

# Semileptonic B decays at Belle II & Belle



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for SUSY 2023 (July 17-21, 2023)

# Outline

## ● The cram course

- for Belle II and Belle experiments (details in Appendix 0)

## ● on $V_{xb}$ ( $x = c, u$ ) tensions

- $V_{ub}$  from exclusive  $B \rightarrow \pi \ell^+ \nu$  (Belle II)
- simultaneous (inclusive & exclusive)  $V_{ub}$  (Belle)

## ● on LFU test

- inclusive ratio  $R(X_{e/\mu})$  (Belle II)
- First Belle II result on  $R(D^*)$

## ● Closing remarks

# The cram course for $B$ -mesons @ Belle & Belle II



$$e^{-} \xrightarrow{8 \text{ GeV}} (\star) \xleftarrow{3.5 \text{ GeV}} e^{+} \quad (1999-2010)$$

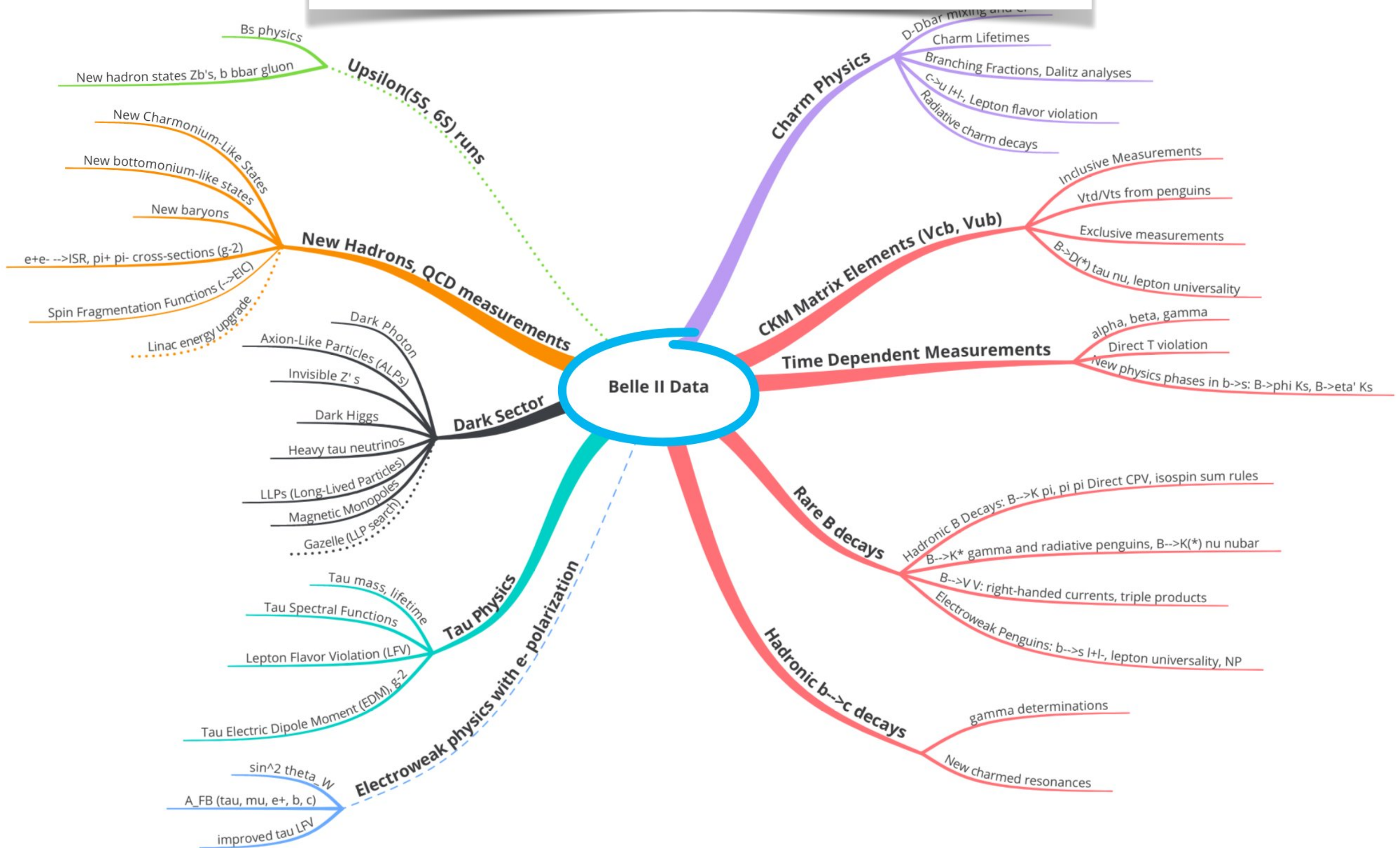


$$e^{-} \xrightarrow{7 \text{ GeV}} (\star) \xleftarrow{4 \text{ GeV}} e^{+} \quad (\text{since 2019})$$

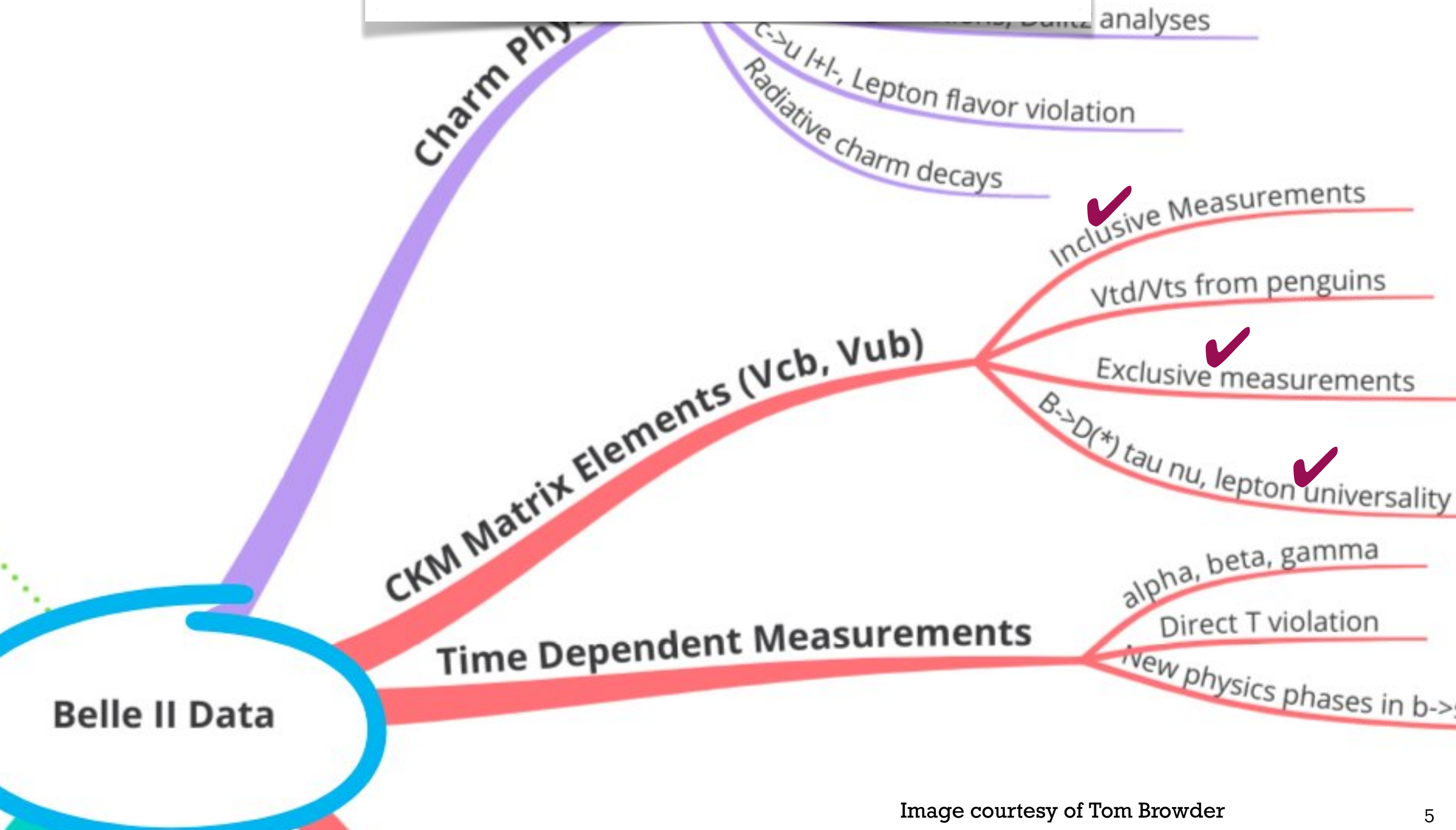
See Appendix 0 (p.25-31)  
for more

- $\sqrt{s} = 10.58 \text{ GeV} = m(\Upsilon(4S))$  for both
- Use  $\Upsilon(4S) \rightarrow B\bar{B}$
- $\exists$  continuum underneath  $\Upsilon(4S)$

# Belle II Physics Mind-map

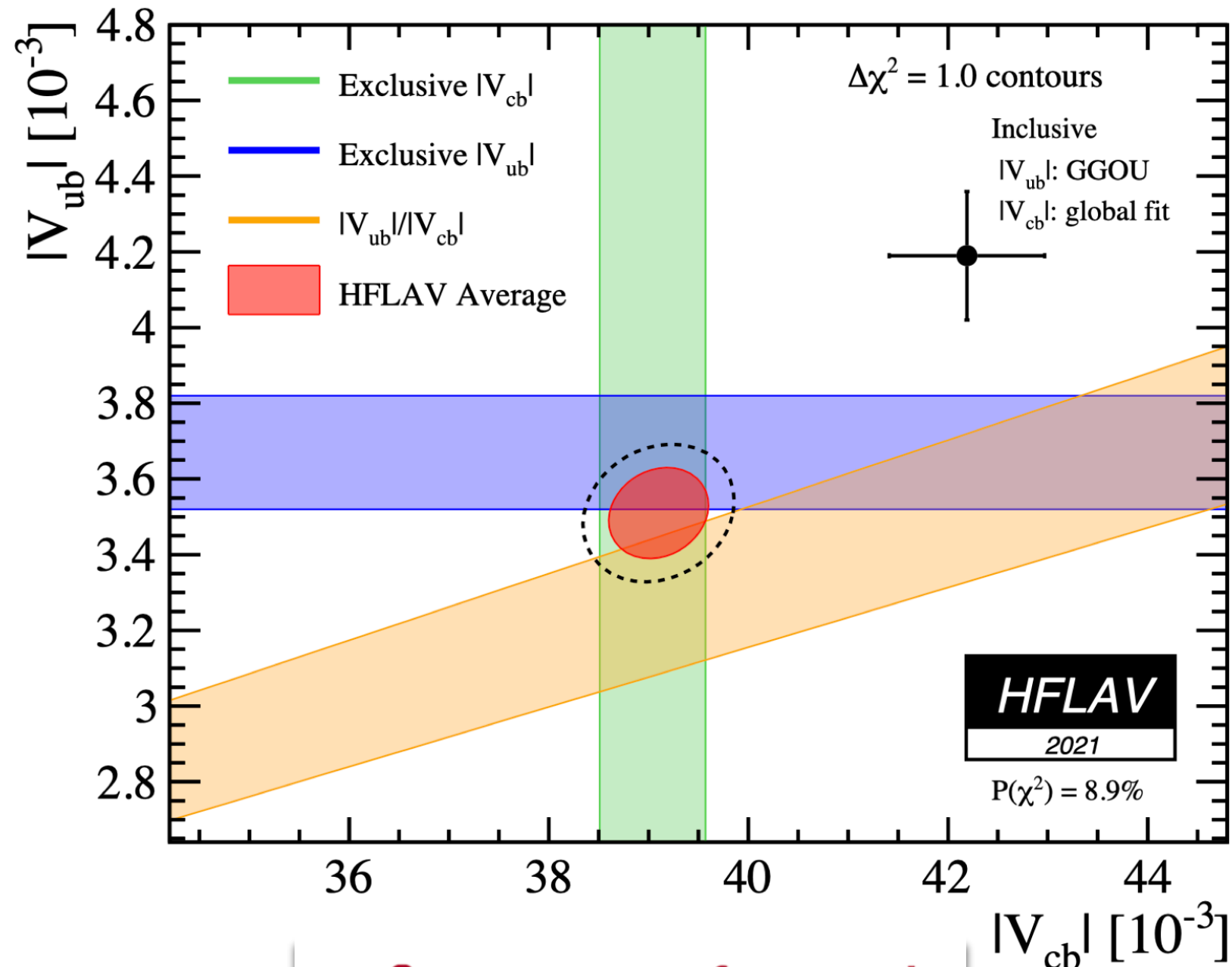


# Belle II Physics Mind-map



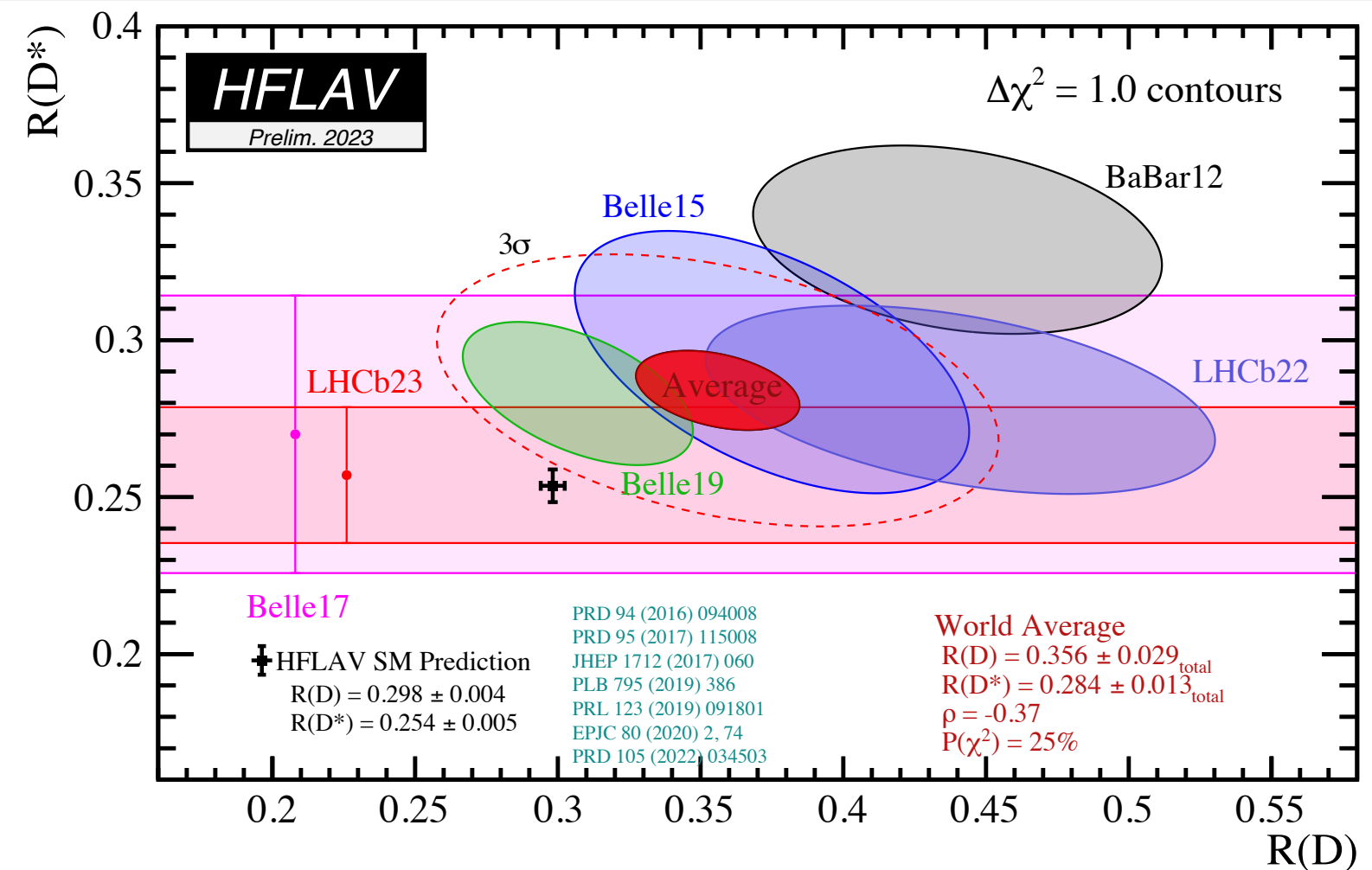
# tensions in semileptonic B decays

## Precision measurements of CKM UT



$\sim 3\sigma$  tension for each  
( $|V_{cb}|$ ,  $|V_{ub}|$ )

## Test of lepton universality in $R(D^{(*)})$



$$R(D^{(*)}) \equiv \frac{\mathcal{B}(B \rightarrow D^{(*)}\tau^+\nu)}{\mathcal{B}(B \rightarrow D^{(*)}\ell^+\nu)}$$

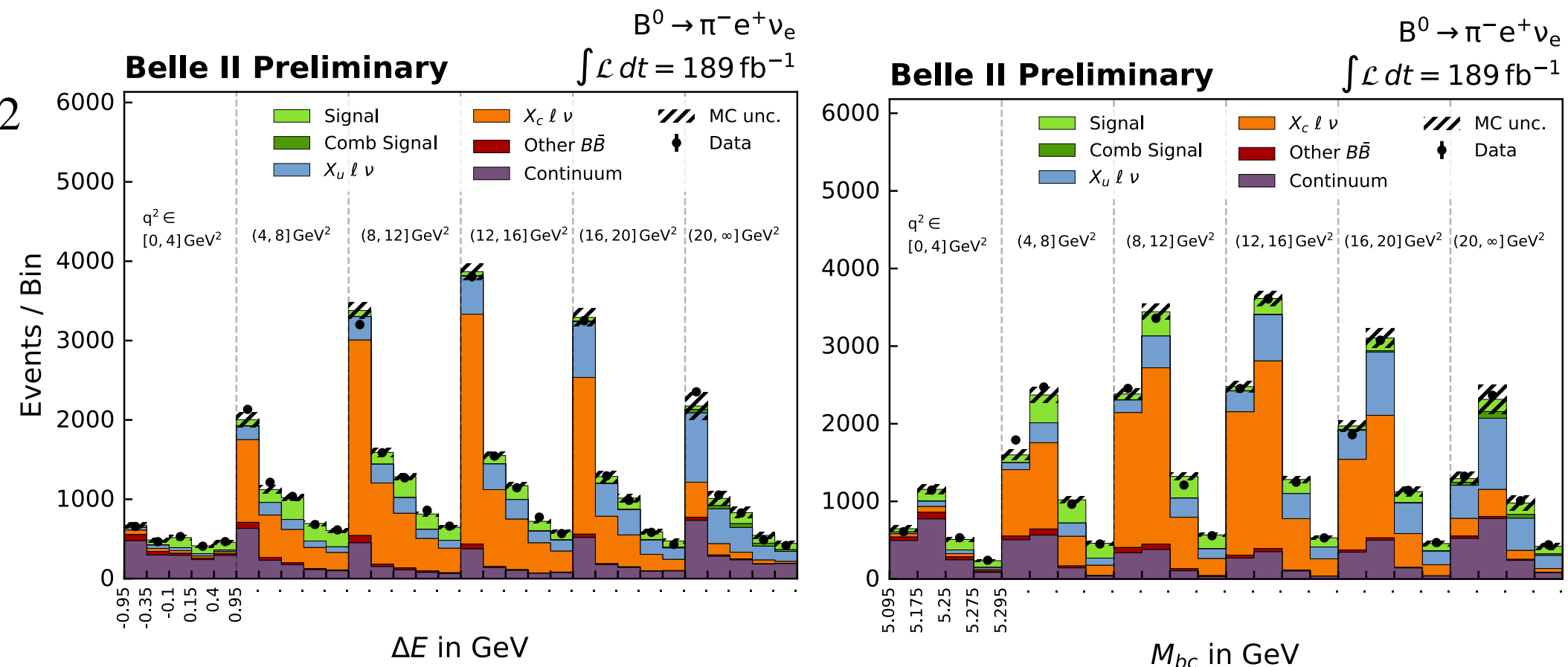
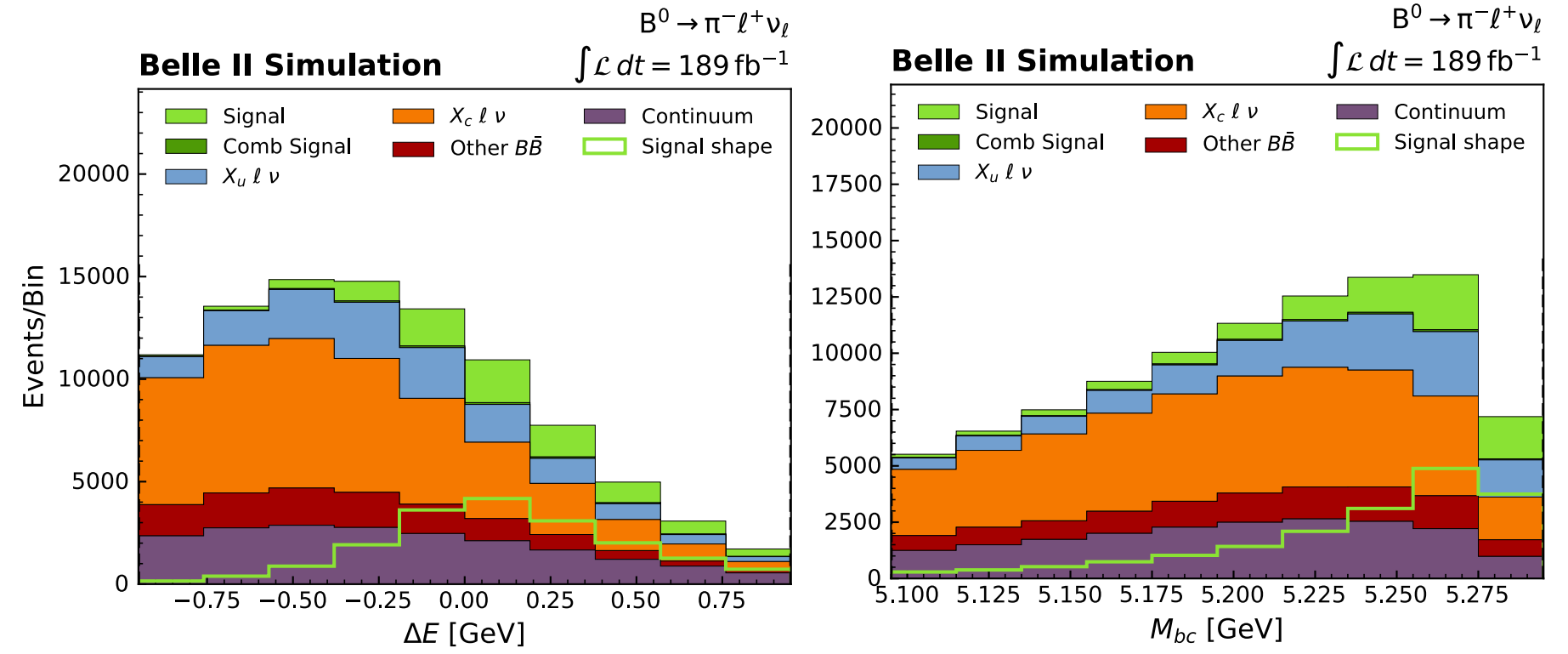
# on $V_{xb}$ ( $x = c, u$ ) tensions

