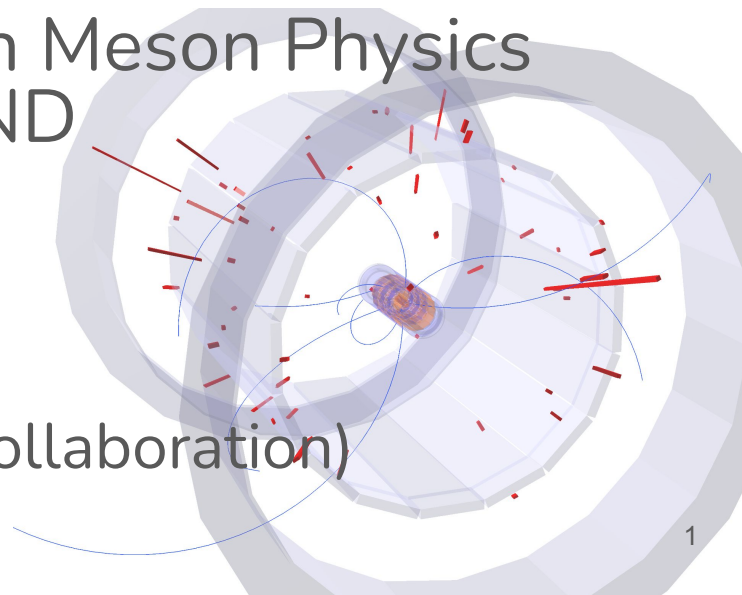


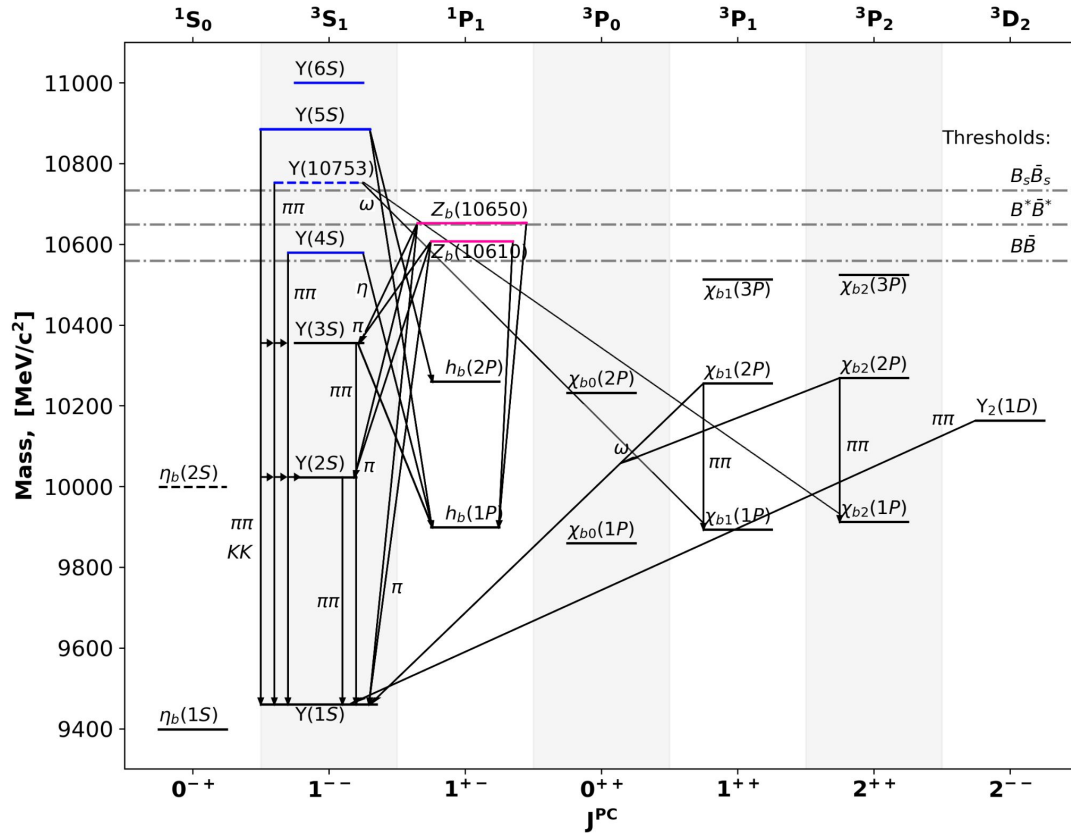
Quarkonium at Belle II

17th International Workshop on Meson Physics
KRAKÓW, POLAND
22nd - 27th June 2023

Pavel Oskin
(on behalf of the Belle II Collaboration)



Bottomonium



Two types of states:

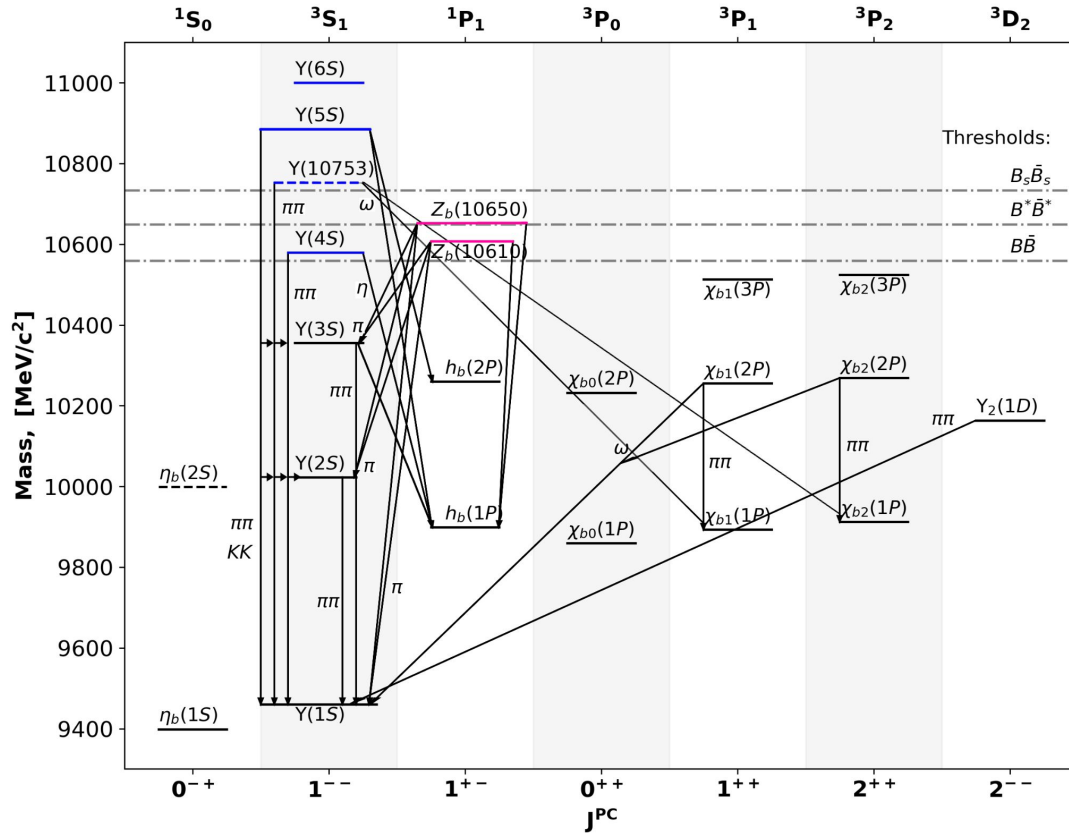
Below B̄B̄ threshold states are well described by the potential models;

Above B̄B̄ threshold states demonstrate unexpected properties:

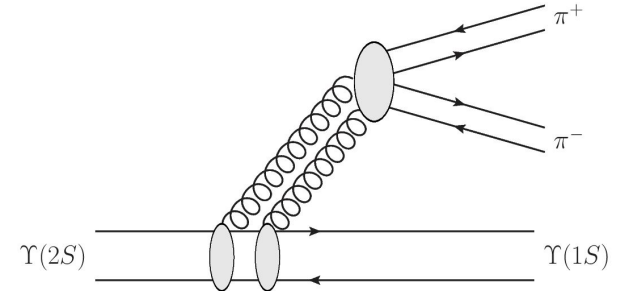
- ❑ Hadronic transitions are strongly enhanced (OZI rule violation);
- ❑ η transitions are not suppressed compare to π⁺π⁻ transitions (HQSS violation);
- ❑ Two charged Z_b⁺ states are observed;

Conventional bottomonium (pure b**̄** states)
 Bottomonium-like states (mix of b**̄** and B̄B̄)
 Purely exotic charged states (Z_b⁺).

