



# $R(D^*)$ at Belle II

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On behalf of Belle II Collaboration

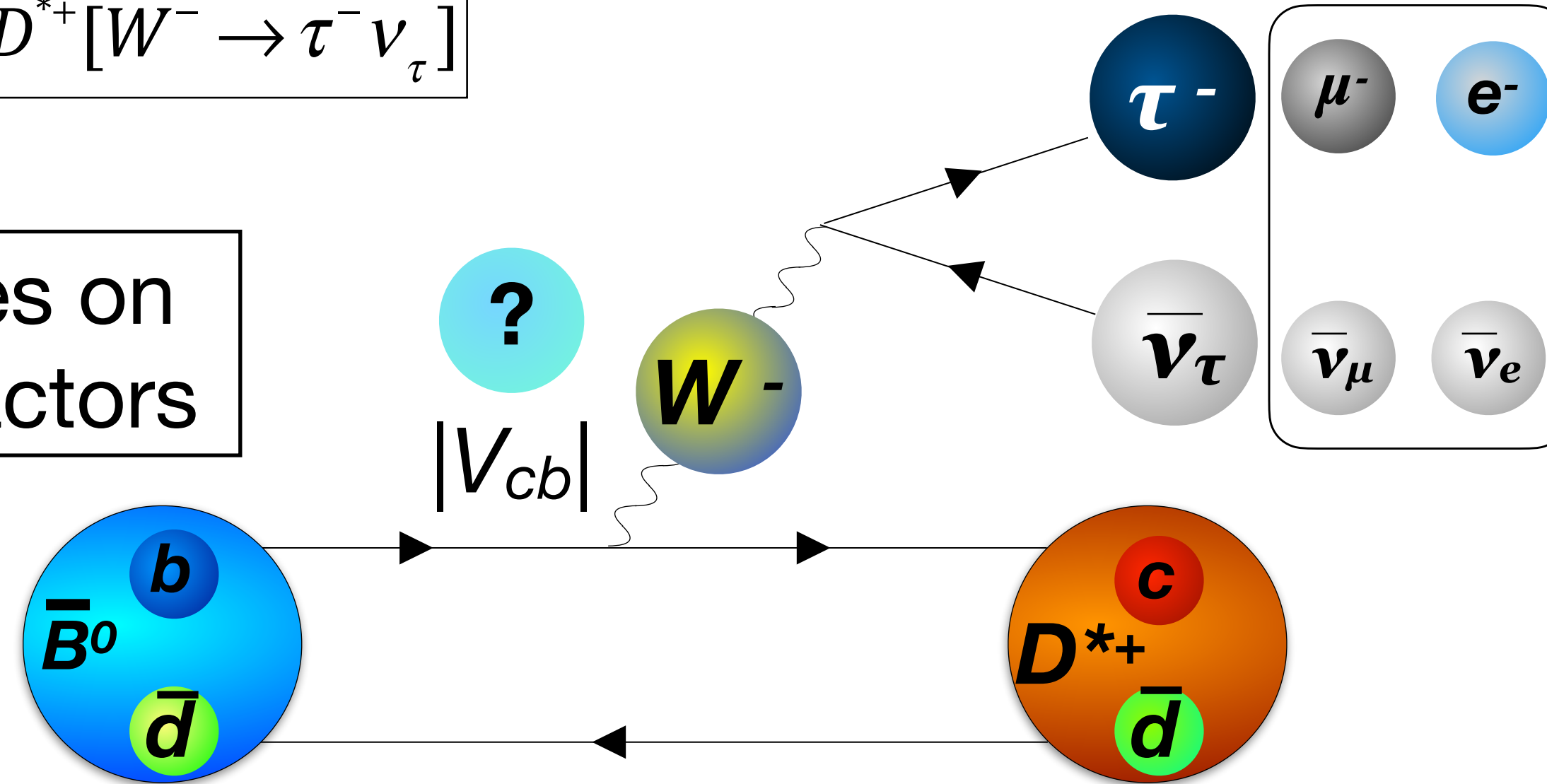
Feb. 9 - 11, 2023, KEK Tsukuba Campus

Accomplishments and mysteries in quark flavor physics (KM 50) /  
KEK Flavor Factories workshop (KEK-FF 2023)

# Semi-tauonic $B$ decay: $B \rightarrow D^{(*)} \tau \nu$

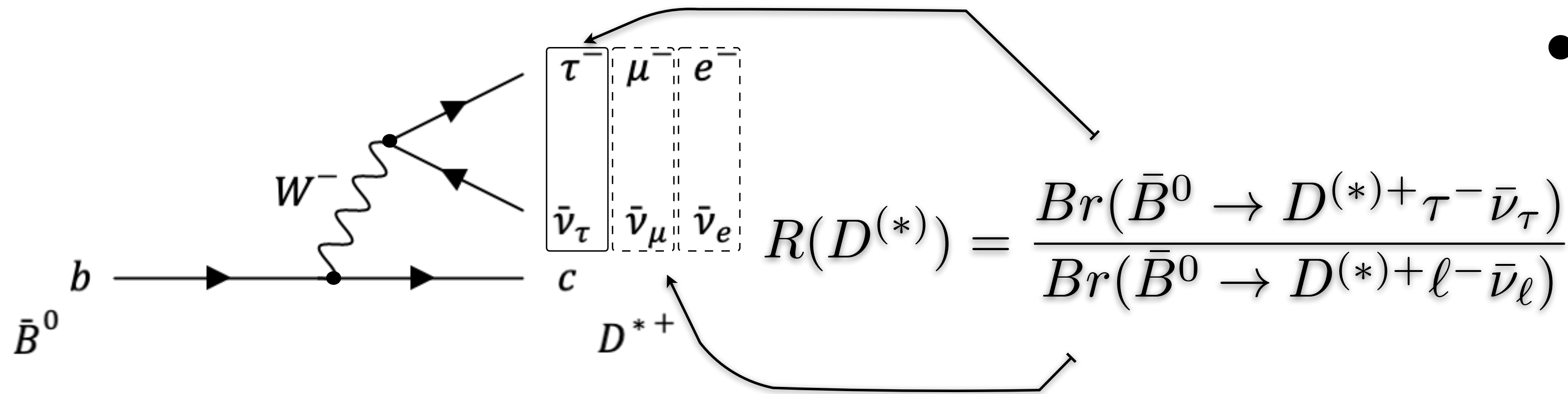
$$\bar{B}^0 \rightarrow D^{*+} [W^- \rightarrow \tau^- \bar{\nu}_\tau]$$

Sizable uncertainties on  $|V_{cb}|$  and the form factors



- Universality of the lepton coupling to the  $W$  gauge boson (Symmetry)
  - Lepton Flavor Universality (LFU) is fundamental theory of Standard Model (SM)
- $B \rightarrow D^{(*)} \tau \nu$  sensitive to New physics (NP) because the massive 3<sup>rd</sup> generation  **$b$  quark** and  **$\tau$  lepton** are involved
  - Flavor-dependent coupling to fermions could violates LFU

# $R(D)$ and $R(D^*)$ anomaly



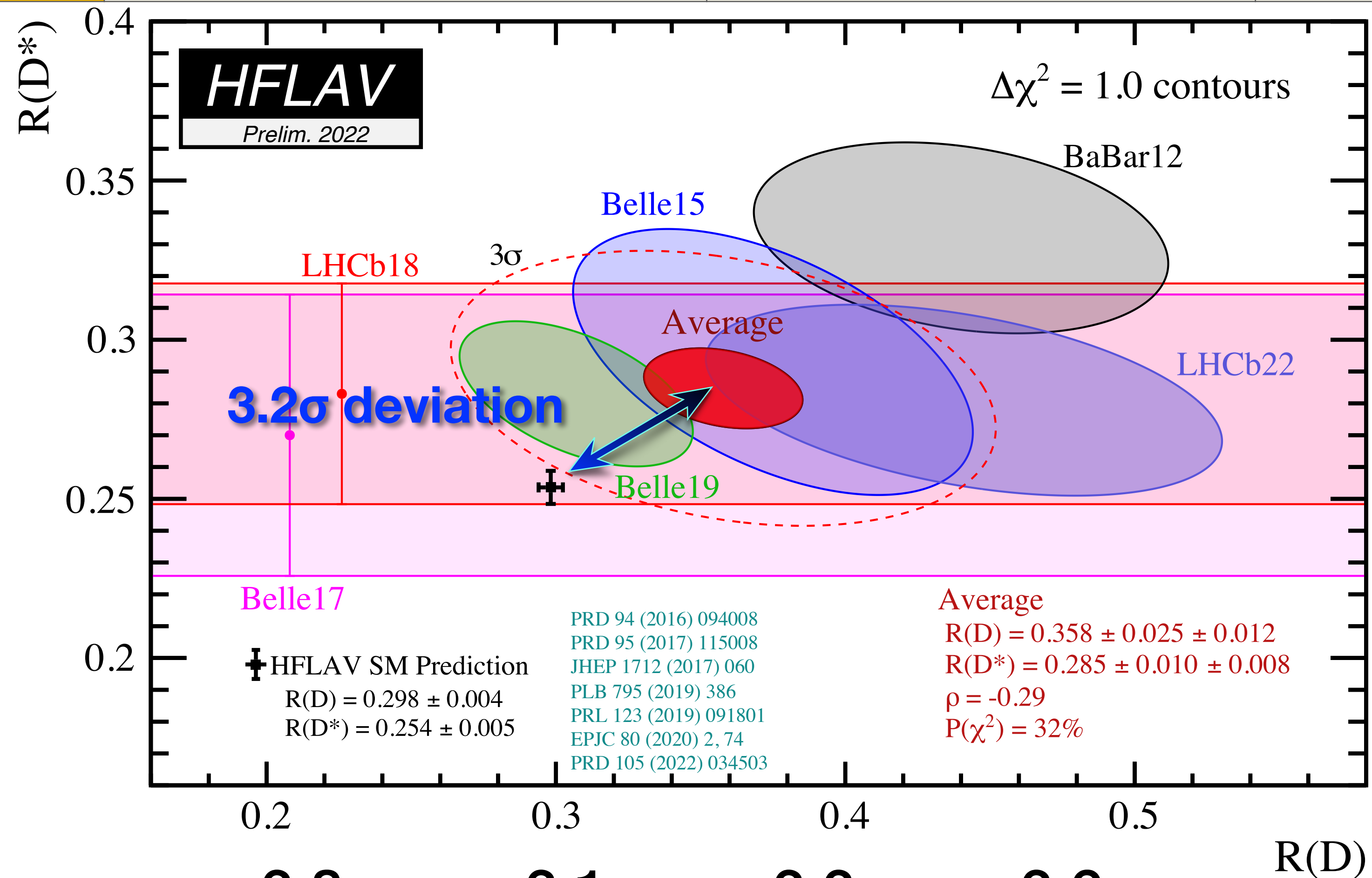
- Ratio of branch fractions cancel out most of the uncertainties on  $|V_{cb}|$ , form factors and the experimental systematics

- Charged lepton mass changes **kinematics** and modifies **form factors in the hadronization**
- QED corrections depend on lepton velocity ( $\tau$  vs.  $\ell$  ( $e, \mu$ ))

Experiment	Tag method	$\tau$ decay	Correlation(stat/syst/total)	$R(D)$	$R(D^*)$
Babar '12	Hadronic	$\ell\nu\nu$	-0.45/-0.07/-0.27	$0.440 \pm 0.058 \pm 0.042$	$0.332 \pm 0.024 \pm 0.018$
Belle '15	Hadronic	$\ell\nu\nu$	-0.56/-0.11/-0.49	$0.375 \pm 0.064 \pm 0.026$	$0.293 \pm 0.038 \pm 0.015$
LHCb '15	-	$\mu\nu\nu$		-	$0.336 \pm 0.027 \pm 0.030$
Belle '16	Semileptonic	$\ell\nu\nu$		-	$0.302 \pm 0.030 \pm 0.011$
Belle '17	Hadronic	$\pi\nu, \rho\nu$		-	$0.270 \pm 0.035^{+0.028}_{-0.025}$
LHCb '18	-	$\pi\pi\pi\nu$		-	$0.283 \pm 0.019 \pm 0.029$
Belle '20	semileptonic	$\ell\nu\nu$	-0.53/-0.51/-0.51	$0.307 \pm 0.037 \pm 0.016$	$0.283 \pm 0.018 \pm 0.014$
LHCb '22	-	$\mu\nu\nu$	-0.49/ /-0.43	$0.441 \pm 0.060 \pm 0.066$	$0.281 \pm 0.018 \pm 0.024$
Average	-	-	-0.43/-0.07/-0.29	$0.358 \pm 0.025 \pm 0.012$	$0.285 \pm 0.010 \pm 0.008$
SM				$0.298 \pm 0.004$	$0.254 \pm 0.005$