- $|V_{cb}|$  from exclusive  $B$  decays (Belle, Belle II) — Appendix 1 in the back-up slides
- $|V_{ub}|$  from exclusive  $B^0 \rightarrow \pi^- \ell^+ \nu$  (Belle II)
- Simultaneous (incl. & excl.)  $|V_{ub}|$  (Belle)

# $B^0 \rightarrow \pi^- \ell^+ \nu$ for $|V_{ub}|$ (untagged)

- Belle II dataset of  $\mathcal{L}_{\text{int}} = 189 \text{ fb}^{-1}$
- “untagged” analysis
  - aiming at highest signal efficiency
  - instead of tagging, just measure ROE for background suppression using  $(E, \vec{p})$  cons.
- suppress  $q\bar{q}$  & combinatoric backgrounds via BDT
- measure partial BF in 6 bins of  $q^2$ 
  - signal extraction by binned 2D fit to  $(M_{bc}, \Delta E)$

$$\mathcal{B}(B^0 \rightarrow \pi^- \ell^+ \nu) = (1.426 \pm 0.056 \pm 0.125) \times 10^{-4}$$





# $B^0 \rightarrow \pi^- \ell^+ \nu$ for $|V_{ub}|$ (untagged)

**Belle II Preliminary**

$\int \mathcal{L} dt = 189 \text{ fb}^{-1}$

- Extract  $|V_{ub}|$  from the partial BF

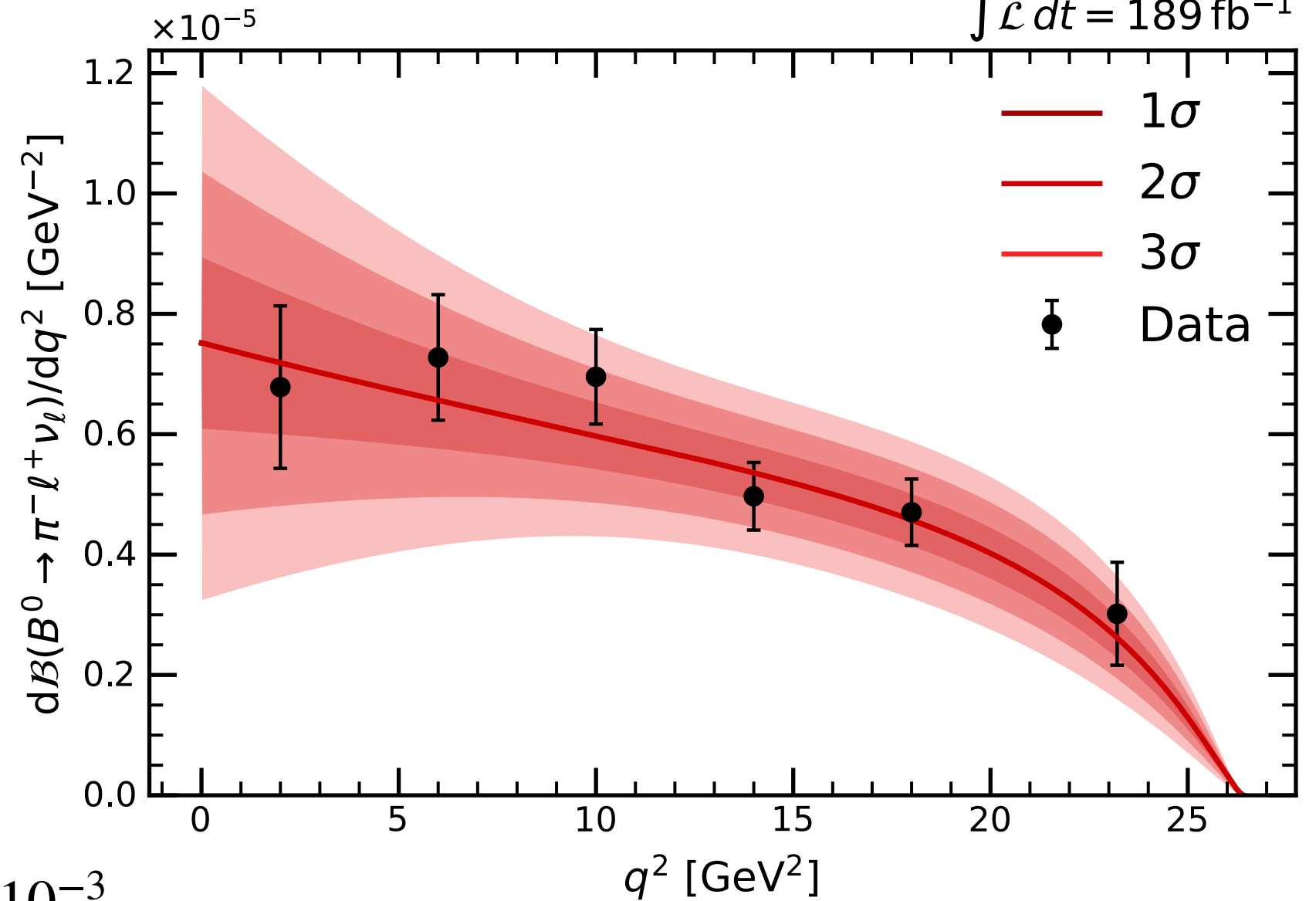
$$\frac{d\Gamma(B \rightarrow \pi \ell^+ \nu)}{dq^2} = \frac{G_F^2}{24\pi^3} |V_{ub}|^2 |p_\pi|^3 |f_+(q^2)|^2$$

in the limit  $m_\ell^2 = 0$

- BCL expansion for  $|V_{ub}|$

- Lattice QCD input from FNAL/MILC on the eight BCL parameters

Bourrely, Lellouch, Caprini, PRD **79**, 013008 (2009)



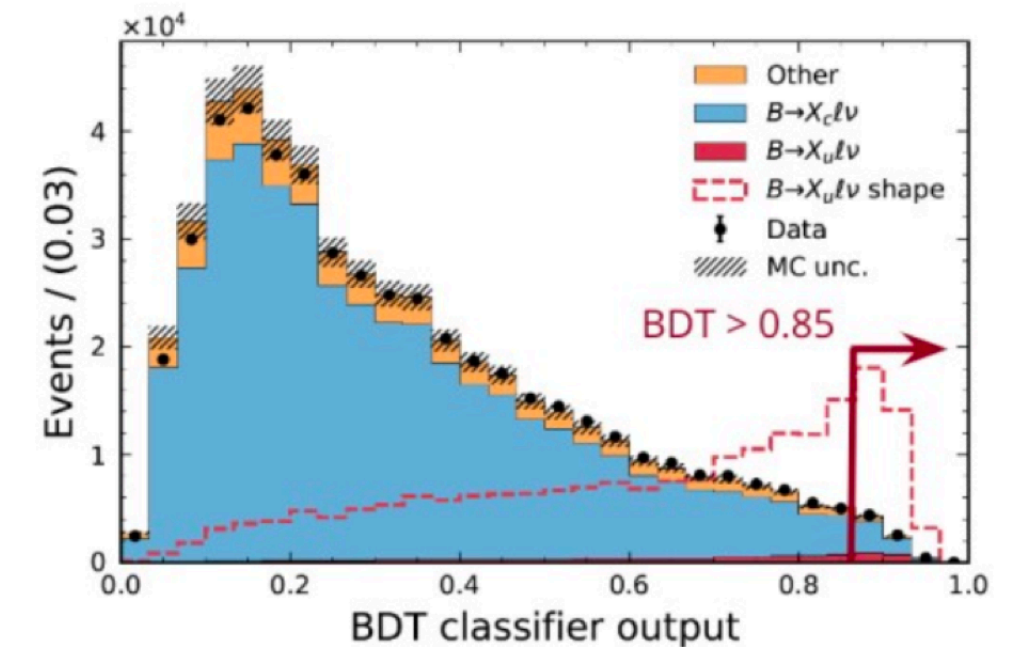
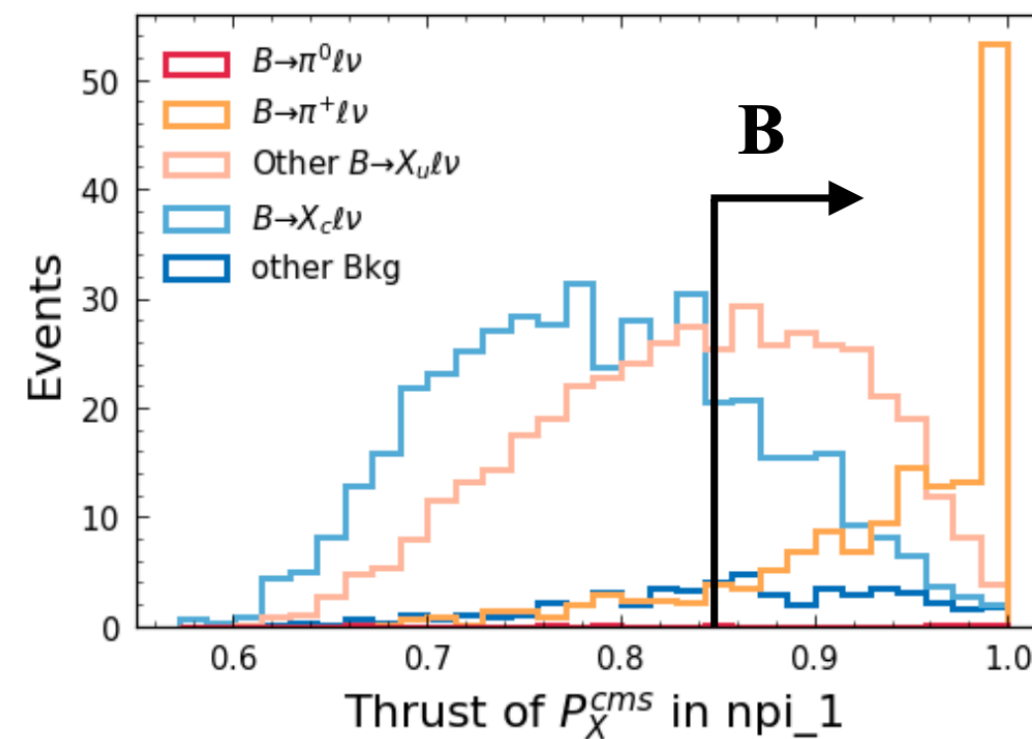
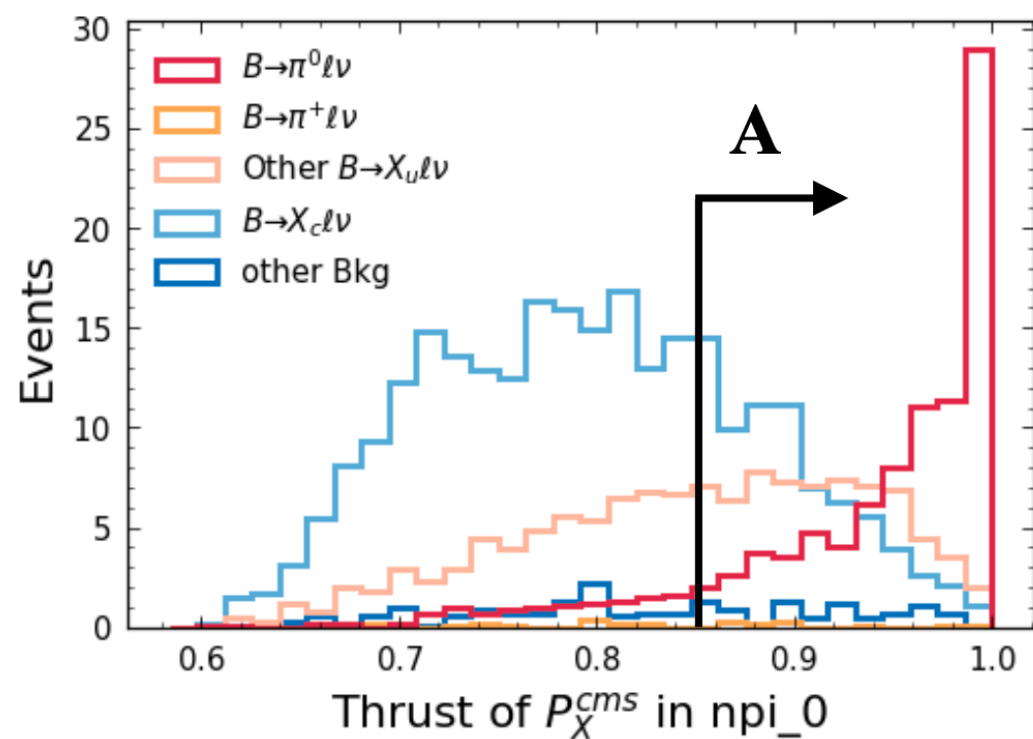
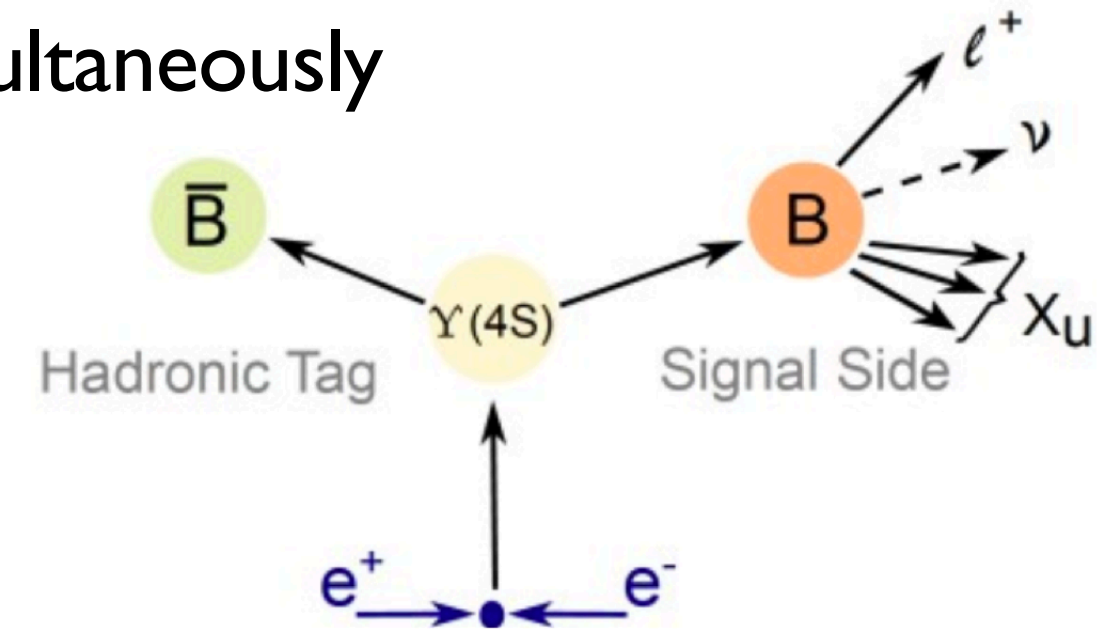
$$|V_{ub}|_{B^0 \rightarrow \pi^- e^+ \nu} = (3.60 \pm 0.18 \pm 0.14 \pm 0.18) \times 10^{-3}$$

$$|V_{ub}|_{B^0 \rightarrow \pi^- \mu^+ \nu} = (3.71 \pm 0.16 \pm 0.15 \pm 0.17) \times 10^{-3}$$

$$|V_{ub}|_{B^0 \rightarrow \pi^- \ell^+ \nu} = (3.55 \pm 0.12 \pm 0.13 \pm 0.17) \times 10^{-3}$$

# Simultaneous (incl. & excl.) $|V_{ub}|$

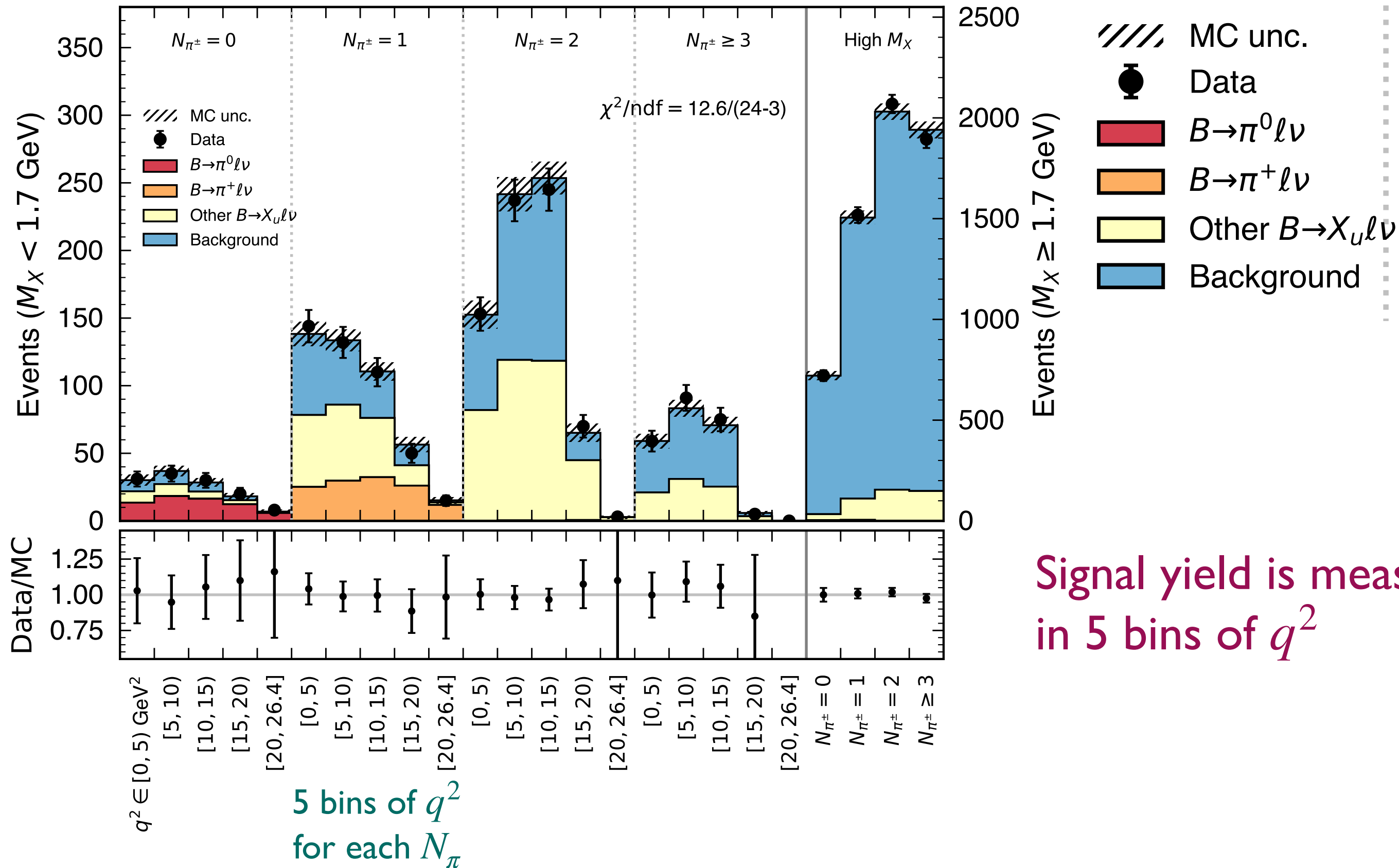
- Measure  $B \rightarrow X_u \ell^+ \nu$ ,  $B^0 \rightarrow \pi^- \ell^+ \nu$ ,  $B^+ \rightarrow \pi^0 \ell^+ \nu$  simultaneously
- B-tagging by hadronic decays
  - ANN-based tagging of companion B
  - allows reconstruction of  $X_u$  in  $B \rightarrow X_u \ell^+ \nu$
- $b \rightarrow c$  is suppressed using  $M_X$ , and further by BDT
  - 11 features for training ( $M_m^2$ ,  $\chi_{\text{vtx}}^2$ ,  $N(K's)$ , etc.)
- use  $X_u$  thrust in the CM frame, for  $B \rightarrow \pi \ell^+ \nu$  significance