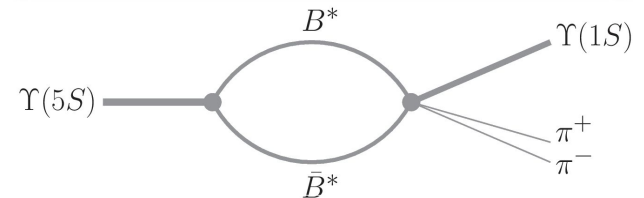
Bottomonium



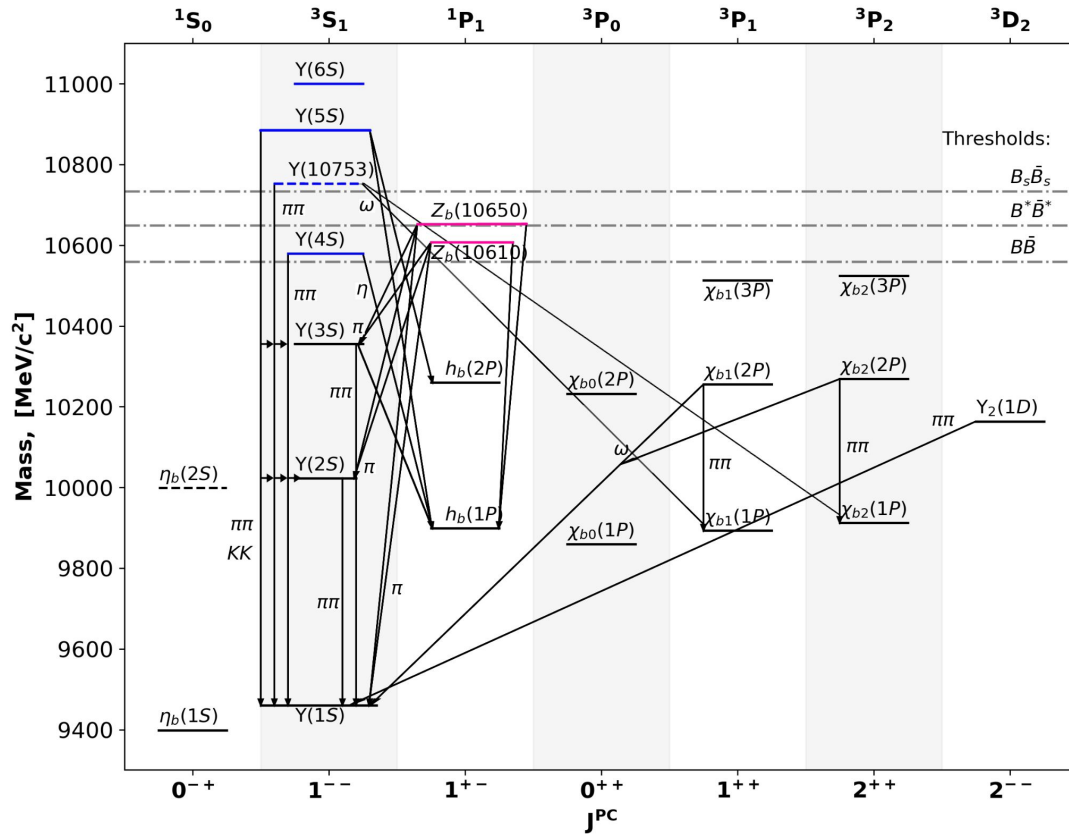
Hadronic transitions from the states **below the B B̄ threshold** are described by gluon emission (QCDME):



Hadronic transitions from the states **above the B B̄ threshold** can be enhanced due to **B B̄ mesons rescattering**:



Bottomonium



Z_b^+ states masses coincide with $B\bar{B}^*$ $B^*\bar{B}^*$ thresholds and decays dominantly to constituent mesons:

Z_b decay mode	Branching fraction
$Z_b^+(10610) \rightarrow \Upsilon(nS)/h_b(mP)\pi^+$	$14.4^{+2.5}_{-1.9}\%$
$Z_b^+(10610) \rightarrow B^+\bar{B}^{*0}/\bar{B}^0B^{*+}$	$85.6^{+2.1}_{-2.9}\%$
$Z_b^+(10650) \rightarrow \Upsilon(nS)/h_b(mP)\pi^+$	$26.6^{+5.0}_{-4.7}\%$
$Z_b^+(10650) \rightarrow B^{*+}\bar{B}^{*0}$	$74^{+4}_{-6}\%$

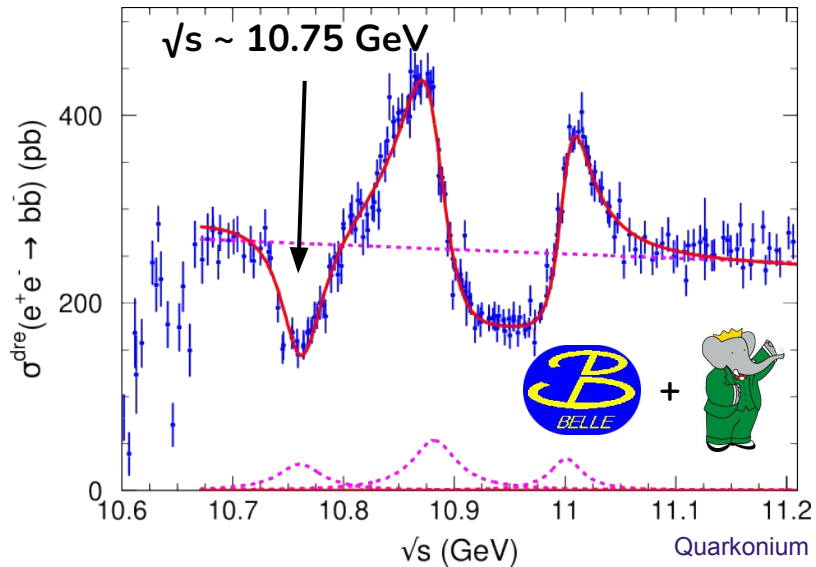
This is a strong indication of the **molecular nature of Z_b^+ states.**

PRL, 108, 122001 (2012)

Discovery of $\Upsilon(10753)$

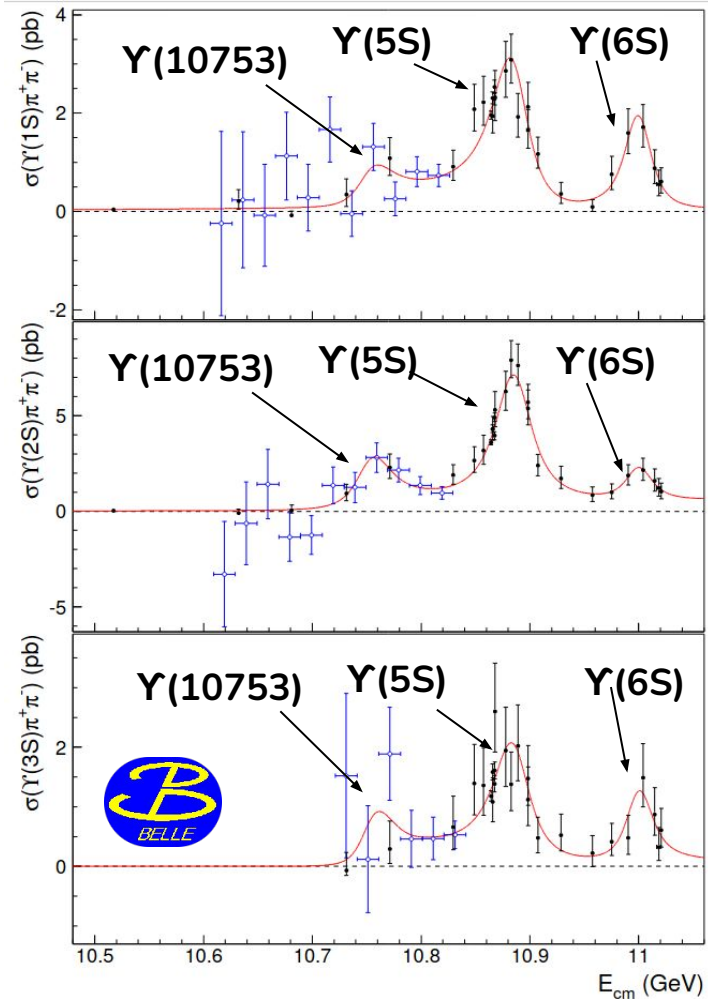
Observed in the $e^+ e^- \rightarrow \Upsilon(nS) \pi^+ \pi^-$ ($n = 1, 2, 3$) cross section energy dependence by Belle (JHEP 10 (2019) 220):

	$\Upsilon(10860)$	$\Upsilon(11020)$	New structure
M (MeV/ c^2)	$10885.3 \pm 1.5^{+2.2}_{-0.9}$	$11000.0^{+4.0}_{-4.5} +^{1.0}_{-1.3}$	$10752.7 \pm 5.9^{+0.7}_{-1.1}$
Γ (MeV)	$36.6^{+4.5}_{-3.9} +^{0.5}_{-1.1}$	$23.8^{+8.0}_{-6.8} +^{0.7}_{-1.8}$	$35.5^{+17.6}_{-11.3} +^{3.9}_{-3.3}$



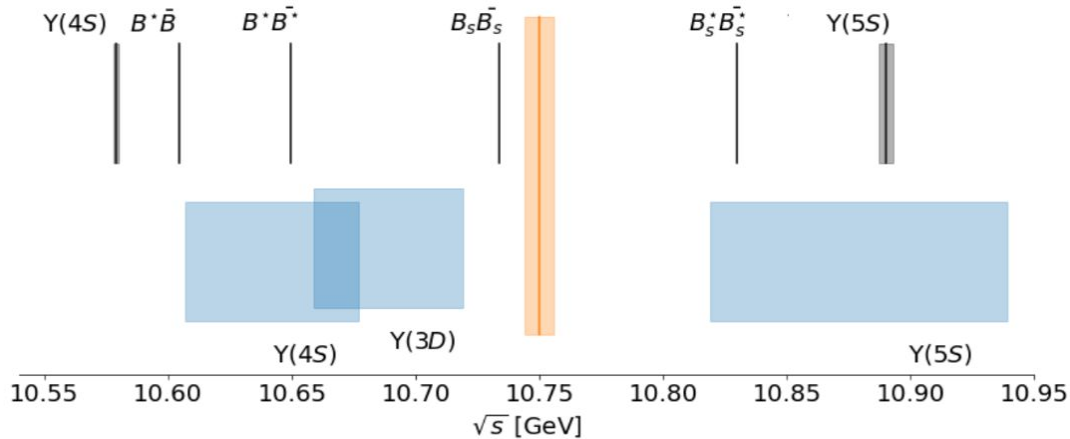
A dip in $\sigma(e^+ e^- \rightarrow b\bar{b})$ can be described by $\Upsilon(10753)$
CPC 44, 8, 083001
(2020)

Quarkonium at Belle II / Pavel Oskin / MESON 2023



What is the nature of $\Upsilon(10753)$?

