



CPV at e^+/e^- colliders

FPCP2024, Chulalongkorn University,
Bangkok Thailand
30/05/2024

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for the Belle II collaboration
INFN Padova

CPV in Standard Model: CKM matrix

- CPV: a key for matter-antimatter asymmetry in the universe
 - In SM, only source is complex phase in CKM matrix
 - (and possible similar phase in PMNS matrix)

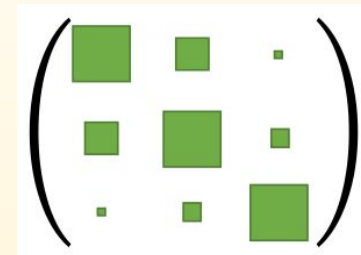


Dirac Medal 2010

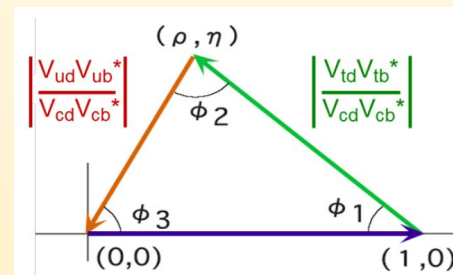


Nobel Prize 2008

$$V = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix}$$

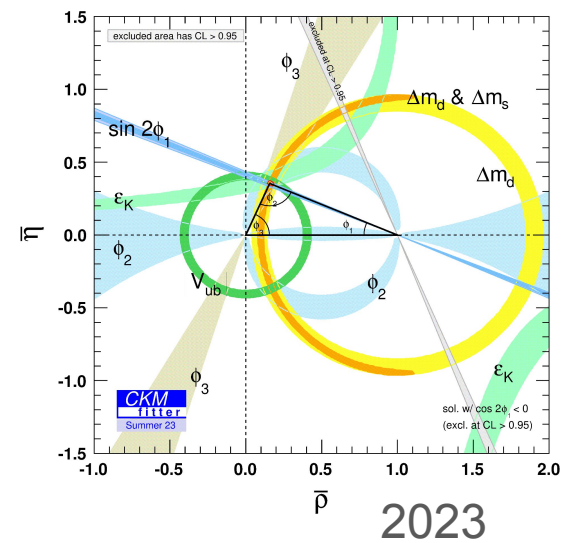
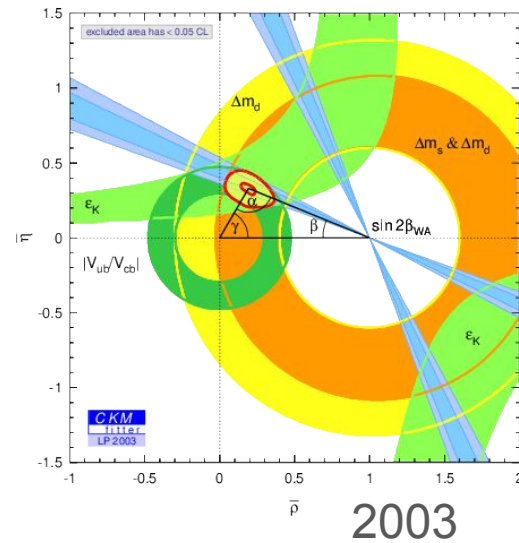
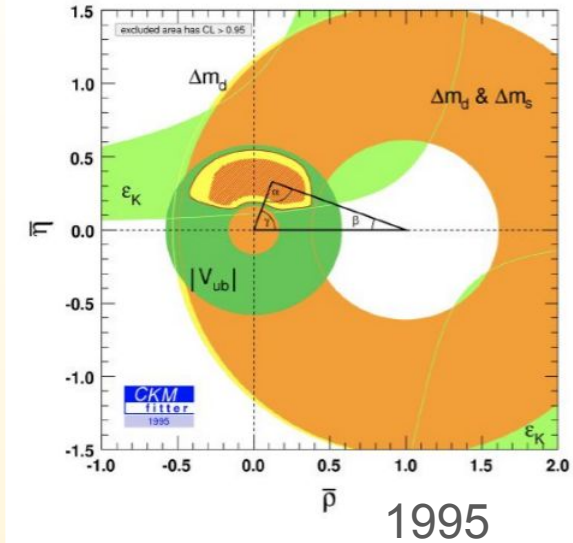


- From CKM unitarity: $V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$
 - Triangle in complex plane
 - Three angles
 - Other triangles exist



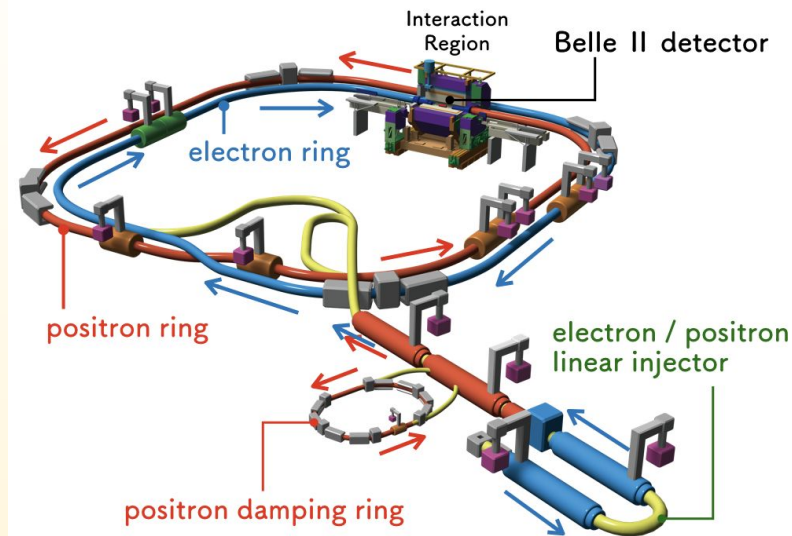
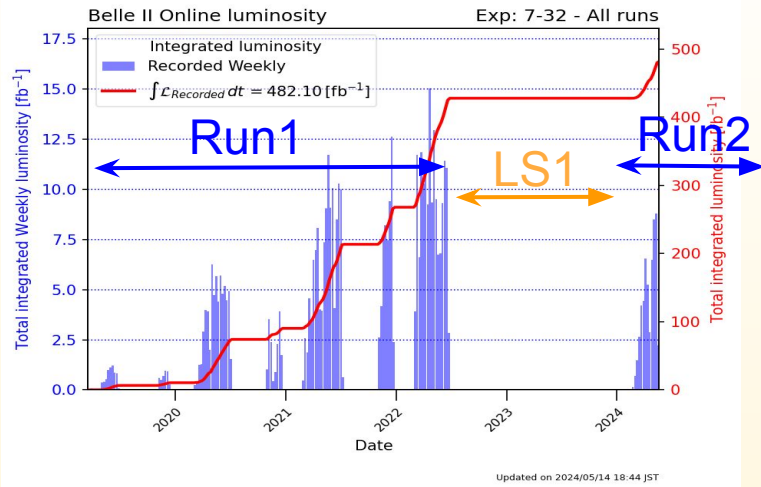
$$\begin{aligned} \phi_1 &= \beta \\ \phi_2 &= \alpha \\ \phi_3 &= \gamma \end{aligned}$$

CPV and Unitarity Triangle



- Precise test of SM by over constraining Unitarity Triangle
- Search for New Physics effects, especially in loop mediated diagrams
- **At e^+/e^- collider:**
 - clean environment, full reconstruction, access to modes with neutrals in the final states