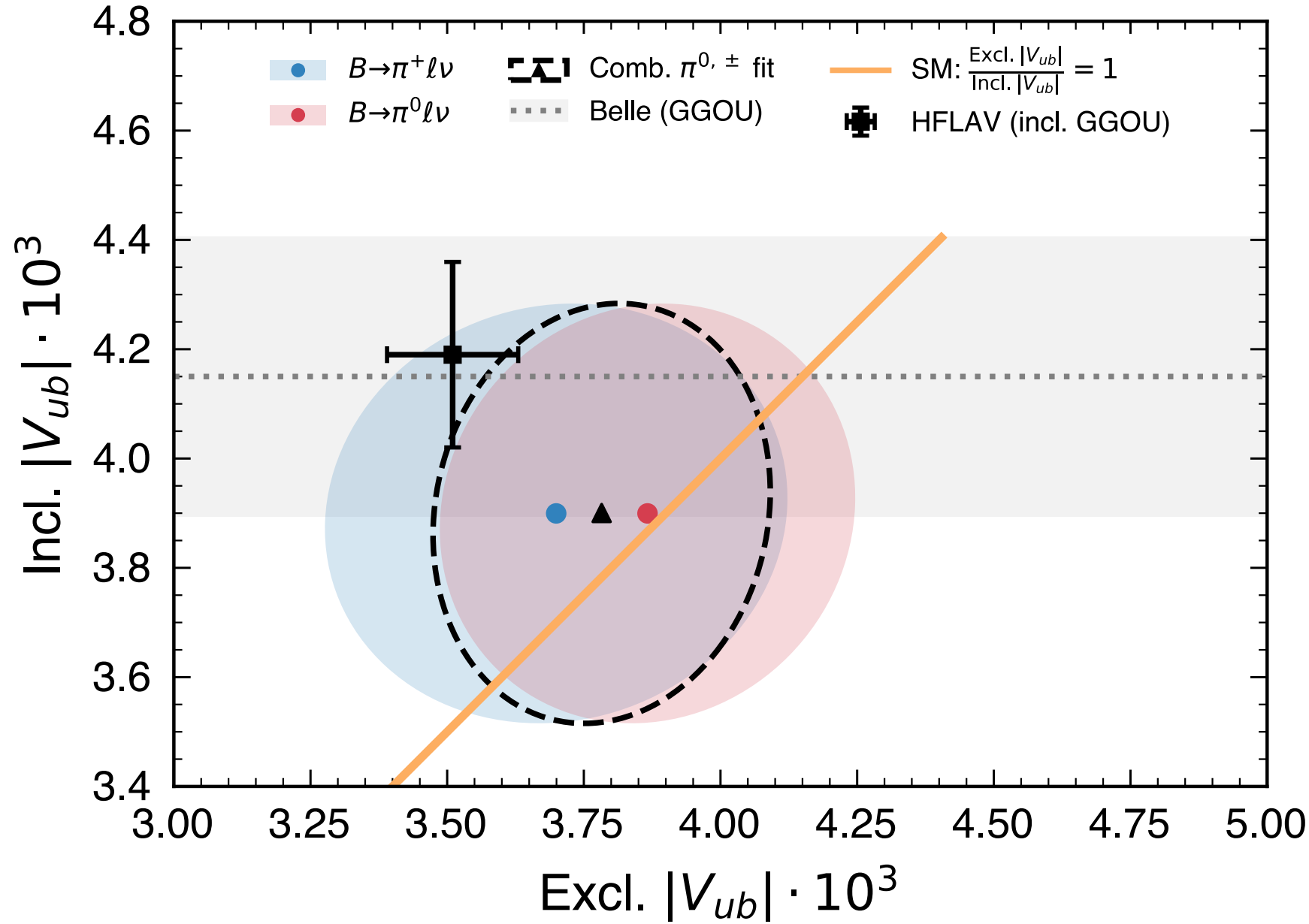
# Simultaneous (incl. & excl.) $|V_{ub}|$

Full Belle dataset

$$\mathcal{L}_{\text{int}} = 711 \text{ fb}^{-1}$$

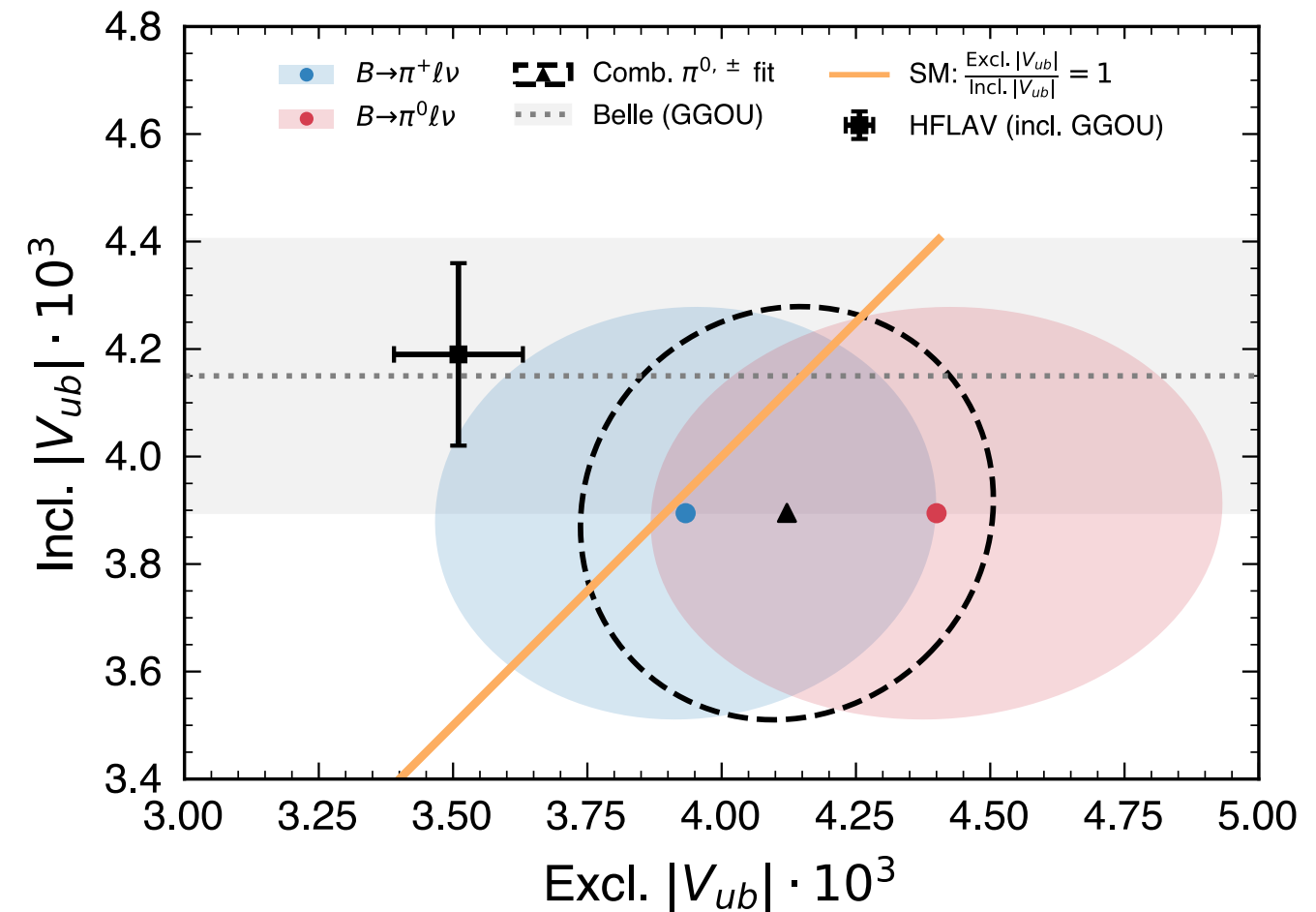


# Simultaneous (incl. & excl.) $|V_{ub}|$



- $|V_{ub}|$  results from fits using LQCD and experimental constraints for the  $B \rightarrow \pi^+ \ell \nu$  form-factor (left)

- $|V_{ub}|$  from fits using LQCD, but w/o form-factor constraints (right)



$$|V_{ub}^{\text{excl.}}| = (3.78 \pm 0.23 \pm 0.16 \pm 0.14) \times 10^{-3}$$

$$|V_{ub}^{\text{incl.}}| = (3.90 \pm 0.20 \pm 0.32 \pm 0.09) \times 10^{-3}$$

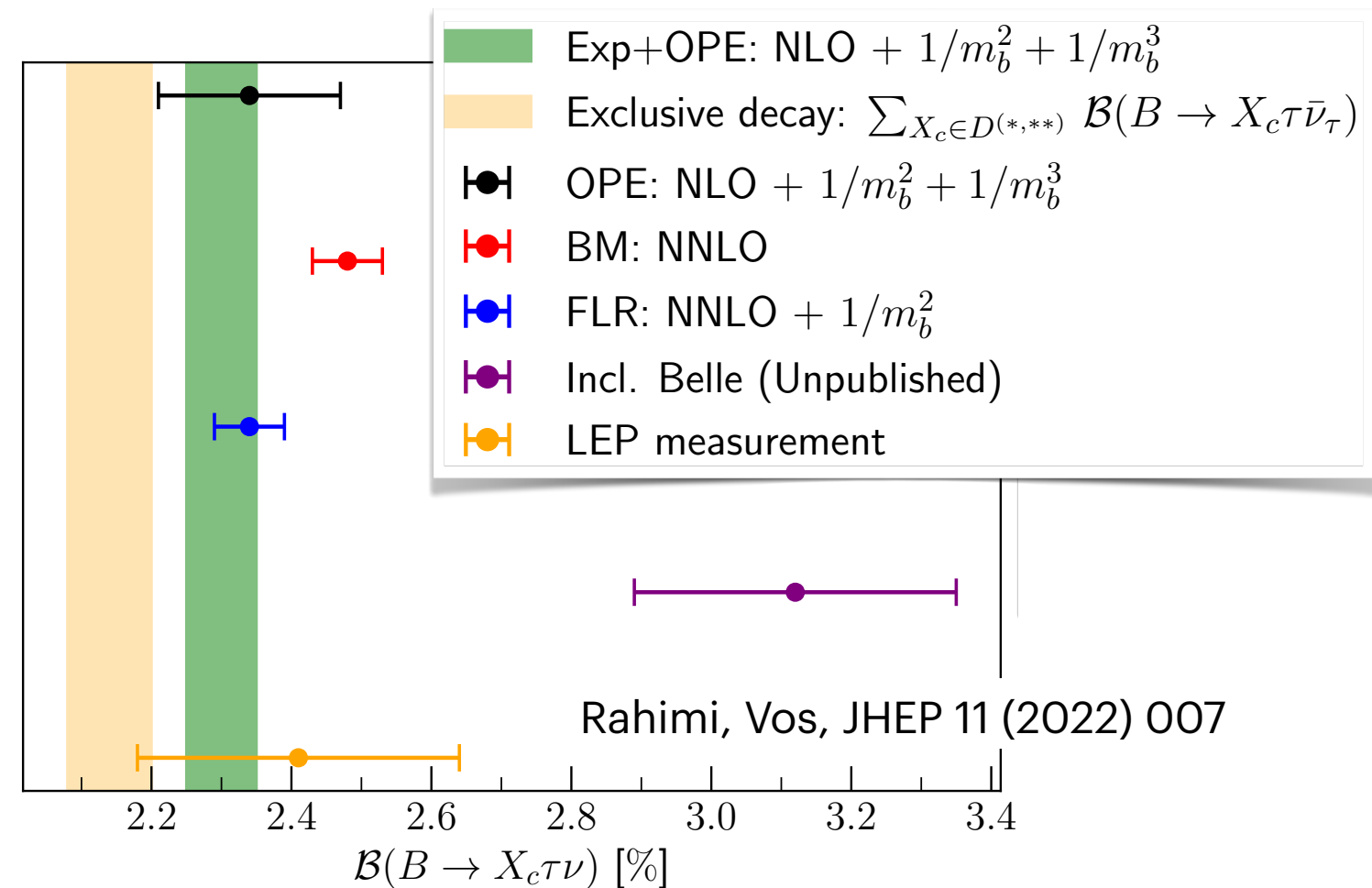
$\pm(\text{stat}) \pm(\text{syst}) \pm(\text{theory})$

$$|V_{ub}^{\text{excl.}}| / |V_{ub}^{\text{incl.}}| = 0.97 \pm 0.12$$

# on the LFU test

## LFU test with inclusive $B \rightarrow X\ell\nu$

- *inclusive* study — complementary to *exclusive* studies
  - existing  $R(D^{(*)})$  are all from exclusive analyses
- one of the unique and high-profile goals of Belle II
- last measured by LEP (!)
- As a first step towards measuring  $R(X_{c,\tau/\ell})$ , we measure  $R(X_{e/\mu})$  at Belle II



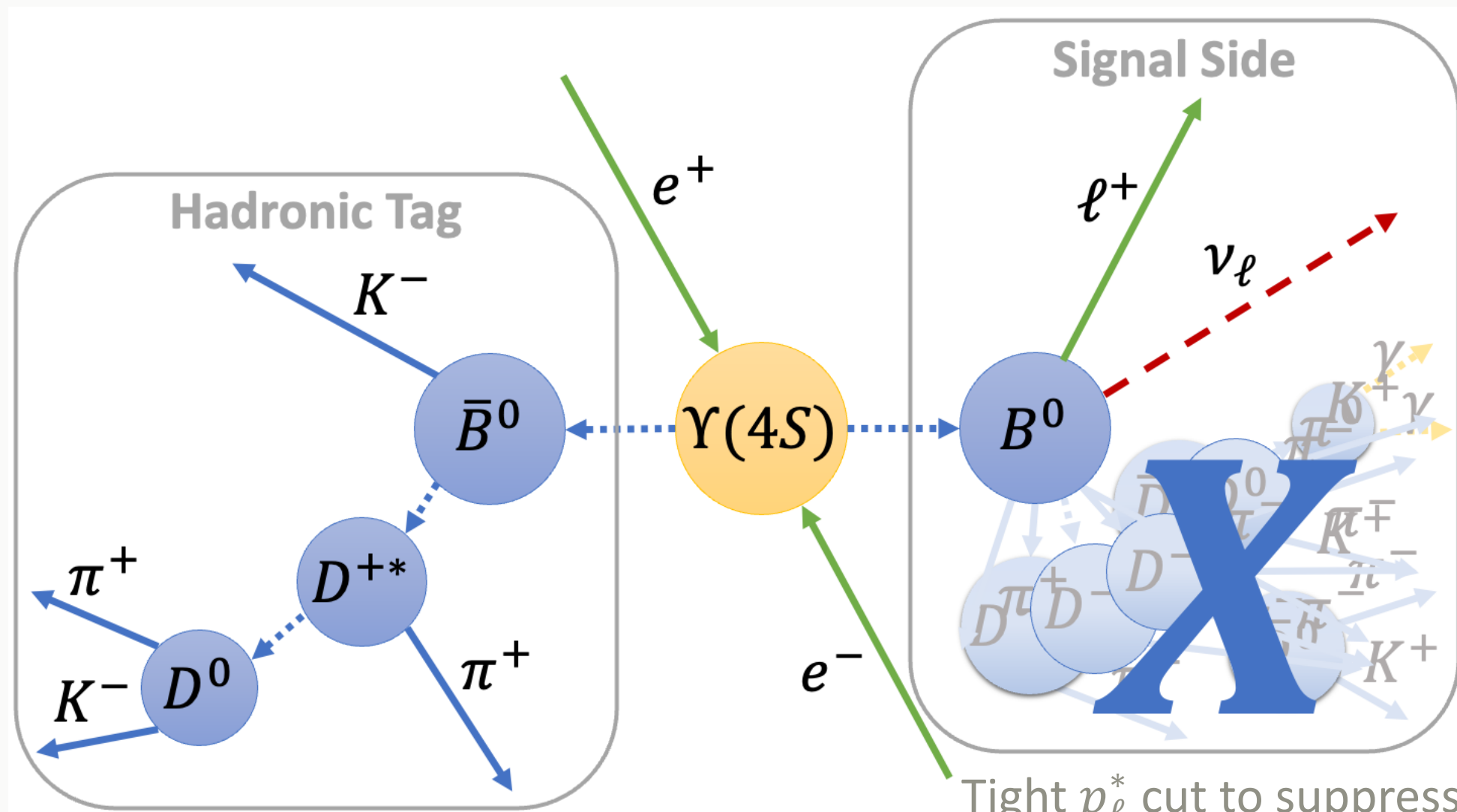
•  $R(X_{c,\tau/\ell})_{\text{SM}} = 0.223 \pm 0.004$

Feytsis, Ligeti, Ruderman, PRD 92, 054018 (2015)

•  $R(X_{e/\mu})_{\text{SM}} = 1.006 \pm 0.001$

Rahimi, Vos, JHEP 11 (2022) 007

# LFU test with inclusive $B \rightarrow X\ell\nu$



- **Reconstruct**  
 $Y(4S) \rightarrow B_{\text{tag}}^- \ell^+ X$   
 $Y(4S) \rightarrow \bar{B}_{\text{tag}}^0 \ell^+ X$
- $p_\ell^* > 1.3 \text{ GeV}$
- **Only basic quality cuts on tracks and calorimeter signals**
- **Tight constraints on tag quality**

$\epsilon = \mathcal{O}(0.1\%)$

Precise knowledge of  $B_{\text{tag}}$  kinematics

Tight  $p_\ell^*$  cut to suppress

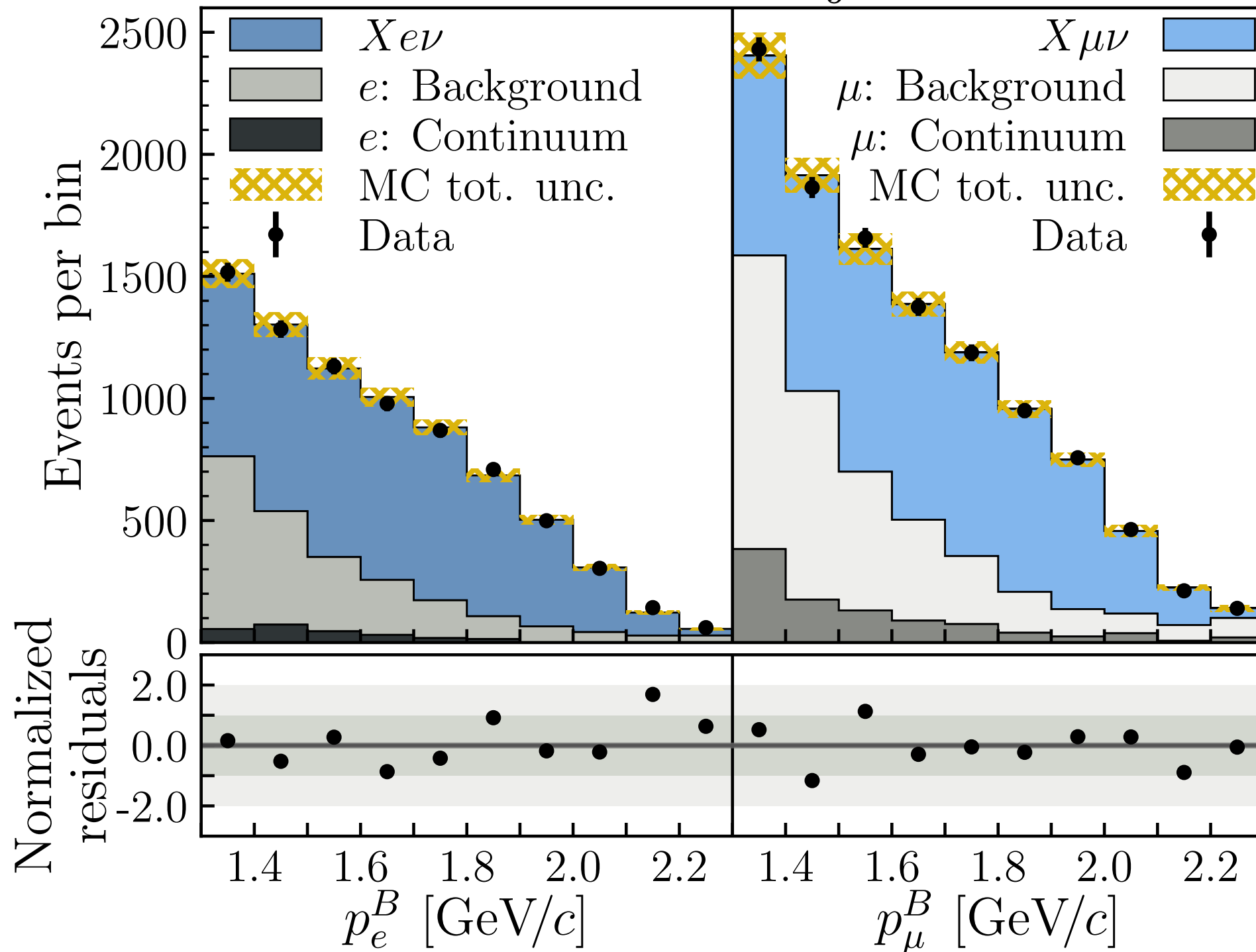
- hadrons faking leptons (“fakes”)
  - secondary leptons from  $b \rightarrow c \rightarrow (\ell, s)$  cascades (“secondaries”)
  - $B \rightarrow X\tau\nu$
- [53% ( $e$ ) / 66% ( $\mu$ ) of selected  $B \rightarrow X\ell\nu$  is retained]

See p.31 for FEI as hadronic B-tagging tool.