- Far from the thresholds;



- Mass does not match $\Upsilon(3D)$ theoretical predictions, and D-wave states are not seen in e^+e^- collisions;
- $\Upsilon(4S) - \Upsilon(3D)$ mixing can be enhanced due to hadron loops.

- Tetraquark state:
[CPC **43**, 12, 123102 \(2019\)](#),
[PLB, **802**, 135217 \(2020\)](#),

- Hadronic molecule with a small admixture of a bottomonium:
[PRD **103**, 074507 \(2021\)](#)

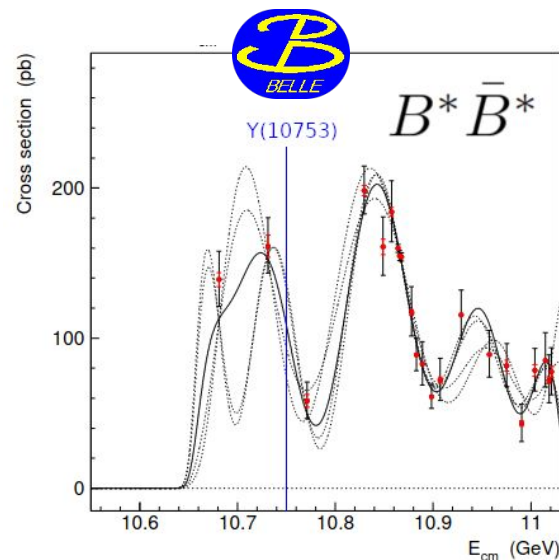
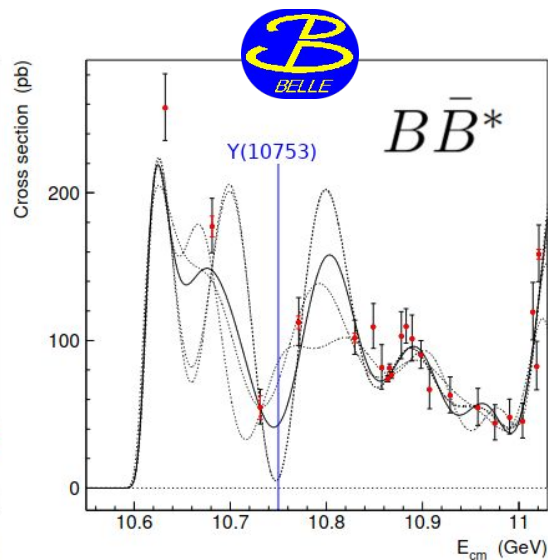
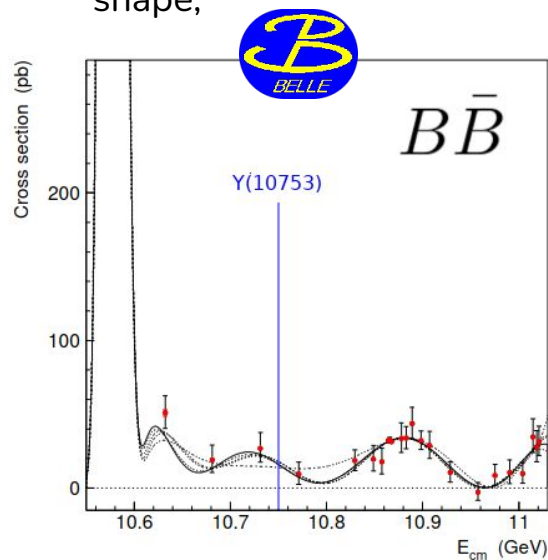
- Hybrid state:
[PRD **99**, 1, 014017 \(2019\)](#)

- Conventional $b\bar{b}$ state:
[EPJC **80**, 1, 59 \(2020\)](#)
[PLB **803**, 135340 \(2020\)](#)
[PRD **102**, 1, 014036 \(2020\)](#)
[PRD **101**, 1, 014020 \(2020\)](#)
[PRD **104**, 034036 \(2021\)](#)
[PRD **105**, 074007 \(2022\)](#)
[PRD **106**, 094013 \(2022\)](#)
[EPJC **137**, 357 \(2022\)](#)

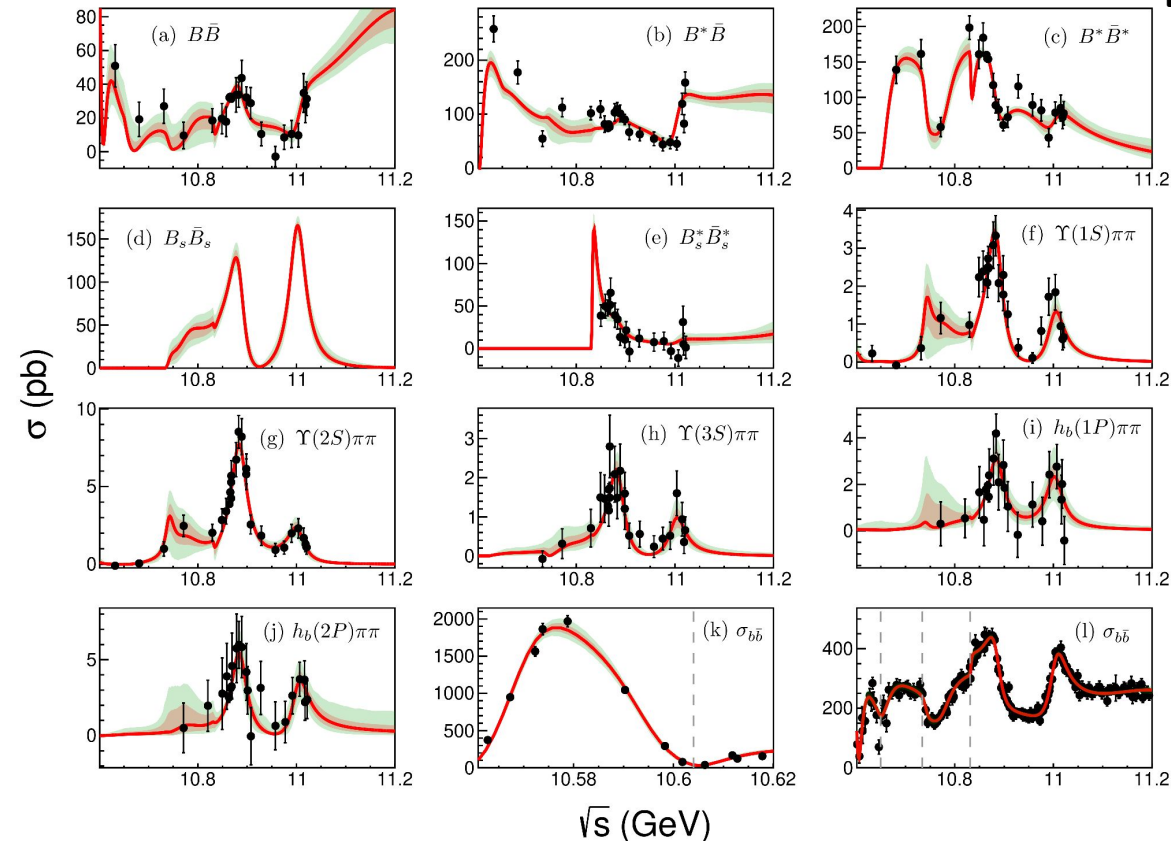
Study of $e^+e^- \rightarrow B^{(*)}\bar{B}^{(*)}$

- ❑ $\sigma(e^+e^- \rightarrow B^{(*)}\bar{B}^{(*)})$ energy dependence show complicated spectra, that hard to describe with resonance shapes;
- ❑ Rescattering and opening of the various $B\bar{B}$ thresholds cause oscillatory behaviour due to the **coupled-channel effect**;
- ❑ **Coupled-channel approach** is necessary to study $\sigma(e^+e^- \rightarrow B^{(*)}\bar{B}^{(*)})$ shape;

JHEP 06 (2021) 137



Global phenomenological analysis



Data:

- ❑ Two-body exclusive cross sections $\sigma(e^+e^- \rightarrow B_{(s)}^{(*)}\bar{B}_{(s)}^{(*)})$;
- ❑ Three-body exclusive cross sections $\sigma(e^+e^- \rightarrow \Upsilon(nS)\pi^+\pi^-)$, $n = 1, 2, 3$;
 $\sigma(e^+e^- \rightarrow h_b(mP)\pi^+\pi^-)$, $m = 1, 2$;
- ❑ Combined Belle and BaBar R_b measurement;
- ❑ **Use coupled-channel approach.**
- ❑ **Poles:** $Y(4S)$, $Y(10753)$, $Y(5S)$ and $Y(6S)$
- ❑ **Results:** pole positions (mass and width), branching fractions, dependence of scattering amplitudes on energy.

