be $1.8 < E_\gamma^B < 2.7$ (GeV)
- Fit strategy:
 1. Determine the well-reconstructed B_{tag} candidates using M_{bc} as a fit variable
 2. Background subtraction in E_γ^B distribution is carried out using MC simulation



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E_γ^B lower threshold	$\frac{1}{\Gamma_B} \frac{d\Gamma_i}{dE_\gamma} (10^{-4})$
1.8	$3.55 \pm 0.78(\text{stat.}) \pm 0.84(\text{syst.})$
2.0	$3.07 \pm 0.56(\text{stat.}) \pm 0.48(\text{syst.})$
2.1	$2.50 \pm 0.47 (\text{stat.}) \pm 0.35 (\text{syst.})$

PRD 77, 051103 (2008)

BaBar's hadronic tag result, $E_\gamma^B > 1.9$ (GeV) (210 fb^{-1})

$$(3.66 \pm 0.85 \pm 0.60) \times 10^{-4}$$

Competitive with BaBar's measurement !

Preparations to test Lepton Flavor Universality

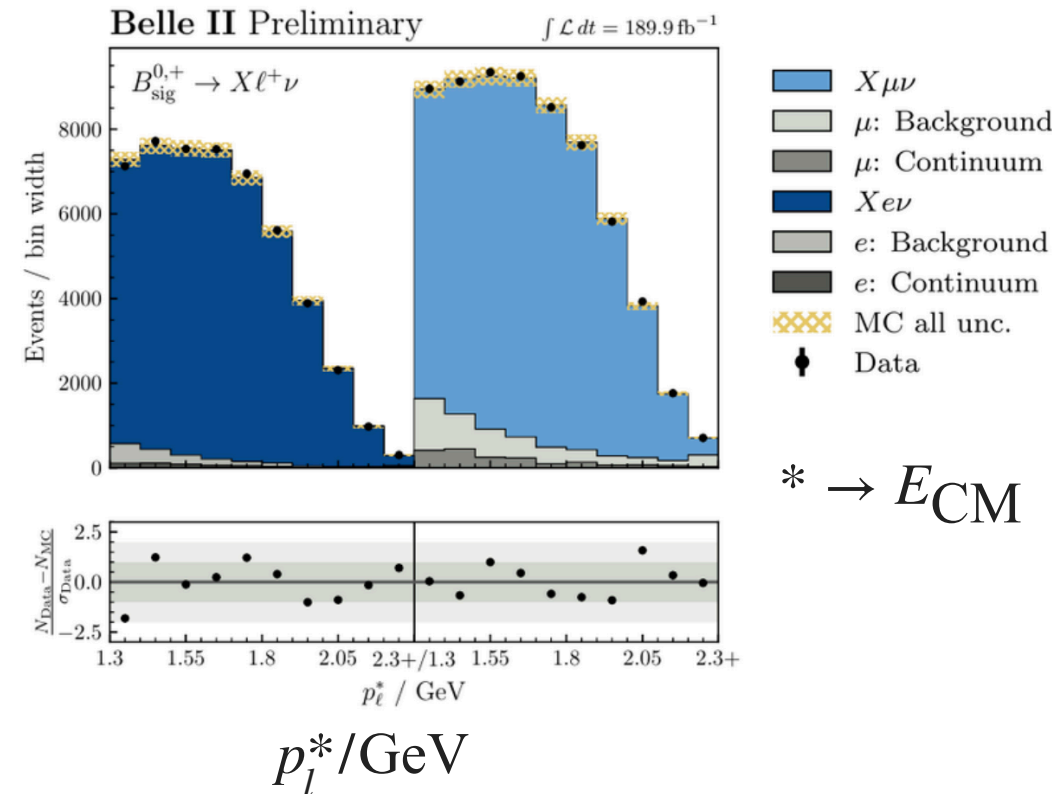
Preparations to test LFU: $\mathcal{R}(X_{e/\mu}) = \mathcal{B}(B \rightarrow X_c e \nu) / \mathcal{B}(B \rightarrow X_c \mu \nu)$

- The SM predicts the coupling strength of the weak interaction to be uniform for all of the lepton families: LFU
- This prediction needs to be experimentally verified and complementary measurements are a necessity
- SM prediction, $\mathcal{B}(B \rightarrow X_c \tau \nu) = (2.45 \pm 0.10) \%$ and sum of exclusive decays, $\mathcal{B}(B \rightarrow D \tau \nu) + \mathcal{B}(B \rightarrow D^* \tau \nu) = (2.30 \pm 0.67) \%$ (dominated by large uncertainties)