SuperKEKB and Belle II



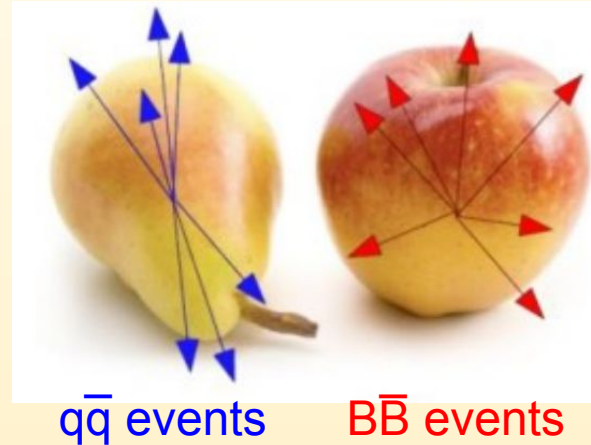
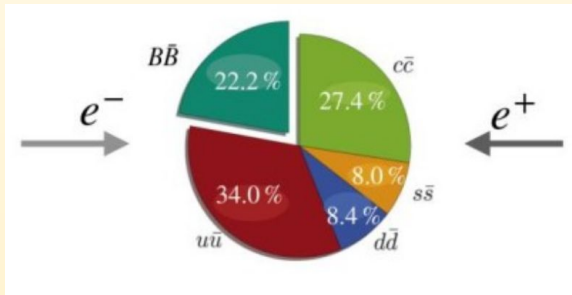
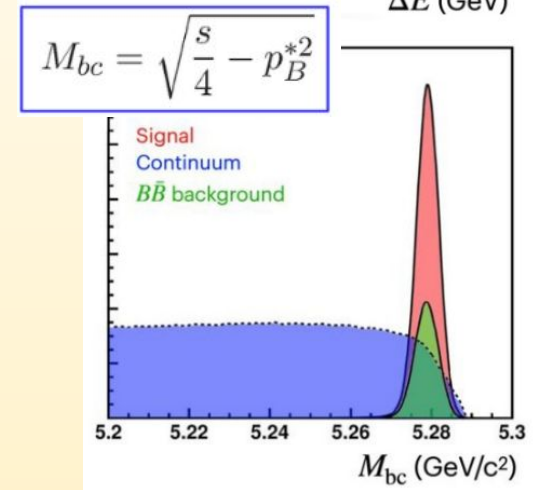
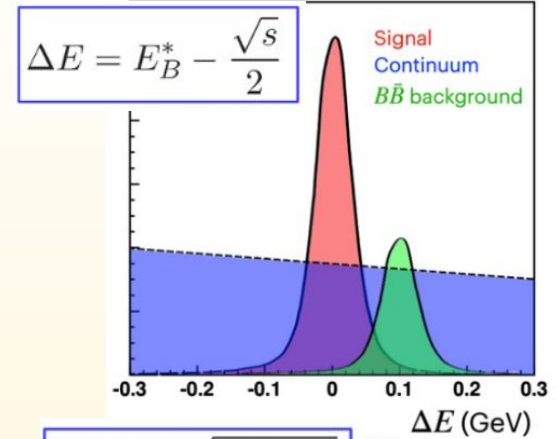
- e^+/e^- (4/7 GeV) at KEK
 - Around $Y(4S)$ resonance
- Run 1 operation 2019-2022
 - 424 fb^{-1} collected - 362 fb^{-1} at $Y(4S)$
- Long Shutdown 1 (LS1) until end of 2023
 - For accelerator and detector upgrades
- Run 2 operation from Jan 2024

Luminosity record $4.7 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$

- 2x KEKB
- Goal to collect multi ab^{-1} of data

B-Factory variables

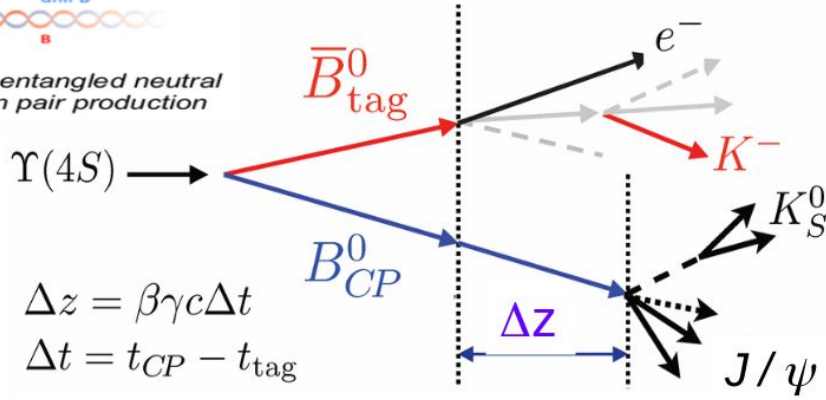
- Two key variables to discriminate fully reconstructed (hadronic) signal from background
 - Background from continuum ($q\bar{q}$) and from $B\bar{B}$
- Discrimination against continuum ($q\bar{q}$) background using event-shape variables via a multivariate classifier



Time-Dependent (TD) CPV analysis



Quantum entangled neutral B meson pair production



$\langle \Delta z \rangle \sim 130 \mu\text{m}$ at Belle II

Flagship measurement at B factories
Still very important at Belle II

$$\mathcal{A}_{CP}(\Delta t) = \frac{\Gamma(B_{tag=B^0}(\Delta t) \rightarrow f_{CP}) - \Gamma(B_{tag=\bar{B}^0}(\Delta t) \rightarrow f_{CP})}{\Gamma(B_{tag=B^0}(\Delta t) \rightarrow f_{CP}) + \Gamma(B_{tag=\bar{B}^0}(\Delta t) \rightarrow f_{CP})} =$$

$$= \mathbf{S} \cdot \sin(\Delta m_d \Delta t) - \mathbf{C} \cdot \cos(\Delta m_d \Delta t)$$

$$\mathcal{S}_{CP} = \sin(2\phi_i^{eff})$$

mixing induced CPV

$$\mathcal{A}_{CP} = -\mathcal{C}_{CP}$$

Direct CPV

- B_{CP} fully reconstructed CP eigenstate
- B_{tag} vertex and flavour information
- Complex analysis, many key elements:
 - high signal efficiency
 - excellent vertex resolution $\sigma_z \sim 26/50 \mu\text{m}$ (signal/tag side)
 - high flavour-tagging efficiency $\epsilon = 37\%$

B flavour tagging: GFlaT

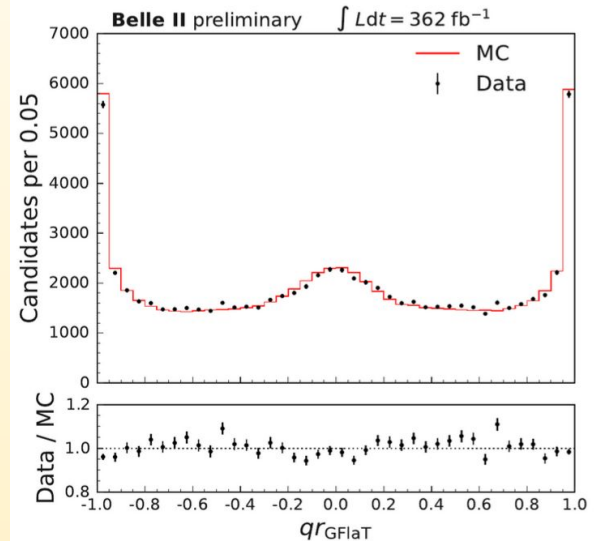
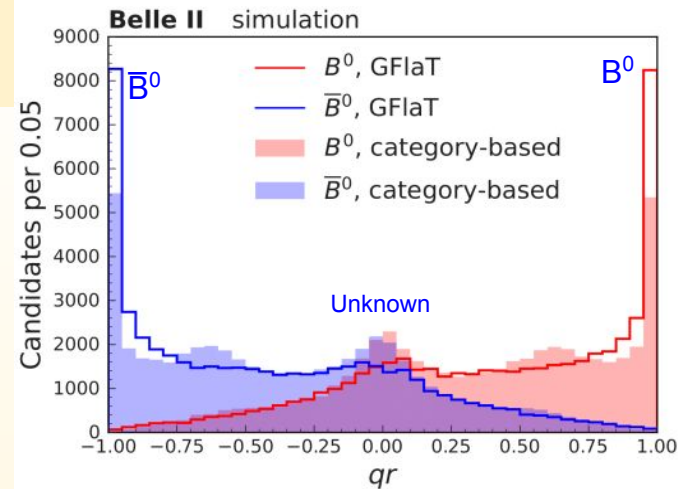
arXiv:2402.17260

Accepted by PRD

- CPV analysis in Belle II used a category-based (CB) algorithm [[Eur. Phys. J 82, 283 \(2022\)](#)]
- A more advanced algorithm GFlaT, based on graph convolutional neural network (GNN), was developed
 - Using 25 variables for each track from the B_{tag} decay
- Performance evaluated on data using self-tagging $B^0 \rightarrow D^{(*)-}\pi^+$ decays
- Significant improvement in performance
 - **+18%** (relative)

$$\varepsilon_{\text{tag}}(\text{CB}) = (31.7 \pm 0.5 \pm 0.4) \%$$

$$\varepsilon_{\text{tag}}(\text{GFlaT}) = (37.4 \pm 0.4 \pm 0.3) \%$$



$\sin(2\phi_1/\beta)$ from $B \rightarrow J/\psi K_S$

- Golden channel, almost background free
- Updated results using improved GFlaT flavour tagger
- Fit ΔE distribution to subtract background
- Fit background-subtracted Δt distribution to extract CPV parameters

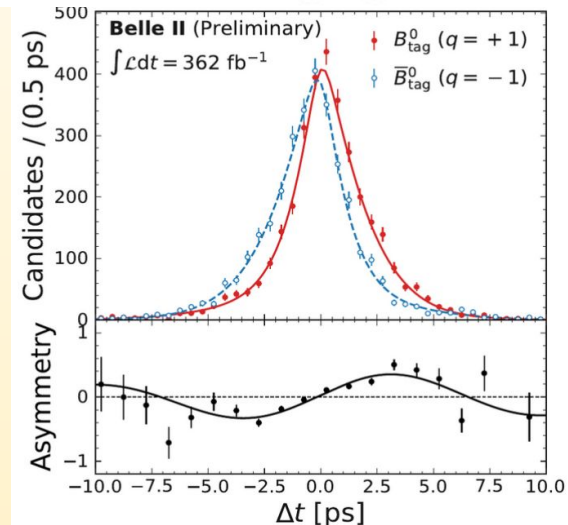
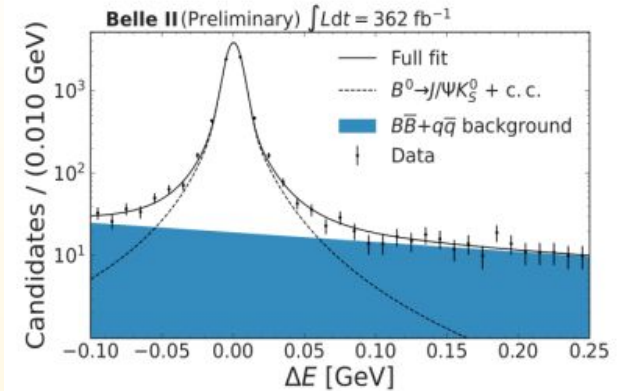
$$S = 0.724 \pm 0.035 \pm 0.014$$
$$C = -0.035 \pm 0.026 \pm 0.013$$