PRD 106 (2022) 9, 094013

More data is necessary

- ❑ To study $Y(10753)$ nature;
- ❑ Improve accuracy below $Y(5S)$;

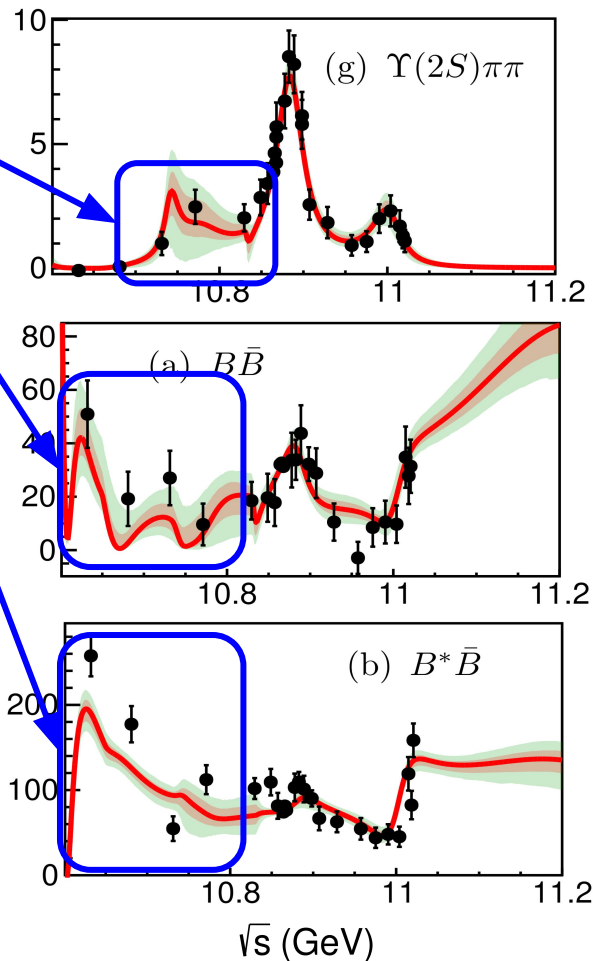


Perform energy scan at the Belle II experiment.

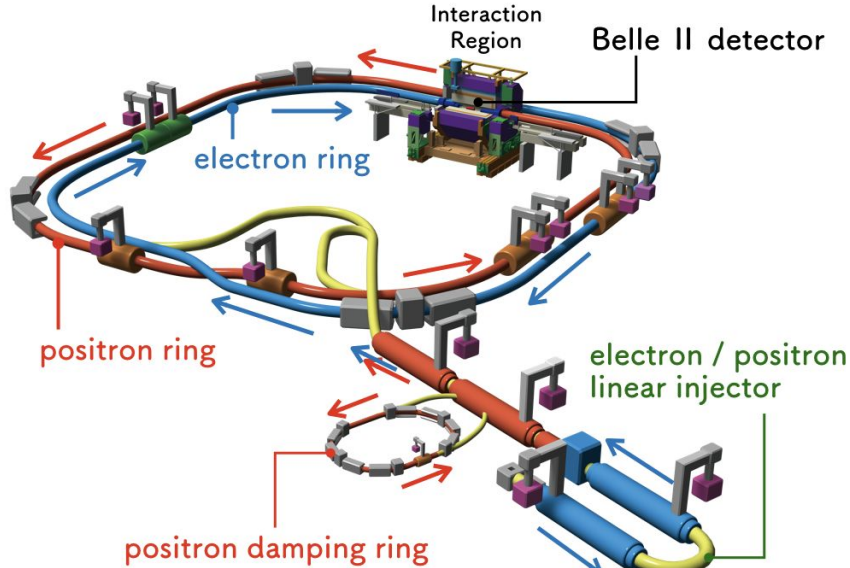


Two Belle II results will be presented:

- ❑ $e^+e^- \rightarrow \omega \chi_{bJ}(1P)$ and $X_b \rightarrow \omega Y(1S)$
- ❑ $e^+e^- \rightarrow B\bar{B}, B\bar{B}^*$ and $B^*\bar{B}^*$

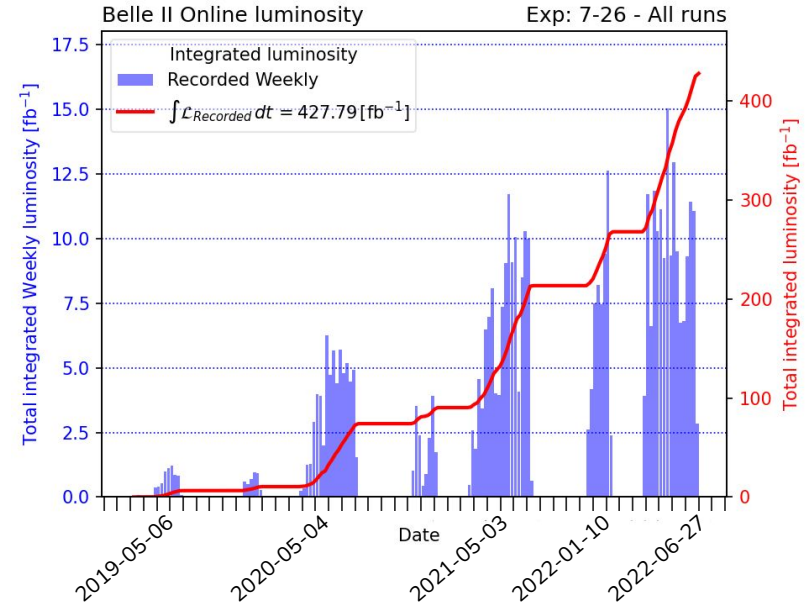


SuperKEKB and Belle II



PTEP 2013, 03A011 (2013)

- Asymmetric e^+e^- collider at KEK (Tsukuba, Japan) provides a unique clean environment;
- Instantaneous luminosity record of $4.7 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$ (x2 of the Belle peak luminosity, current world record);



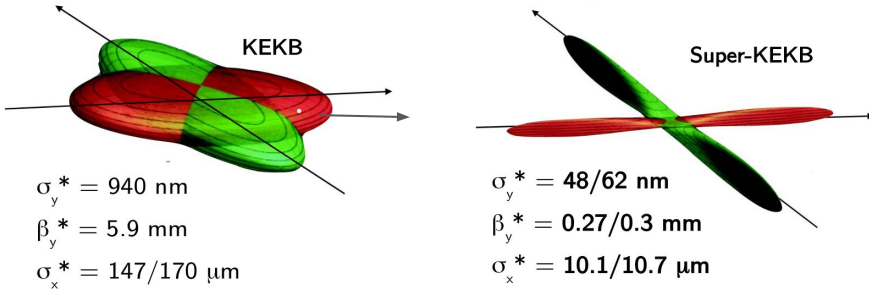
SuperKEKB and Belle II

Beam current increased by **x1.5**.

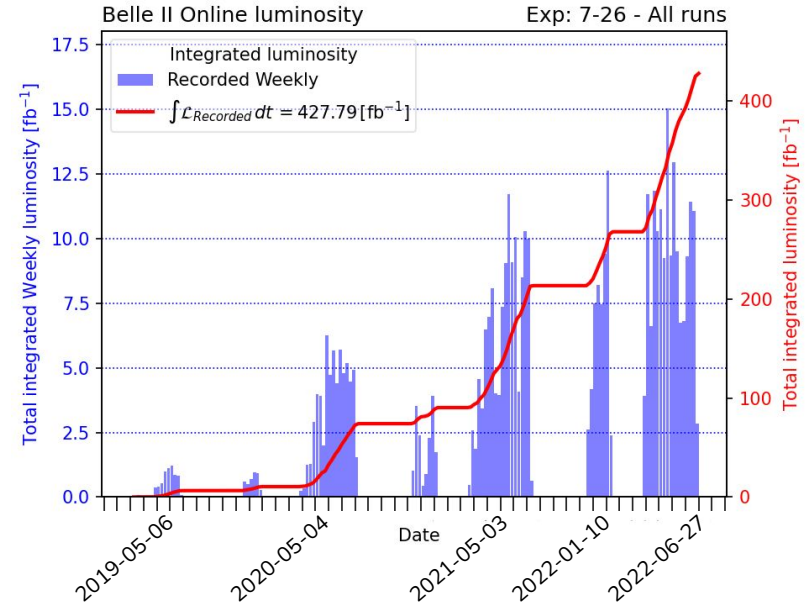
$$L = \frac{\gamma_{\pm}}{2er_e} \left(1 + \frac{\sigma_y^*}{\sigma_x^*} \right) \left(\frac{I_{\pm} \xi_{sy\pm}}{\beta_y^*} \right) \left(\frac{R_L}{R_{\xi_y}} \right)$$

Vertical beta function at IP reduced by **1/20**
"Nano-beam" scheme.

x30 instantaneous luminosity increase



- Asymmetric e^+e^- collider at KEK (Tsukuba, Japan) provides a unique clean environment;
- Instantaneous luminosity record of $4.7 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$ (x2 of the Belle peak luminosity, current world record);