- Target: To measure light lepton ratio and validate the analysis strategy

Analysis strategy

- An event is identified as: $\Upsilon(4S) \rightarrow B_{tag} + (l^\pm + ROE)$
- B_{tag} candidates are reconstructed using FEI hadronic tagging algorithm
- Continuum and other B backgrounds affect the analysis
- Continuum is constrained with off-resonance data and B backgrounds are suppressed using background enriched control regions



ICHEP 2022	Most precise measurement!
$\mathcal{R}(X_{e/\mu})(p_l^* > 1.3 \text{ GeV})$	$1.033 \pm 0.010 \text{ (stat.)} \pm 0.020 \text{ (syst.)}$
Belle ($\mathcal{R}(D_{e/\mu}^*)$) (exclusive)	$1.01 \pm 0.01 \text{ (stat.)} \pm 0.03 \text{ (syst.)}$ PRD 100 052007 (2019)

Next step: $\mathcal{R}(X) = \frac{\mathcal{B}(B \rightarrow X \tau \nu)}{\mathcal{B}(B \rightarrow X l \nu)}$

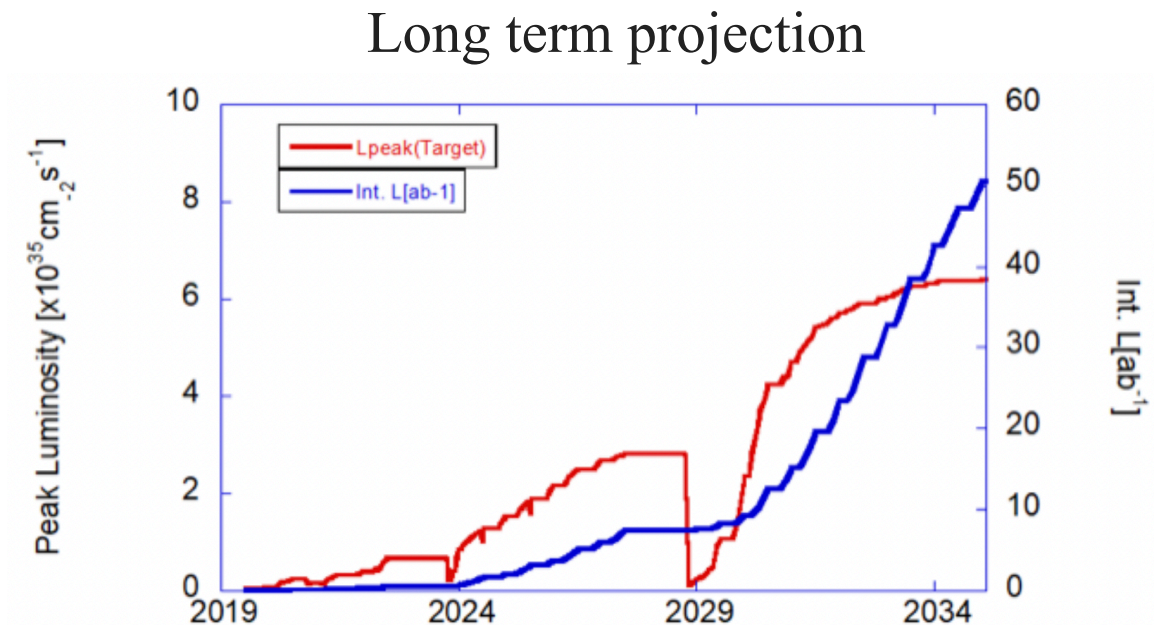
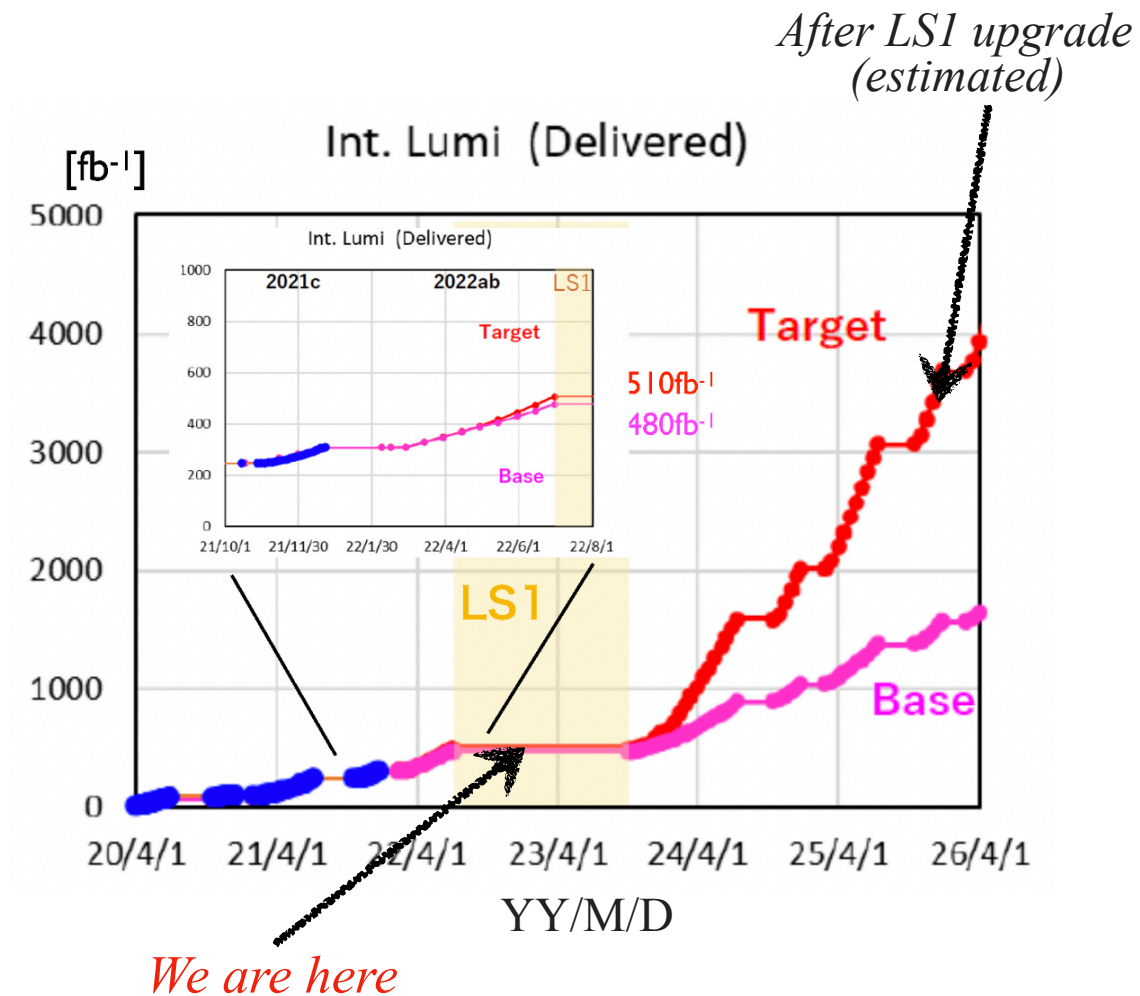
Compatible with exclusive Belle measurement at 0.6σ