# $R(D)$ and $R(D^*)$ anomaly

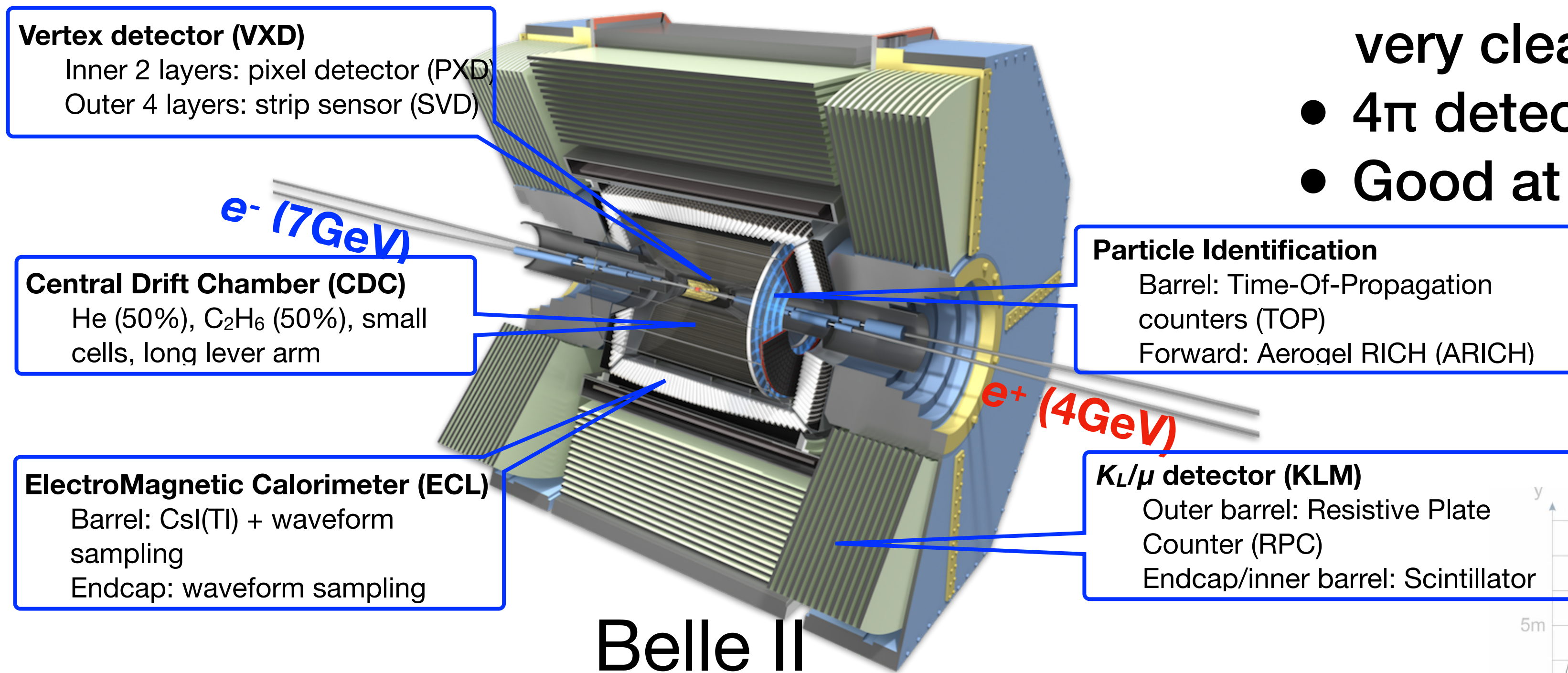
	Correlation(stat/syst/total)	$R(D)$	$R(D^*)$
Average	-0.43/-0.07/-0.29	$0.358 \pm 0.025 \pm 0.012$	$0.285 \pm 0.010 \pm 0.008$
SM		$0.298 \pm 0.004$	$0.254 \pm 0.005$



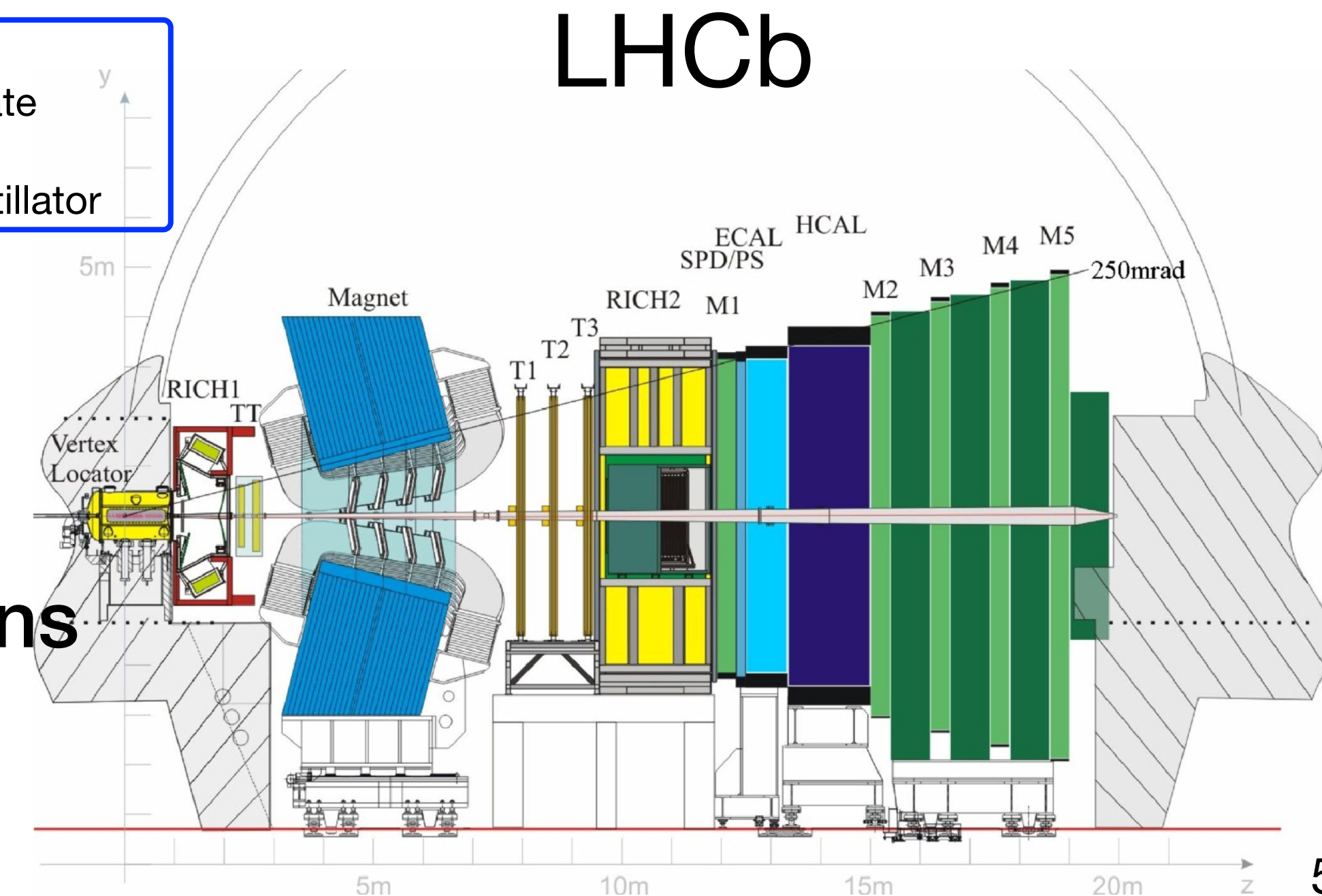
**3.8σ → 3.1σ → 3.3σ → 3.2σ**  
**LHCb18 Belle19 2021 LHCb22**

# $R(D)$ and $R(D^*)$ experiments

- Experiments at  $B$  factory
  - $e^+e^- \rightarrow \gamma(4S) \rightarrow B\bar{B}$  :
    - very clean and well-known initial state
  - $4\pi$  detector surrounding the IP
  - Good at also measuring neutrals,  $\pi^0$ ,  $\gamma$



- LHCb
  - Large amount of  $b$  hadrons produced in p-p collisions
  - Single arm detector covers forward region
  - Large boost, good separation of vertices



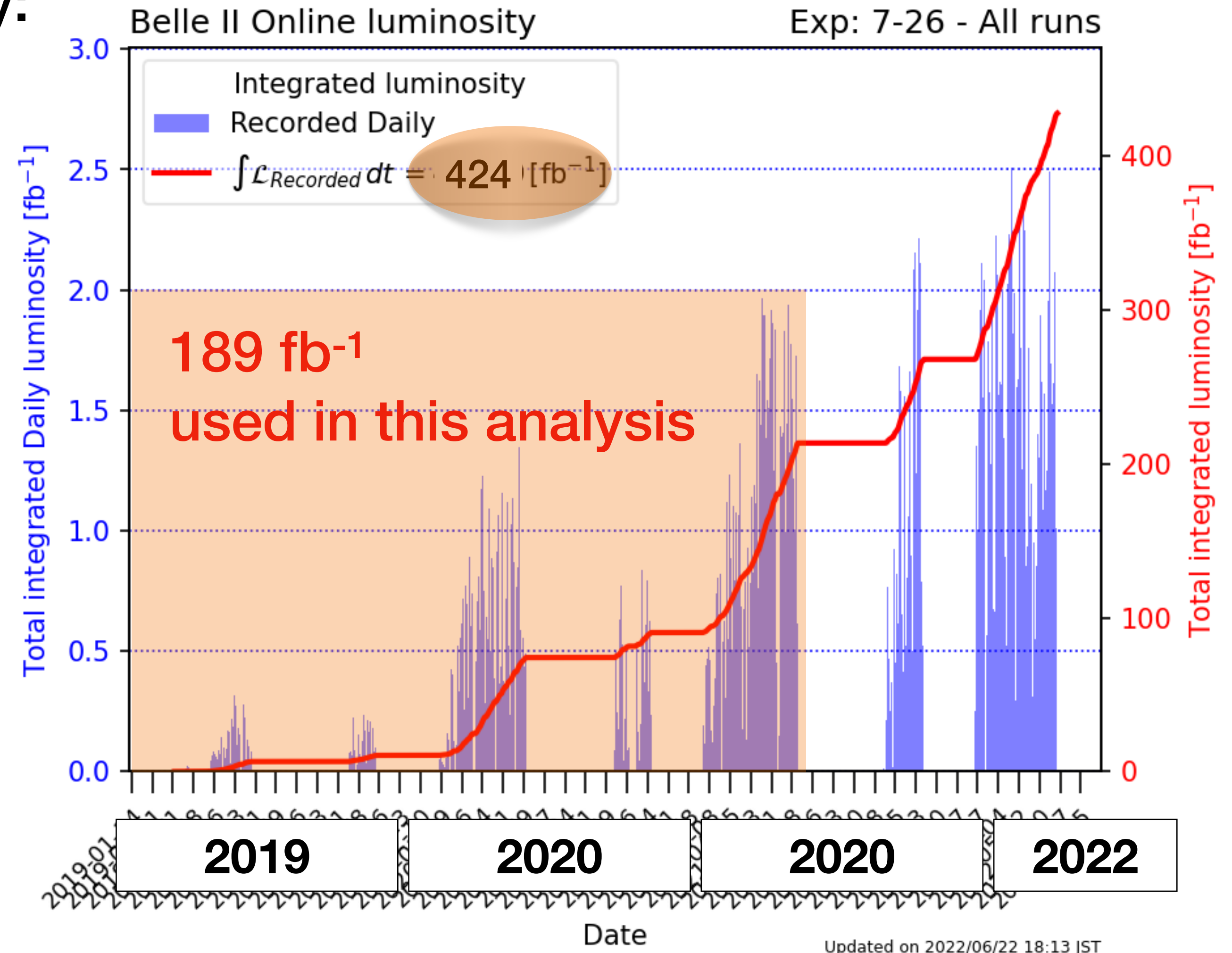
# Data set for $R(D^*)$ measurement

- World's highest instantaneous luminosity:

$$L = 4.7 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$$

KEKB record:  $2.1 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$

- Belle II data taking efficiency  $\sim 90\%$
- 424  $\text{fb}^{-1}$  until Long Shutdown (LS) 1,  $\sim 363 \text{ fb}^{-1}$  on  $\Upsilon(4S)$ 
  - Belle:  $1 \text{ ab}^{-1}$
- First  $R(D^*)$  measurement at Belle II using  $189 \text{ fb}^{-1}$  data-set targeting the end of spring 2023



# Tagging methods

- B tagging is necessary to measure  $B \rightarrow D^* \tau \nu$ ,  $B \rightarrow D^* l \nu$  ( $\nu \geq 2$ ) simultaneously

- Hadronic tag

- Exclusive tag

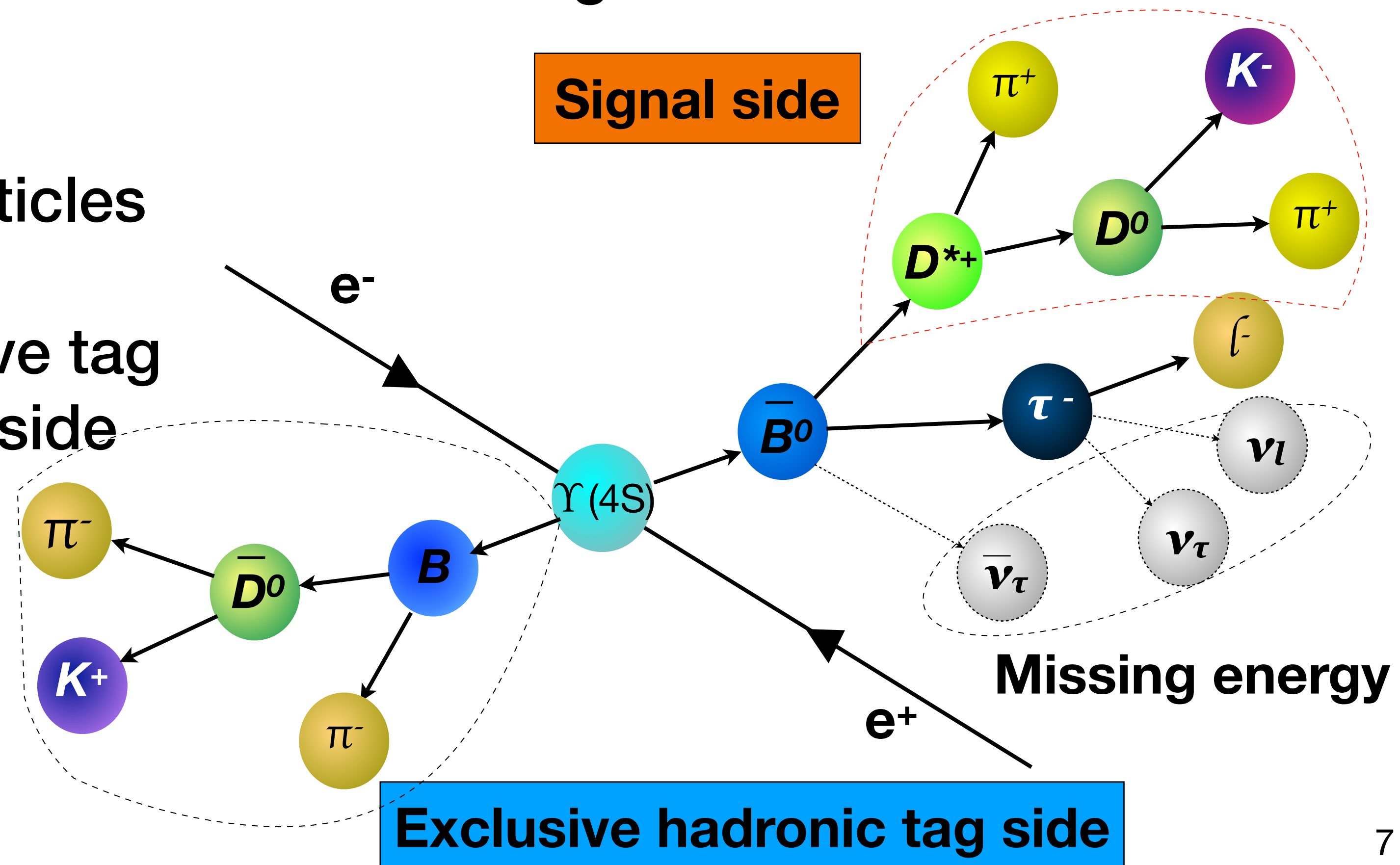
- Fully reconstruct  $B \rightarrow D^{(*)} (|J/\psi/\Lambda) X$
    - Tagging efficiency 0.2~0.4%
    - less background