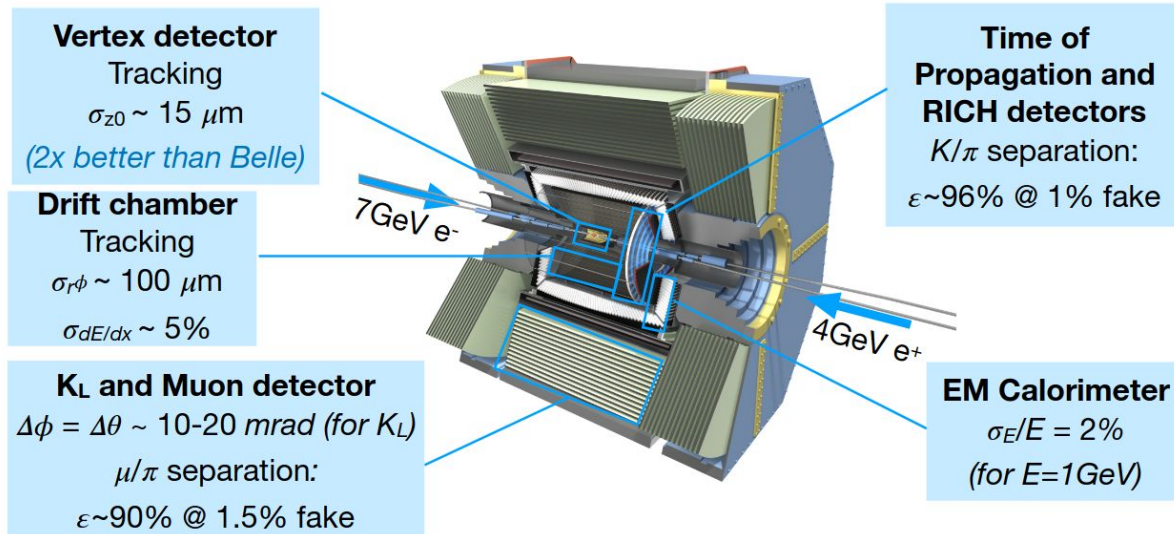


SuperKEKB and Belle II

4π spectrometer with good vertexing, tracking, efficient PID and calorimetry;

PTEP 2020 (2020) 2, 029201

- ❑ Designed to measure CPV in B-mesons decays;
- ❑ Collect the data mostly at $Y(4S)$;
- ❑ Have a reach physics program beyond CPV;

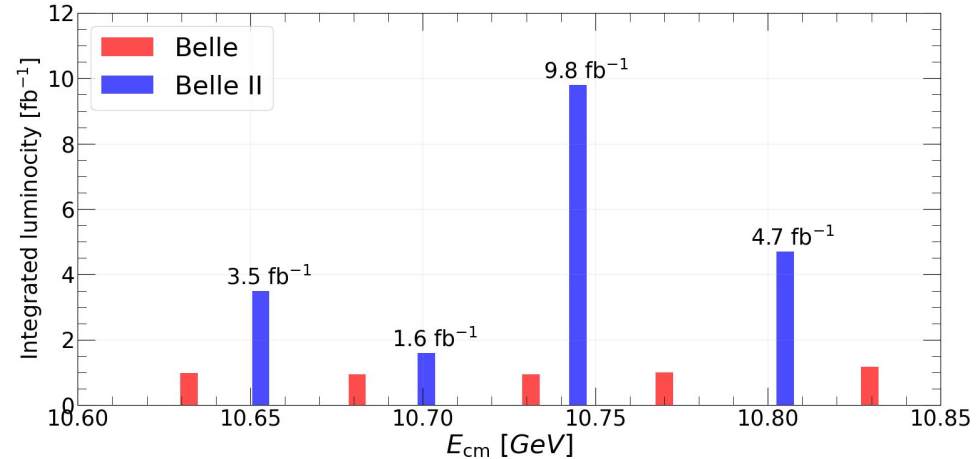
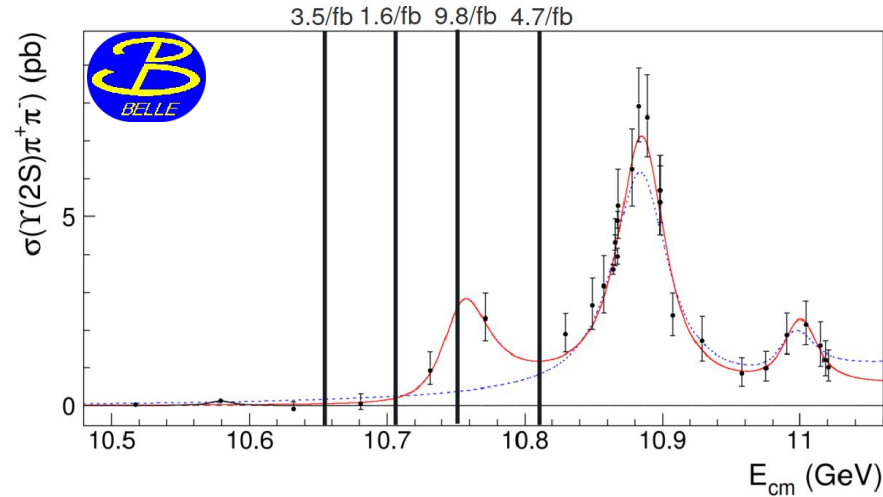


Belle II detector upgrades:

- ❑ Radiation tolerant;
- ❑ Improved vertexing;
- ❑ Better resolution;
- ❑ Faster trigger and DAQ;

SuperKEKB and Belle II

$Y(10753)$ state was observed in the $e^+ e^- \rightarrow Y(nS) \pi^+ \pi^-$ ($n = 1,2,3$) cross section energy dependence by Belle (JHEP 10 (2019) 220).



- ❑ 19 fb^{-1} scan around $Y(10753)$ was collected in November 2021;
- ❑ Belle II collected the data in the gaps between Belle energy scan points;
- ❑ The point with highest statistic (9.8 fb^{-1}) is near $Y(10753)$ peak;

Search for $e^+e^- \rightarrow \omega \chi_{bJ}(1P)$ and $X_b \rightarrow \omega \Upsilon(1S)$

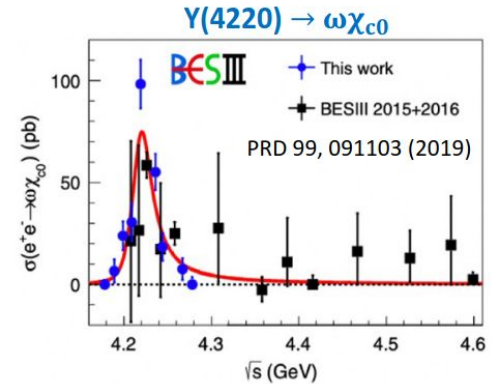
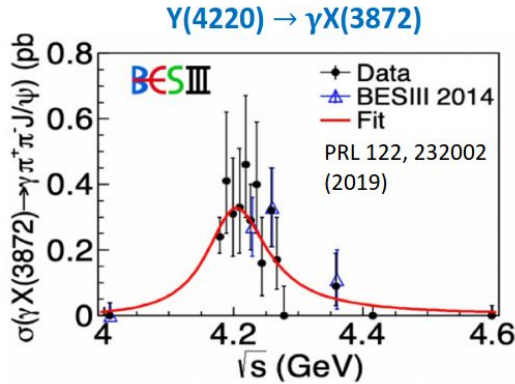
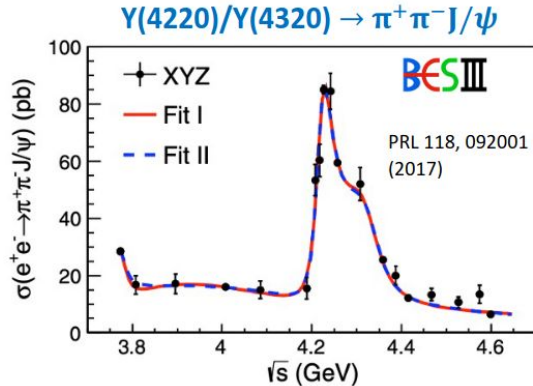
Motivation to search for $Y(10753) \rightarrow \omega \chi_{bJ}(1P)$

Theory:

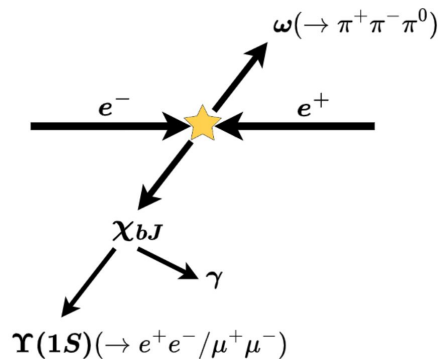
- Mixed $Y(4S) - Y(3D)$ state: $\omega \chi_{bJ}$ could be enhanced (PRD 104, 034036 (2021)).

Charmonium sector:

- Similar to $Y(10753)$ structure $Y(4220)$ was observed in $e^+e^- \rightarrow J/\psi \pi^+\pi^-$ cross section dependence by BES III (PRL 118, 092001 (2017)).
- $Y(4220)$ peak was observed in $\gamma X(3872)$ and $\omega \chi_{c0}$ final states by BES III (PRL, 122, 232002 (2019), PRD 99, 091103(R) (2019)).
- We can expect $Y(10753)$ to decay into $\gamma[X_b \rightarrow \omega Y(1S)]$ and $\omega \chi_{bJ}$ final states.