- ✓ Presented results corresponding to an integrated luminosity of 190 fb^{-1} on the following topics
 - * Charm lifetime measurements
 - * Tagged and untagged exclusive measurements on $|V_{cb}|$ and $|V_{ub}|$
 - * Measurements to verify the isospin sum rule
 - * α/ϕ_2 measurement
 - * Time dependent CP violation measurements on three body decays
 - * Electroweak and radiative penguin decays
 - * Preparations to test the lepton flavor universality
- ✓ All these measurements agree well with the world average values and in some does better than the previous generation e^+e^- colliders (Babar/Belle) with limited statistics
- ❖ Some interesting results from the dark sector, charmonium and τ physics could not be accomodated here, due to the broad physics program of Belle II

Observables	Exp. theor. accuracy	Exp. experim. uncertainty	50 ab ⁻¹
UT angles and sides			
ϕ_1 [°]	***	0.4	Belle II
ϕ_2 [°]	**	1.0	Belle II
ϕ_3 [°]	***	1.0	LHCb/Belle II
$ V_{cb} $ incl.	***	1%	Belle II
$ V_{cb} $ excl.	***	1.5%	Belle II
$ V_{ub} $ incl.	**	3%	Belle II
$ V_{ub} $ excl.	**	2%	Belle II/LHCb
CP violation			
$S(B \rightarrow \phi K^0)$	***	0.02	Belle II
$S(B \rightarrow \eta' K^0)$	***	0.01	Belle II
$\mathcal{A}(B \rightarrow K^0 \pi^0)$ [10 ⁻²]	***	4	Belle II
$\mathcal{A}(B \rightarrow K^+ \pi^-)$ [10 ⁻²]	***	0.20	LHCb/Belle II
(Semi-)leptonic			
$\mathcal{B}(B \rightarrow \tau \nu)$ [10 ⁻⁶]	**	3%	Belle II
$\mathcal{B}(B \rightarrow \mu \nu)$ [10 ⁻⁶]	**	7%	Belle II
$R(B \rightarrow D \tau \nu)$	***	3%	Belle II
$R(B \rightarrow D^* \tau \nu)$	***	2%	Belle II/LHCb
Radiative and EW penguins			
$\mathcal{B}(B \rightarrow X_s \gamma)$	**	4%	Belle II
$A_{CP}(B \rightarrow X_{s,d} \gamma)$ [10 ⁻²]	***	0.005	Belle II
$S(B \rightarrow K_S^0 \pi^0 \gamma)$	***	0.03	Belle II
$S(B \rightarrow \rho \gamma)$	**	0.07	Belle II
$\mathcal{B}(B_s \rightarrow \gamma \gamma)$ [10 ⁻⁶]	**	0.3	Belle II
$\mathcal{B}(B \rightarrow K^* \nu \bar{\nu})$ [10 ⁻⁶]	***	15%	Belle II
$R(B \rightarrow K^* \ell \ell)$	***	0.03	Belle II/LHCb
Charm			
$\mathcal{B}(D_s \rightarrow \mu \nu)$	***	0.9%	Belle II
$\mathcal{B}(D_s \rightarrow \tau \nu)$	***	2%	Belle II
$A_{CP}(D^0 \rightarrow K_S^0 \pi^0)$ [10 ⁻²]	**	0.03	Belle II
$ q/p (D^0 \rightarrow K_S^0 \pi^+ \pi^-)$	***	0.03	Belle II
$A_{CP}(D^+ \rightarrow \pi^+ \pi^0)$ [10 ⁻²]	**	0.17	Belle II
Tau			
$\tau \rightarrow \mu \gamma$ [10 ⁻¹⁰]	***	< 50	Belle II
$\tau \rightarrow e \gamma$ [10 ⁻¹⁰]	***	< 100	Belle II
$\tau \rightarrow \mu \mu \mu$ [10 ⁻¹⁰]	***	< 3	Belle II/LHCb