slide taken from Belle II ICHEP2022 talk by H. Junkerkalefeld

# LFU test with inclusive $B \rightarrow X\ell\nu$

Belle II **wrong-sign**  $\int \mathcal{L} dt = 189 \text{ fb}^{-1}$



Signal extraction by fitting  $p_\ell^B$

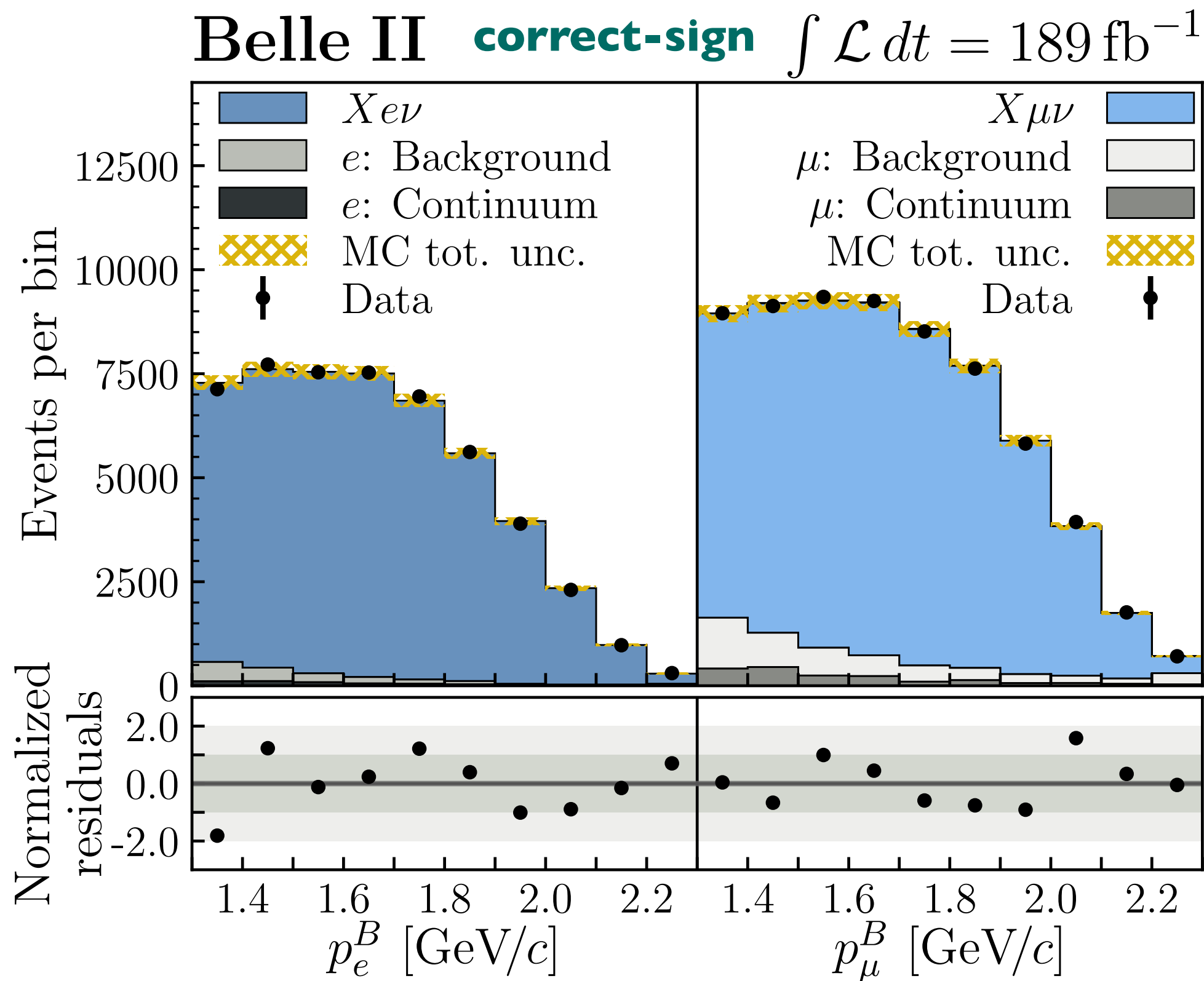
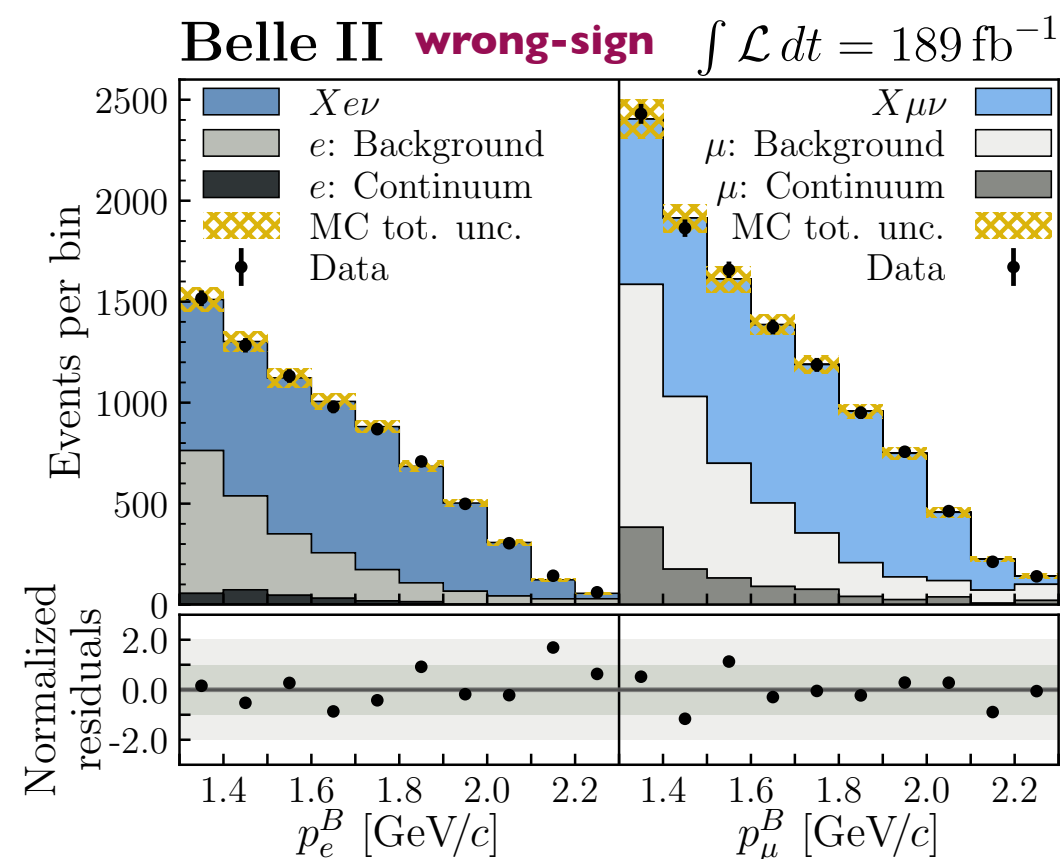
- Continuum bkgd. is Gaussian-constrained by off-resonance data
- Exploit  $B_{\text{tag}} - \ell$  charge correlation

✓ For  $B_{\text{tag}}^+$ , signal lepton is  $\ell^-$

✓ For  $B_{\text{tag}}^0$ , signal lepton is  $\ell^-$ , except for  $B\bar{B}$  mixing

✓ Fake & secondary leptons are Gaussian-constrained by simultaneously fitting the  $p_\ell^B$  in wrong-sign sample (left)

# LFU test with inclusive $B \rightarrow X\ell\nu$



$$R(X_{e/\mu})$$

$$= 1.007 \pm 0.009 \pm 0.019$$

*the most precise BF-based LFU test,  
and consistent with SM*



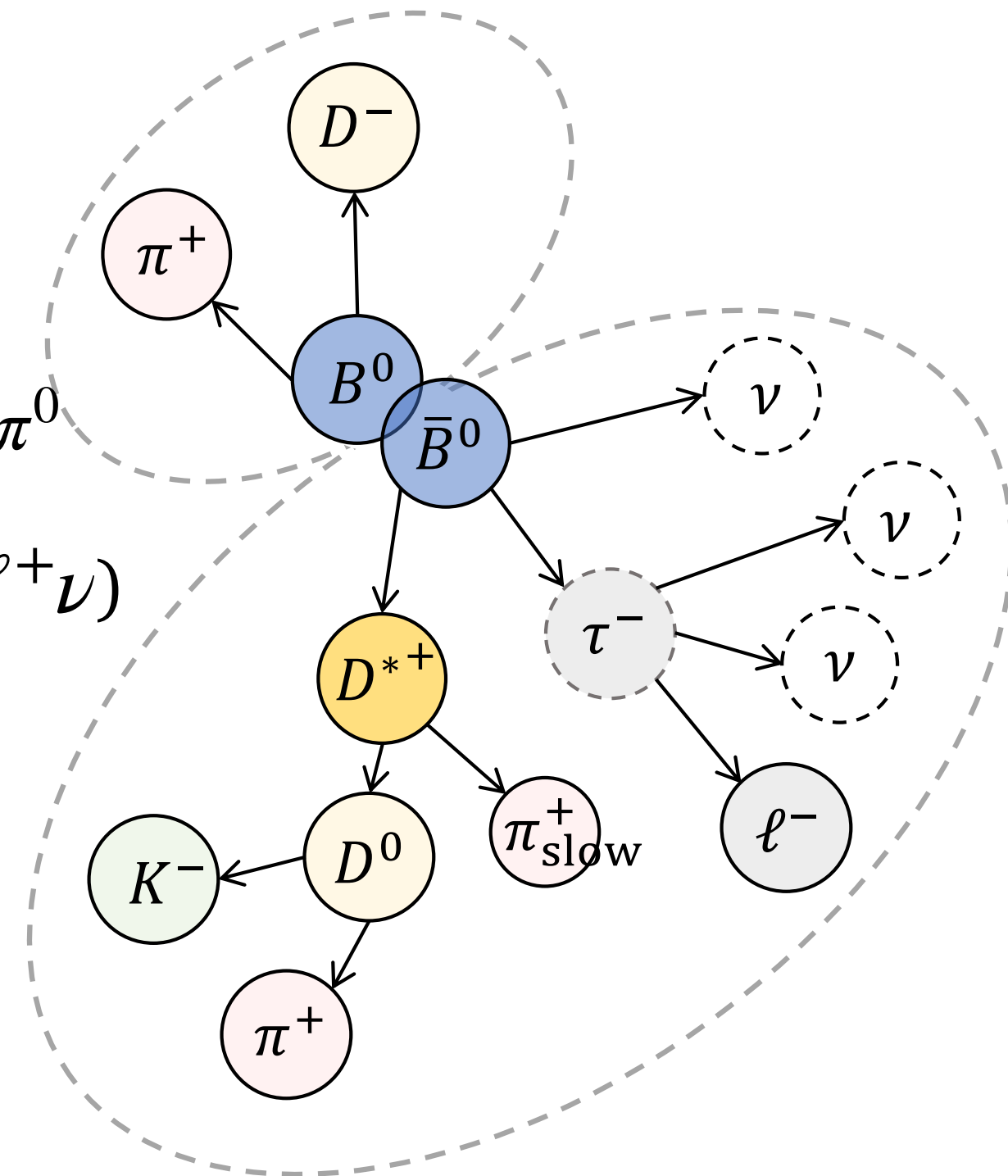
# $R(D^*)$ from Belle II

$$R(D^*) \equiv \frac{\mathcal{B}(B \rightarrow D^* \tau^+ \nu)}{\mathcal{B}(B \rightarrow D^* \ell^+ \nu)}$$

- First  $R(D^*)$  result from Belle II
- Analysis features
  - Use hadronic B-tagging with FEI (slide 31)
  - leptonic  $\tau$  decays,  $\tau^+ \rightarrow \ell^+ \nu_\ell \bar{\nu}_\tau$
  - three  $D^*$  modes:  $D^{*+} \rightarrow D^0 \pi^+$ ,  $D^+ \pi^0$  and  $D^{*0} \rightarrow D^0 \pi^0$
- Signal ( $B \rightarrow D^* \tau^+ \nu$ ) & Normalization ( $B \rightarrow D^* \ell^+ \nu$ )
  - extracted simultaneously
  - by fitting 2D  $(M_{\text{miss}}^2, E_{\text{ECL}})$

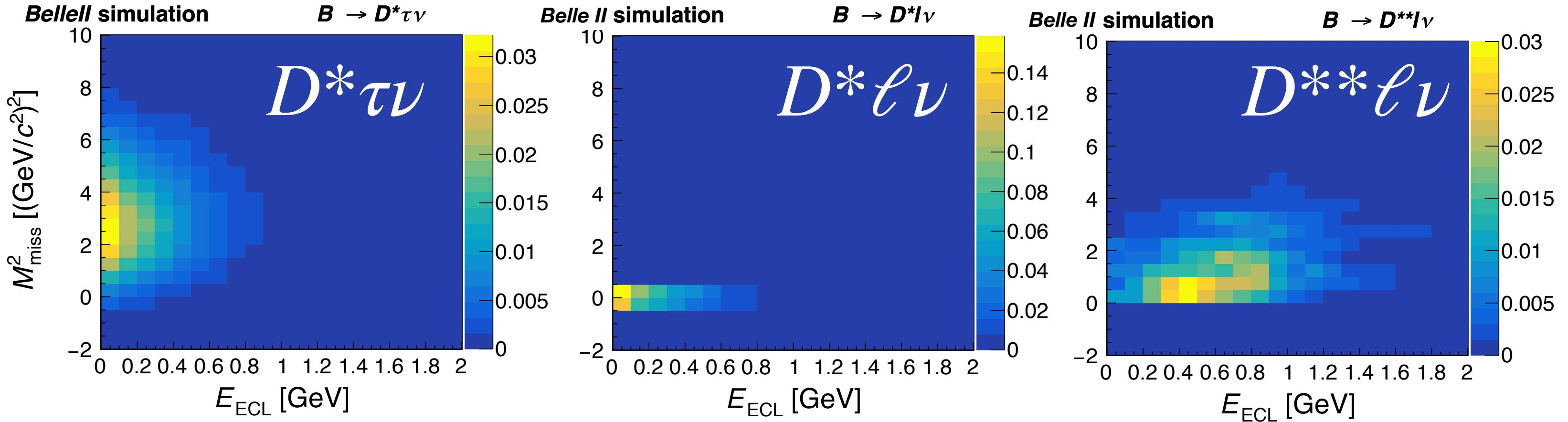
$$M_{\text{miss}}^2 \equiv (p_{e^+e^-} - p_{B_{\text{tag}}} - p_{D^*} - p_\ell)^2$$

$E_{\text{ECL}}$  = extra energy (unmatched) in the EM calorimeter



# $R(D^*)$ from Belle II

New for July, 2023  
Preliminary



## ● Signal ( $B \rightarrow D^* \tau^+ \nu$ ) & Normalization ( $B \rightarrow D^* \ell^+ \nu$ )

- extracted simultaneously
- by fitting 2D  $(M_{\text{miss}}^2, E_{\text{ECL}})$

$$M_{\text{miss}}^2 \equiv (p_{e^+e^-} - p_{B_{\text{tag}}} - p_{D^*} - p_{\ell})^2$$

$E_{\text{ECL}}$  = extra energy (unmatched) in the EM calorimeter

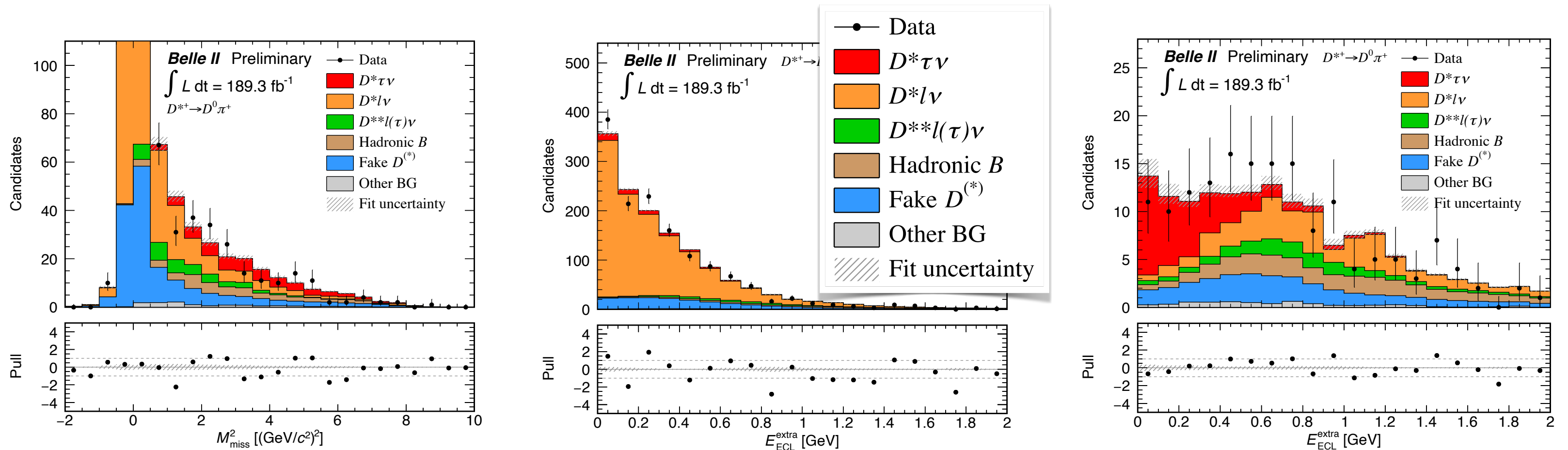
# $R(D^*)$ from Belle II

$\mathcal{L}_{\text{int}} = 189 \text{ fb}^{-1}$

New for July, 2023  
Preliminary



## Fit projections for the sub-mode $D^{*+} \rightarrow D^0 \pi^+$



$M^2_{\text{miss}}$  (peak-bin yield  $\sim O(600)$ )

$E_{\text{ECL}}^{\text{extra}}$  for entire  $M^2_{\text{miss}}$  region

$E_{\text{ECL}}^{\text{extra}}$  for signal-enhanced region  
 $1.5 < M^2_{\text{miss}} < 6.0 \text{ GeV}^2$

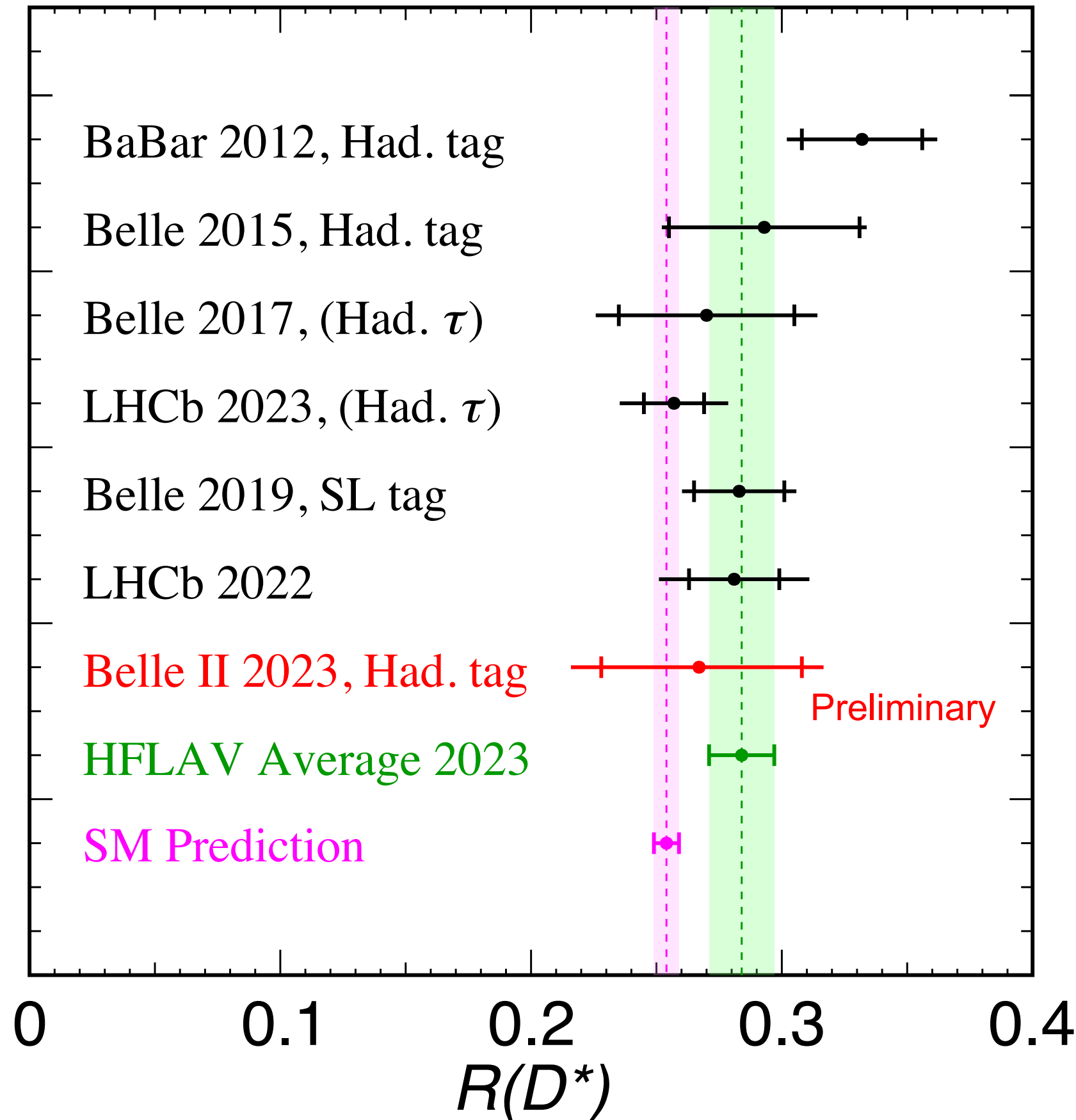
$$R(D^*) = 0.267^{+0.041+0.028}_{-0.039-0.033}$$