World average (K_S mode only):

$$S_{CP} = 0.695 \pm 0.019$$

$$A_{CP} = 0.000 \pm 0.020$$

- Statistical uncertainties **8%** smaller than with category-based Flavour Tagger



TDCPV in Charmless B decay

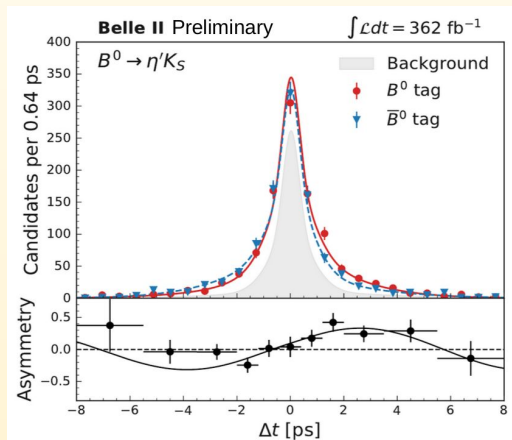
See also S.Raiz [talk](#) on Tue



- $B \rightarrow \eta' K_S$ [arXiv:2402.03713](#)
 - $\eta' \rightarrow \eta (\rightarrow \gamma\gamma) \pi^+ \pi^-$
 - $\eta' \rightarrow \rho\gamma$
- High \mathcal{B} , theoretically clean
 - ~ 800 signal events

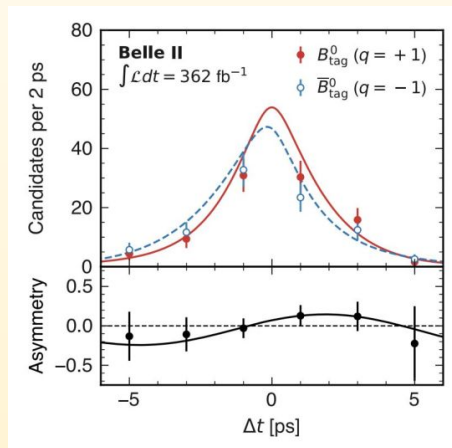
- $B \rightarrow \phi K_S$ [PRD 108, 072012 \(2023\)](#)
- Challenge: non resonant background with opposite-CP
 - ~ 160 signal events

- $B \rightarrow K_S K_S K_S$ [arXiv:2403.02590](#) Accepted by PRD
- Challenge: no prompt tracks from B vertex
 - Use $K_S \rightarrow \pi^+ \pi^-$ extrapolated to IP
 - ~ 160 signal events



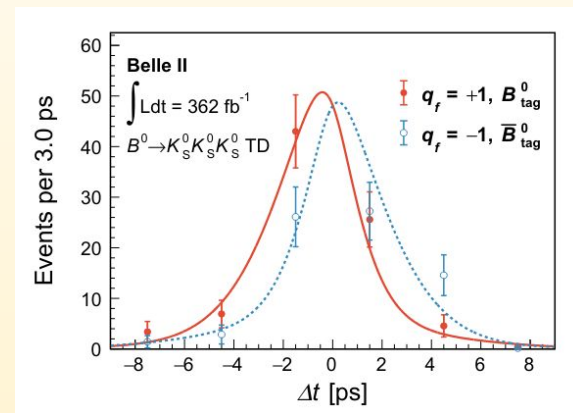
$$S = 0.67 \pm 0.10 \pm 0.04$$

$$C = -0.19 \pm 0.08 \pm 0.03$$



$$S = 0.54 \pm 0.26^{+0.06}_{-0.08}$$

$$C = -0.31 \pm 0.20 \pm 0.05$$



$$S = -1.37^{+0.35}_{-0.45} \pm 0.03$$

$$C = -0.07 \pm 0.20 \pm 0.05$$



- $B^0 \rightarrow K_S \pi^0 \gamma$ is expected to have small/none mixing induced CPV in SM
 - $b \rightarrow s \gamma_R$ is helicity suppressed (m_s/m_b) wrt $b \rightarrow s \gamma_L$
 - $B^0 \rightarrow s \gamma_L$ vs $B^0 \rightarrow \bar{B}^0 \rightarrow s \gamma_R$
- Vertex from $K_S \rightarrow \pi^+ \pi^-$ and IP constraint
- Measured separately for **resonant** $K^{*0} (\rightarrow K_S \pi^0) \gamma$

See also S.Raiz [talk](#) on Tue

$$S = 0.00^{+0.27}_{-0.26} \pm 0.03$$

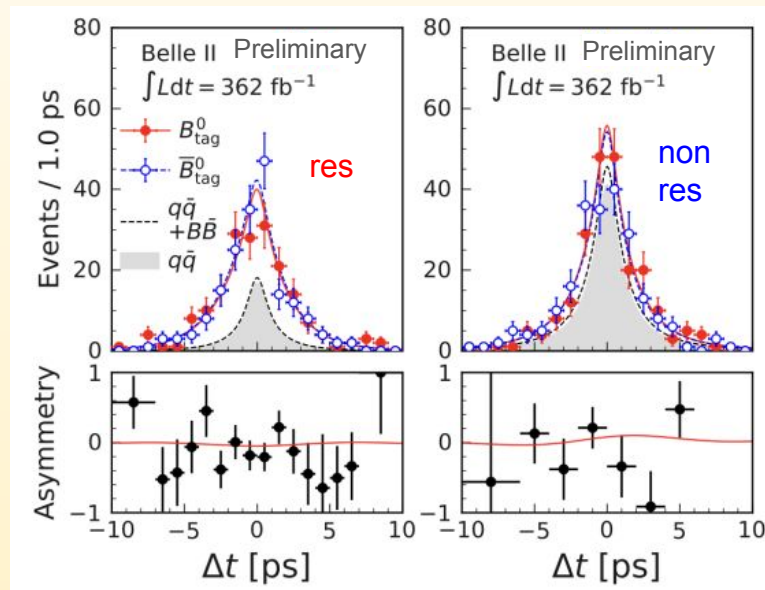
$$C = 0.10 \pm 0.13 \pm 0.03$$

- and inclusive (**non resonant**) decay $K_S \pi^0 \gamma$

$$S = 0.04^{+0.45}_{-0.44} \pm 0.10$$

$$C = -0.06 \pm 0.25 \pm 0.07$$

Most precise result so far



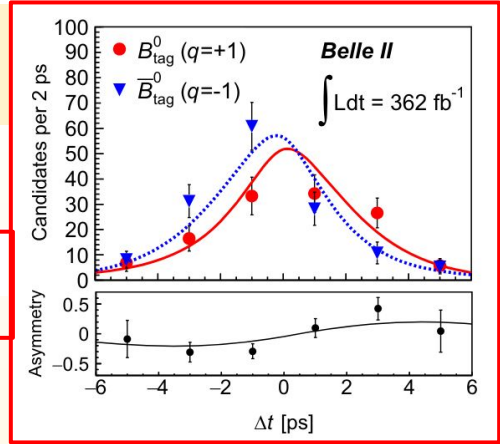
CPV in $B^0 \rightarrow K_S^0 \pi^0$

[PRL 131, 111803 \(2023\)](#)
[PRD 109, 012001 \(2024\)](#)

- First Belle II measurement of TDCPV in $B^0 \rightarrow K_S \pi^0$
 - Signal yield: 415^{+26}_{-25} events
- Key ingredient in Isospin Sum Rule

$$S = 0.75^{+0.20}_{-0.23} \pm 0.04,$$

$$C = -0.04^{+0.14}_{-0.15} \pm 0.05$$



$$I_{K\pi} = \mathcal{A}_{CP}^{K^+\pi^-} + \mathcal{A}_{CP}^{K^0\pi^+} \frac{\mathcal{B}(K^0\pi^+)}{\mathcal{B}(K^+\pi^-)} \frac{\tau_{B^0}}{\tau_{B^+}} - 2\mathcal{A}_{CP}^{K^+\pi^0} \frac{\mathcal{B}(K^+\pi^0)}{\mathcal{B}(K^+\pi^-)} \frac{\tau_{B^0}}{\tau_{B^+}} - 2\mathcal{A}_{CP}^{K^0\pi^0} \frac{\mathcal{B}(K^0\pi^0)}{\mathcal{B}(K^+\pi^-)} \approx 0 \quad (\text{within } \sim 1\%)$$