Belle II holds promise in giving us new insights through precision measurements



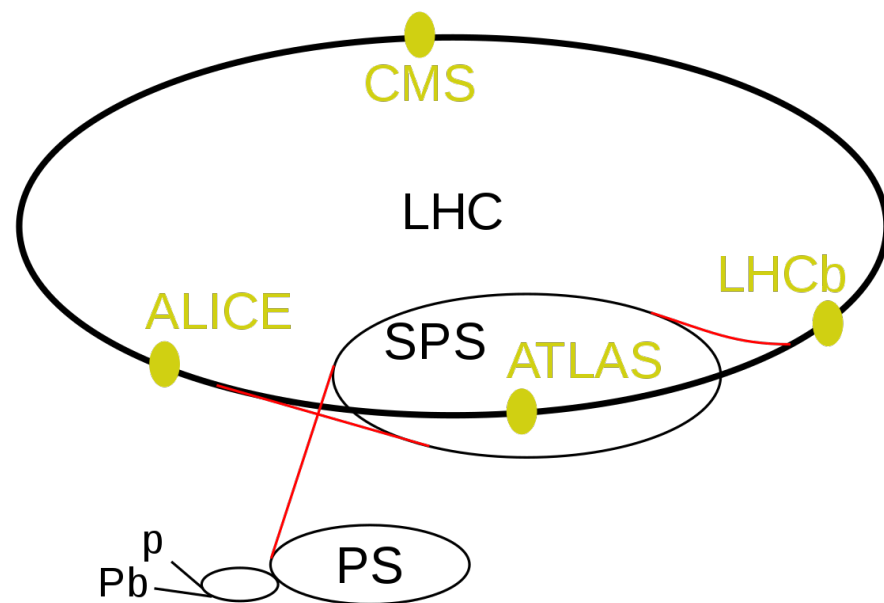
Thank You

Additional slides

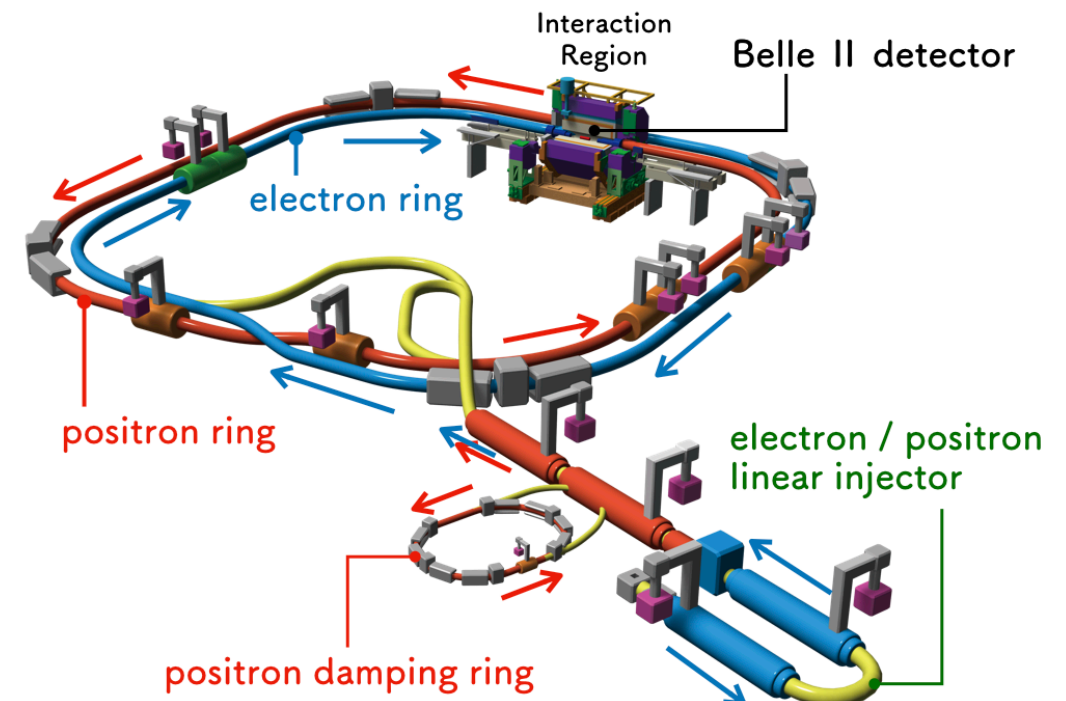
Types of colliders

- At present (on earth), colliders are the only way to create an environment similar to our early universe

Hadron Collider



Electron-Positron Collider

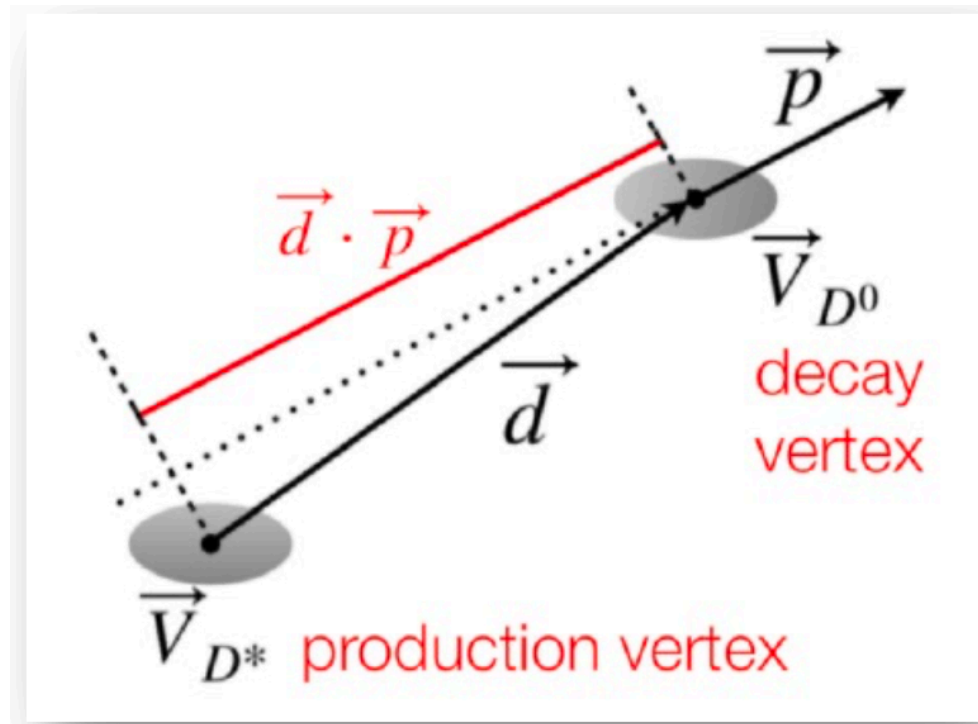


- Energy frontier (13.6 TeV, $\sim 2.06 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$)
- Capability to produce almost all SM particles
- Huge amount of backgrounds from pp collisions
(~ 20 inelastic events per crossing (30M crossing/sec))