## Systematics

- dominant sources:  $E_{\text{ECL}}$  PDF shape, MC statistics

# $R(D^*)$ from Belle II

New for July, 2023  
Preliminary



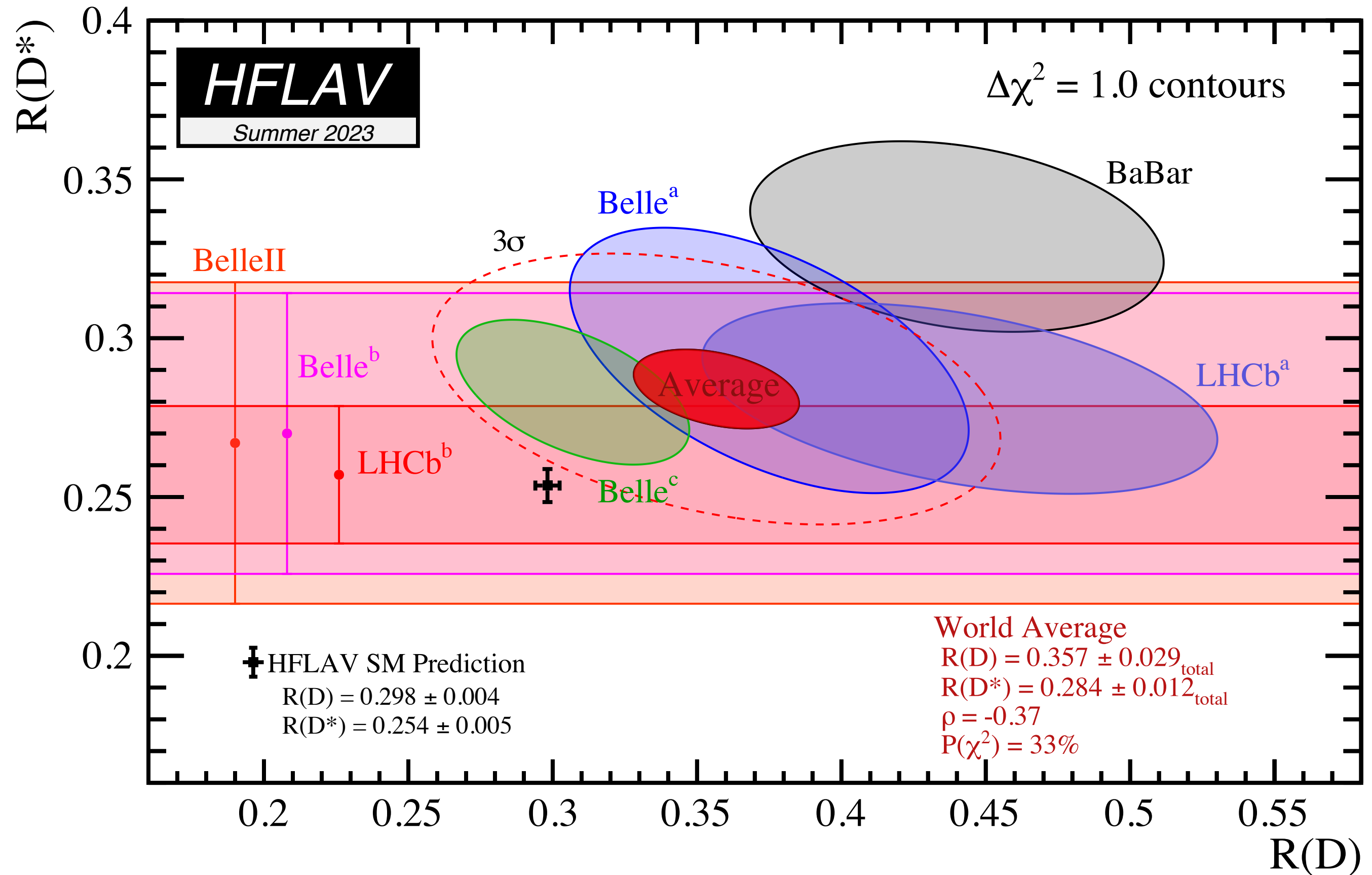
	5 ab <sup>-1</sup>	50 ab <sup>-1</sup>
$R_D$	(±6.0 ± 3.9)%	(±2.0 ± 2.5)%
$R_{D^*}$	(±3.0 ± 2.5)%	(±1.0 ± 2.0)%
$P_\tau(D^*)$	±0.18 ± 0.08	±0.06 ± 0.04

Belle II expected precision, from  
The Belle II Physics Book, PTEP 2019 (2019) 123C01

**new Belle II result is consistent with both  
the SM and the HFLAV average**

$$R(D^*) = 0.267^{+0.041}_{-0.039} +0.028_{-0.033}$$

# $R(D)$ vs. $R(D^*)$ , updated



# Closing remarks

- Precise determination of the CKM matrix elements is crucial for testing the Standard Model. The magnitudes of these elements, in particular,  $V_{cb}$  and  $V_{ub}$ , are best measured by using B-meson semileptonic decays.
- Moreover, semileptonic B-meson decays provide a great testing ground for lepton universality of charged-current weak interaction processes.
- We reported recent unique and/or competitive results of inclusive and exclusive B-meson semileptonic decays, from the Belle II and Belle experiments.
- For some of these results, tag-side reconstruction of a companion B-meson decay has been exploited, which is now a unique feature of Belle II.
- For bottom line, using  $189 \text{ fb}^{-1}$  data sample, Belle II has made 1) precise measurement of inclusive ratio,  $R(X_{e/\mu})$  and 2) its first contribution to  $R(D^*)$ .

*Thank you!*

# *Appendices*

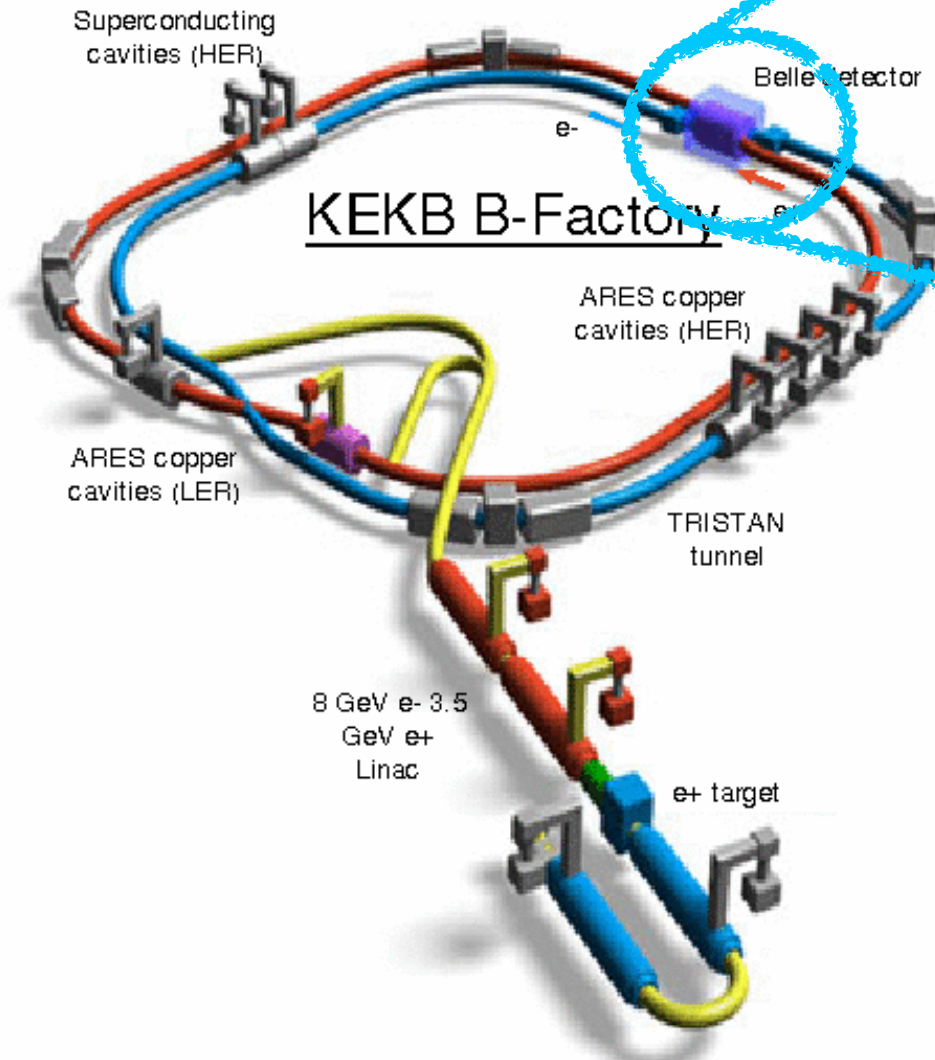


# *Appendix 0 The apparatuses*



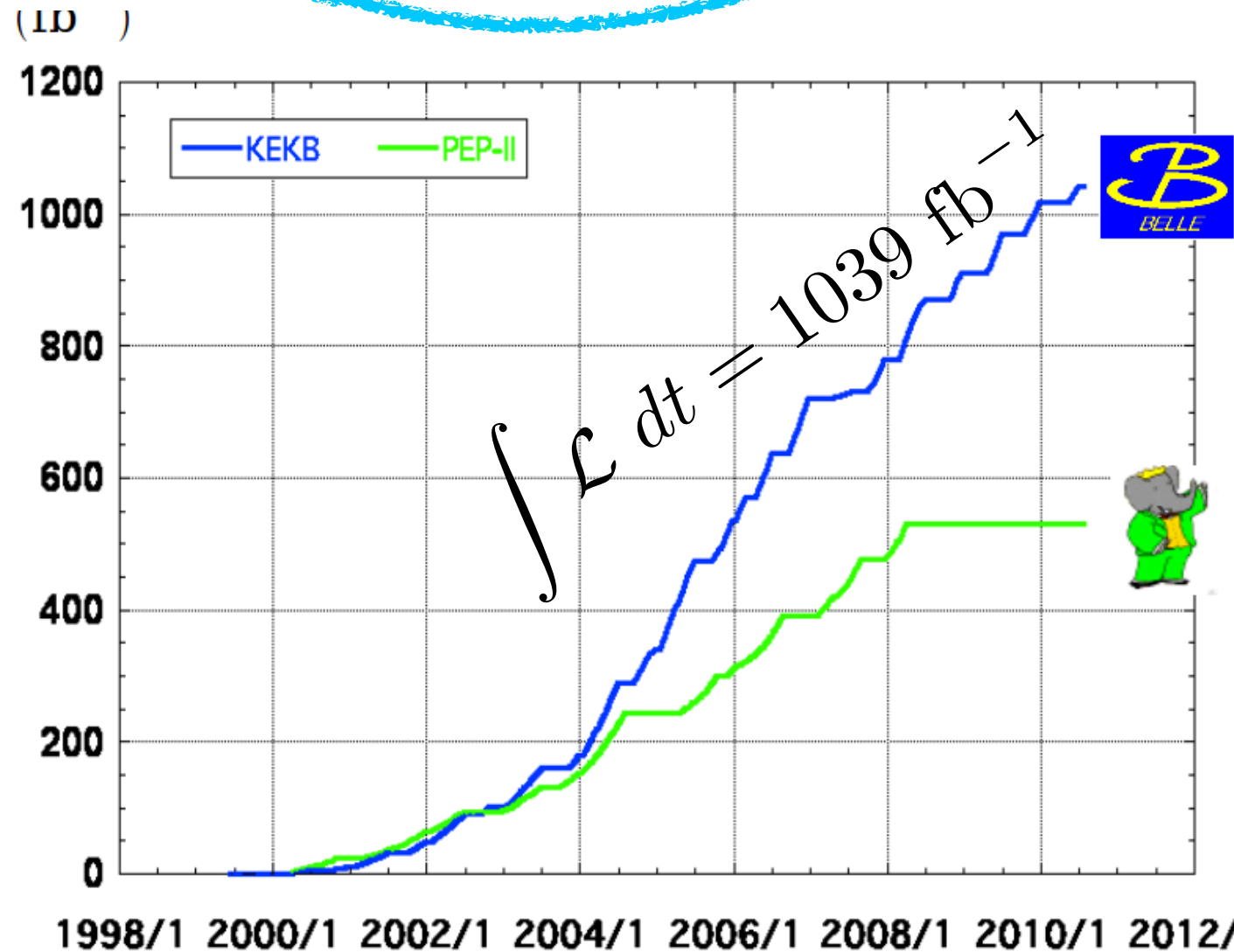
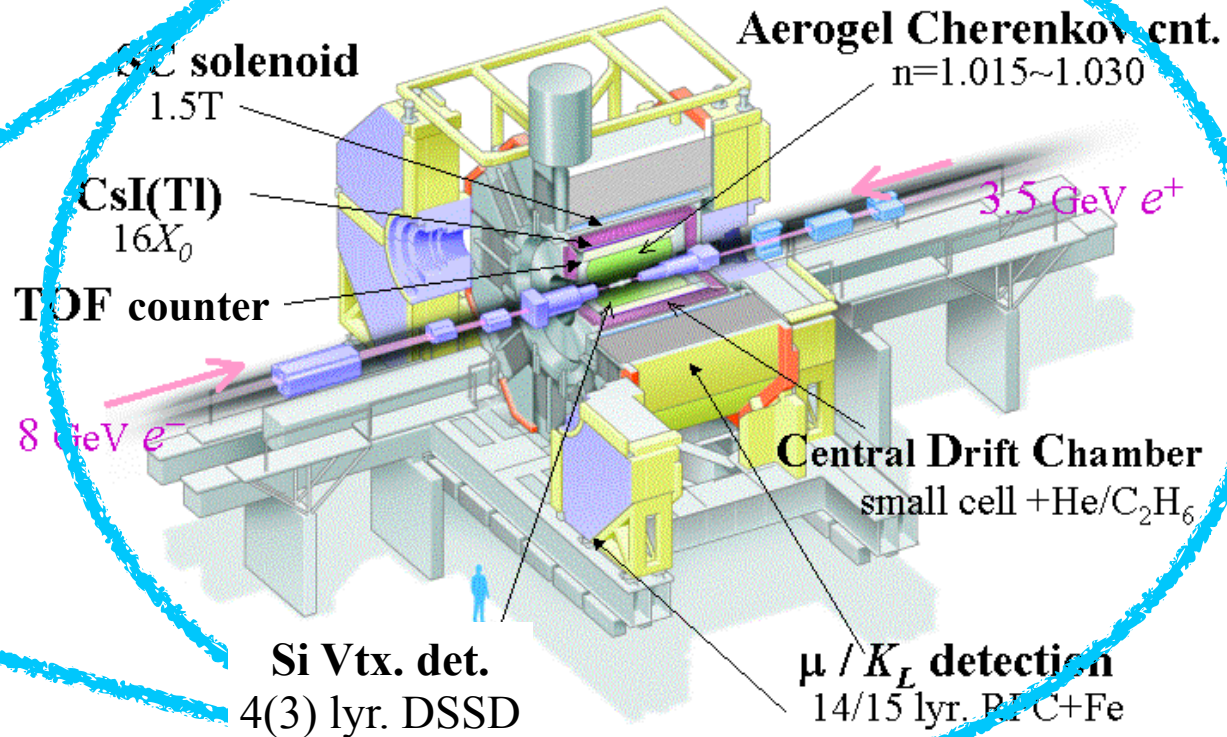
22 countries  
100 institutions  
~450 members

$$\mathcal{L}_{\text{peak}} = 21.1 \text{ nb}^{-1} \text{ s}^{-1}$$



$$e^- \xrightarrow{8 \text{ GeV}} (\star) \xleftarrow{3.5 \text{ GeV}} e^+$$

# Belle Detector

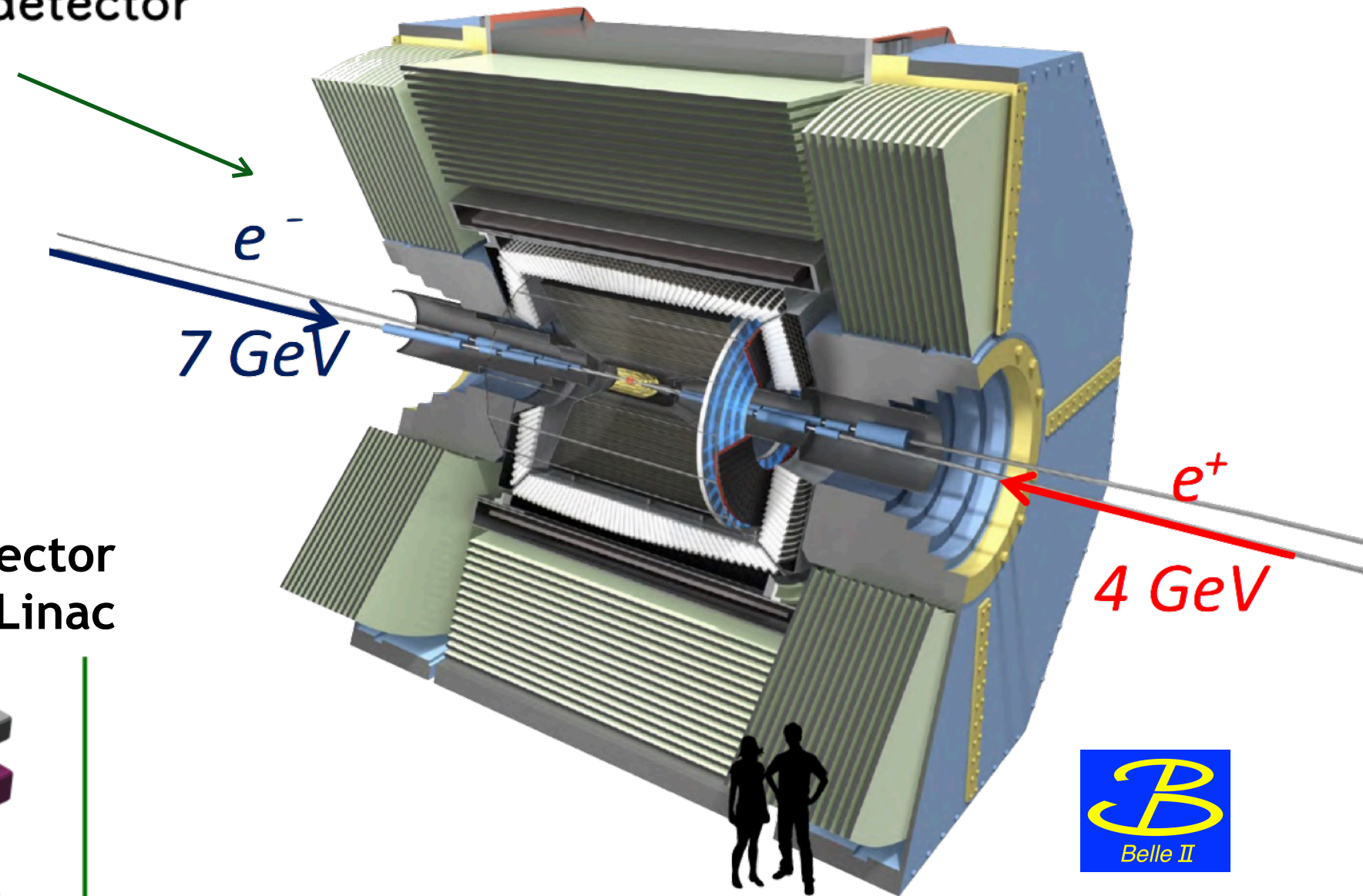
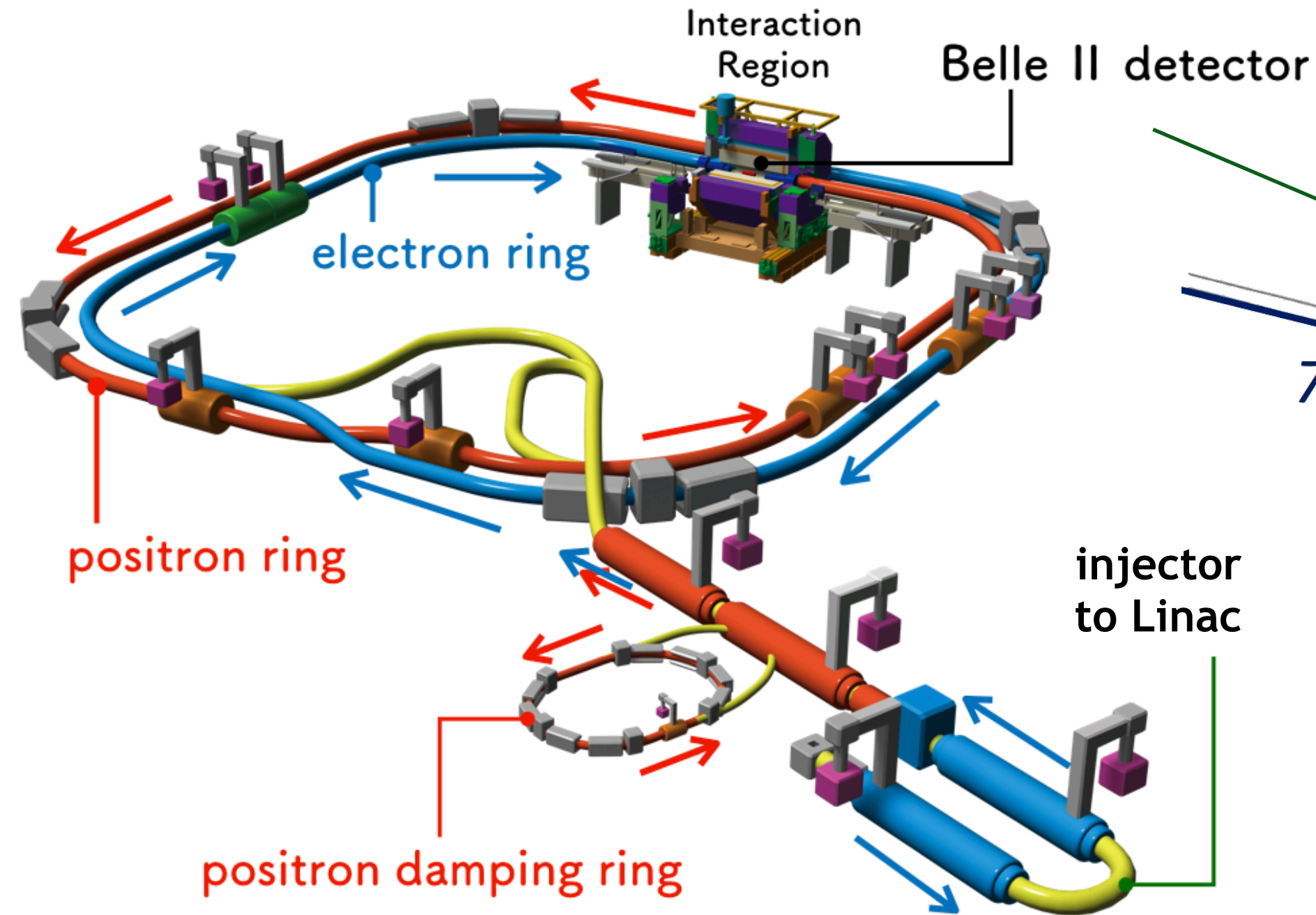


**> 1 ab<sup>-1</sup>**  
**On resonance:**  
 $\Upsilon(5S): 121 \text{ fb}^{-1}$   
 $\Upsilon(4S): 711 \text{ fb}^{-1}$   
 $\Upsilon(3S): 3 \text{ fb}^{-1}$   
 $\Upsilon(2S): 25 \text{ fb}^{-1}$   
 $\Upsilon(1S): 6 \text{ fb}^{-1}$   
**Off reson./scan:**  
 $\sim 100 \text{ fb}^{-1}$