- Inclusive tag

- Reconstruct tag  $B$  with all particles except signal  $B$
    - Higher efficiency than exclusive tag
    - Low purity, need clean signal-side final state

- Semileptonic tag

- Reconstruct  $B \rightarrow D^{(*)} l \nu$
  - Tagging efficiency ~0.5%
  - More background

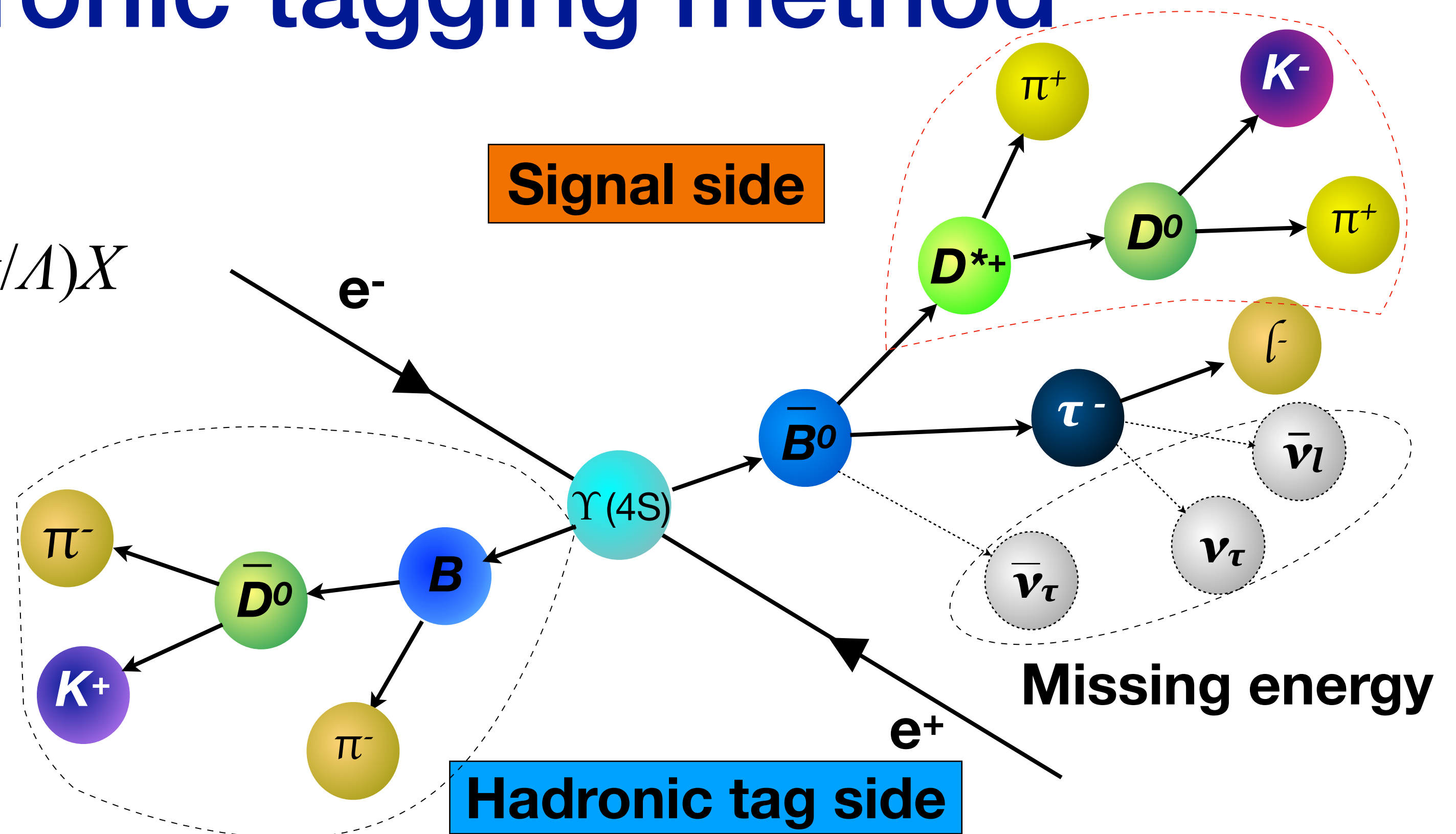


# Exclusive hadronic tagging method

- Hadronic tag

- Exclusive tag

- Fully reconstruct  $B \rightarrow D^{(*)} (J/\psi/\Lambda) X$
    - Tagging efficiency 0.2~0.4%
    - less background



- Fully reconstruct one of the  $B$  mesons ( $B$  tag), possible to measure momentum of other  $B$  meson ( $B$  signal)
- Indirectly measure missing momentum of neutrinos in signal  $B$  decays

- $M^2_{\text{miss}} = (\mathbf{p}_{\text{beam}} - \mathbf{p}_{B\text{tag}} - \mathbf{p}_{D^{(*)}} - \mathbf{p}_f)^2$

- $E_{\text{ECL}}$  unassigned neutral energy in the calorimeter  $E_{\text{ECL}} = \sum_i E_i^\gamma$  } Fitting variables for yields determination



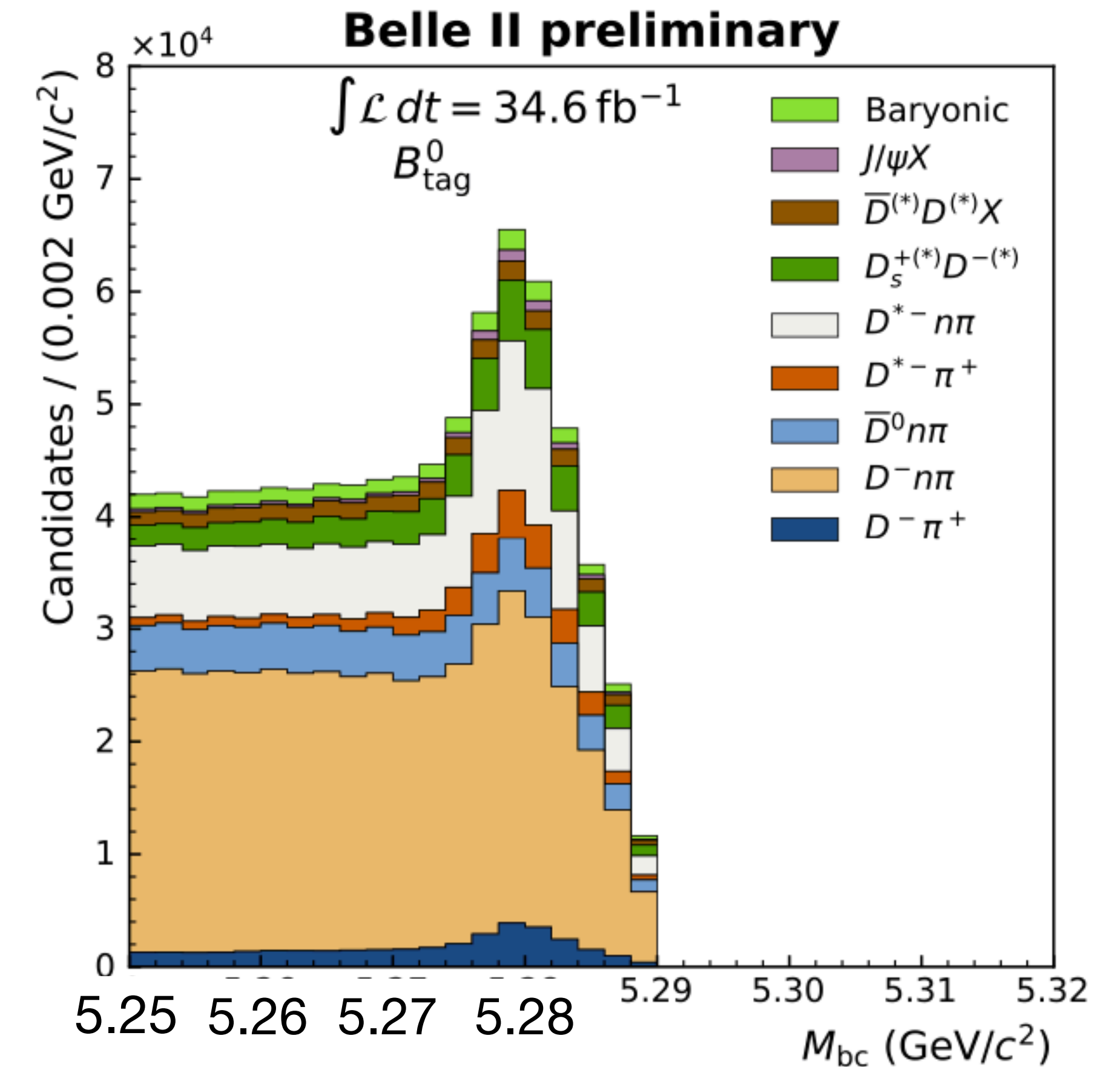
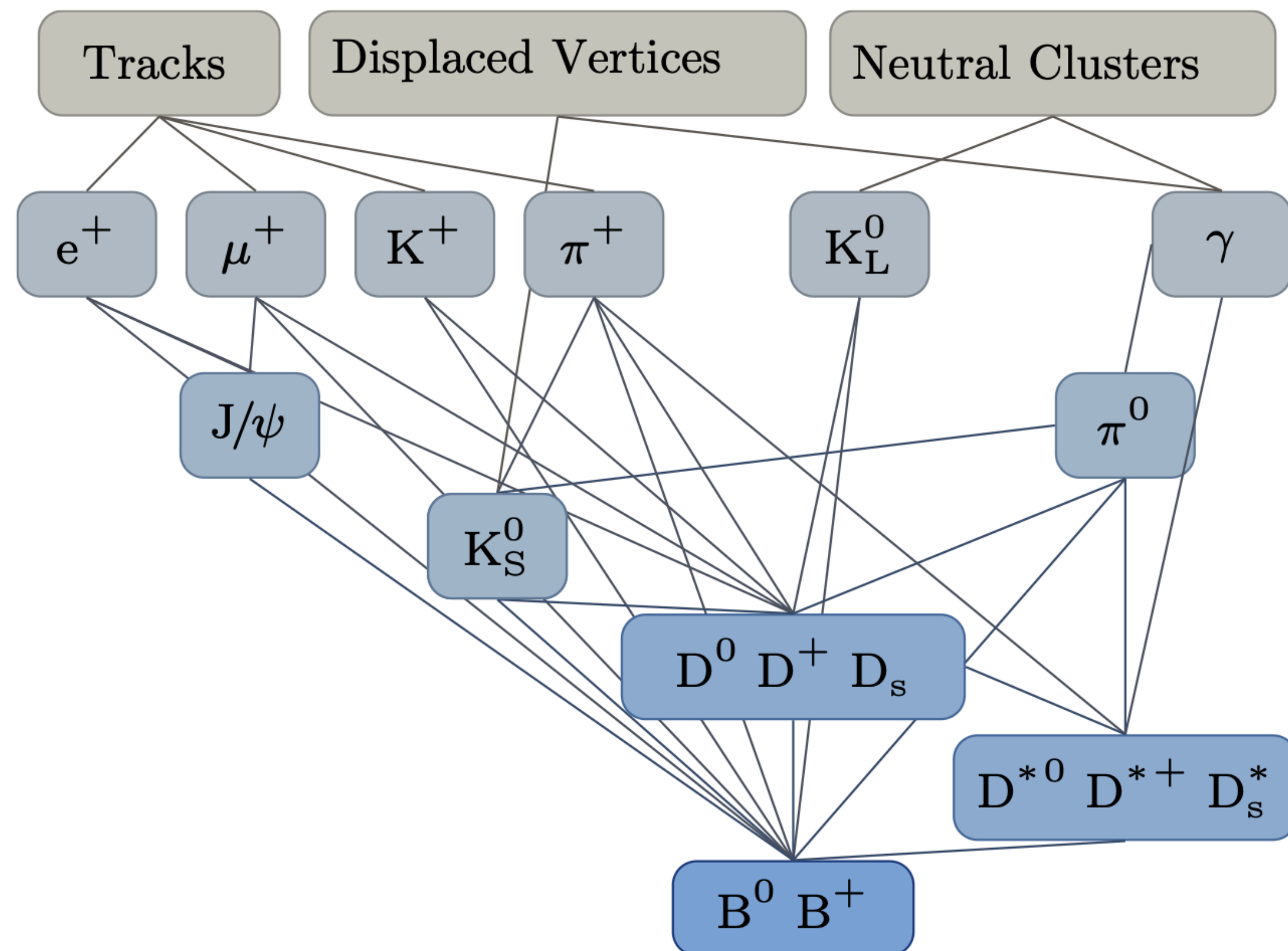
# Hadronic tag reconstruction at Belle II

- Hadronic tagging reconstruction : Full Event Interpretation (FEI) trained 200 Boost Decision Tree (BDT) to reconstruct ~100 decay channels, ~10,000  $B$  decay chains

arXiv:2008.06096

- $\epsilon=0.35\%$  for  $B^\pm$
- $\epsilon=0.27\%$  for  $B^0$

Comp. and Soft. For Big Sci. 3, 6 (2019)