- Luminosity frontier (Design $\mathcal{L} = 6 \times 10^{35} \text{ cm}^{-2}\text{s}^{-1}$)
- Threshold production of particles
- Compared to pp collisions, e^+e^- collisions produce fewer backgrounds: a clean environment

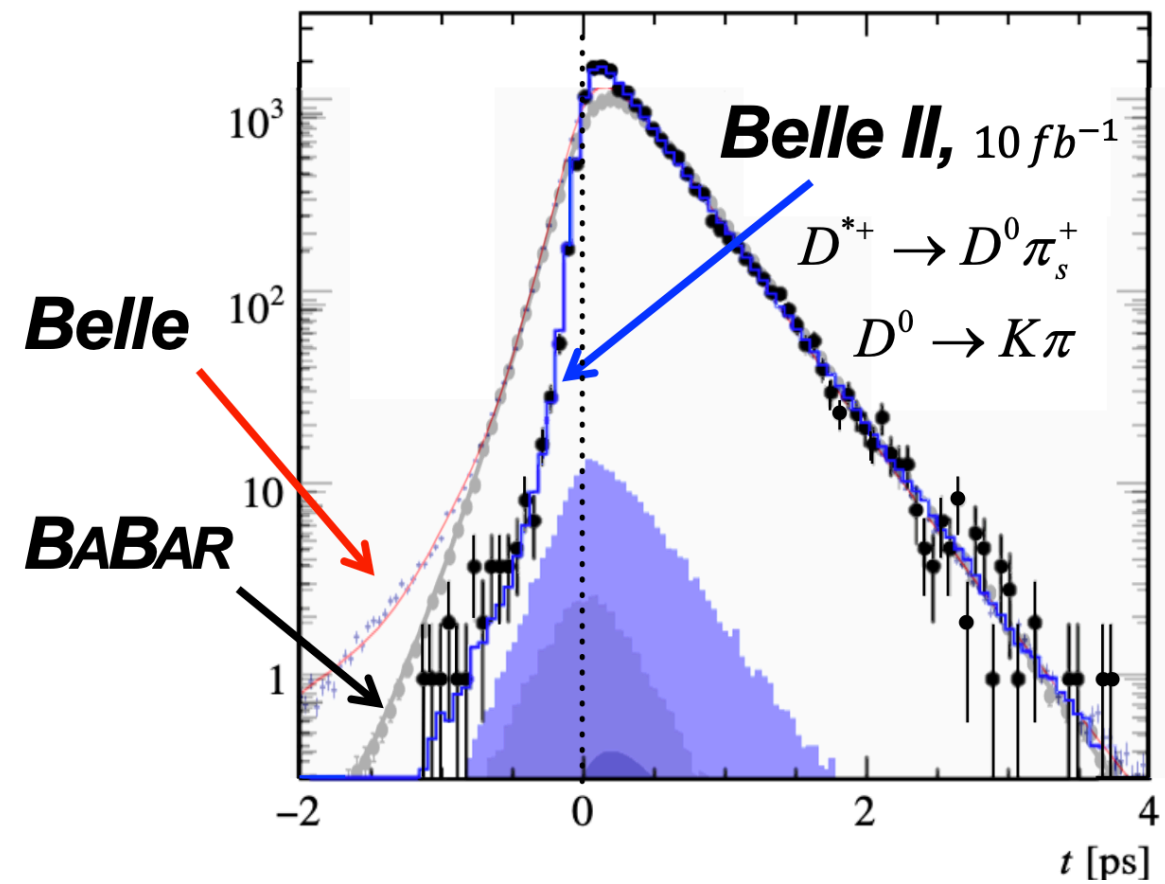
(Belle II)

Both frontiers are necessary for understanding the Nature !