Gronau (Phys. Lett. B 627 (2005) no.1, 82-88)

$B^0 \rightarrow K^+\pi^-$

$\mathcal{B}(K^+\pi^-) = (20.67 \pm 0.37 \pm 0.62) \times 10^{-6}$
 $\mathcal{A}_{CP}(K^+\pi^-) = -0.072 \pm 0.019 \pm 0.007$

$B^+ \rightarrow K^+\pi^0$

$\mathcal{B}(K^+\pi^0) = (13.93 \pm 0.38 \pm 0.84) \times 10^{-6}$
 $\mathcal{A}_{CP}(K^+\pi^0) = +0.013 \pm 0.027 \pm 0.005$

$B^+ \rightarrow K_S^0\pi^+$

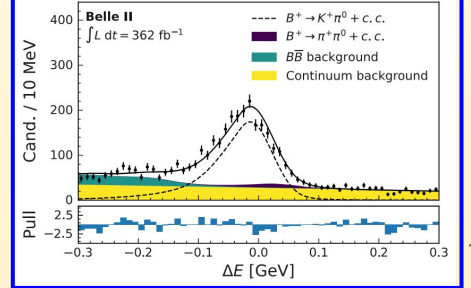
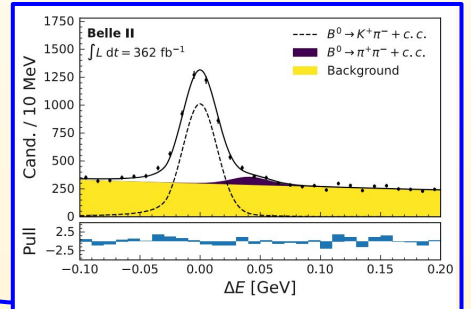
$\mathcal{B}(K_S^0\pi^+) = (24.40 \pm 0.71 \pm 0.86) \times 10^{-6}$
 $\mathcal{A}_{CP}(K_S^0\pi^+) = +0.046 \pm 0.029 \pm 0.007$

$B^0 \rightarrow K_S^0\pi^0$

$\mathcal{B} = (10.50 \pm 0.62 \pm 0.67) \times 10^{-6}$
 $\mathcal{A}_{CP} = -0.01 \pm 0.12 \pm 0.05$

→ $I_{K\pi} = -0.03 \pm 0.13 \pm 0.05$
 (world average 0.13 ± 0.11)

world's best
 precision on par with W/A!
 → 5% uncertainty achievable @ 10 ab⁻¹



Toward ϕ_2/α : $B^0 \rightarrow \pi^0 \pi^0$

New for FPCP 2024



See also S.Raiz [talk](#) on Tue

Previous results
[\[PRD107 \(2023\) 112009\]](#)

- Update on \mathcal{B} and A_{CP} using full Run1 statistics:
- Improved selections, new flavour tagger (GFlaT), reduction of systematics
 - Background dominated by continuum, then $B\bar{B}$ ($B^+ \rightarrow \rho^+ (\rightarrow \pi^+ \pi^0) \pi^0$, $B^0 \rightarrow K^0_S (\rightarrow \pi^0 \pi^0) \pi^0$)
 - Photons selected with BDT, continuum suppression trained on off-resonance data
 - 4D fit including M_{BC} , ΔE , cont.suppression, w (wrong tag probability - unbinned)
 - Validated on $B^+ \rightarrow K^+ \pi^0$ / $B^0 \rightarrow \bar{D}^0 (K^+ \pi^- \pi^0) \pi^0$

$$\mathcal{B} = (1.26 \pm 0.20 \pm 0.11) \times 10^{-6}$$

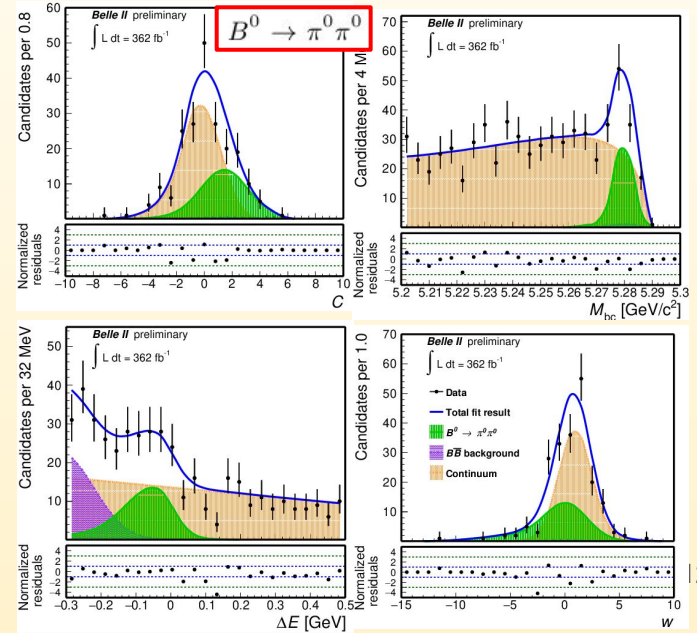
$$A_{CP} = 0.06 \pm 0.30 \pm 0.06$$

- Compatible with known values
- World-best B determination.
- A_{CP} on par with world best

$$\mathcal{B} = (1.59 \pm 0.26) \times 10^{-6}$$

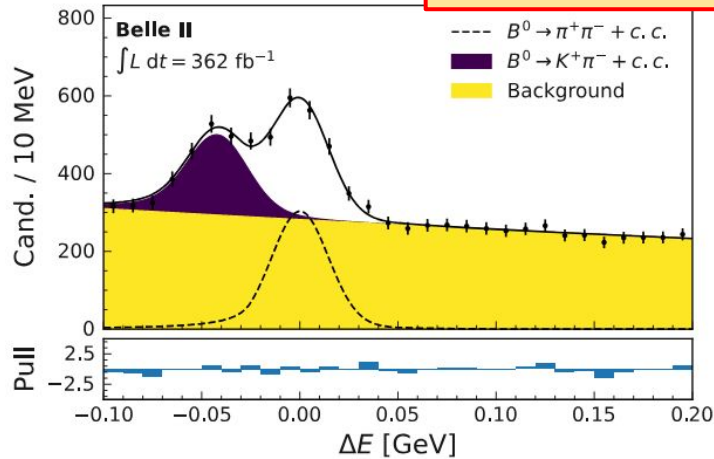
$$A_{CP} = 0.30 \pm 0.20 \quad \text{WA}$$

Signal enhanced region

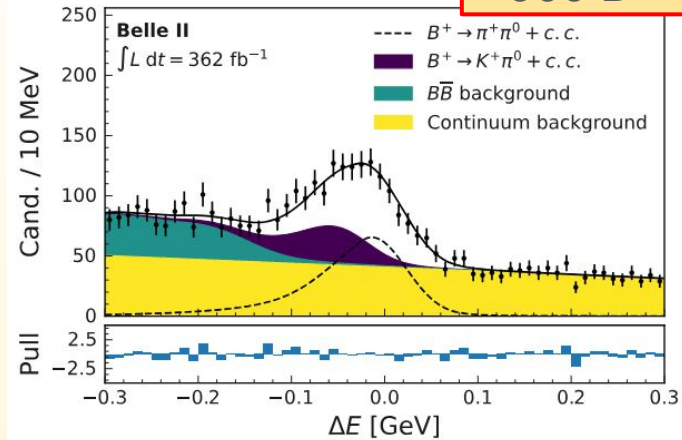


Toward ϕ_2/α : $B \rightarrow \pi\pi$

$\sim 1500 B^0 \rightarrow \pi^+\pi^-$



$\sim 900 B^+ \rightarrow \pi^+\pi^0$



$$\mathcal{B}(B^0 \rightarrow \pi^+\pi^-) = (5.83 \pm 0.22 \pm 0.17) \times 10^{-6}$$

world's best

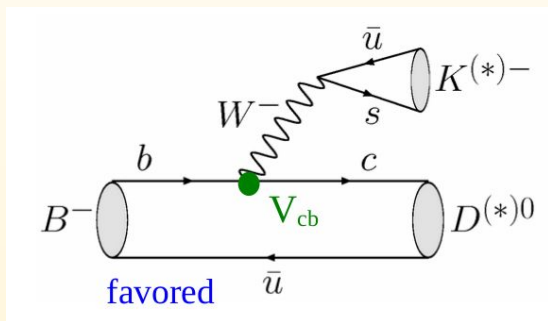
$$\mathcal{B}(\pi^+\pi^0) = (5.10 \pm 0.29 \pm 0.32) \times 10^{-6}$$

$$A_{CP}(\pi^+\pi^0) = -0.081 \pm 0.054 \pm 0.008$$

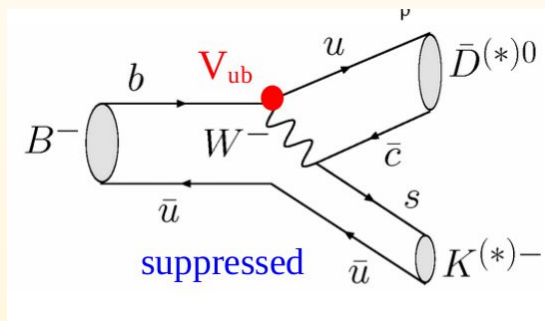
- Compatible and competitive with WA
- Modes with π^0 limited by π^0 systematics: will be reduced with more data