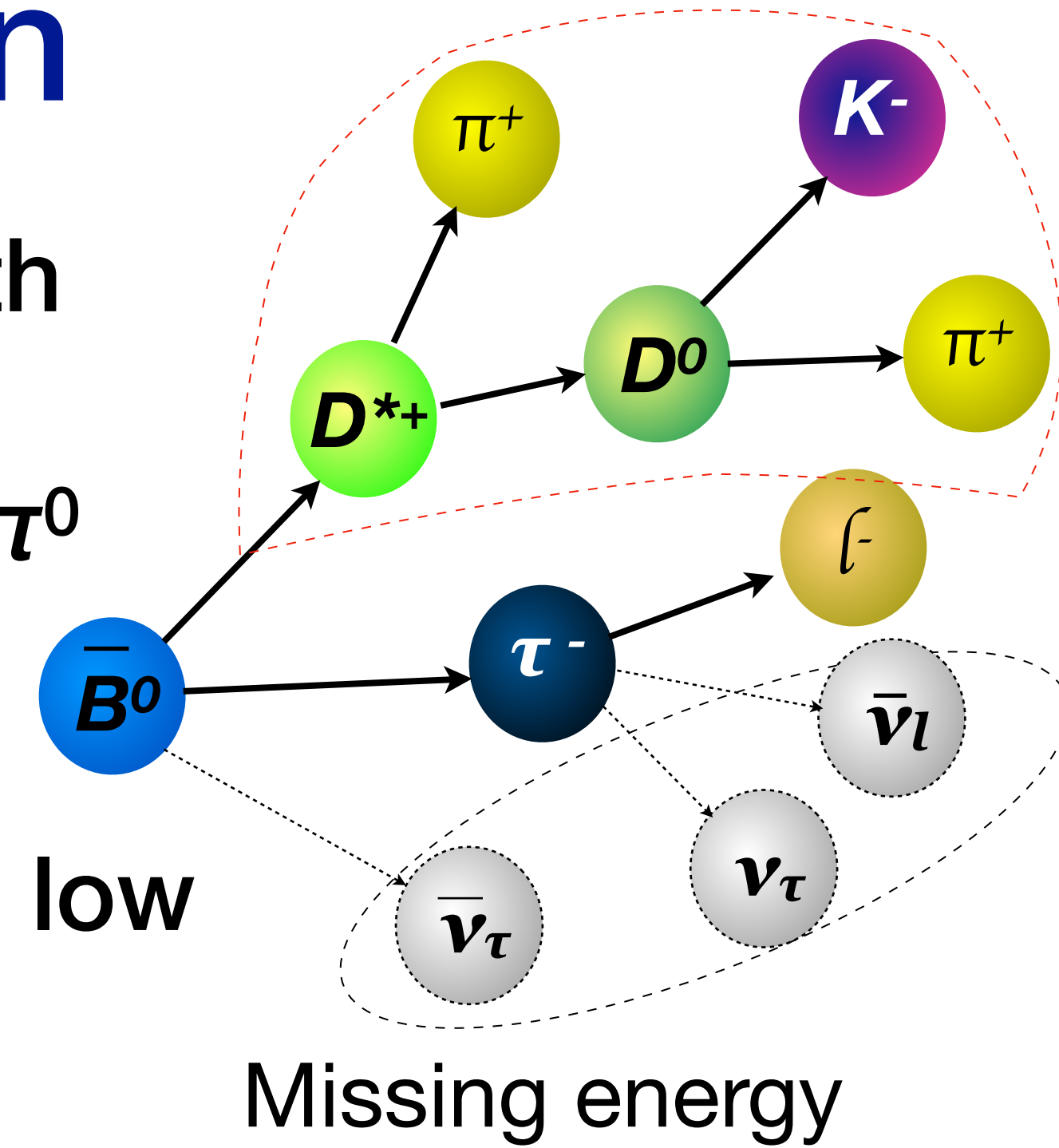


$$m_{bc} = \sqrt{(E_{\text{beam}}^*)^2 - (p_B^*)^2}$$

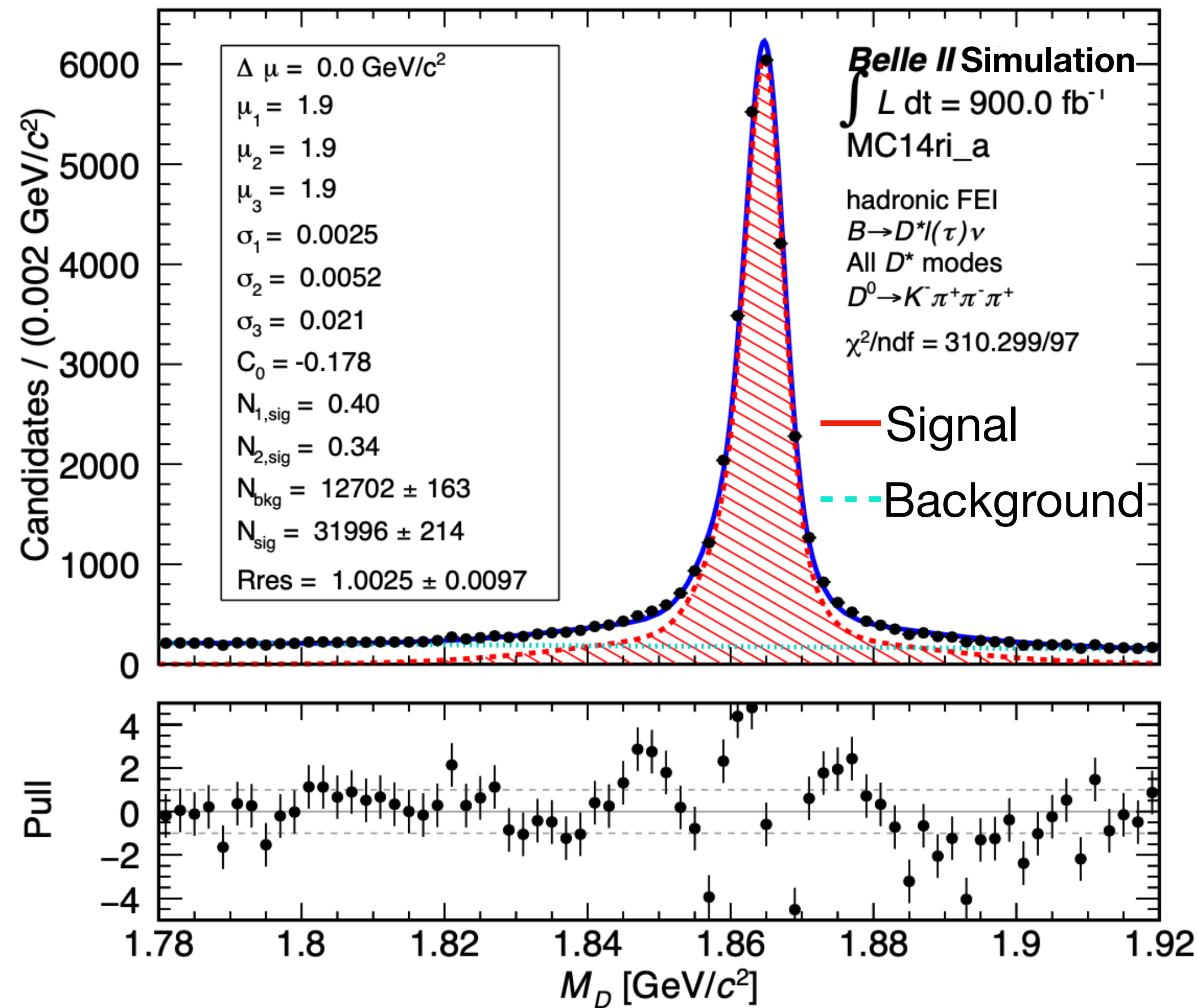
# Signal side reconstruction

$D^*$ decays	$D$ decays
$D^{*+} \rightarrow D^0 \pi^+$	$D^0 \rightarrow K^- \pi^+ \pi^0$
	$D^0 \rightarrow K^- \pi^+ \pi^- \pi^+$
	$D^0 \rightarrow K_S^0 \pi^+ \pi^- \pi^0$
	$D^0 \rightarrow K^- \pi^+$
	$D^0 \rightarrow K_S^0 \pi^+ \pi^-$
	$D^0 \rightarrow K_S^0 \pi^0$
	$D^0 \rightarrow K^- K^+$
	$D^0 \rightarrow \pi^+ \pi^-$
$D^{*+} \rightarrow D^+ \pi^0$	$D^+ \rightarrow K^- \pi^+ \pi^+$
	$D^+ \rightarrow K_S^0 \pi^+$
	$D^+ \rightarrow K^- K^+ \pi^+$
	$D^+ \rightarrow K_S^0 K^+$
$D^{*0} \rightarrow D^0 \pi^0$	$D^0 \rightarrow K^- \pi^+ \pi^0$
	$D^0 \rightarrow K^- \pi^+ \pi^- \pi^+$
	$D^0 \rightarrow K_S^0 \pi^+ \pi^- \pi^0$
	$D^0 \rightarrow K^- \pi^+$
	$D^0 \rightarrow K_S^0 \pi^+ \pi^-$
	$D^0 \rightarrow K_S^0 \pi^0$
	$D^0 \rightarrow K^- K^+$
$D^0 \rightarrow \pi^+ \pi^-$	

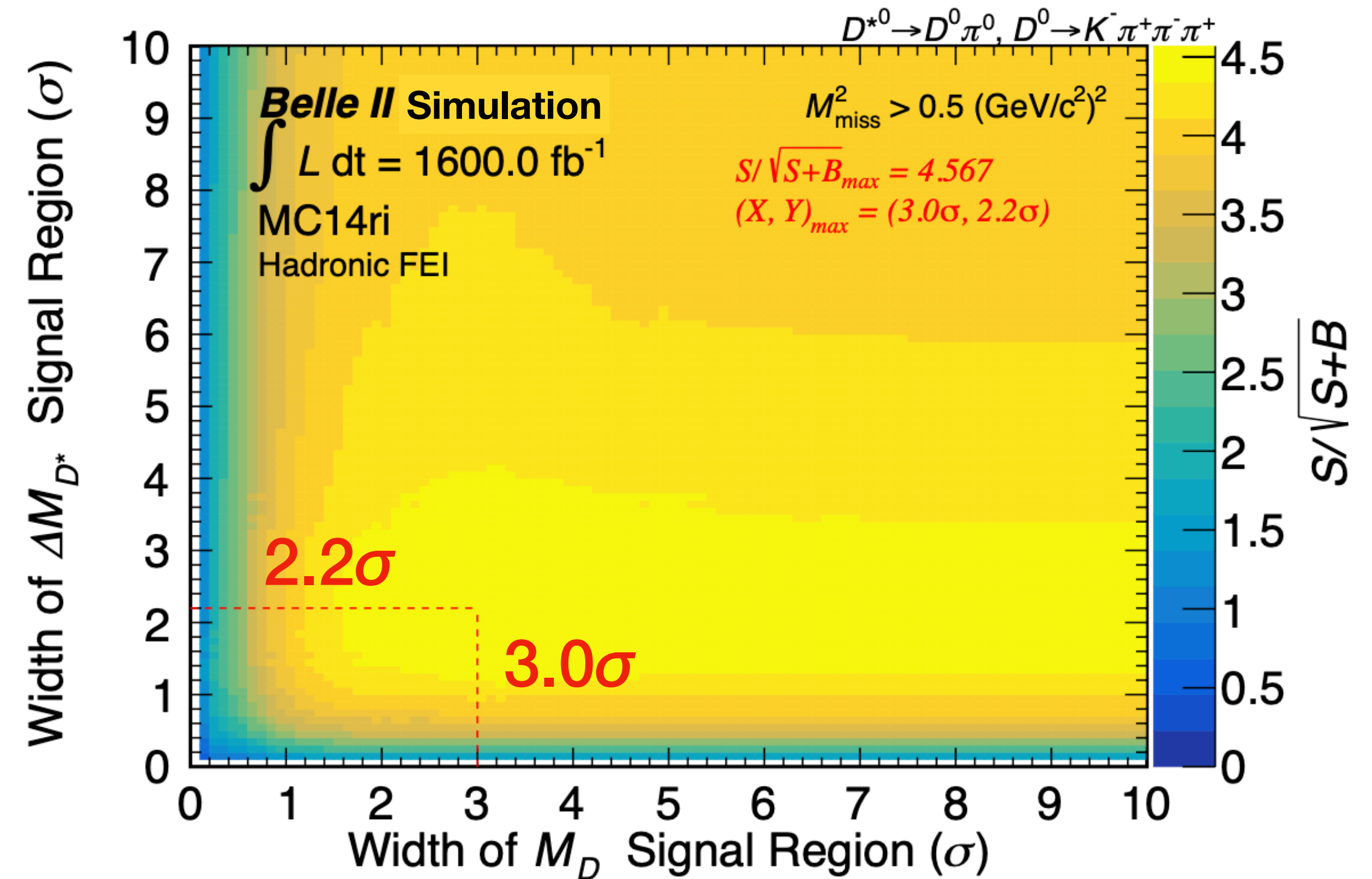
- Reconstruct  $B \rightarrow D^* \tau \nu$  and  $B \rightarrow D^* l \nu$  with same selections
- $D$  meson reconstruct with  $K^\pm, \pi^\pm, K_S, \pi^0$ 
  - 8  $D^0$  modes (Br ~36%)
  - 4  $D^+$  modes (Br ~12.3%)
- $D^*$  meson reconstruct with  $D^+/D^0$  and low momentum  $\pi^+/\pi^0$ 
  - $D^{*+} \rightarrow D^0 \pi^+ / D^+ \pi^0$  (Br ~98%)
  - $D^{*0} \rightarrow D^0 \pi^0$  (Br ~65%)
- $\tau$  lepton reconstruct with  $l (e, \mu) \bar{\nu} \nu$
- Both neutral and charged  $B^\pm / B^0$  mesons reconstruct with  $D^{*+} / D^{*0}$  and  $\tau / l = (e, \mu)$