$$t_h = \frac{m_h}{p^2} \vec{d} \cdot \vec{p}$$

D^0 lifetime distribution comparison



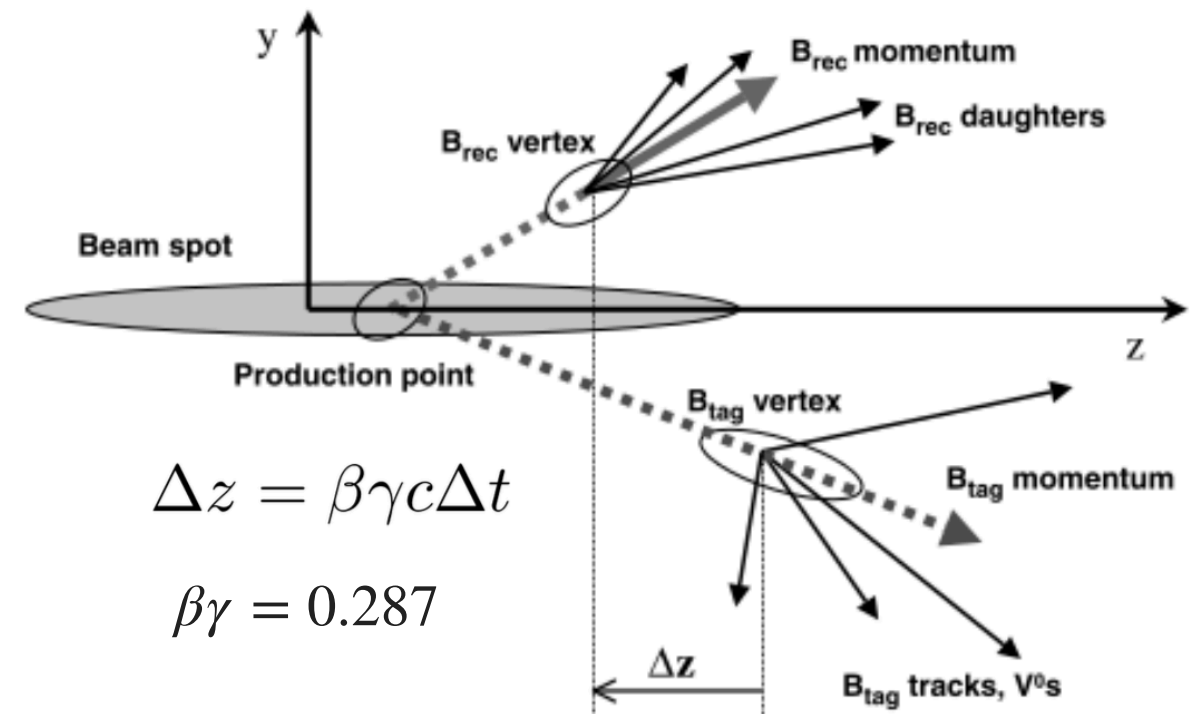
Improvement of Belle 2 over Belle

- 2 times better vertex resolution
- 20 times smaller beam spot size

$$\mathcal{A}_{\text{CP}}^{B \rightarrow f}(\Delta t) \equiv \mathcal{S} \sin(\Delta m_d \Delta t) + \mathcal{A} \cos(\Delta m_d \Delta t) \quad \text{Sensitive to } \Delta t$$

Determination of Δt :

- Requires the measurement of Δz .
- Δz measurement requires the correct reconstruction of B_{tag} and B_{rec} vertices.
- Vertex reconstruction can be done only from tracks.
- First, B_{rec} is fully reconstructed and the remaining tracks are assigned to rest-of-event (ROE) category.
- ROE events are subjected to selection criteria (min. hits in vtx. detector, IP constraints etc.)
- Subsequently, all tracks from ROE are combined to form the B_{tag} vertex (on the basis of some FOM, χ^2)



Factors affecting Δt resolution :

- B_{tag} , B_{rec} vertex resolution
- Resolution of the boost factor, $\beta \gamma$ determined from the beam energy

- For a typical $\Delta z \sim 100 \mu\text{m}$
- Δt resolution is $0.6 \text{ ps} < \tau_B (1.5 \text{ ps})$
- Δt resolution is $0.6 \text{ ps} < \tau_{B \rightarrow \bar{B}} (12.5 \text{ ps})$

B_{tag} is B or \bar{B} ? \rightarrow Flavor tagging

- Target : Measurement of \mathcal{B} and direct \mathcal{A}_{CP}
- Process mediates via $b \rightarrow sq\bar{q}$ 'loop' diagrams.
- To address the $K\pi$ puzzle, precise measurement of \mathcal{B} and \mathcal{A}_{CP} is important.