**~ 550 fb<sup>-1</sup>**  
**On resonance:**  
 $\Upsilon(4S): 433 \text{ fb}^{-1}$   
 $\Upsilon(3S): 30 \text{ fb}^{-1}$   
 $\Upsilon(2S): 14 \text{ fb}^{-1}$   
**Off resonance:**  
 $\sim 54 \text{ fb}^{-1}$

# SuperKEKB

# Belle II



$$e^- \xrightarrow{7 \text{ GeV}} (\star) \xleftarrow{4 \text{ GeV}} e^+$$

$$\mathcal{L} = 6.5 \times 10^{35} \text{ cm}^{-2} \text{ s}^{-1}$$

$$\int^{\text{goal}} \mathcal{L} dt = 50 \text{ ab}^{-1}$$

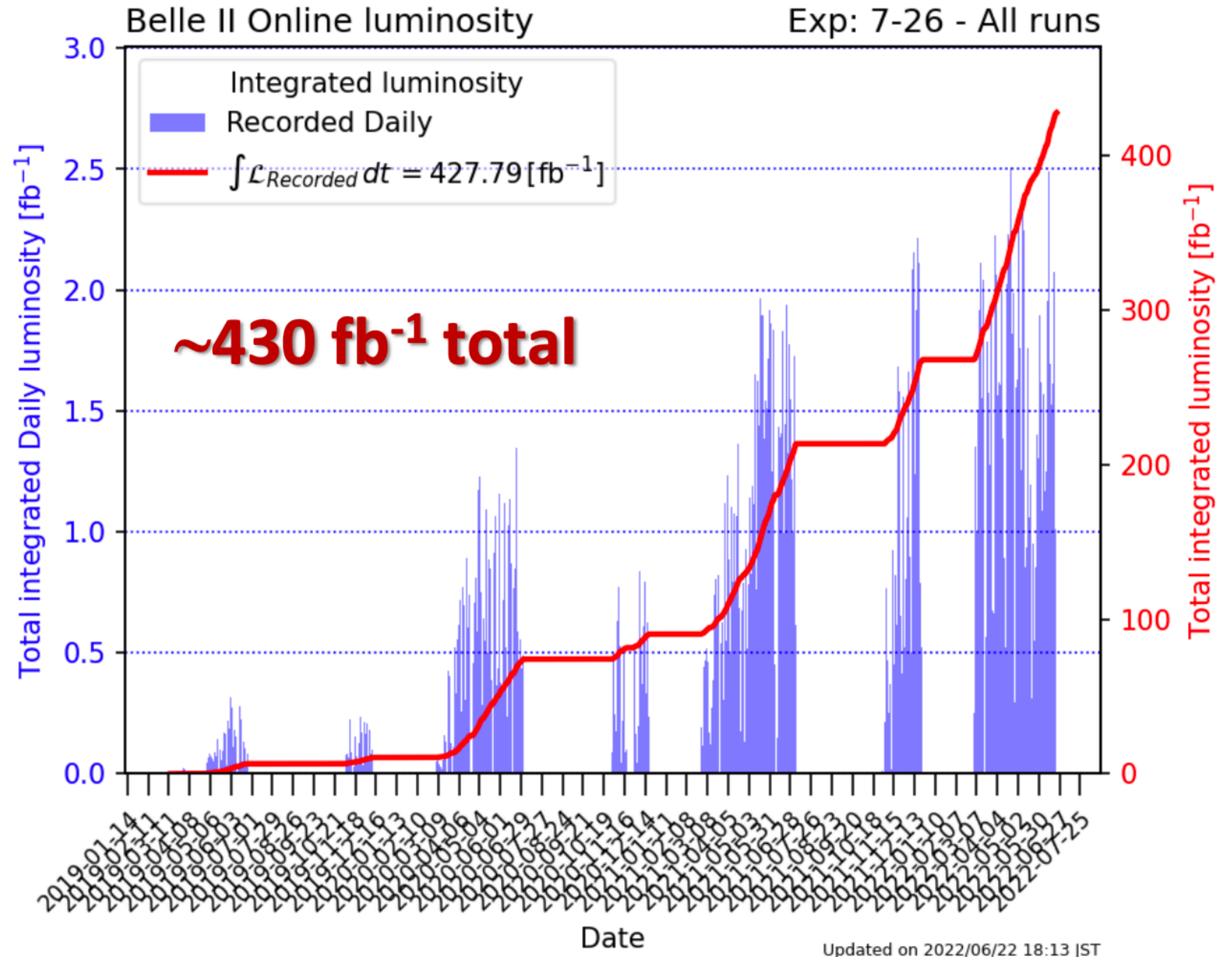


# Belle II

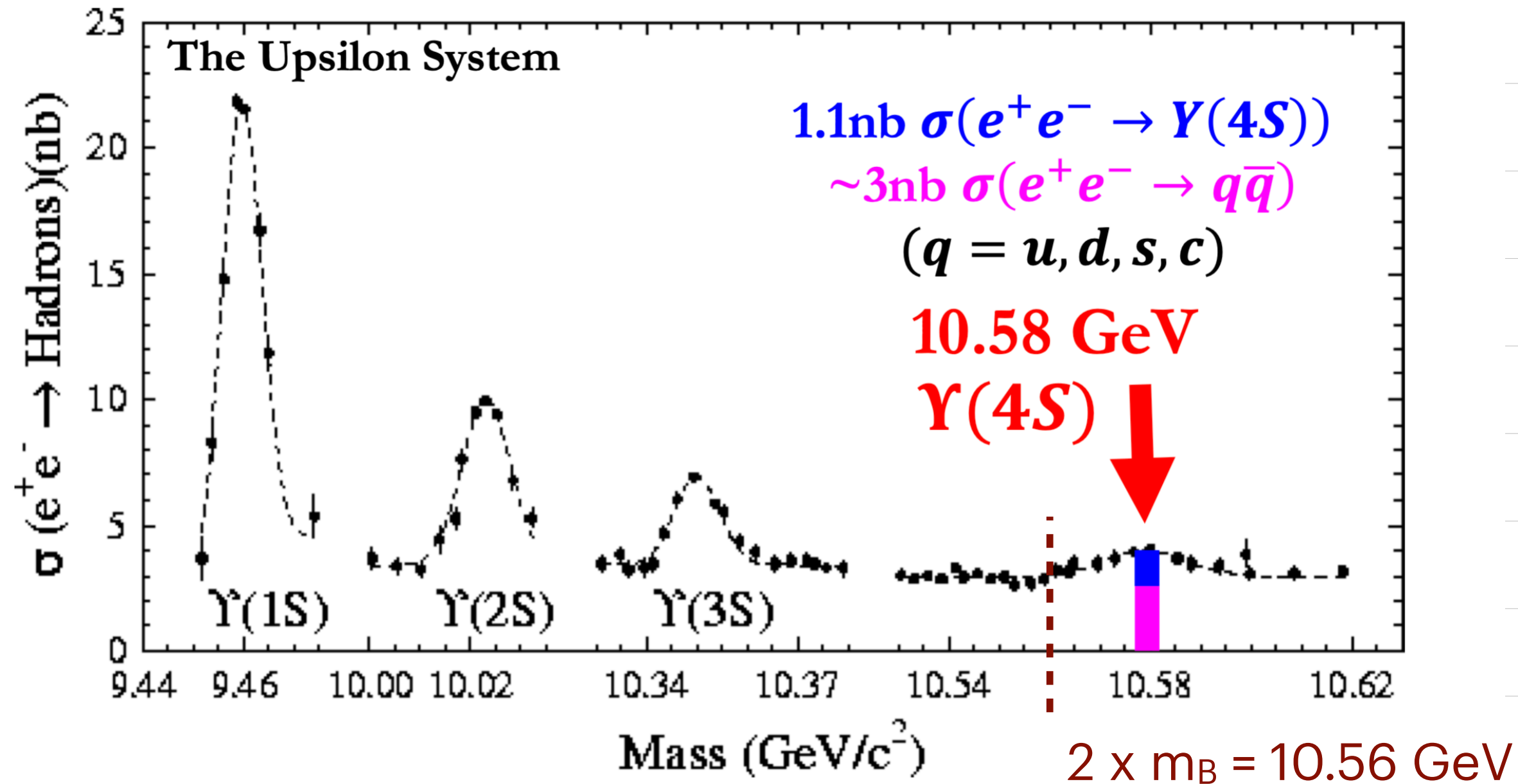
## Collected luminosity before LS1 (2019-2022)

Belle II was in operation through the Pandemic era, with modified working mode in accordance with the anti-pandemic policy.

**peak luminosity world record**  
 $4.7 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$



# $e^+e^- \rightarrow \Upsilon(4S)$ as a $B$ -factory

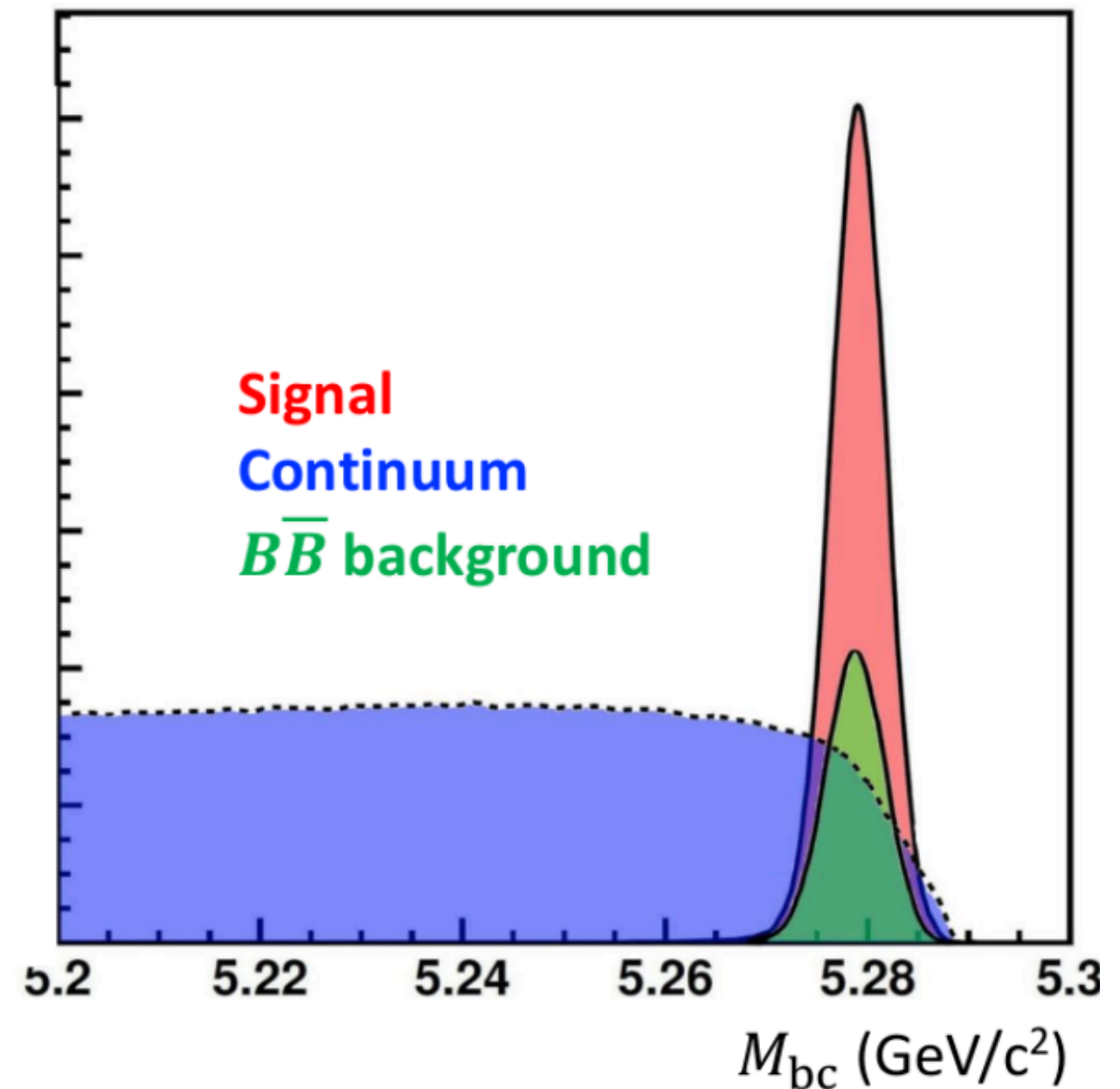
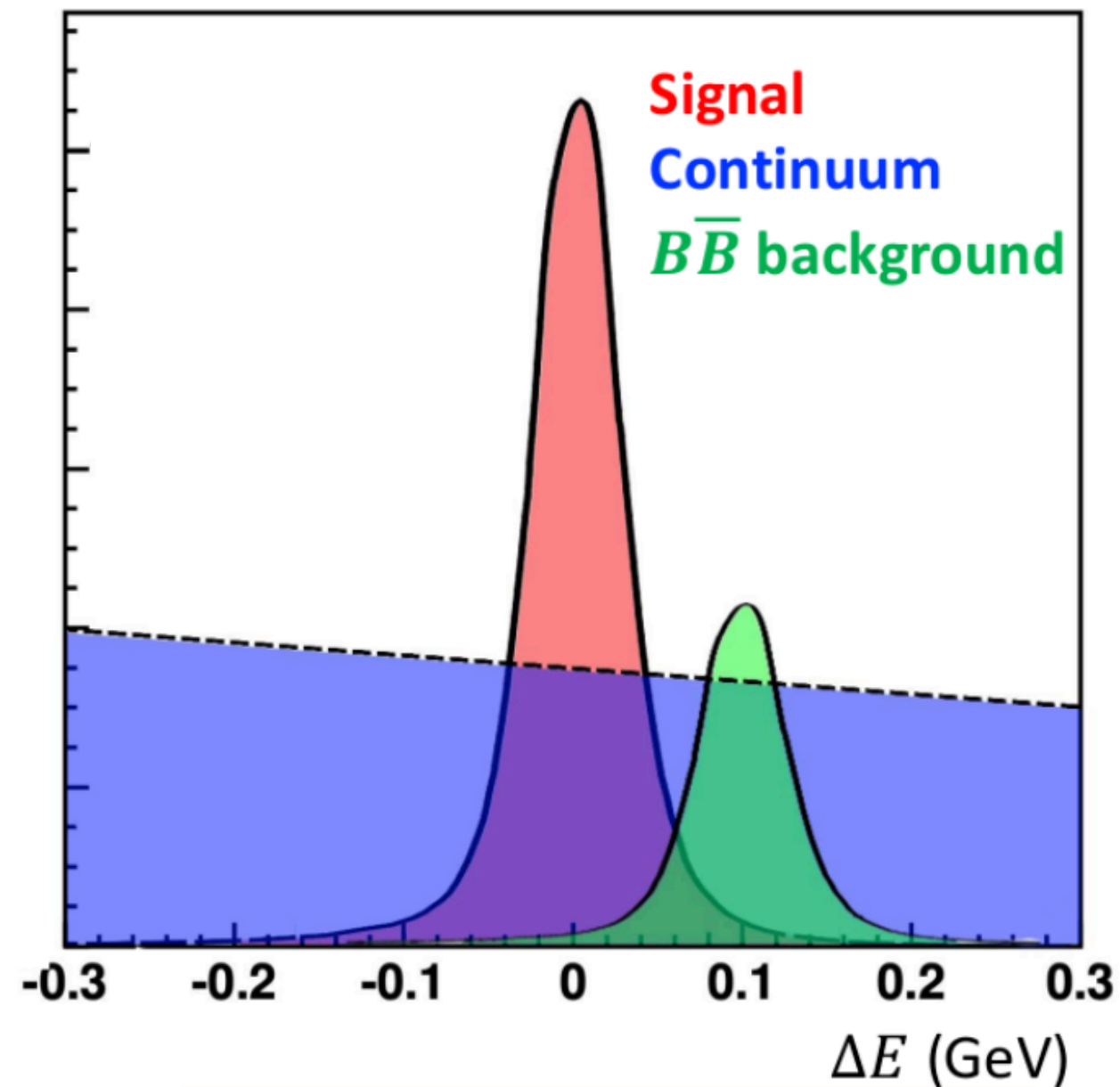


- $\mathcal{B}(Y(4S) \rightarrow B\bar{B}) > 96\%$ , with  $p_B^{CM} \sim 0.35 \text{ GeV}/c$
- nothing else but  $B\bar{B}$  in the final state  
 $\therefore$  if we know  $(E, \vec{p})$  of one  $B$ , the other  $B$  is also constrained