# Improvement of reconstruction at Belle II



$$\Delta M_{D^*} (= M_{D^*} - M_D)$$

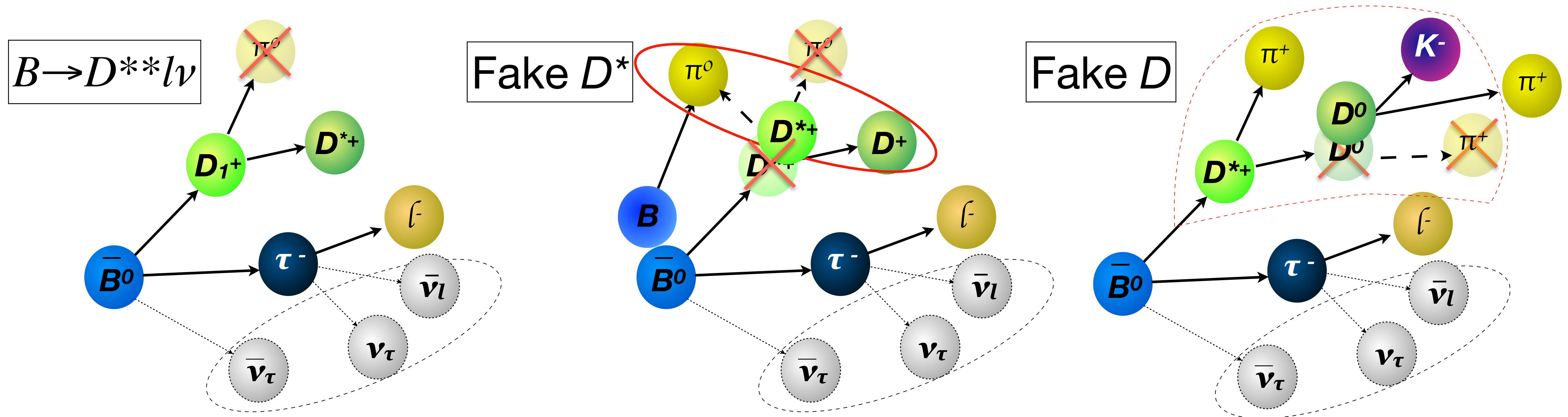


- Improve the reconstruction methodology at Belle II
  - Keep reasonably large reconstruction candidates
  - Found the maximum of FOM  $N_{\text{signal}} / \sqrt{N_{\text{signal}} + N_{\text{background}}}$ , by scanning the optimal selections
  - Improve **35%** of FOM vs. Belle '15 hadronic tag  $R(D^{(*)})$  analysis

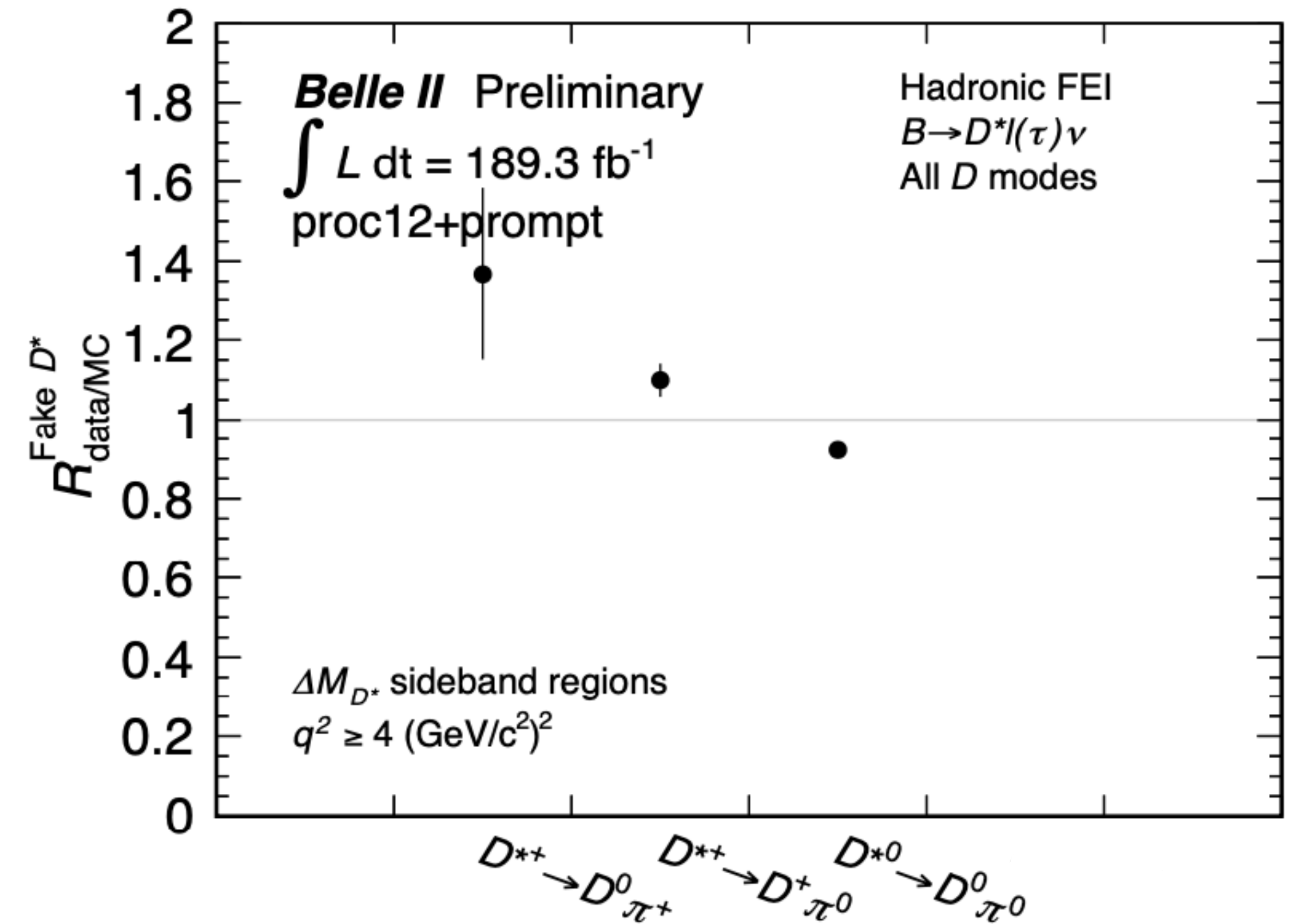
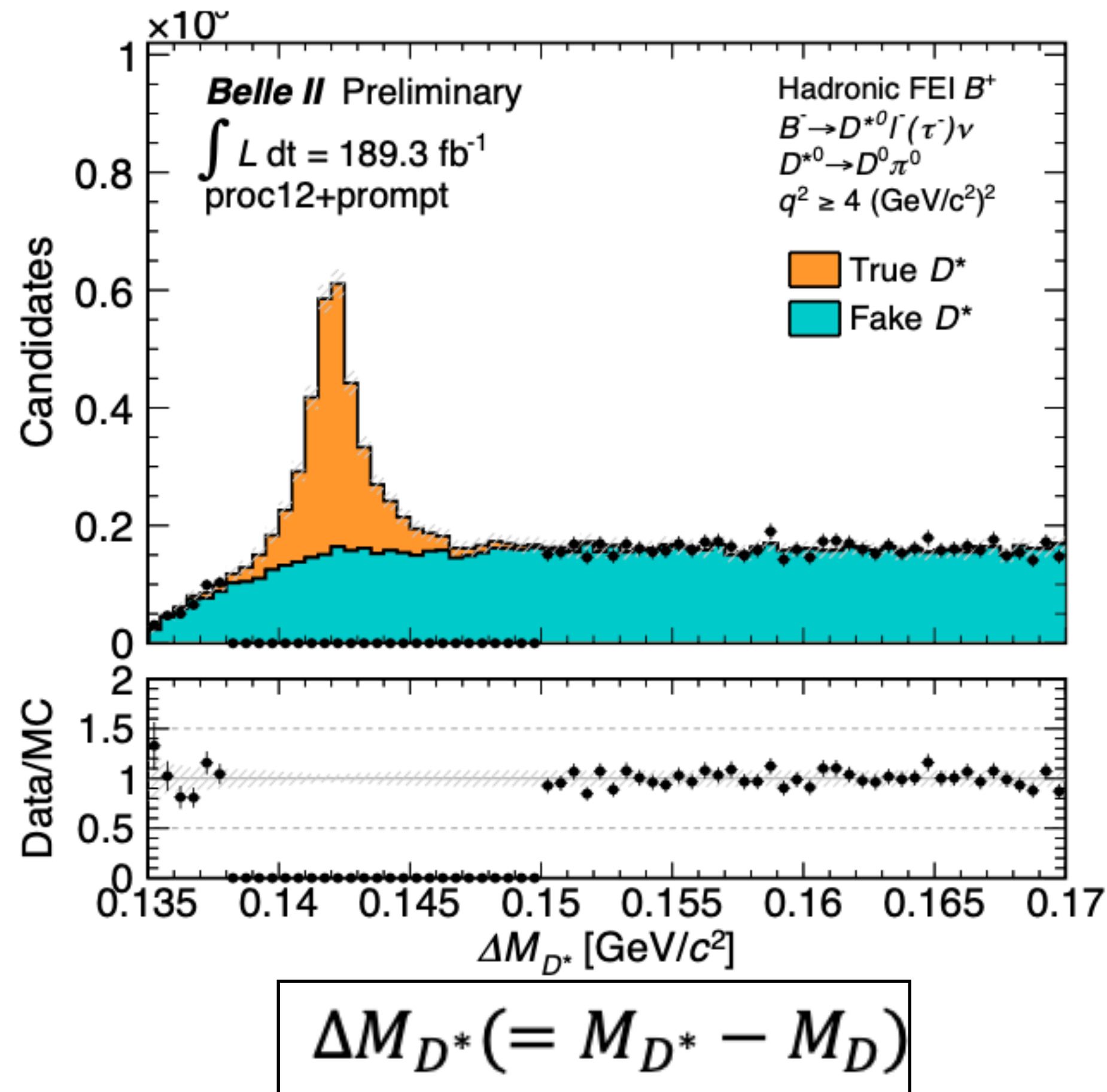
# Dominant backgrounds

- Fraction of survived  $B$  candidates in each category after event selections are estimated based on Belle II MC simulation

$B$ candidates	$B \rightarrow D^* \tau \nu$	$B \rightarrow D^* l \nu$	Background Truth $D^{(*)}$	Background Fake $D^{(*)}$
			$B \rightarrow D^{**} l \nu, B \rightarrow D^{(*)} X, B^0 \leftrightarrow B^\pm, \dots$	
$B^0$	2.7%	65.5%	12.5%	19.2%
$B^\pm$	1.7%	34.7%	5.9%	57.8%