Observation of $\Upsilon(10753) \rightarrow \omega \chi_{bJ}(1P)$



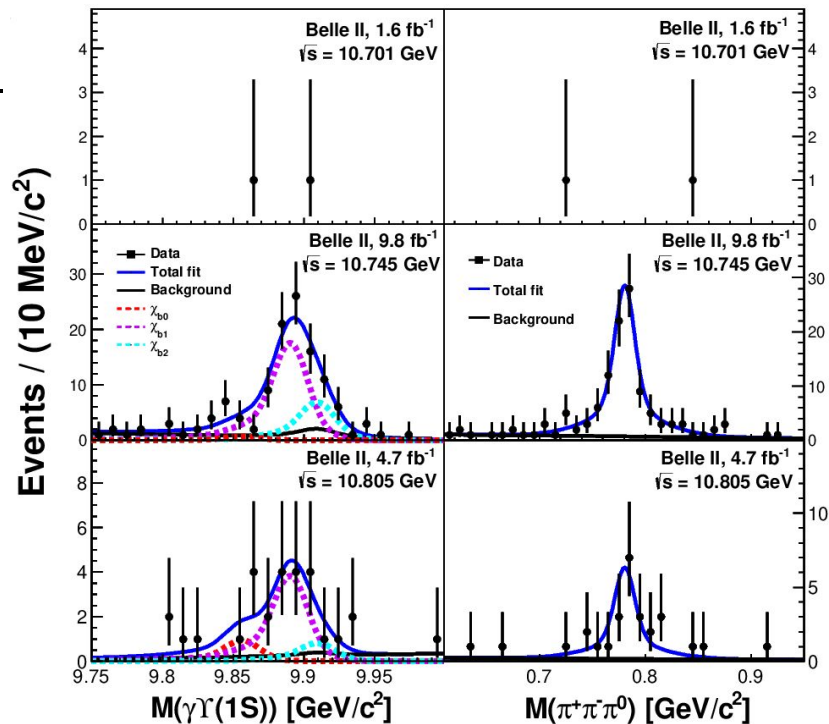
PRL 130, 091902 (2023)

Channel	\sqrt{s} (GeV)	N^{sig}	$\Sigma(\sigma)$	σ_B (pb)
$e^+e^- \rightarrow \omega \chi_{b0}$	10.701	< 3.0	-	< 16.6
$e^+e^- \rightarrow \omega \chi_{b1}$		< 3.9	-	< 1.2
$e^+e^- \rightarrow \omega \chi_{b2}$		< 4.0	-	< 2.5
$e^+e^- \rightarrow \omega \chi_{b0}$	10.745	< 12.0	0.5	< 11.3
$e^+e^- \rightarrow \omega \chi_{b1}$		$68.9^{+13.7}_{-13.5}$	5.9	$3.6^{+0.7}_{-0.7} \pm 0.5$
$e^+e^- \rightarrow \omega \chi_{b2}$		$27.6^{+11.6}_{-10.0}$	3.1	$2.8^{+1.2}_{-1.0} \pm 0.4$
$e^+e^- \rightarrow \omega \chi_{b0}$	10.805	< 9.9	1.2	< 11.4
$e^+e^- \rightarrow \omega \chi_{b1}$		$15.0^{+6.8}_{-6.2}$	2.7	< 1.7
$e^+e^- \rightarrow \omega \chi_{b2}$		$3.3^{+5.3}_{-3.8}$	0.8	< 1.6

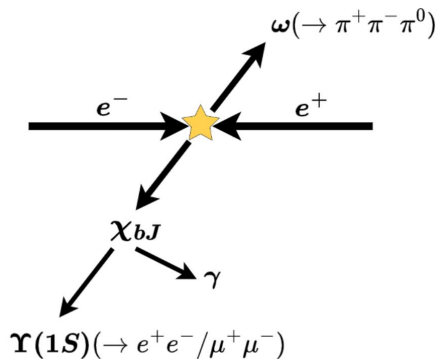
11σ

4.5σ

2D fit to $M(\gamma\Upsilon(1S))$ and $M(\pi^+\pi^-\pi^0)$:



Observation of $Y(10753) \rightarrow \omega \chi_{bJ}(1P)$



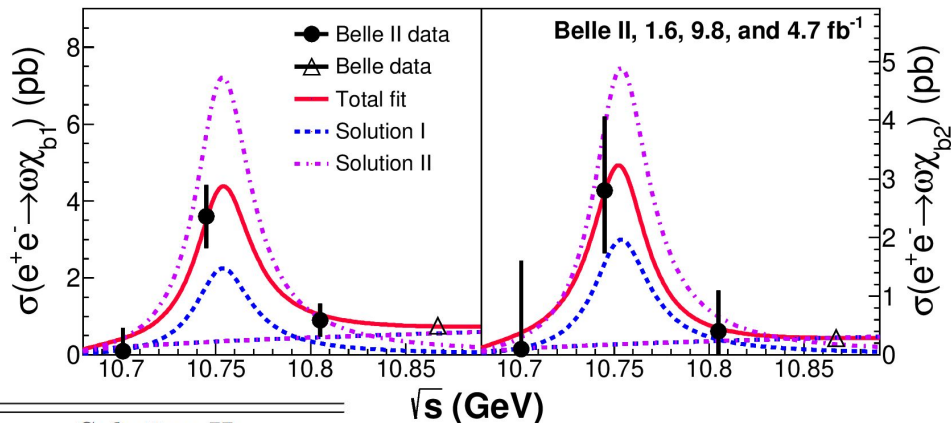
PRL 130, 091902 (2023)

- ❑ Confirms $Y(10753)$ state;
- ❑ No peak at $Y(5S)$;
- ❑ $\sigma(\chi_{b1}\omega)/\sigma(\chi_{b2}\omega) \sim 1$;
- ❑ $\sigma(\chi_{b1}\omega)/Y(2S)\pi^+\pi^- \sim 1.5$;

- ❑ Fit with coherent sum of PHSP and BW.

$$\left| \sqrt{\Phi_2(\sqrt{s})} + \frac{\sqrt{12\pi\Gamma_{ee}\mathcal{B}_f\Gamma}}{s - M^2 - iM\Gamma} \sqrt{\frac{\Phi_2(\sqrt{s})}{\Phi_2(M)}} e^{i\phi} \right|^2$$

- ❑ M and Γ are fixed to 10752.7 MeV and 35.5 MeV



$\Gamma_{ee}\mathcal{B}_f$	Solution I	Solution II
	(constructive interference)	(destructive interference)
$\Gamma_{ee}\mathcal{B}_f(Y(10753) \rightarrow \omega\chi_{b1})$	$(0.63 \pm 0.39 \pm 0.20)$ eV	$(2.01 \pm 0.38 \pm 0.46)$ eV
$\Gamma_{ee}\mathcal{B}_f(Y(10753) \rightarrow \omega\chi_{b2})$	$(0.53 \pm 0.46 \pm 0.15)$ eV	$(1.32 \pm 0.44 \pm 0.55)$ eV

Discussion

Previously Belle measured $\sigma(e^+e^- \rightarrow \chi_{bJ}(1P)\omega)$ at $\sqrt{s} = 10.867$ GeV (PRL **113** (2014) 14, 142001);

- $\Upsilon(5S)$ and $\Upsilon(10753)$ have same quantum numbers and similar masses, but there is a difference:

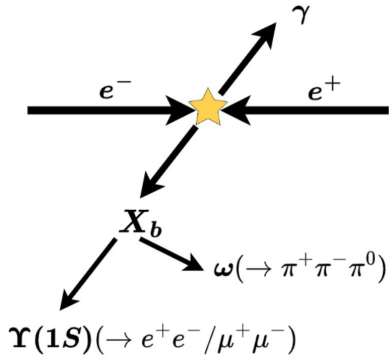
$$\frac{\sigma(e^+e^- \rightarrow \chi_{bJ}(1P)\omega)}{\sigma(e^+e^- \rightarrow \Upsilon(nS)\pi^+\pi^-)} \sim \begin{cases} \sim 1.5 & \text{at } \sqrt{s} = 10.745 \text{ GeV} \\ \sim 0.15 & \text{at } \sqrt{s} = 10.867 \text{ GeV} \end{cases}$$

- Order of magnitude difference is observed for this ratio at $\Upsilon(5S)$ and $\Upsilon(10753)$



It indicates the difference in the internal structures of these two states.

Search for $\Upsilon(10753) \rightarrow \gamma X_b [-\rightarrow \omega \Upsilon(1S)]$



PRL **130**, 091902 (2023)

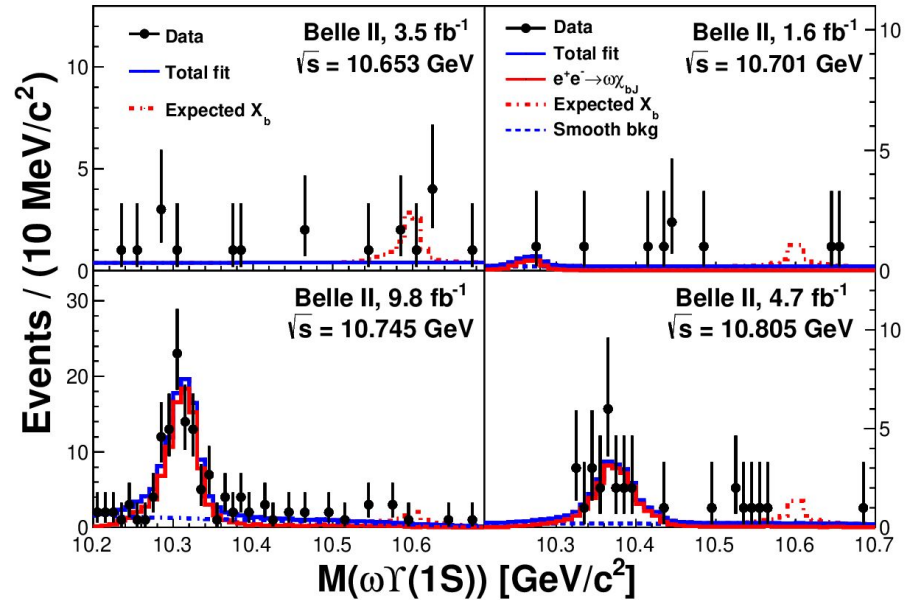
- Upper limits on cross sections are set for $M(X_b) \in [10.45; 10.65]$ GeV;

$$\sigma_{X_b}^{\text{UL}} = \sigma_B^{\text{UL}}(e^+e^- \rightarrow \gamma X_b) \mathcal{B}(X_b \rightarrow \omega \Upsilon(1S))$$