Results on γ/ϕ_3

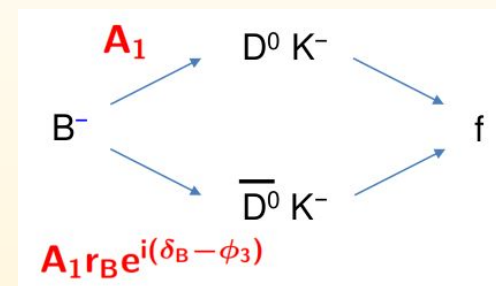
- γ/ϕ_3 from interference of tree level amplitudes:
 - Fundamental input of CKM UT fit
- ϕ_3 can be measured using interference $B \rightarrow DK$ and $B \rightarrow \bar{D}K$ (or D^*K^* , $D\pi$)



$$B^- \rightarrow D^0 K^- \approx V_{cb} V_{us}^* A_1$$



$$B^- \rightarrow \bar{D}^0 K^- \approx V_{ub} V_{cs}^* A_1 r_B e^{i(\delta_B - \phi_3)}$$



- Amplitude ratio r_B and strong phase δ_B are mode-dependent

- Several methods used

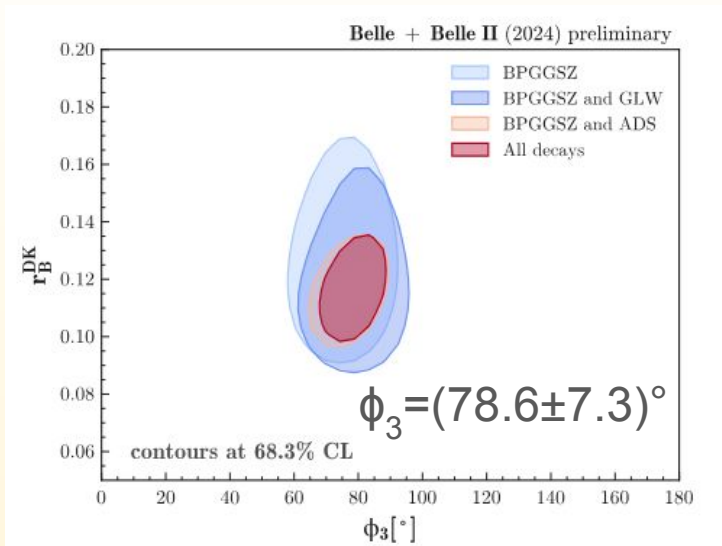
- GLW $B^\pm \rightarrow D^0_{CP} K^\pm$ [arXiv:2308.05048 \[hep-ex\]](https://arxiv.org/abs/2308.05048)
 - Use CP eigenstate of D meson
- ADS [PRL 78 \(1997\) 3257](https://doi.org/10.1103/PhysRevLett.78.3257)
 - Enhancement of CP violation by using doubly Cabibbo suppressed decays.
- BPGGSZ $D^0 \rightarrow K_S h^+ h^-$ [JHEP 2022\(2022\), 63](https://arxiv.org/abs/2202.063)
 - Different amplitude and strong phase in different region of Dalitz plot.
- GLS $D^0 \rightarrow K_S K\pi$ [JHEP 09\(2023\)146](https://arxiv.org/abs/2309.146)

- D-decay strong phase from CLEO-c & BESIII

- Need improvement by BESIII

LHCb: $\phi_3 = (63.8 \pm 3.6)^\circ$ [LHCb-CONF-2022-003](https://arxiv.org/abs/2203.003)

Few ab^{-1} needed for a meaningful comparison



- Likelihood with 60 input observables
 - including 15 auxiliary inputs (D-decay)
 - 16 free parameters
- $r_B(\delta_B)$ with little high-fluctuation
 - Worse precision with WA values

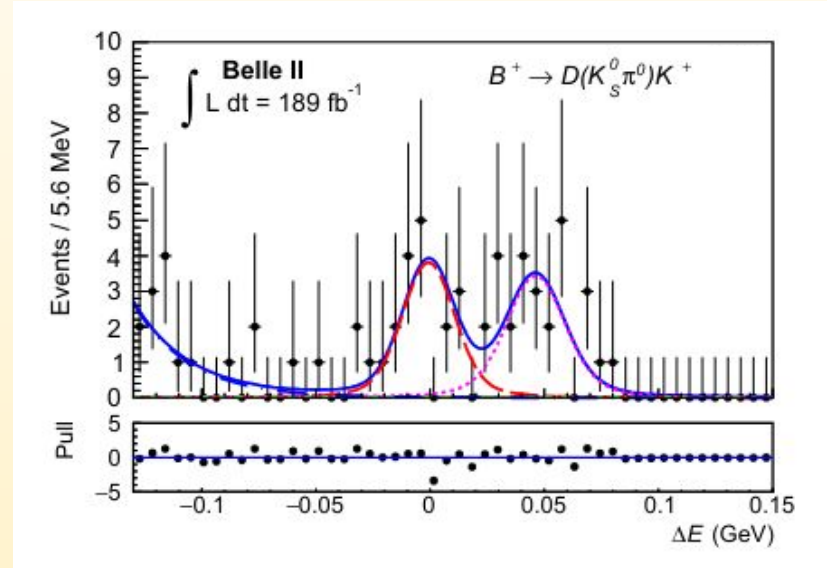
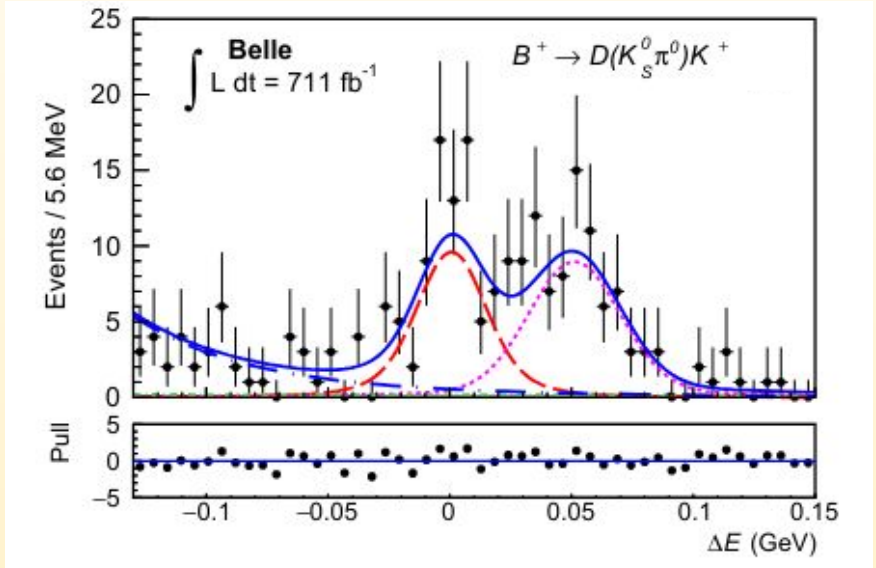
Belle + Belle II Combined γ/ϕ_3

arXiv:2308.05048



- Example:
 - $B^\pm \rightarrow D_{CP} K^\pm$ (GLW)
 - CP-odd $D_{CP} \rightarrow K_S \pi^0$: only in Belle(II)
 - Combined Belle and BelleII analysis

B decay	D decay	Method	Data set (Belle + Belle II) [fb^{-1}]
$B^+ \rightarrow Dh^+$	$D \rightarrow K_S^0 \pi^0, K^- K^+$	GLW	711 + 189
$B^+ \rightarrow Dh^+$	$D \rightarrow K^+ \pi^-, K^+ \pi^- \pi^0$	ADS	711 + 0
$B^+ \rightarrow Dh^+$	$D \rightarrow K_S^0 K^- \pi^+$	GLS	711 + 362
$B^+ \rightarrow Dh^+$	$D \rightarrow K_S^0 h^- h^+$	BPGGSZ (m.i.)	711 + 128
$B^+ \rightarrow Dh^+$	$D \rightarrow K_S^0 \pi^- \pi^+ \pi^0$	BPGGSZ (m.i.)	711 + 0
$B^+ \rightarrow D^* K^+$	$D^* \rightarrow D\pi^0, D \rightarrow K_S^0 \pi^0, K_S^0 \phi, K_S^0 \omega,$ $K^- K^+, \pi^- \pi^+$	GLW	210+0
$B^+ \rightarrow D^* K^+$	$D^* \rightarrow D\pi^0, D\gamma, D \rightarrow K_S^0 \pi^- \pi^+$	BPGGSZ (m.d.)	605 + 0