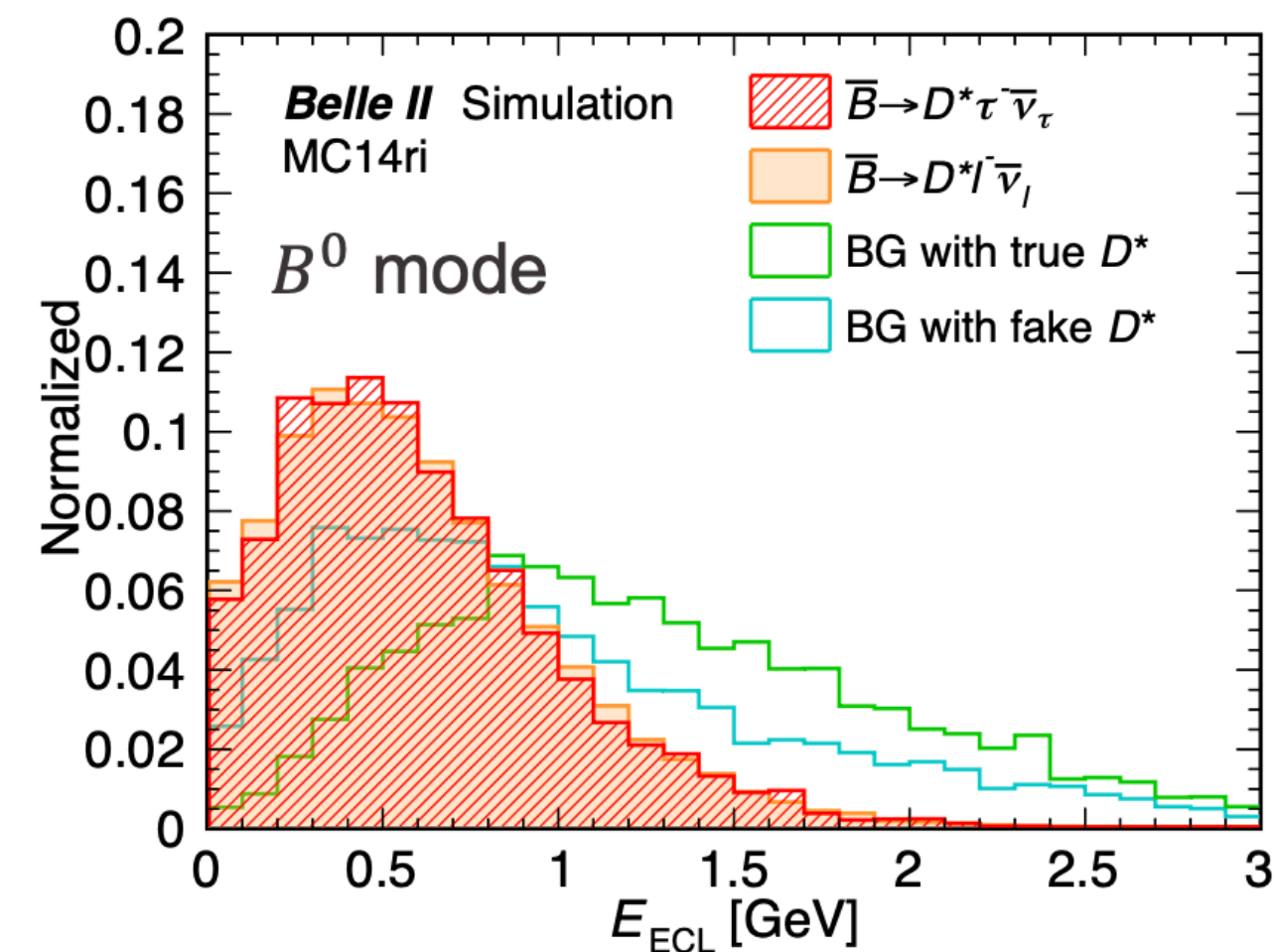
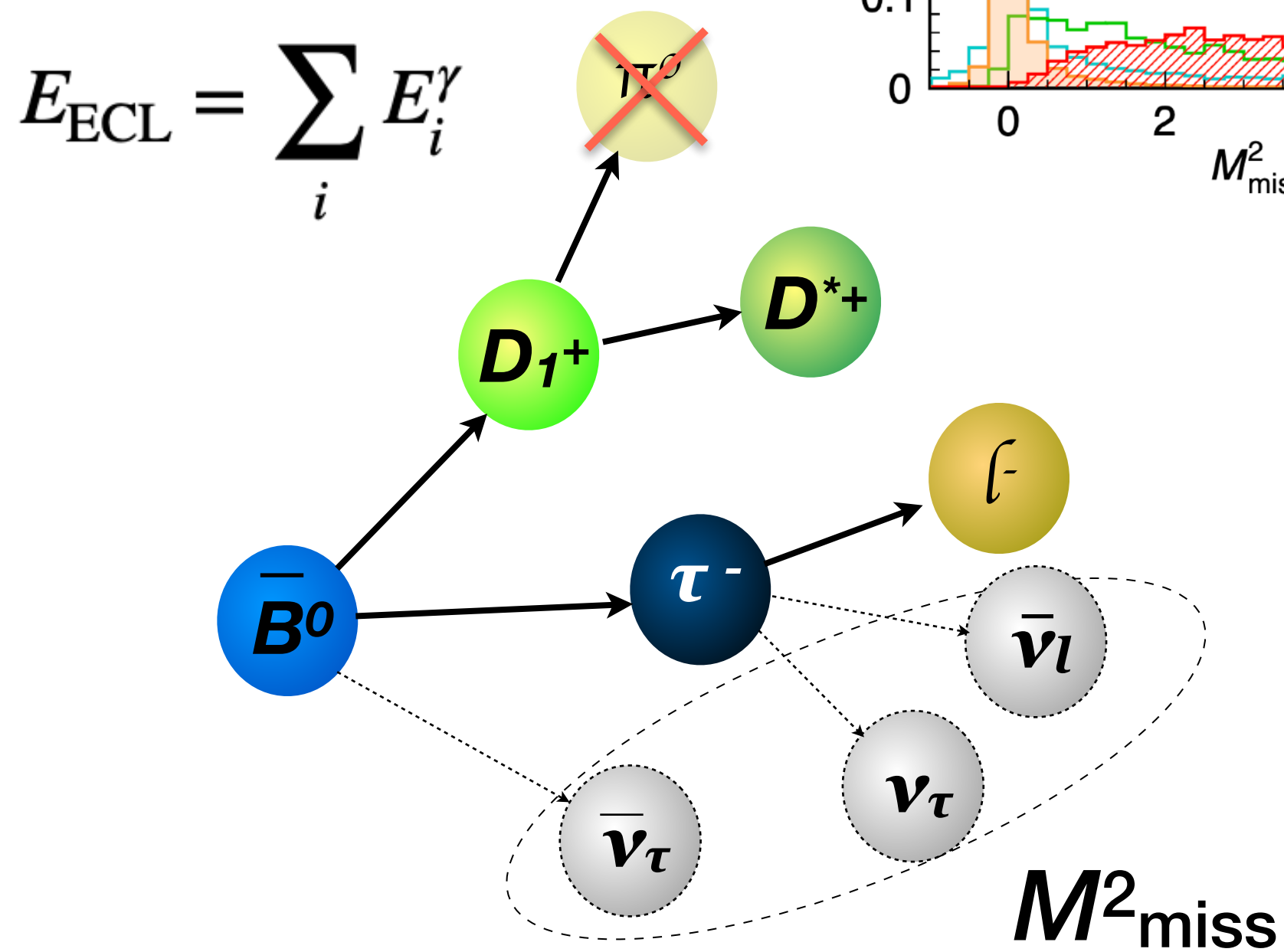
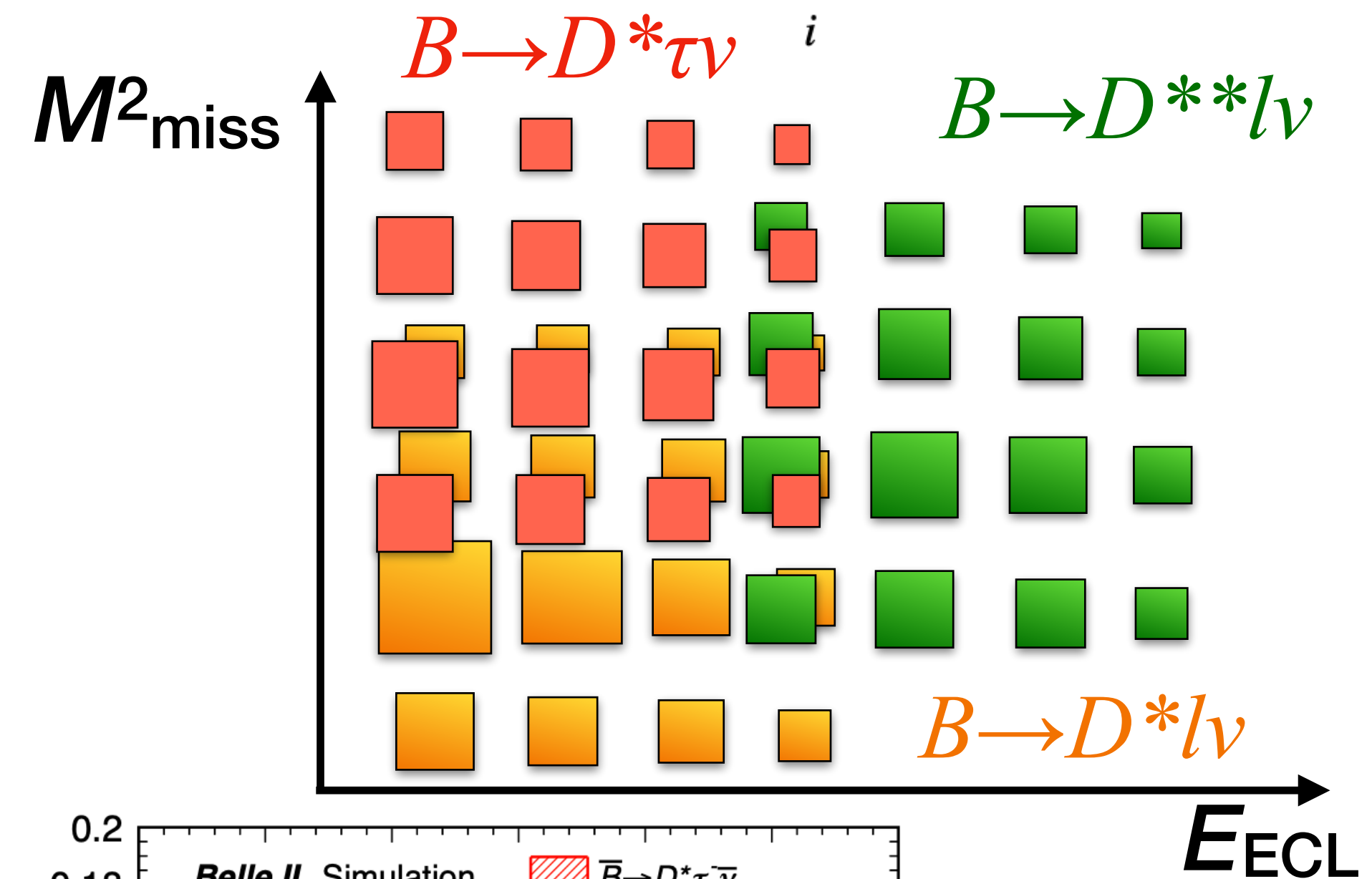
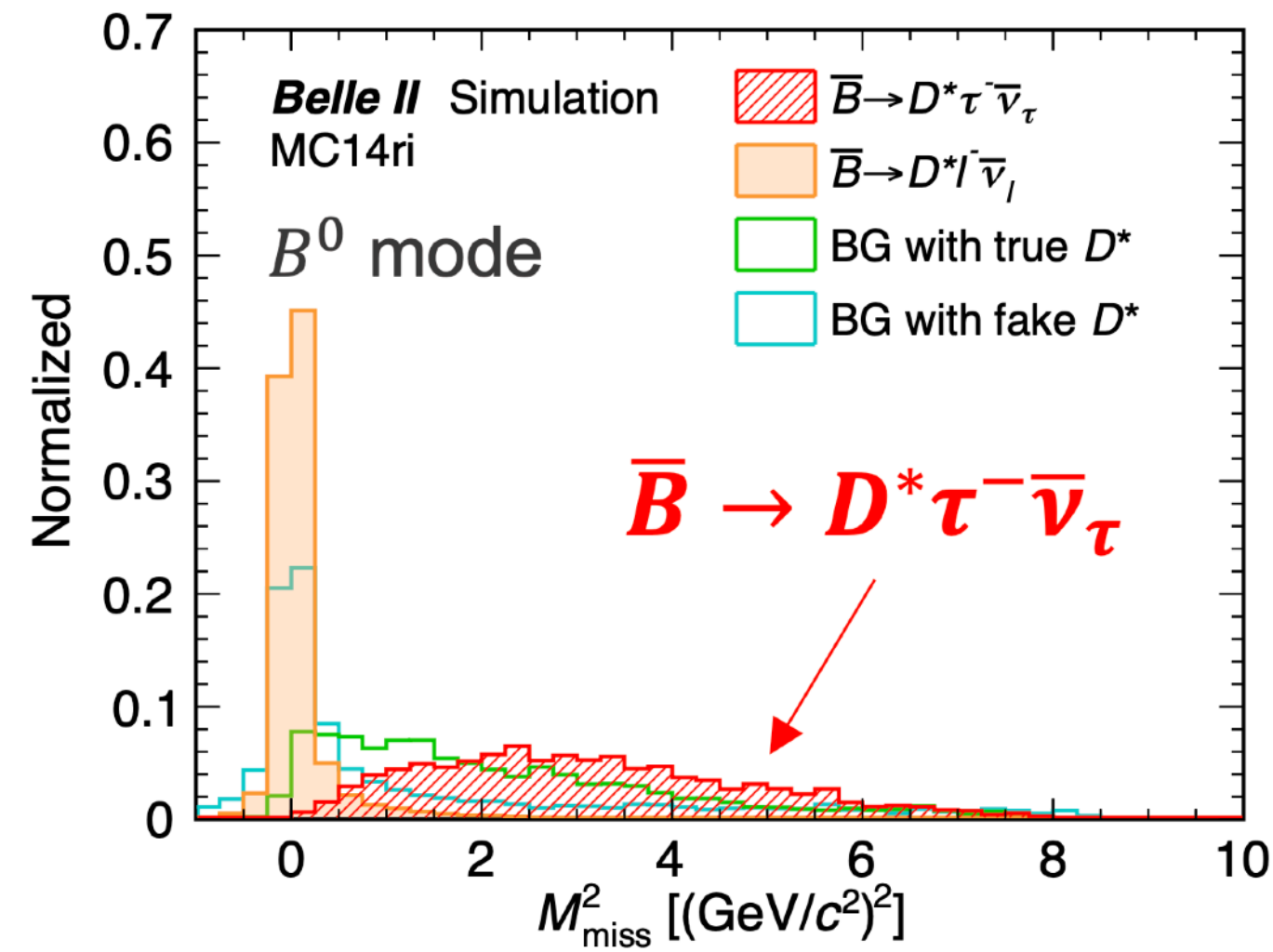
# Calibration of fake $D^*$ background on $\Delta M_{D^*}$ sideband



- Estimate the most dominate background (fake  $D^*$ ) using  $\Delta M_{D^*}$  sideband
  - Fit  $\Delta M_{D^*}$  distribution at sideband, threshold or Chebychev functions
  - Obtain a calibration factor