# Key variables of $B$ decays

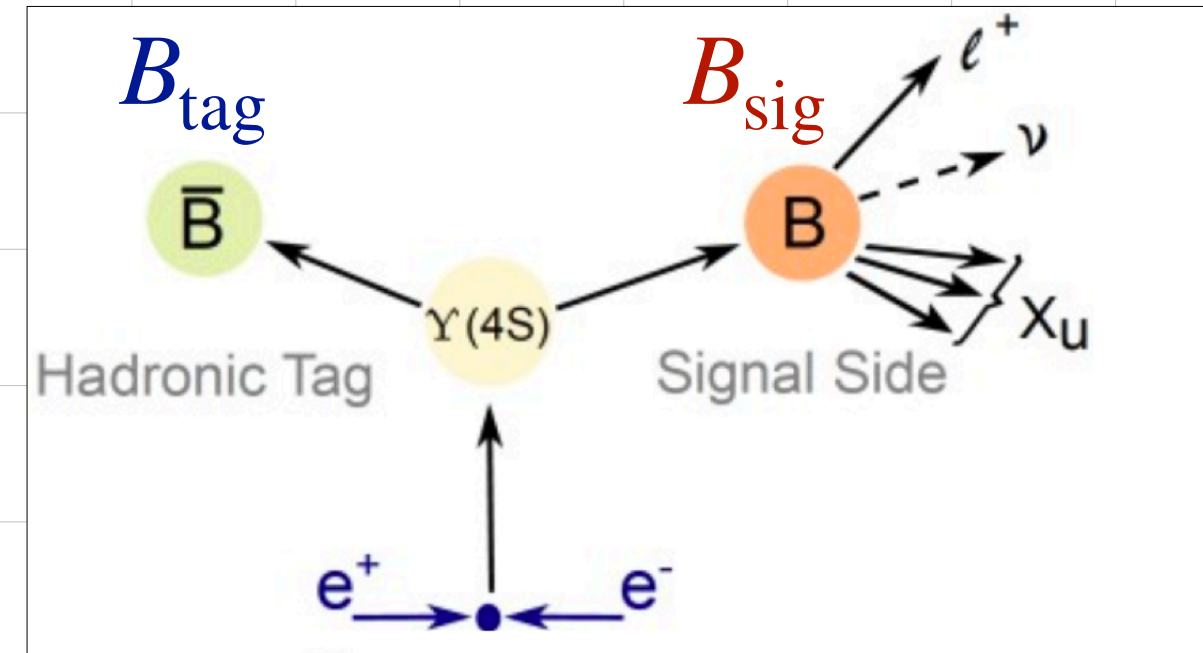
$$\Delta E = E_B^* - \sqrt{s}/2$$

$$M_{bc} = \sqrt{(\sqrt{s}/2)^2 - \vec{p}_B^{*2}}$$

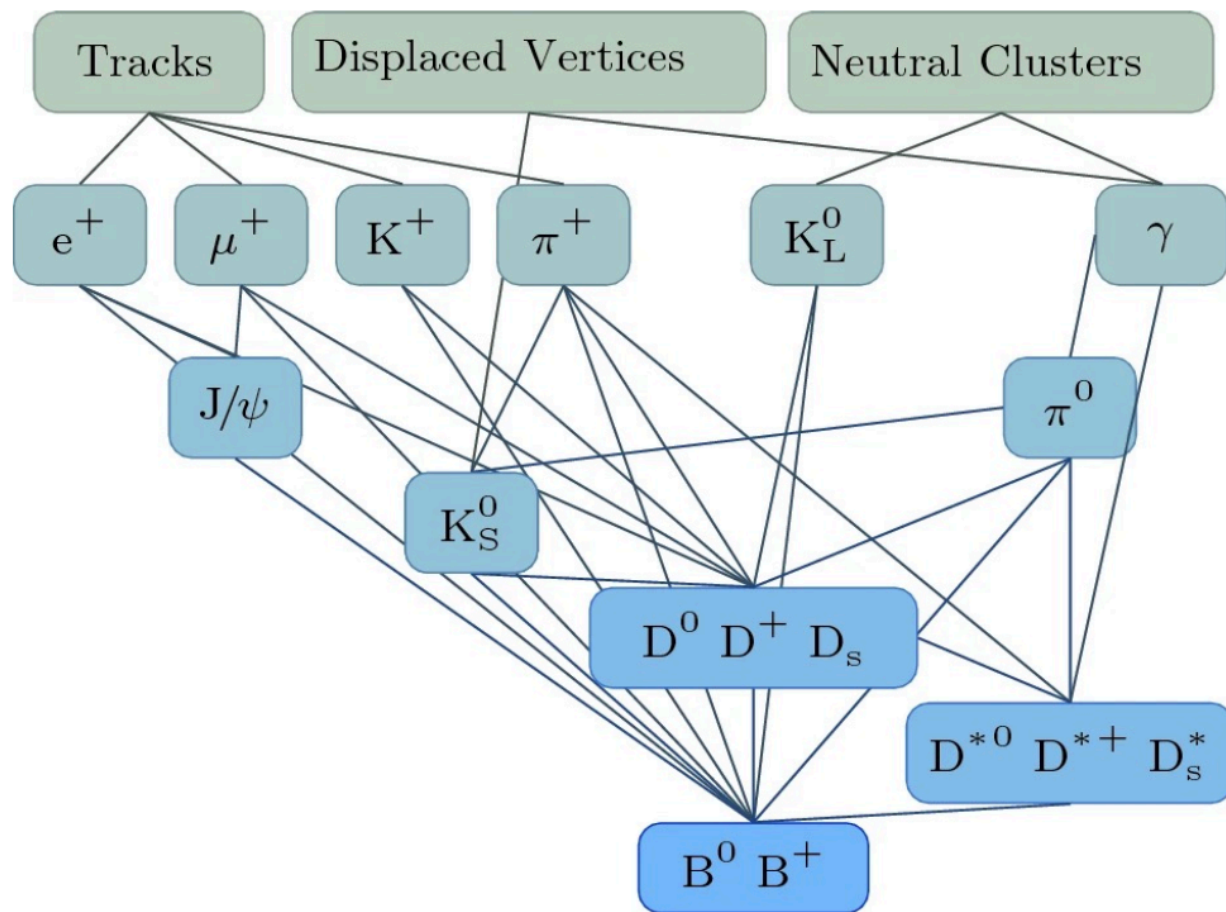


# Full Event Interpretation (FEI)

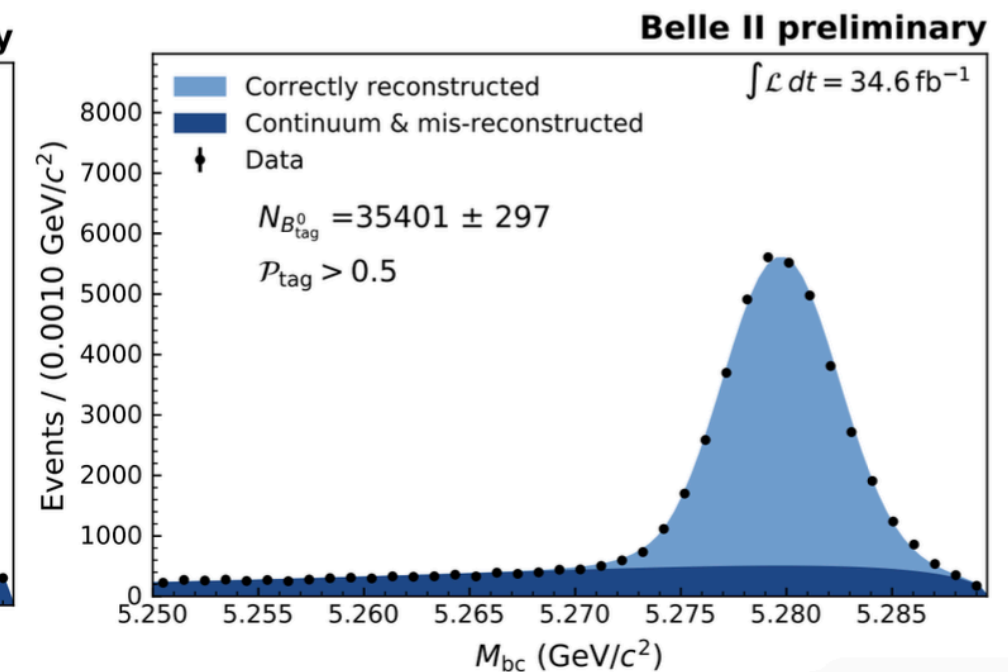
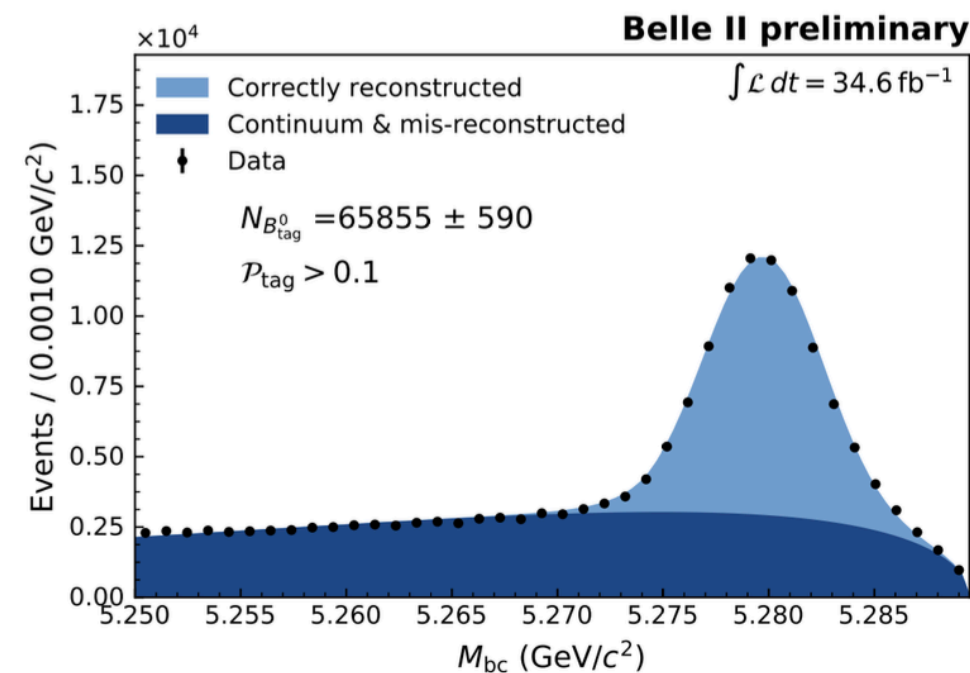
- FEI algorithm to reconstruct  $B_{\text{tag}}$ 
  - uses  $\sim 200$  BDT's to reconstruct  $\mathcal{O}(10^4)$  different  $B$  decay chains
  - assign signal probability of being correct  $B_{\text{tag}}$



Comput Softw Big Sci 3, 6 (2019)



arXiv:2008.060965



# *Appendix 1 Exclusive*

*$B \rightarrow D^{(*)} \ell^+ \nu$  for  $V_{cb}$*



# $B \rightarrow D^* \ell^+ \nu$ shapes & $|V_{cb}|$

## Differential shapes (normalized) of $B \rightarrow D^* \ell^+ \nu$

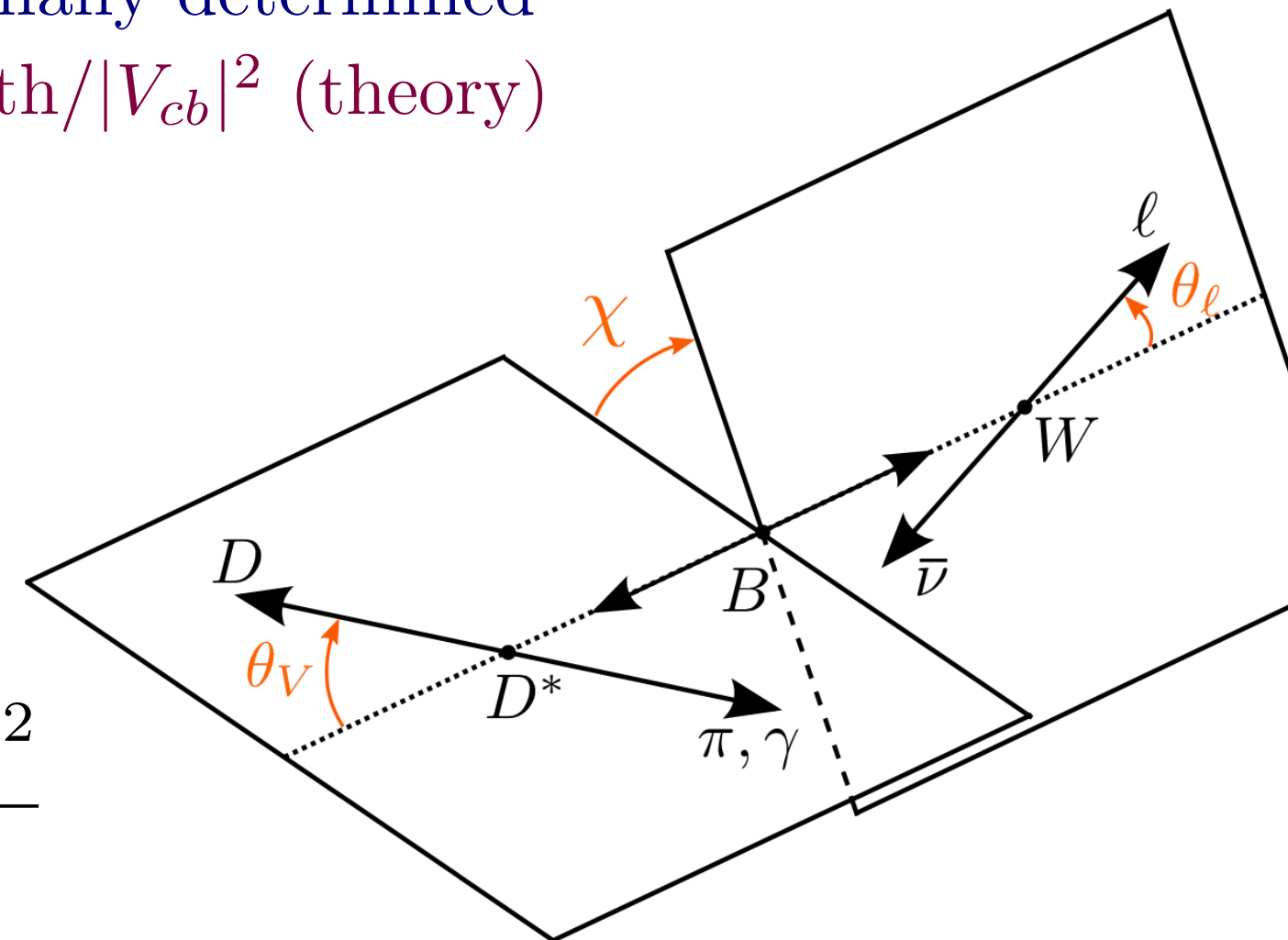
- as input to determine the non-perturbative form factor
- once FF shape is known, it can be combined with L-QCD (or other methods) for the absolute normalization to determine  $|V_{cb}|$

$$|V_{cb}| = \sqrt{\frac{\mathcal{B}(B \rightarrow D^* \ell \bar{\nu}_\ell)}{\tau_B \Gamma(B \rightarrow D^* \ell \bar{\nu}_\ell)}}$$

$\mathcal{B}$  – externally determined  
 $\Gamma = \text{decay width}/|V_{cb}|^2$  (theory)

- use hadronic  $B$ -tagging via FEI
- L-QCD at zero recoil ( $w = 1$ ) is used for  $|V_{cb}|$

$$\begin{aligned} w &= v \cdot v' \\ &= \frac{m_B^2 + m_{D^*}^2 - q^2}{2m_B m_{D^*}} \end{aligned}$$



# $B \rightarrow D^* \ell^+ \nu$ shapes & $|V_{cb}|$

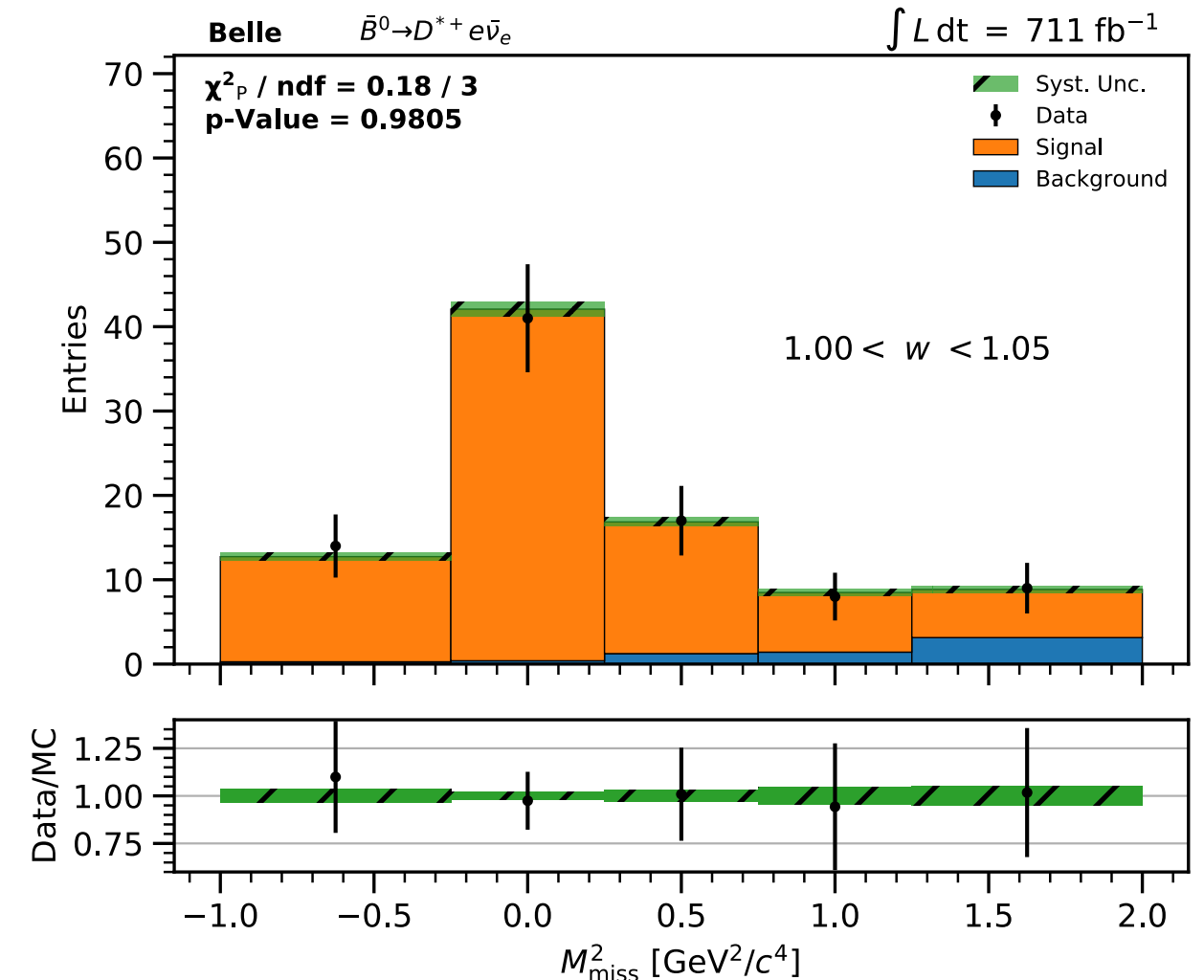
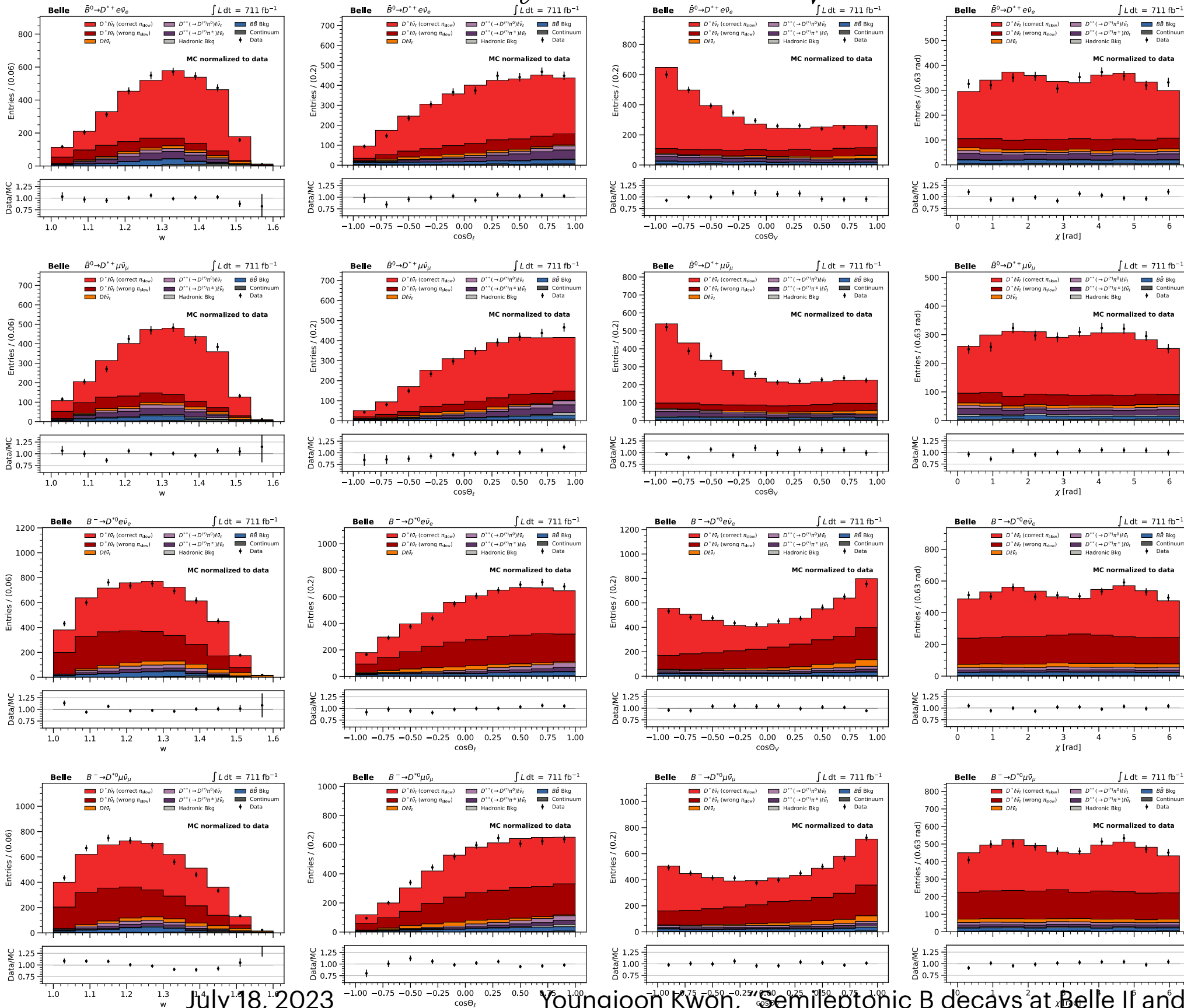
$w$

$\cos \theta_\ell$

$\cos \theta_V$

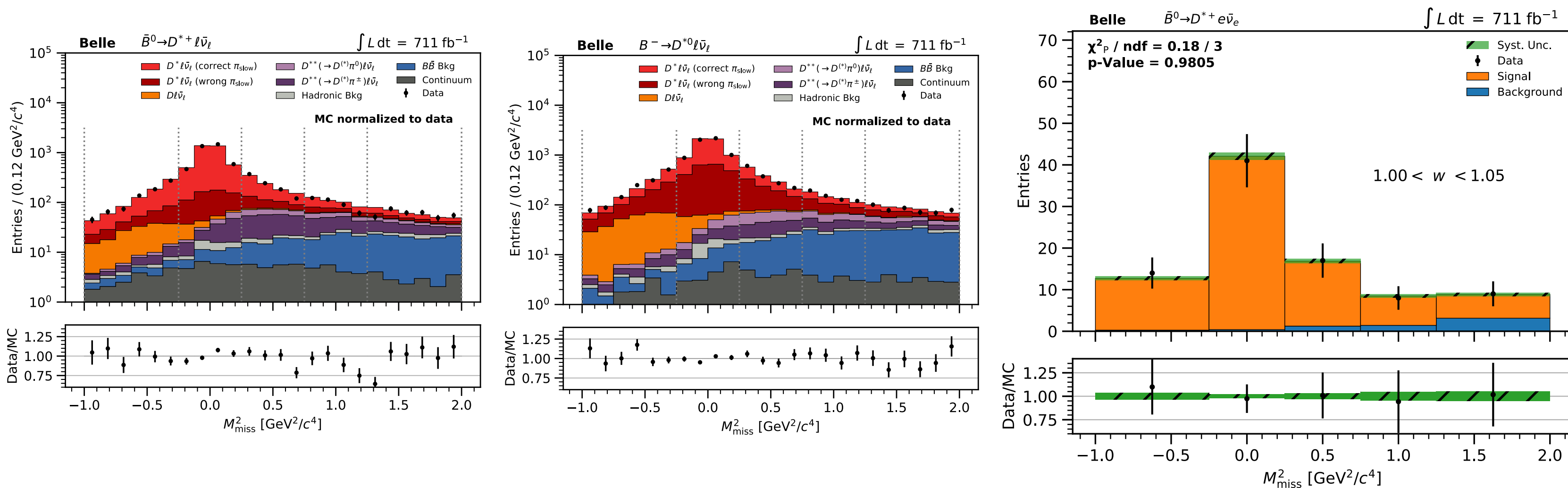
$\chi$

- Full correlations b/w the projections are also determined
- Bkgd. subtraction, with binned likelihood fits to  $M_{\text{miss}}^2$