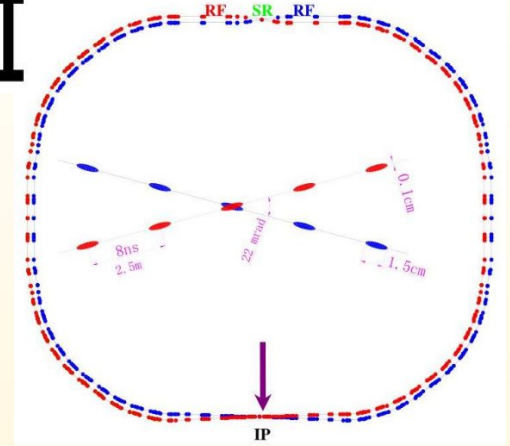


BESIII @ Beijing Electron-Positron Collider (BEPC-II)



- CM Energies: [2-4.95] GeV: τ -charm region
 - Luminosity: $\sim 10^{33} \text{ cm}^{-2}\text{s}^{-1}$
- Collected 10 billion J/ψ and 3 billion $\psi(2S)$
 - Possible to study CPV on **hyperons**
 - $\sim 10^7$ entangled hyperon pairs

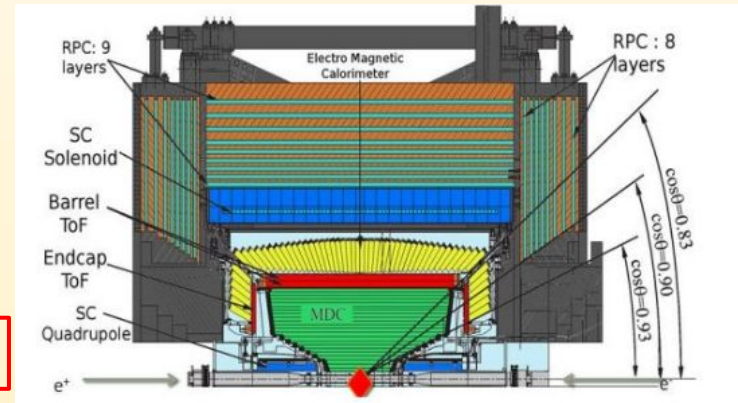
BESIII



Decay	\mathcal{B} (10^{-5})	Events at BESIII
$J/\psi \rightarrow \Lambda \bar{\Lambda}$	189 ± 9	18.9×10^6
$J/\psi \rightarrow \Sigma^+ \bar{\Sigma}^-$	150 ± 24	15.0×10^6
$J/\psi \rightarrow \Xi \bar{\Xi}$	97 ± 8	9.7×10^6
$\psi(2S) \rightarrow \Sigma \bar{\Sigma}$	23.2 ± 1.2	116×10^3
$\psi(2S) \rightarrow \Omega \bar{\Omega}$	5.66 ± 0.30	28×10^3

[Front. Phys. 12\(5\), 121301 \(2017\)](#)

More on BESIII and BEPC-II
on Luyan Tao [talk](#) on Monday

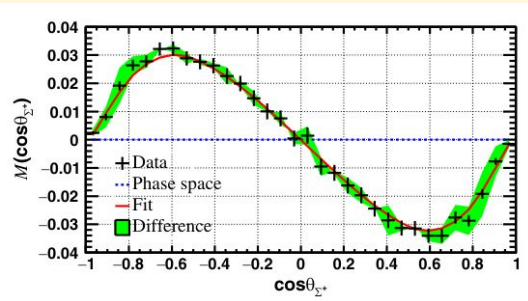


- Polarized and entangled pair of hyperons from J/ψ decays
- Decay asymmetry parameters α from S-wave (parity conserving) and P-wave (parity violating) amplitudes. $\bar{\alpha}$ for anti-hyperons

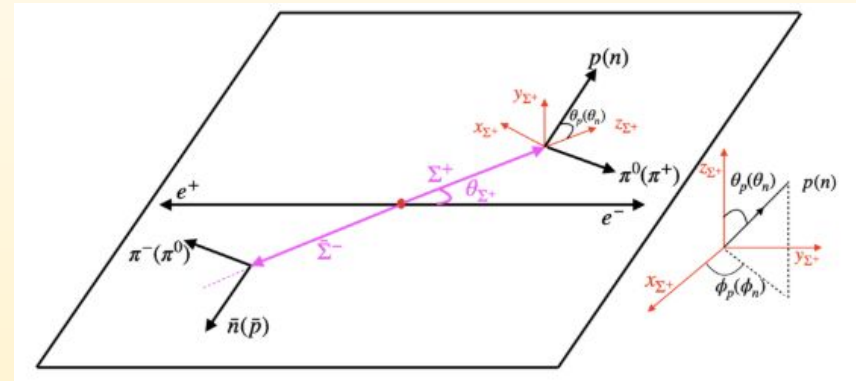
$$\frac{dN}{d\Omega} = \frac{1}{4\pi} (1 + \alpha \mathbf{P}_{\Sigma^+} \cdot \hat{\mathbf{n}})$$

- α is CP-odd
- **Non zero** $A_{CP} = \frac{\alpha_+ + \bar{\alpha}_-}{\alpha_+ - \bar{\alpha}_-} \Rightarrow$ **CP violation**
- Events: $J/\psi \rightarrow \Sigma^+ \text{ anti-}\Sigma^-, \Sigma^+ \rightarrow n\pi^+, \text{ anti-}\Sigma^- \rightarrow \bar{p}\pi^0$ or c.c.
 - 10 billion $J/\psi \rightarrow \Sigma^+ \text{ anti-}\Sigma^-$
 - Complex angular analysis: 5 observables
 - **First CPV result with neutron in the final state**

Moment of polarization



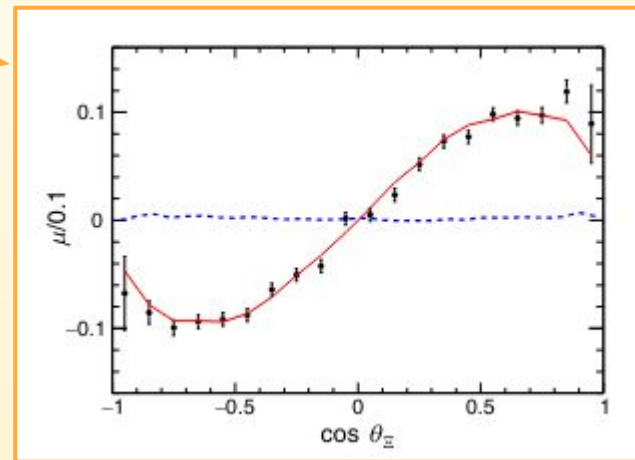
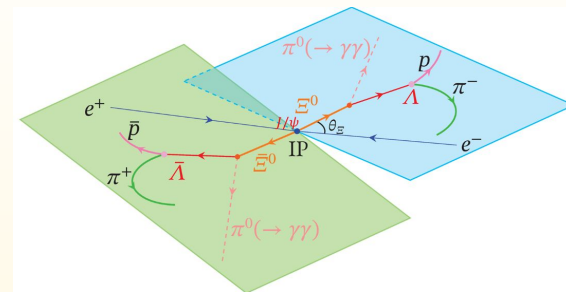
Non flat \Rightarrow polarization observed



$$A_{CP} = 0.080 \pm 0.052 \pm 0.028$$

$$e^+e^- \rightarrow J/\psi \rightarrow \Xi^0 \text{anti-}\Xi^0, \Xi^0 \rightarrow \Lambda (\rightarrow p\pi^-) \pi^0 + \text{cc}$$

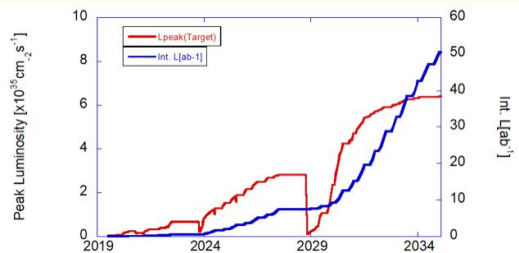
- Even more complex angular analysis (9 helicity angles)
- 8 free parameters (plus other in daughter's decay)
 - 10 billion J/ψ events: [PhysRevD.108.L031106 \(2023\)](#)
 - 320k signal events with little background
- Results:
 - Ξ^- polarization observed (first time)
 - Independent measurement of Λ decay parameters
 - First measurement of weak phase difference in Ξ decay
 - **Three independent CP test**



Parameter	This work	Previous result
A_{CP}^{Ξ}	$(-5.4 \pm 6.5 \pm 3.1) \times 10^{-3}$	$(-0.7 \pm 8.5) \times 10^{-2}$ [49]
$\Delta\phi_{CP}^{\Xi}(\text{rad})$	$(-0.1 \pm 6.9 \pm 0.9) \times 10^{-3}$	$(-7.9 \pm 8.3) \times 10^{-2}$ [49]
A_{CP}^{Λ}	$(6.9 \pm 5.8 \pm 1.8) \times 10^{-3}$	$(-2.5 \pm 4.8) \times 10^{-3}$ [20]