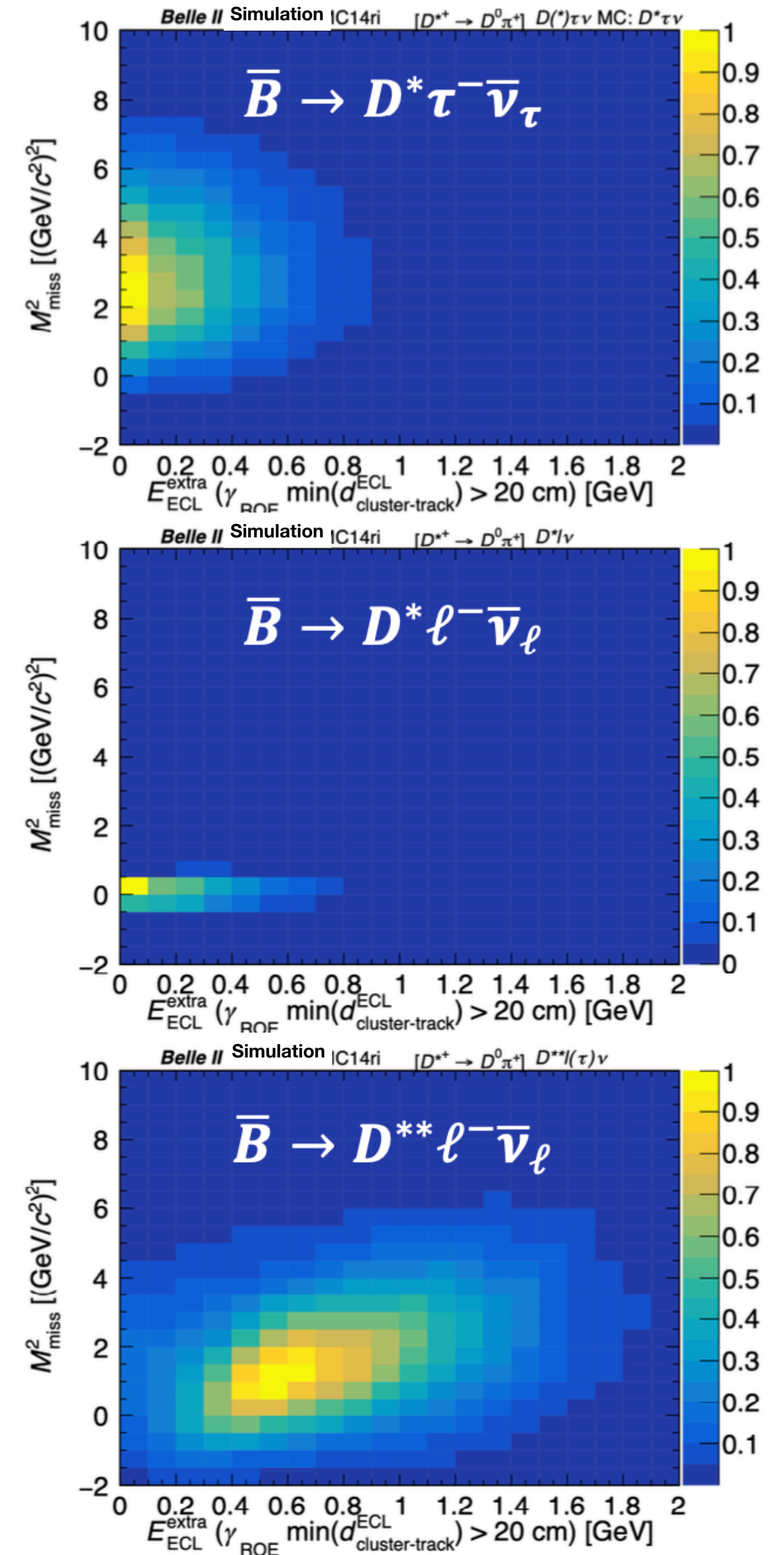
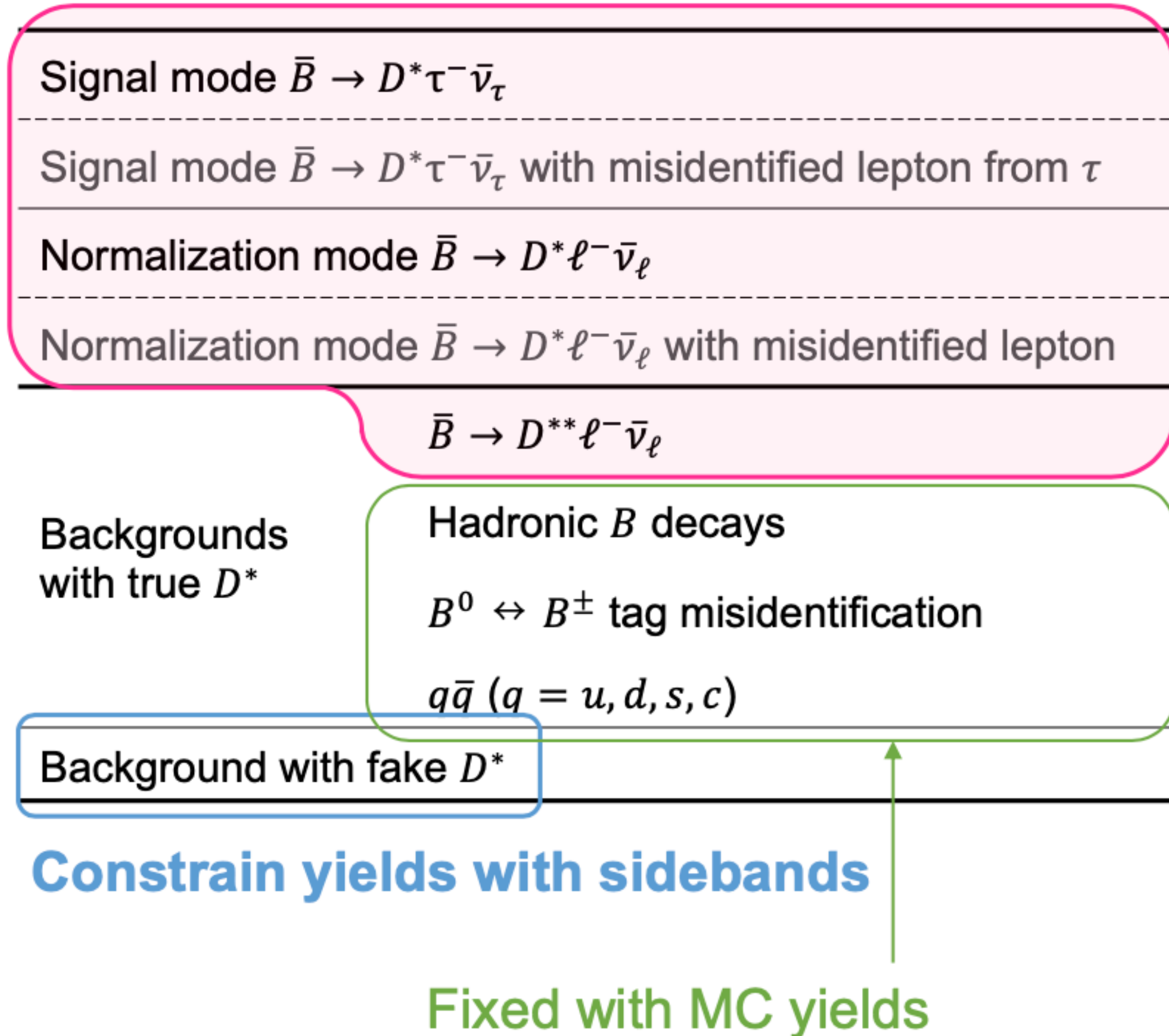
# Fitting methodology and variables

- Extracting  $B \rightarrow D^* \tau \nu$ ,  $B \rightarrow D^* l \nu$  yields by a two-dimensional simultaneously fit
  - $M^2_{\text{miss}} = (\mathbf{p}_{\text{beam}} - \mathbf{p}_{B\text{tag}} - \mathbf{p}_{D^*} - \mathbf{p}_l)^2$
  - $E_{\text{ECL}}$  unassigned neutral energy in the calorimeter  $E_{\text{ECL}} = \sum_i E_i^\gamma$



# Fit configuration

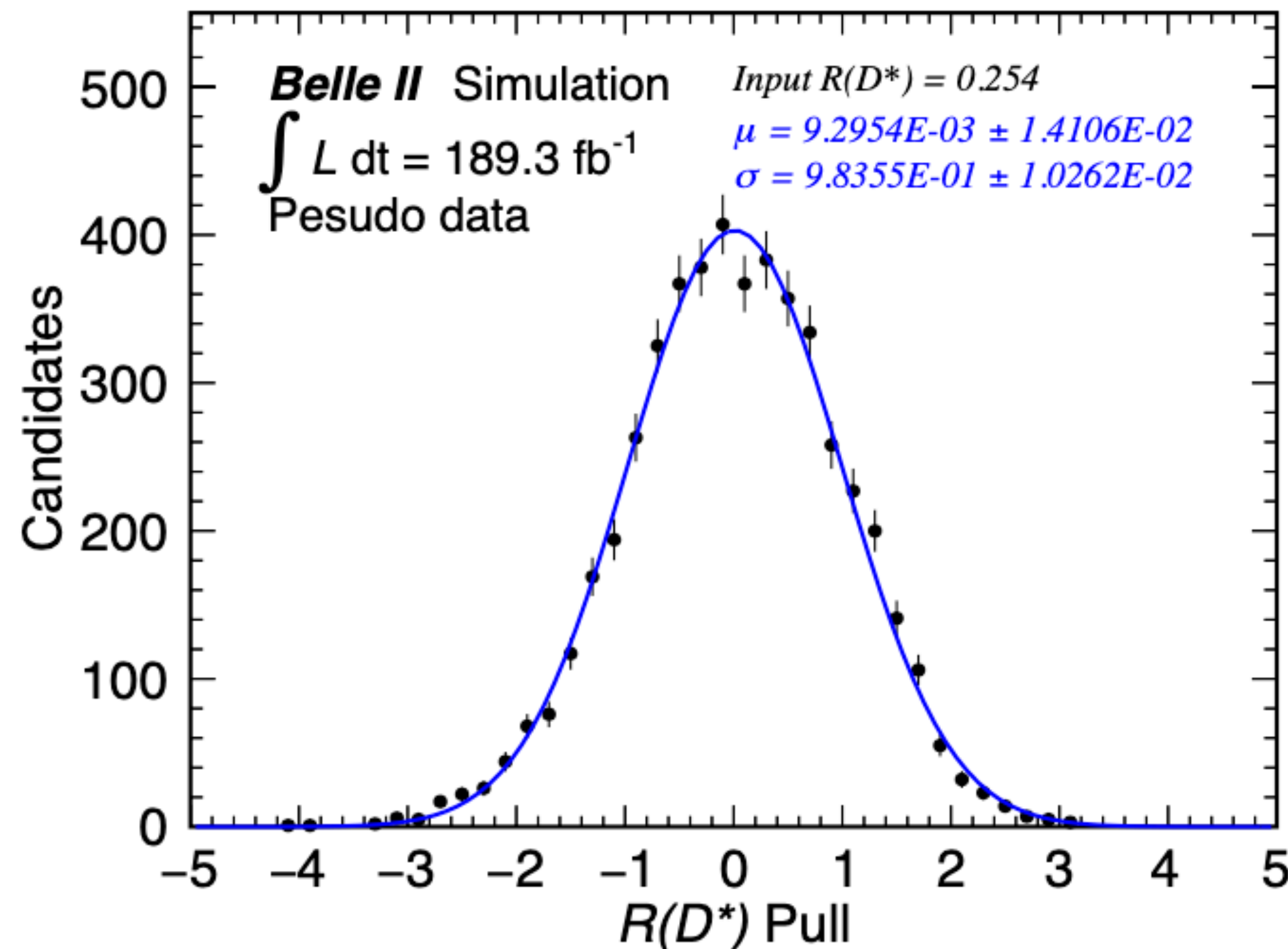
- PDFs in two dimensions with uniform 24  $M^2_{\text{miss}}$  bins and 20  $E_{\text{ECL}}$  bins after kernel density estimation
- $R(D^*)$  obtained by simultaneous fits among three  $D^*$  modes



# Fitter validation with pseudo data

- Producing 5000 random pseudo data set with  $189 \text{ fb}^{-1}$  based on PDF where  $R(D^*) = 0.254$  (SM expectation)
- The fitter performance confirmed by  $R(D^*)$  pull distribution
- Linearity check of fitter has also been confirmed based on Asimov fit method, by scanned input  $R(D^*)$  in the range of 0.01 to 5.0

↑  
[Eur.Phys.J.C71:1554,2011](#)

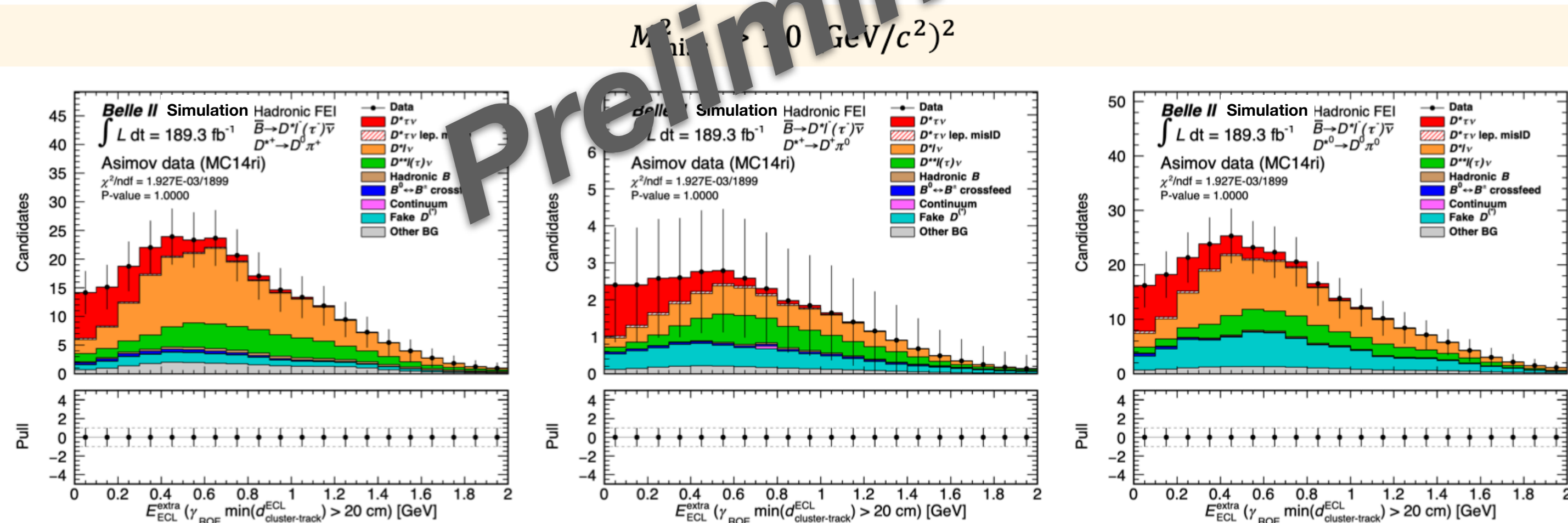
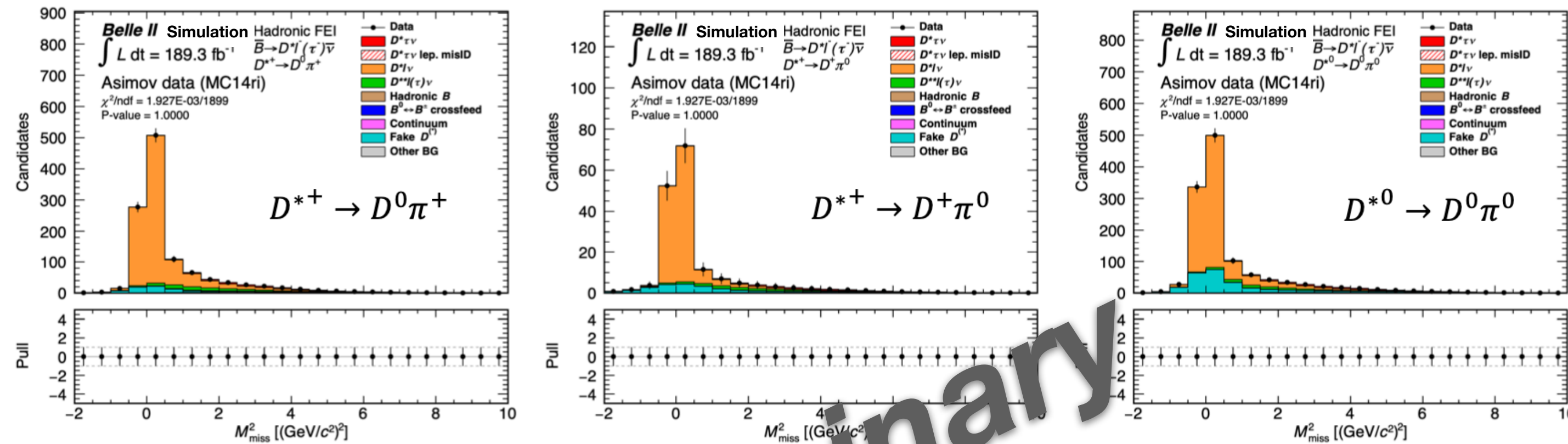


$$\mu = 0.009 \pm 0.014$$
$$\sigma = 0.984 \pm 0.010$$



# Belle II $R(D^*)$ sensitivity at $189 \text{ fb}^{-1}$

- Producing **Asimov MC data set** with  $189 \text{ fb}^{-1}$  based on PDF where  $R(D^*) = 0.254$  (SM expectation)
- The fit returns  $R(D^*) = 0.254$ , statistical uncertainty is **+18/-17%** at  $189 \text{ fb}^{-1}$
- Belle '15 statistical uncertainty is 13% (15% @  $R(D^*) = 0.254$ )



$$R(D^*) = 0.254^{+0.046}_{-0.043} \left( \begin{array}{l} +18 \\ -17 \end{array} \% \right)$$