\sqrt{s} (GeV)	M_{X_b} (GeV)	$\sigma_{X_b}^{\text{UL}}$ (pb)
10.653	10.59	< 0.55
10.701	10.45	< 0.84
10.745	10.45	< 0.14
10.805	10.53	< 0.47

- No evidence of X_b (partner of $X(3872)$ in bottomonium) signal;
- Only $\omega X_b(1P)$ reflections are seen;

Fit to $M[\omega \Upsilon(1S)]$



Energy dependence of the $e^+e^- \rightarrow B^{(*)}\bar{B}^{(*)}$ cross section

Energy dependence of the $e^+e^- \rightarrow B^{(*)}\bar{B}^{(*)}$ cross section

Previous Belle analysis: [JHEP 06 \(2021\), 137](#)

- ❑ One B meson is fully reconstructed using hadronic channels;
- ❑ $B^* \rightarrow B\gamma$ decays are not reconstructed;

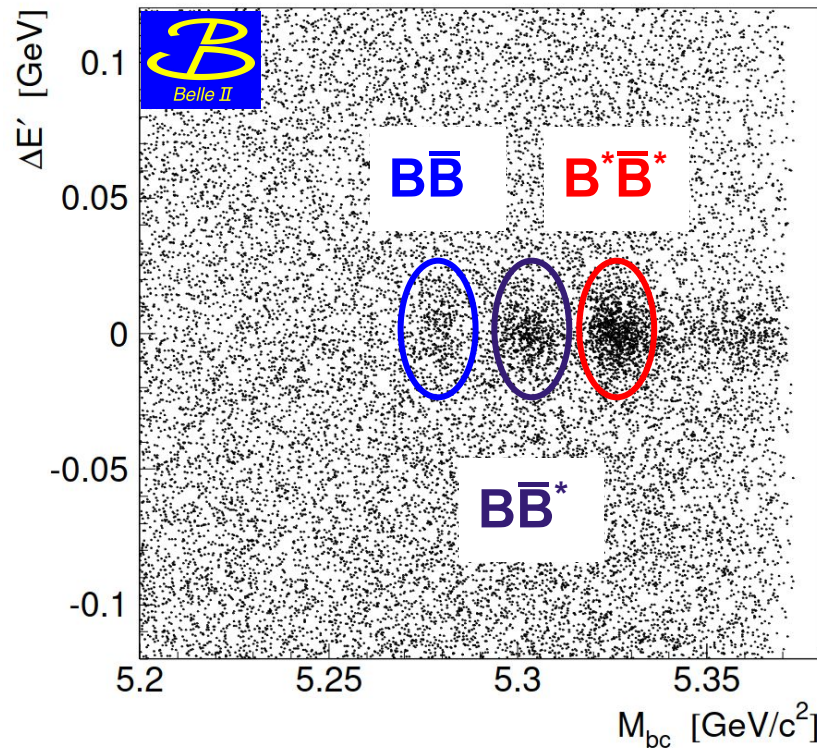
$$\Delta E = E_B - E_{\text{cm}}/2$$

$$\Delta E' = \Delta E + M_{\text{bc}} - m_B$$

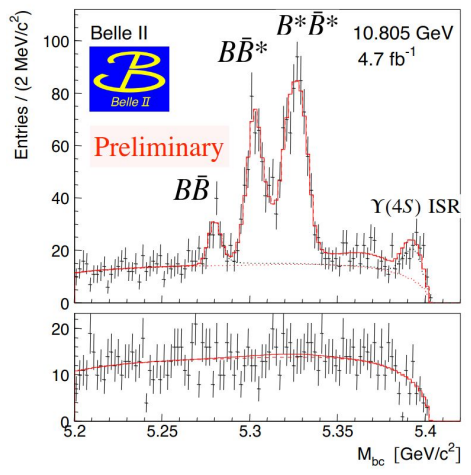
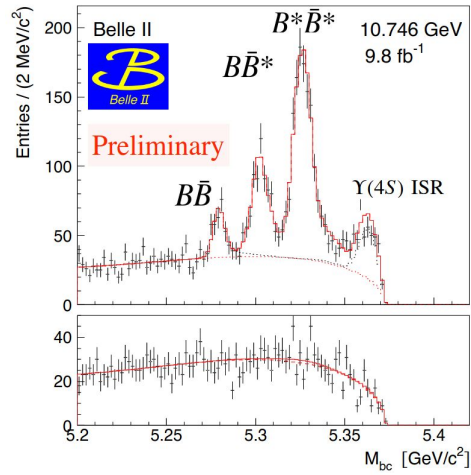
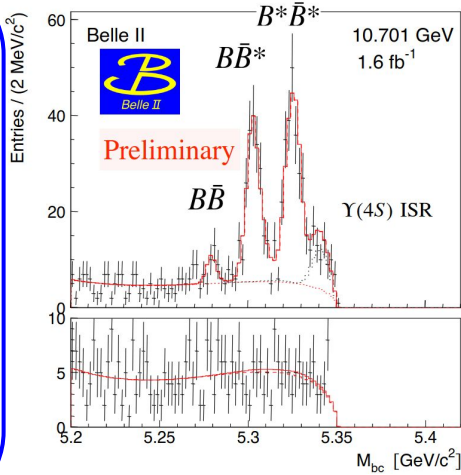
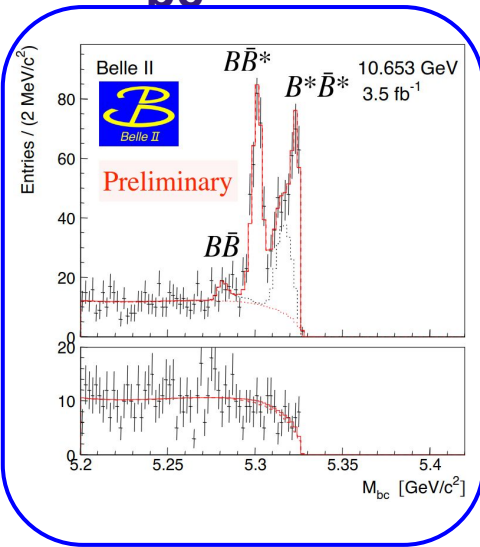
- ❑ $|\Delta E'| < 18$ MeV;
- ❑ Signal is identified using M_{bc} :

$$M_{\text{bc}} = \sqrt{E_{\text{cm}}^2/4 - p_B^2}$$

$\Delta E'$ vs M_{bc} at $E_{\text{cm}} = 10.746$ GeV



M_{bc} fit at scan energies



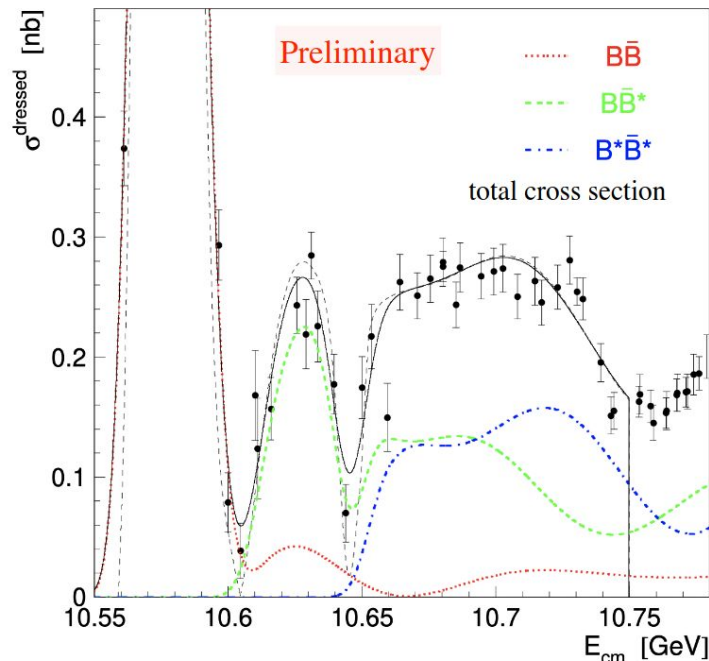
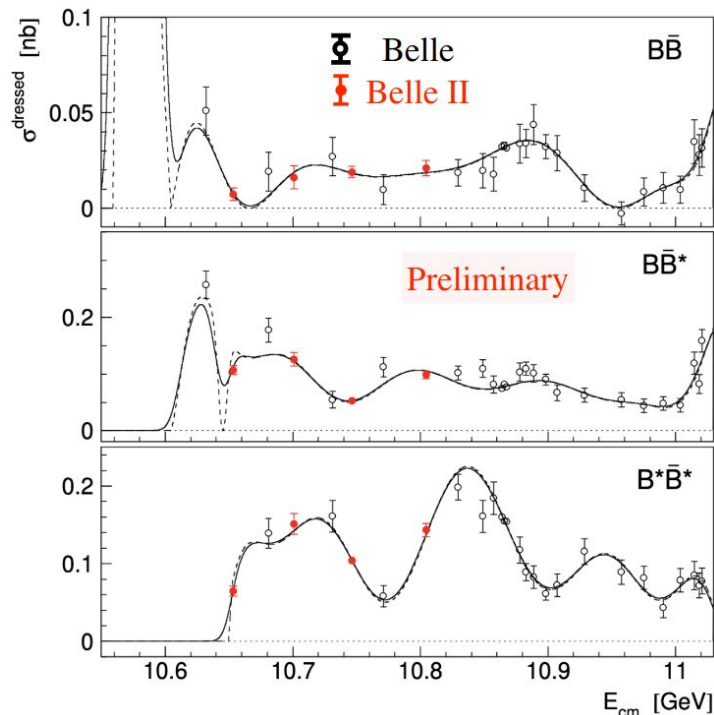
- ❑ Good description of the M_{bc} in data;
- ❑ Contribution of $\Upsilon(4S) \rightarrow B\bar{B}$ production via ISR is visible well described by the fit;
- ❑ E=10.653 GeV sharp cut of the data at right edge \Rightarrow fast rise of $B^*\bar{B}^*$ near threshold;