Similar results for $e^+e^- \rightarrow J/\psi \rightarrow \Xi^+\Xi^- \rightarrow \Lambda(\rightarrow p\pi^-)\pi^- \bar{\Lambda}(\rightarrow \bar{n}\pi^0)\pi^+$
[PhysRevLett.132.101801](#)

- Belle II goal: $L=6 \times 10^{35} \text{ cm}^{-2} \text{ s}^{-1}$; $L_{\text{int}} \sim 50 \text{ ab}^{-1}$



[PTEP (2019) 123C01]

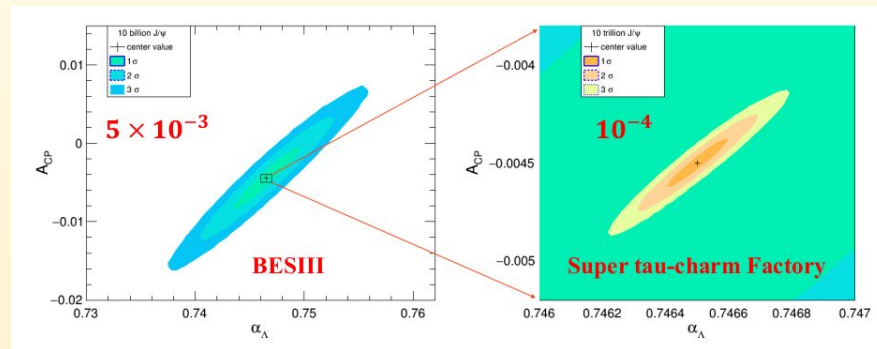
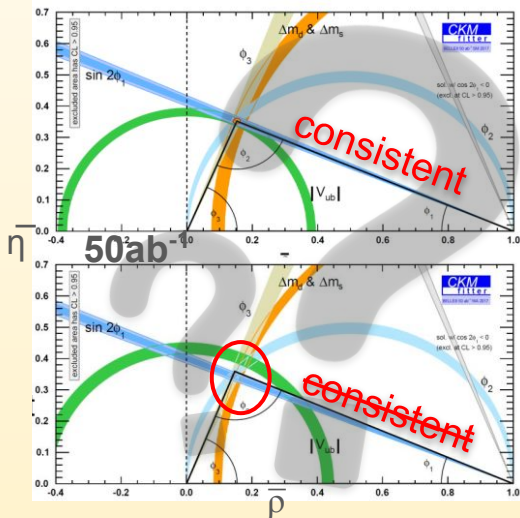
- BESIII and Super Tau-Charm Facility

- today $10^{10} J/\psi$
- At super J/ψ factory $10^{12} J/\psi$ per year
 - $L \sim 10^{35} \text{ cm}^{-2} \text{ s}^{-1}$
 - polarized beam (phase II)

- CPV sensitivity in hyperon's decay

- $10^{-4} - 10^{-5}$
- challenging SM predictions

- Together with LHCb will further constrain UT
- Unique measurements in many modes
- UT consistent with SM or not?



More on STCF on Qipeng Hu
[talk](#) later today

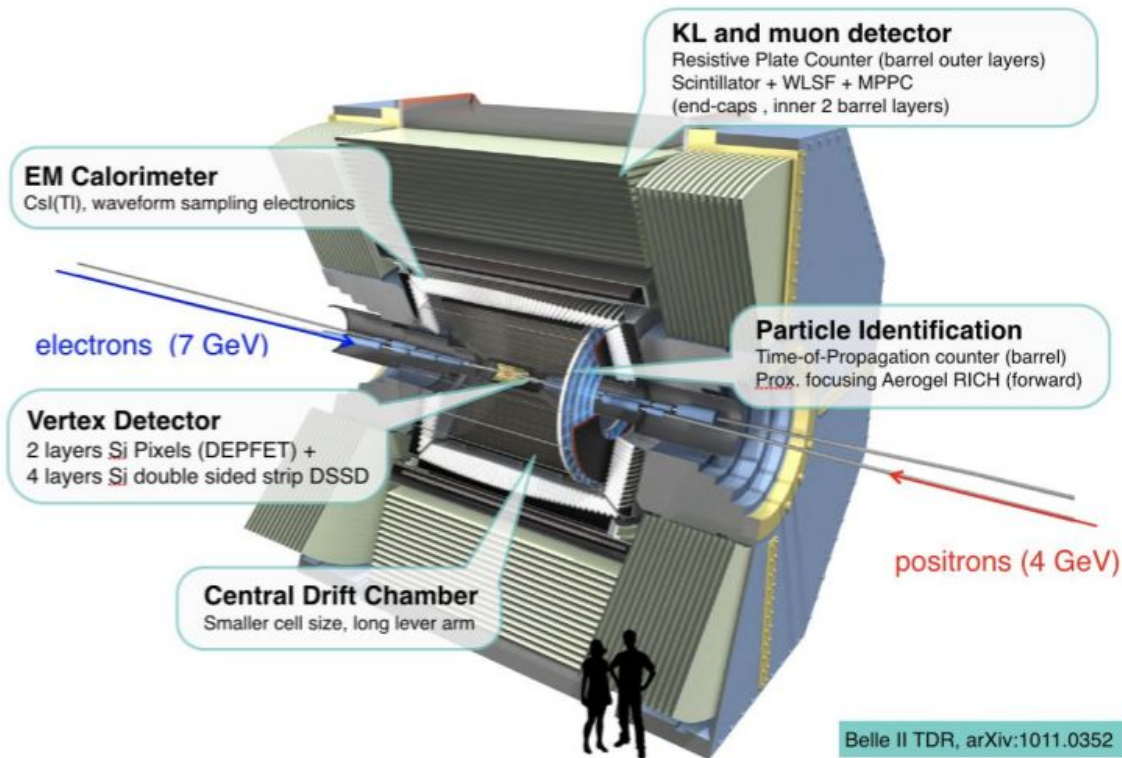
- CPV studies are a key ingredient of e^+/e^- colliders
- Large CPV program in B physics at Belle II
 - Precise measurement of Unitary Triangles
 - Search for new physics
 - Results on Run1 show significantly better performance compared to Belle
- Hyperon polarization in J/ψ , $\psi(2S)$ decays at BESIII
 - new way to study CPV

Backup



Luminosity Frontier experiment

- Asymmetric e^+e^- colliders- B factories, also charm and τ factories
- Belle Belle II: e^+ (3.5 GeV) e^- (8 GeV) e^+ (4 GeV) e^- (7 GeV)
- Improved vertex resolution allows lower boost
- 424 fb^{-1} (362 fb^{-1} at $Y(4S)$) collected at Belle II so far; Goal: 50 ab^{-1}



Belle II TDR, arXiv:1011.0352

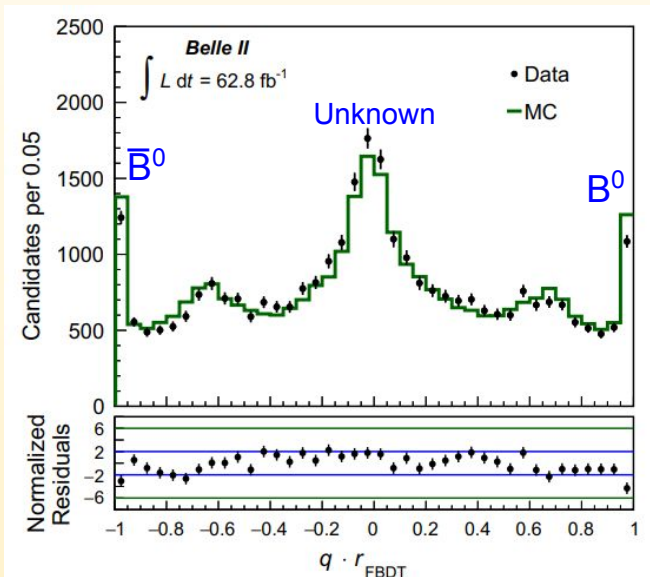
$\sin(2\phi_1/\beta)$ future

- Expected to be dominated by systematics with 50/ab
- Mostly from alignment of vertex detector and tag-side interference
- Penguin pollution will need to be constrained from $B \rightarrow J/\psi\pi^0$

Belle II Physics Book

	No improvement	Vertex improvement	Leptonic categories
<i>$S_{c\bar{c}s}$</i> (50 ab ⁻¹) <i>time dependent CP parameter</i>			
stat.	0.0027	0.0027	0.0048
syst. reducible	0.0026	0.0026	0.0026
syst. irreducible	0.0070	0.0036	0.0035
<i>$A_{c\bar{c}s}$</i> (50 ab ⁻¹) <i>direct CP asymmetry</i>			
stat.	0.0019	0.0019	0.0033
syst. reducible	0.0014	0.0014	0.0014
syst. irreducible	0.0106	0.0087	0.0035

- Used to determine the quark-flavour of B_{tag}
- Many different final states considered, combined with two layers of MVA discriminators.
 - Developed also a **Deep Neural Network** with similar performance



Categories	Targets
Electron	e^-
Intermediate Electron	e^+
Muon	μ^-
Intermediate Muon	μ^+
KinLepton	e^-
Intermediate KinLepton	ℓ^+
Kaon	K^-
KaonPion	K^-, π^+
SlowPion	π^+
FastHadron	π^-, K^-
MaximumP	ℓ^-, π^-
FSC	ℓ^-, π^+
Lambda	Λ
Total= 13	