# Preliminary systematic uncertainties

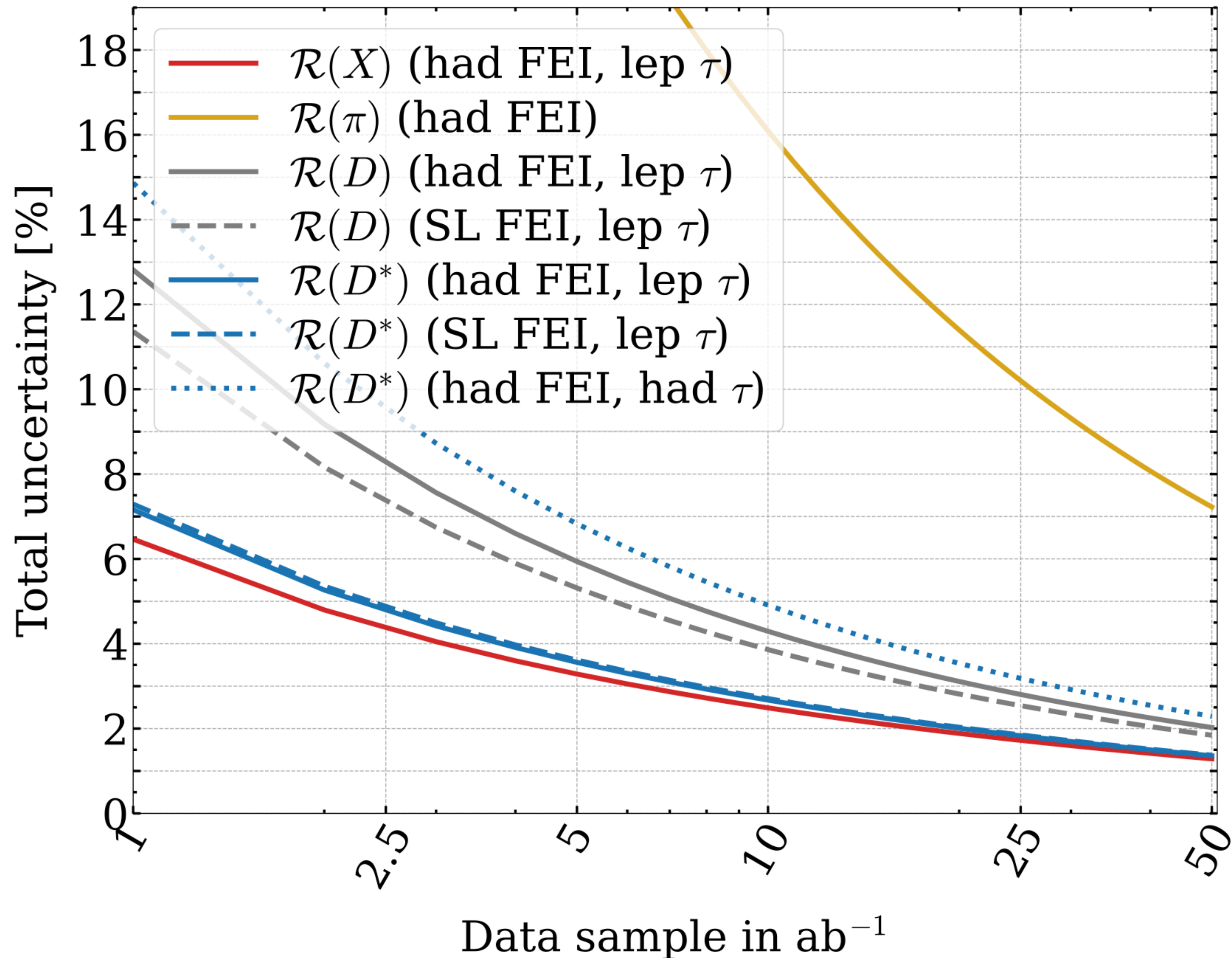
- Each source of the uncertainty changes the PDF shape, consequently modify the fitted  $R(D^*)$  value
  - Generate PDFs by fluctuating one of the uncertainty sources
  - Fitting the fluctuated PDFs to the nominal pseudo data (un-fluctuated PDF)
  - Repeating the fit by 1000 times (fluctuate PDFs follow Gaussian) to obtain the  $\Delta R(D^*)$
- Asymmetric errors  $\mu+\sigma$  and  $\mu-\sigma$  from fitting  $\Delta R(D^*)$  distribution as systematic uncertainties

Source	Uncertainty	
Statistical uncertainty	+0.046 -0.043	+18.1% -17.0%
MC statistics	+0.010 -0.007	+4.1% -2.7%
$B \rightarrow D^{**} l \nu$ branching ratios	+0.012 -0.010	+2.7% -1.9%
...		

Statistical uncertainty dominated

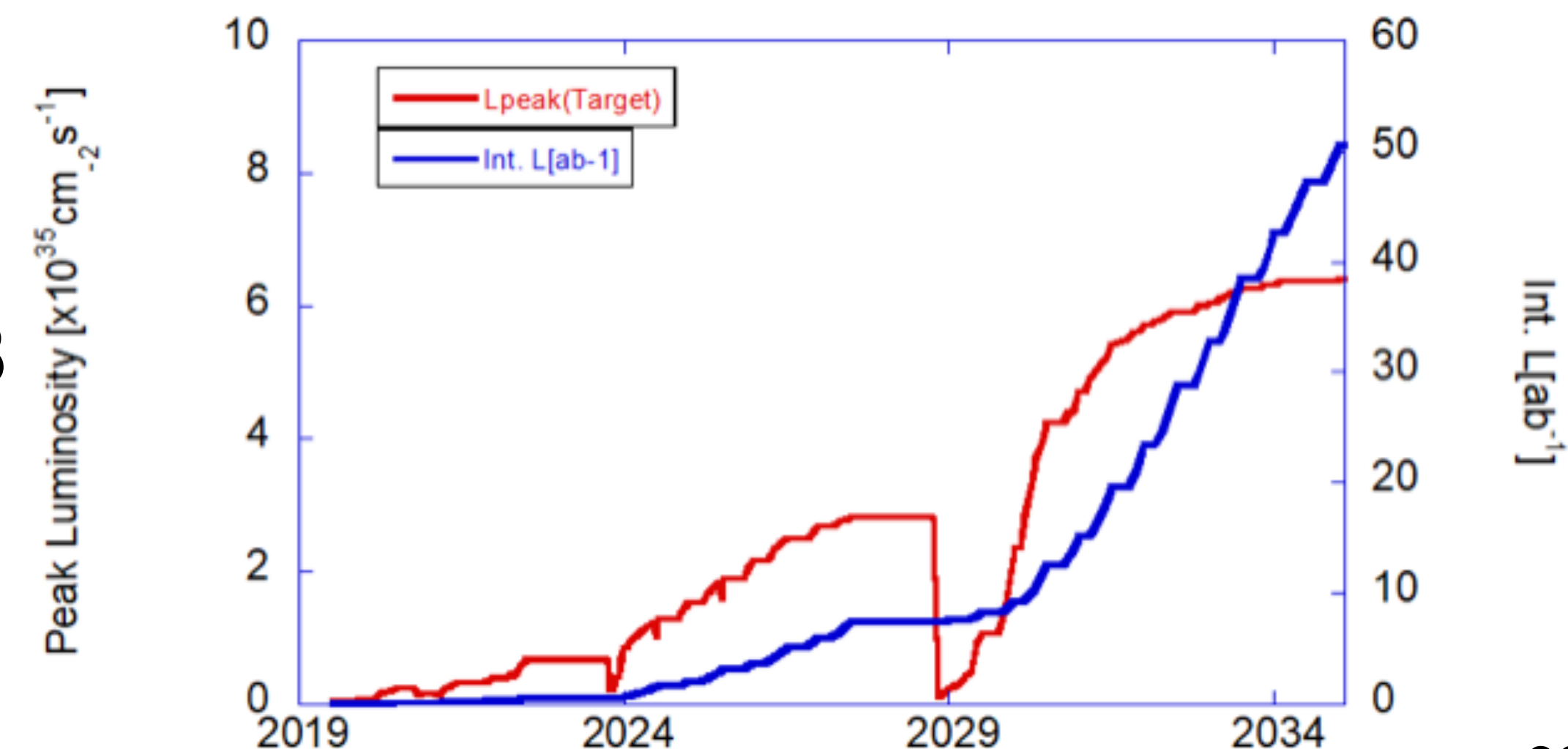
# Expected sensitivity of $R(D^*)$ at Belle II

[arXiv:2207.06307](https://arxiv.org/abs/2207.06307)



# Summary and prospects

- $R(D^*)$  shows  $3.2\sigma$  deviation between experimental average value and standard model prediction
  - Hint of Lepton Flavor Universality Violation
- Measurement of  $R(D^*)$  with hadronic tagging based on **189 fb<sup>-1</sup>** Belle II data
  - Established the analysis framework
  - Selection optimization improve FOM by **35%** compare to Belle '15 analysis
  - Expected statistical uncertainty is **+18/-17%** at 189 fb<sup>-1</sup>
  - Evaluated most of the systematic uncertainty, <- statistical uncertainty dominated with 189 fb<sup>-1</sup> data
- First  $R(D^*)$  measurement at Belle II using 189 fb<sup>-1</sup> data-set targeting the end of spring 2023



# Backup

# Reconstruction selections

$B_{\text{tag}}$	$\mathcal{P}_{B_{\text{tag}}} > 0.001$ and $M_{bc, B_{\text{tag}}} > 5.27 \text{ GeV}/c^2$ and $-0.15 < \Delta E_{B_{\text{tag}}} < 0.1 \text{ GeV}$	
good track	$dr < 2.0$ and $ dz  < 4.0$ and $p_t > 0.1 \text{ GeV}/c$	
# of tracks	The number of good tracks $> 4$	
$\pi^+, K^+$ from $D$	[good track] and $n\text{CDCHits} > 20$ and $\mathcal{P}_K^{\text{binary}} > 0.1, \mathcal{P}_\pi^{\text{binary}} > 0.1$	
$\pi^0$	$\text{pi0:eff40\_May2020}$ and $\gamma: \text{clusterTiming}  < 200 \text{ ns}$	
$K_S^0$	$\text{KS0:merged}$ and $\text{significanceOfDistance} > 3$ (before $B_{\text{sig}}$ vertex fit)	
$D$	$1.78 < M_D < 1.92 \text{ GeV}/c^2$	
$\gamma_{\text{low}}$	$\text{gamma:eff40\_May2020}$ and $ \text{clusterTiming}  < 200 \text{ ns}$	
$\pi_{\text{slow}}^0$	$\text{pi0:eff50\_May2020}$ and $\gamma: \text{clusterTiming}  < 200 \text{ ns}$	
$\pi_{\text{slow}}^+$	$dr < 2.0$ and $ dz  < 4.0$ and $p > 0.05 \text{ GeV}/c$	
$D^*$	$0.130 < \Delta M_{D^*} < 0.170 \text{ GeV}/c^2$ ( $0.100 < \Delta M_{D^*} < 0.190 \text{ GeV}/c^2$ ) for $D^{*+}(D^{*0})$	
$e, \mu$	[good track] and $\mathcal{P}_\mu^{\text{global}} > 0.9, \mathcal{P}_e^{\text{global}} > 0.9$	
$B_{\text{sig}}$ vertex fit	<ol style="list-style-type: none"> <li><code>treeFit('B0(B+):sig', conf_level=0.0, ipConstraint=False, updateAllDaughters=True, massConstaint=[K_S0, pi0], path=path)</code></li> <li><code>treeFit('B0(B+):sig', conf_level=-1.0, ipConstraint=False, updateAllDaughters=True, massConstaint=[D*0, D*+, D0, D+, K_S0, pi0], path=path)</code></li> </ol>	
ROE	Charged	$ dr  < 5.0$ and $ dz  < 20.0$ and $p_t > 0.1 \text{ GeV}/c$ and $n\text{CDCHits} > 0$
	Neutral	$\text{gamma:eff40\_May2020}$ and $ \text{clusterTiming}  < 200 \text{ ns}$
		$\text{roeCharge} == 0$ and $\text{ROE\_nTracks} == 0$

Tag  $B$  meson

Tracks

Hadrons

Neutrals

Leptons

Constraint  $D^{(*)}$  daughter's masses to improve  $D^{(*)}$  selections

Constraint  $D^{(*)}$  masses additionally to improve  $M_{\text{miss}}^2$  resolution

Vertex

Neutrals of Rest of event

# Belle II - LHCb comparison