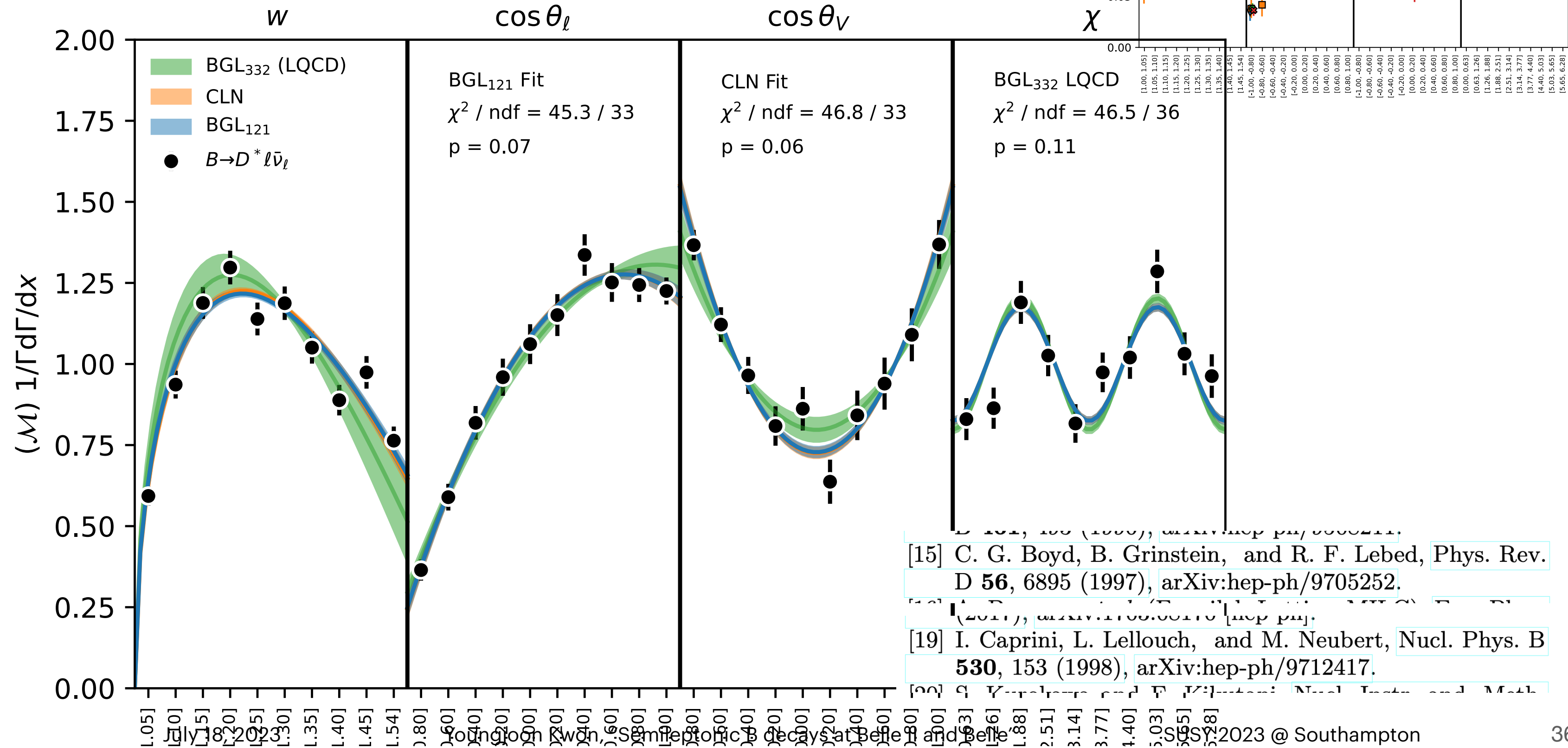
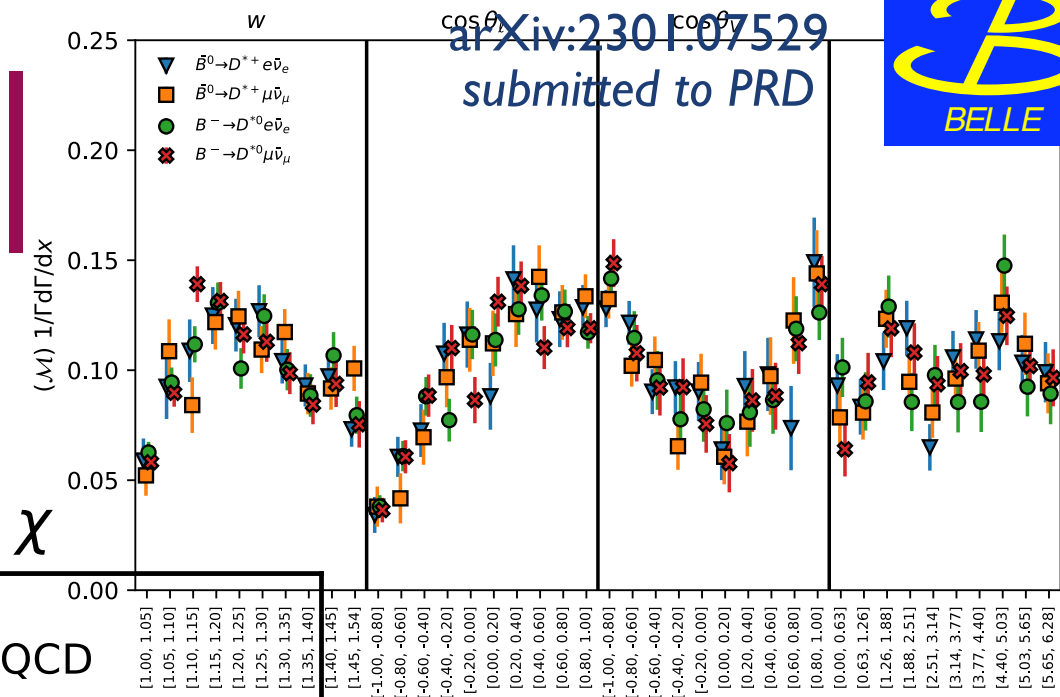
# $B \rightarrow D^* \ell^+ \nu$ shapes & $|V_{cb}|$

background subtraction, with binned likelihood fits to  $M_{\text{miss}}^2$



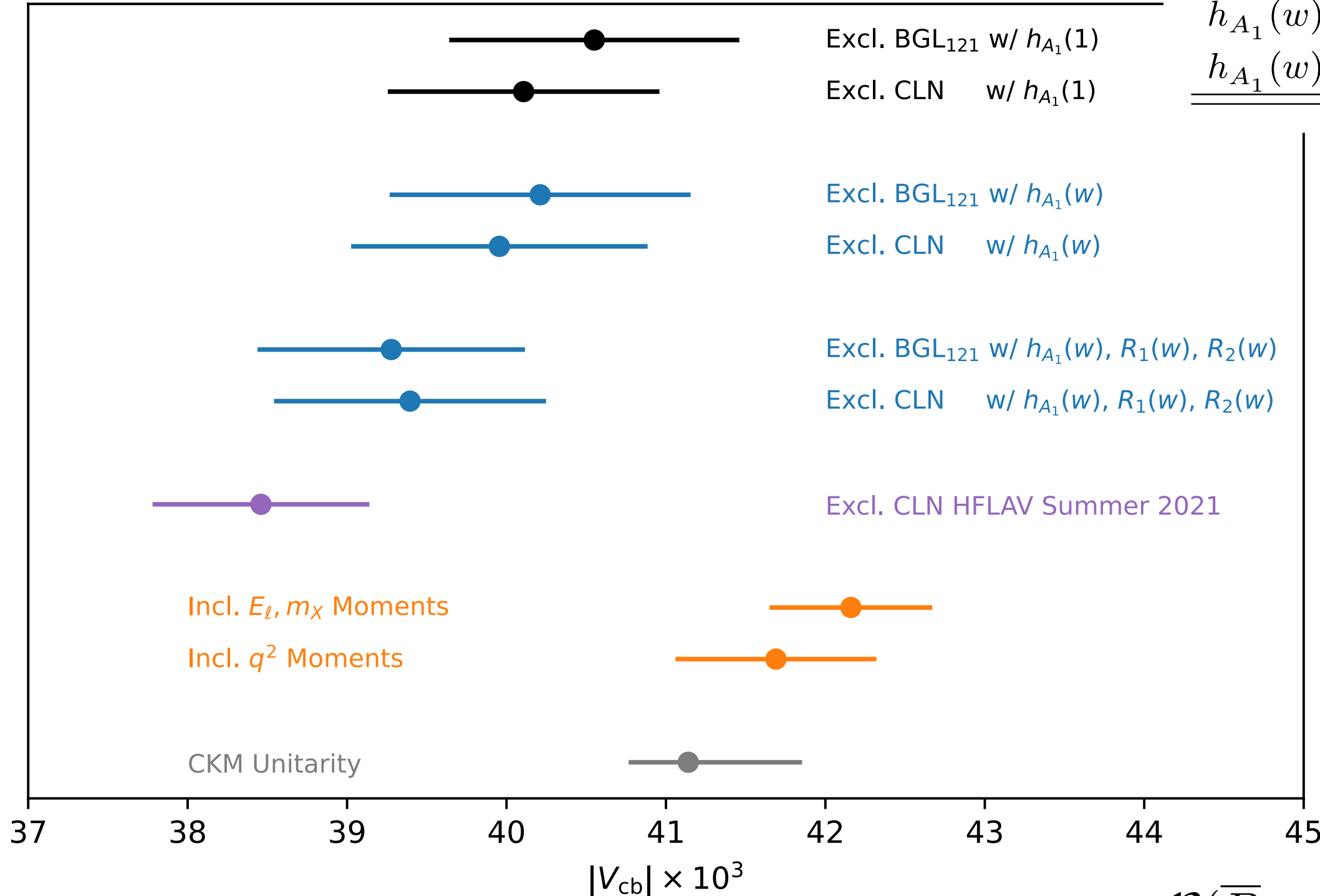
# $B \rightarrow D^* \ell^+ \nu$ shapes & $|V_{cb}|$

fitted shapes to BGL & CLN models



# $B \rightarrow D^* \ell^+ \nu$ shapes & $|V_{cb}|$

## $|V_{cb}|$ and other results



	BGL <sub>121</sub>	CLN
$h_{A_1}(1)$	$40.6 \pm 0.9$	$40.1 \pm 0.9$
$h_{A_1}(w)$	$40.2 \pm 0.9$	$40.0 \pm 0.9$
$h_{A_1}(w), R_1(w), R_2(w)$	$39.3 \pm 0.8$	$39.4 \pm 0.9$

$$\Delta A_{\text{FB}} = A_{\text{FB}}^\mu - A_{\text{FB}}^e$$

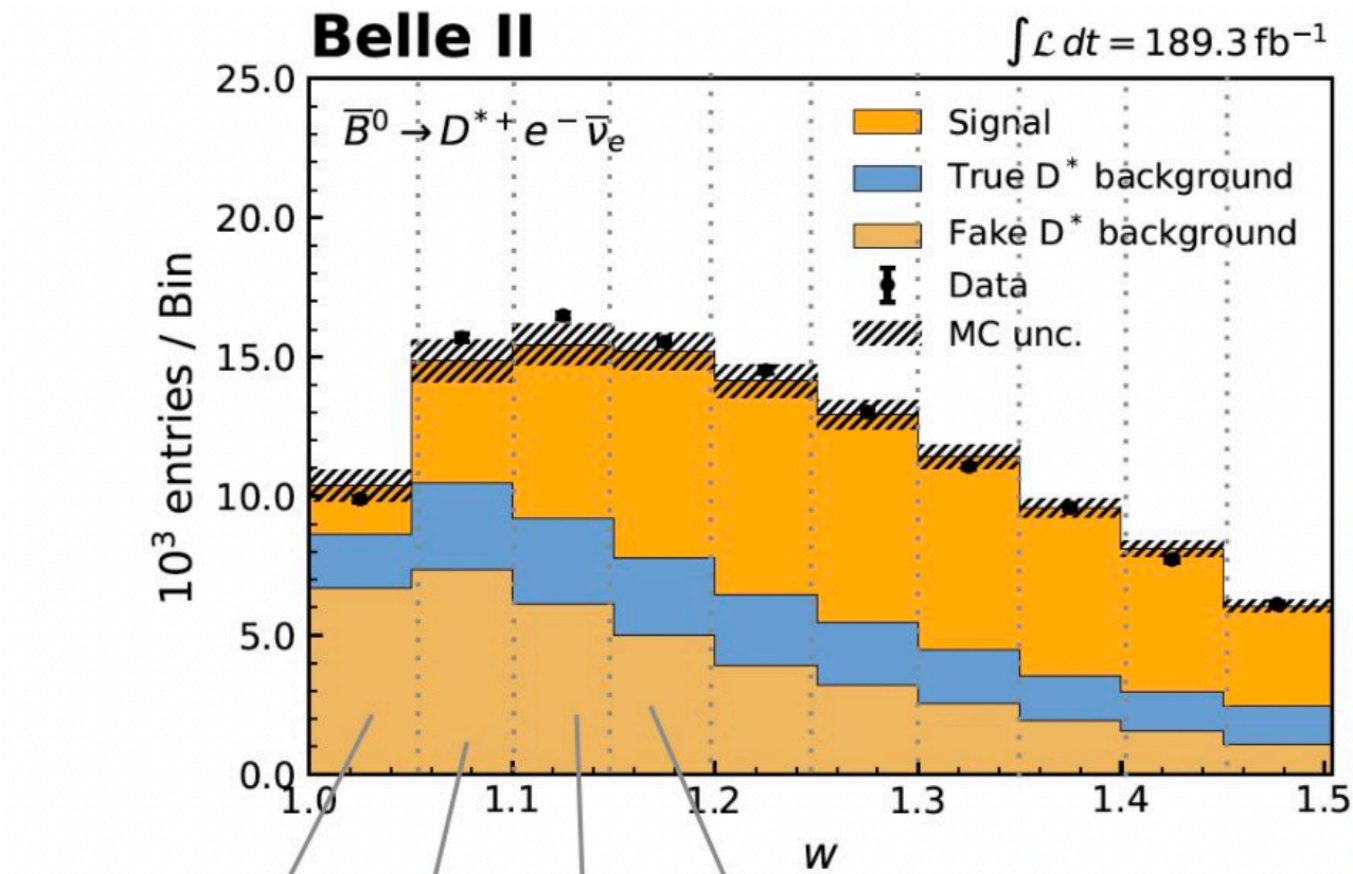
	$\Delta A_{\text{FB}}$
$\bar{B}^0 \rightarrow D^{*+} \ell \bar{\nu}_\ell$	$0.062 \pm 0.044 \pm 0.011$
$B^- \rightarrow D^{*0} \ell \bar{\nu}_\ell$	$-0.003 \pm 0.033 \pm 0.009$
$B \rightarrow D^* \ell \bar{\nu}_\ell$	$0.022 \pm 0.026 \pm 0.007$

$$\Delta F_L = F_L^\mu - F_L^e$$

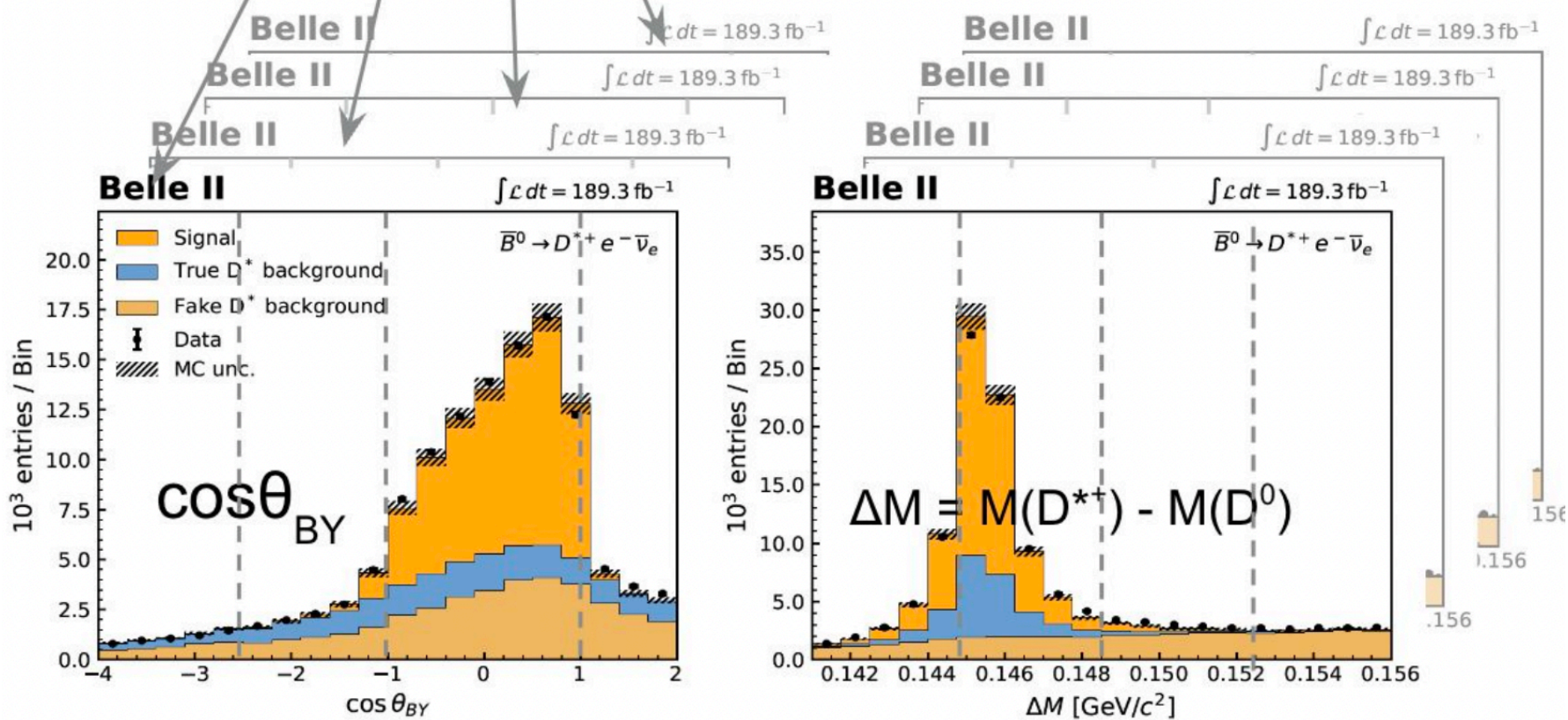
	$\Delta F_L^{D^*}$
$\bar{B}^0 \rightarrow D^{*+} \ell \bar{\nu}_\ell$	$0.032 \pm 0.033 \pm 0.010$
$B^- \rightarrow D^{*0} \ell \bar{\nu}_\ell$	$0.025 \pm 0.035 \pm 0.010$
$B \rightarrow D^* \ell \bar{\nu}_\ell$	$0.034 \pm 0.024 \pm 0.007$

$$R_{e/\mu} = \frac{\mathcal{B}(\bar{B} \rightarrow D^* e \bar{\nu}_e)}{\mathcal{B}(\bar{B} \rightarrow D^* \mu \bar{\nu}_\mu)} = 0.990 \pm 0.021 \pm 0.023$$

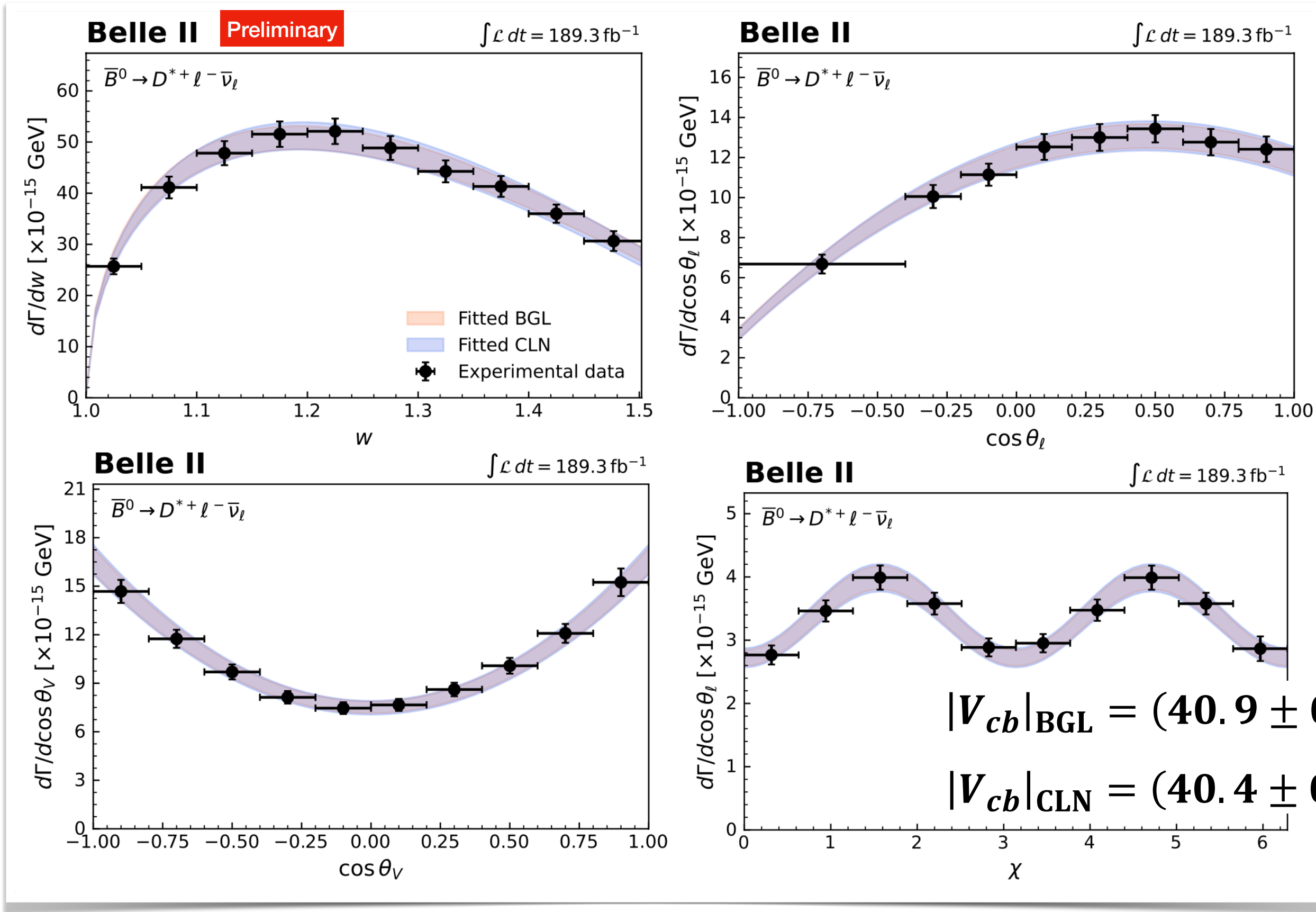
# $B \rightarrow D^* \ell^+ \nu$ shapes & $|V_{cb}|$ from Belle II



- The yield in 10 (8) bin of  $w$  and the three cosine angles is extracted by fitting  $\cos \theta_{BY}$  and  $\Delta M$  for  $D^*$
- Bin-to-bin migration is corrected with SVD unfolding
- main challenges: background modeling, slow-pion tracking, and stat. correlations b/w bins



# $B \rightarrow D^* \ell^+ \nu$ shapes & $|V_{cb}|$ from Belle II



$$|V_{cb}|_{\text{BGL}} = (40.9 \pm 0.3 \pm 1.0 \pm 0.6) \times 10^{-3} \quad (\text{QCD input})$$

$$|V_{cb}|_{\text{CLN}} = (40.4 \pm 0.3 \pm 1.0 \pm 0.6) \times 10^{-3}$$