$$\left. \begin{array}{l} B^0 \rightarrow K^+ \pi^- \\ B^+ \rightarrow K^0 \pi^+ \end{array} \right\} 62.8 \text{ fb}^{-1}$$

New

$$\left. \begin{array}{l} B^+ \rightarrow K^+ \pi^0 \\ B^0 \rightarrow K^0 \pi^0 \end{array} \right\} 190 \text{ fb}^{-1}$$

2D signal extraction function

- $M_{bc} = \sqrt{E_{beam}^{*2} - p_B^{*2}}$
- $\Delta E = E_B^* - E_{beam}^*$
- M_{bc} and ΔE correlations are taken into account

Backgrounds analyzed

- $e^+e^- \rightarrow q\bar{q}$ ($q = u, d, s, c$)
- $b \rightarrow c$ mediated decays
- $b \rightarrow u, d, s$ mediated decays
- Multivariate analysis is employed to suppress continuum

Charged track identification

- Tracks momentum information from dE/dx in CDC
- Particle identification using Cherenkov detectors
- pion/Kaon misidentification is 9%/11%

Neutral pion reconstruction

- Reconstructed from γ 's deposited in ECL
- ECL selection criteria (forward/barrel/backward)

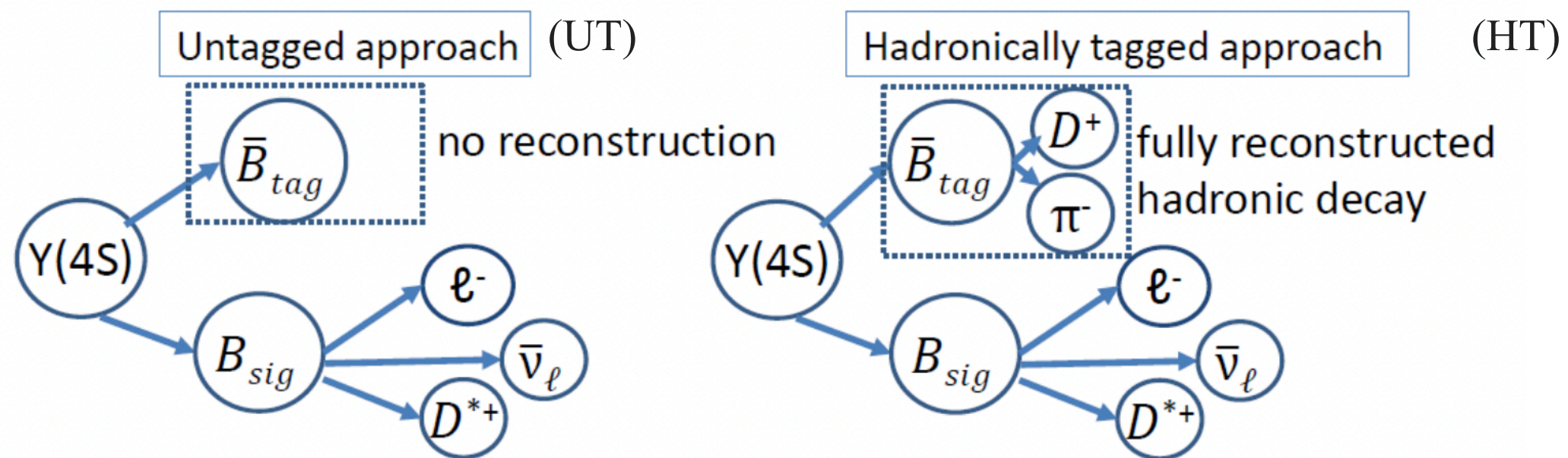
K_s^0 reconstruction (**challenges**)

- Dipion invariant mass 'cuts'
- K_s^0 flight distance
- Angle between dipion momentum and K_s^0 flight direction

Analyses mostly affected by continuum backgrounds

$|V_{cb}|$ and $|V_{ub}|$ measurements strategy

- $|V_{cb}|, |V_{ub}|$ measurements are experimentally very challenging owing to missing particles in the final state
- Both untagged and tagged approaches are adopted to complement each other.
- Untagged approach provides higher efficiency in signal reconstruction with a trade-off in signal purity
- Whereas tagged approach has lower signal efficiency but has higher purity



Advantages at Belle II

- Threshold production of $B\bar{B}$ pairs
- e^+e^- provides a 'clean' environment for reconstruction
- Missing momentum of undetected particles can be calculated due to 4π detection of other particles in an event