Energy dependence of the cross sections

Simultaneous fit to:

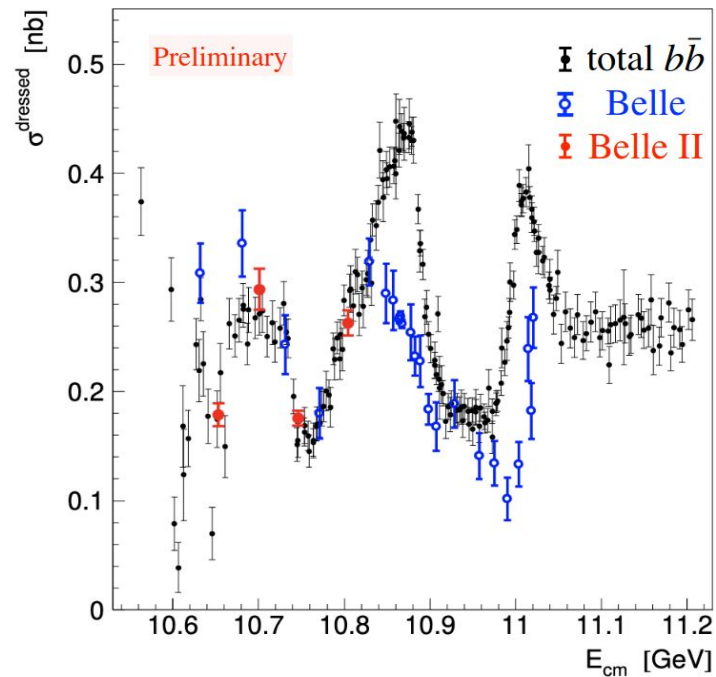
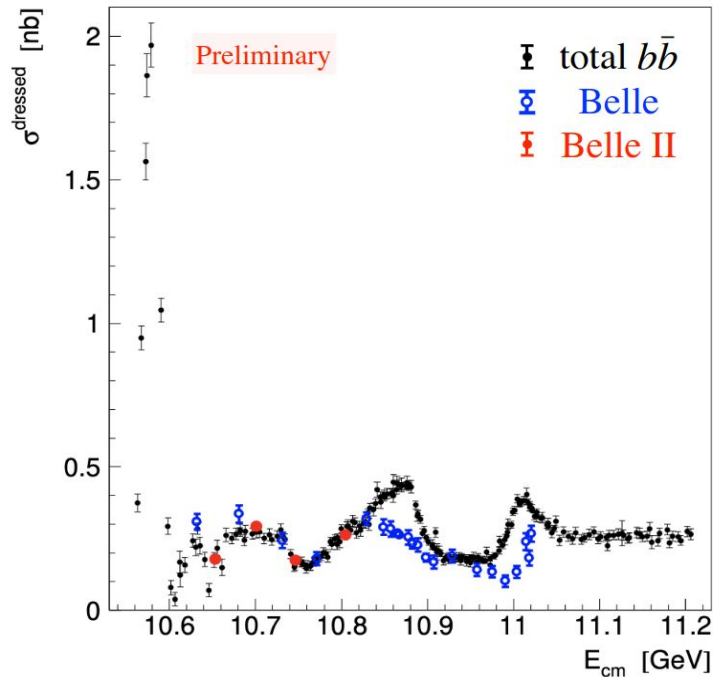
- Exclusive cross sections measured by in this work and previous Belle study (JHEP 06 (2021), 137);

- Total cross section (CPC 44, 8, 083001 (2020))



Comparison of $\sigma_{b\bar{b}}$ and $\sigma_{B\bar{B}} + \sigma_{B\bar{B}^*} + \sigma_{B^*\bar{B}^*}$

- ❑ Good agreement at low energies;
- ❑ Difference at higher energy is due to $B_s^{(*)}\bar{B}_s^{(*)}$, multi-body $B^{(*)}\bar{B}^{(*)}\pi(\pi)$ and bottomonia;



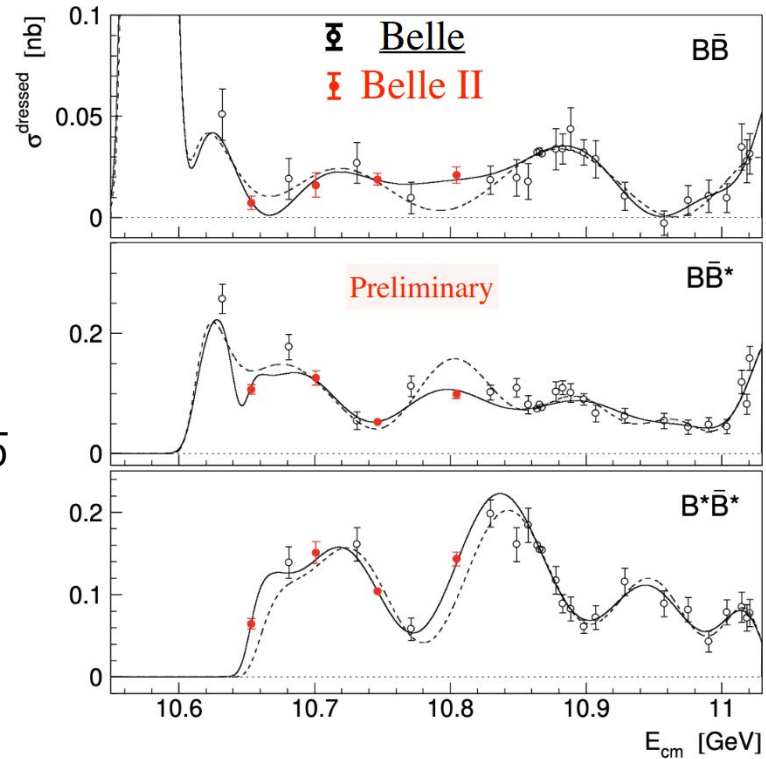
Discussion

New measurement complements previous Belle result:

- ❑ Solid curve – combined Belle + Belle II data fit
- ❑ Dashed curve – Belle data fit only

$\sigma(e^+e^- \rightarrow B^*\bar{B}^*)$ rises rapidly above $B^*\bar{B}^*$ threshold:

- ❑ Similar behaviour was seen for $D^*\bar{D}^*$ cross section ([PRD 97, 012002 \(2018\)](#));
- ❑ **Possible interpretation:** resonance or bound state ($b\bar{b}$ or $B^*\bar{B}^*$) near threshold ([MPL A 21, 2779 \(2006\)](#));
- ❑ Also explains a narrow dip in $\sigma(e^+e^- \rightarrow B\bar{B}^*)$ near $B^*\bar{B}^*$ threshold by destructive interference between $e^+e^- \rightarrow B\bar{B}^*$ and $e^+e^- \rightarrow B^*\bar{B}^* \rightarrow B\bar{B}^*$;
- ❑ $\Upsilon \pi^+ \pi^-$ and $h_b \eta$ final states could also be enhanced ([PRD 87, 094033 \(2013\)](#)).



Conclusion

Observation of $e^+e^- \rightarrow \omega\chi_{bj}(1P)$ at $\sqrt{s} = 10.75$ GeV

- ❑ $\sigma[e^+e^- \rightarrow \omega\chi_{bj}(1P)]$ has a peak at 10.75 GeV
- ❑ Confirmation of $Y(10753)$ and observation of its new decay channel;

Energy dependence of $e^+e^- \rightarrow B\bar{B}, B\bar{B}^*$ and $B^*\bar{B}^*$

- ❑ Confirmation of “oscillatory” behavior, improvement of the accuracy;
- ❑ Rapid rise of $\sigma(e^+e^- \rightarrow B^*\bar{B}^*)$ above threshold - signal of molecular $B^*\bar{B}^*$ state?

Scan above $Y(4S)$ gives an opportunity for a lot of unique studies:

- ❑ $Y(10753)$ decays to different final states. Study of its properties;
- ❑ Energy dependence of the various final states production;

Golden Modes
$e^+e^- \rightarrow \pi^+\pi^-\Upsilon(pS)(\rightarrow \ell^+\ell^-)$
$B\bar{B}$ decomposition Preliminary result
$\pi^+\pi^-$ Dalitz
$Y_b \rightarrow \omega\eta_b(1S)$
$Y_b \rightarrow \omega\chi_{bJ}(1P)$ PRL 130, 091902 (2023)
Silver Modes
$Y_b \rightarrow \pi^+\pi^-X$ (inclusive)
$Y_b \rightarrow \eta X$ (inclusive)
$Y_b \rightarrow \eta\Upsilon(1S, 2S)(\rightarrow \ell^+\ell^-)$
$Y_b \rightarrow \eta'\Upsilon(1S)(\rightarrow \ell^+\ell^-)$
$Y_b \rightarrow \Upsilon(1S)$ (inclusive)
Bronze Modes
$Y_b \rightarrow \gamma X_b$
$Y_b \rightarrow \pi^0\pi^0\Upsilon(pS)(\rightarrow \ell^+\ell^-)$
$Y_b \rightarrow KK(\phi)\Upsilon(pS)(\rightarrow \ell^+\ell^-)$
$Y_b \rightarrow \pi^0\pi^0X$ (inclusive)
$Y_b \rightarrow \pi^0X$ (incl. or excl.)
...

Thank you!