Performance measured on data using $B^0 \rightarrow D^{(*)} h^+$ decays

- Effective efficiency:

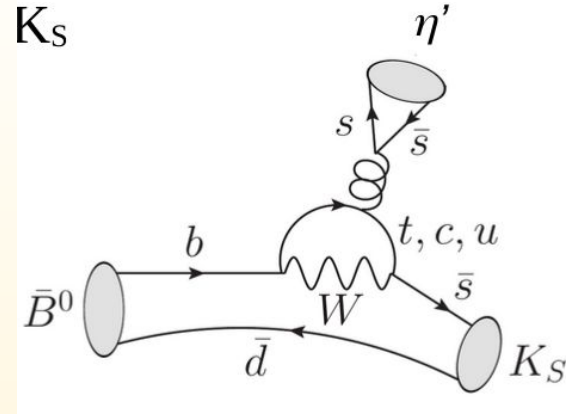
$$\begin{aligned} \epsilon_{eff} &= \sum_i \epsilon_i (1 - 2w_i)^2 \\ &= (30.0 \pm 1.2 \pm 0.4)\% \end{aligned}$$

Time dependent $B \rightarrow \eta' K_S$

arXiv:2402.03713

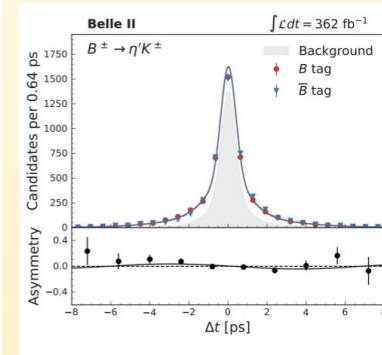
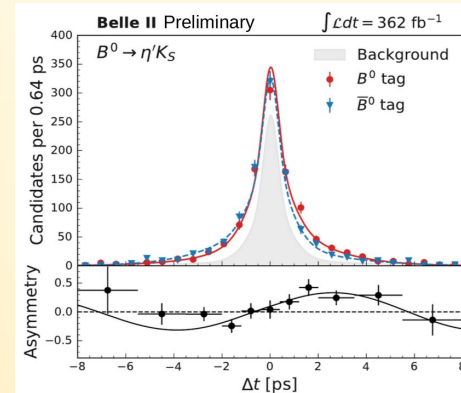


- Mediated by loop diagram, CPV expected to be the same as in $B^0 \rightarrow J/\psi K_S$ (tree)
- Deviation would be indication of new physics in the loop
- Reconstruct in 2 sub-channels:
 - $\eta' \rightarrow \eta(\rightarrow \gamma\gamma)\pi^+\pi^-$, $\eta' \rightarrow \rho\gamma$ (and $\eta' \rightarrow \eta(\rightarrow \pi^+\pi^-\pi^0)\pi^+\pi^-$)
- Found ~ 800 signal in total, performed time dependent fit in ΔE , M_{BC} , ContSupp and ΔT variables



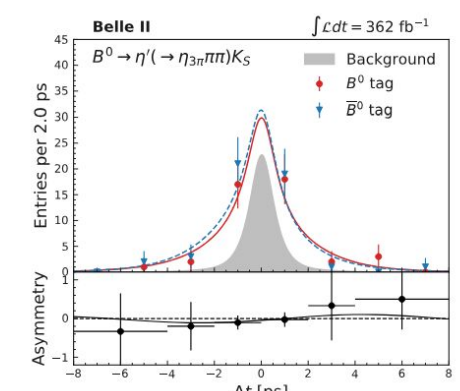
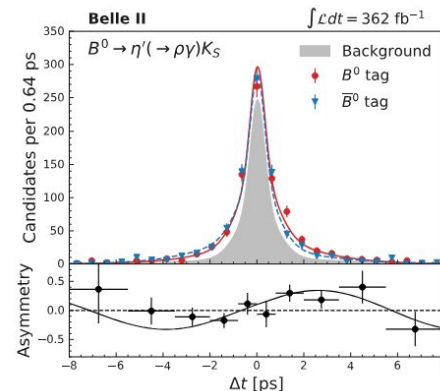
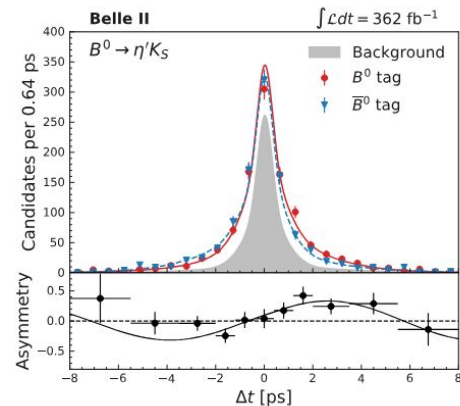
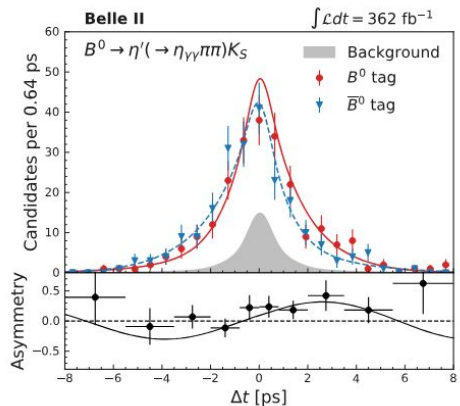
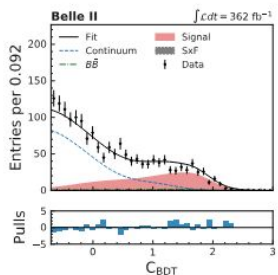
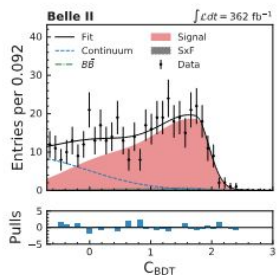
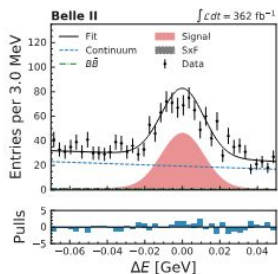
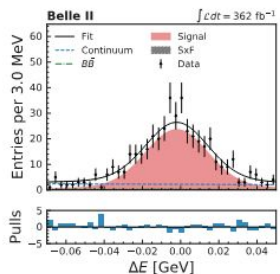
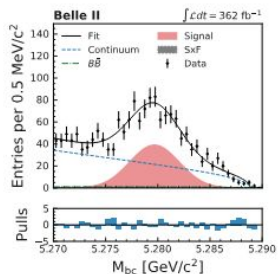
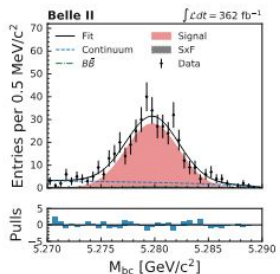
Channel	Signal yield	$C_{\eta'K_S^0}$	$S_{\eta'K_S^0}$
$\eta' \rightarrow \eta_{\gamma\gamma}\pi^+\pi^-$	358 ± 20	-0.10 ± 0.13	0.69 ± 0.14
$\eta' \rightarrow \rho\gamma$	471 ± 29	-0.24 ± 0.10	0.65 ± 0.13
$\eta' \rightarrow \eta_{3\pi}\pi^+\pi^-$	55 ± 8	0.11 ± 0.32	0.25 ± 0.50
Sim. fit	829 ± 35	-0.19 ± 0.08	0.67 ± 0.10

- In agreement with WA and $B^0 \rightarrow J/\psi K_S$ result



Time dependent $B \rightarrow \eta' K_S$

arXiv:2402.03713



Time dependent $B \rightarrow \varphi' K_S$

arXiv:2307.02802

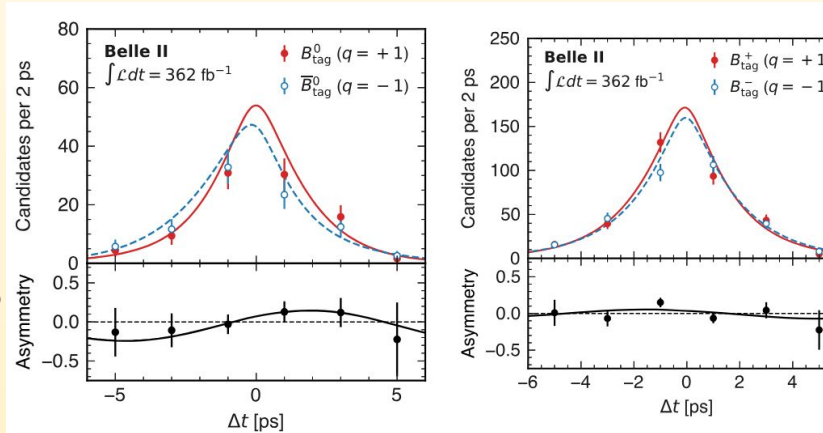
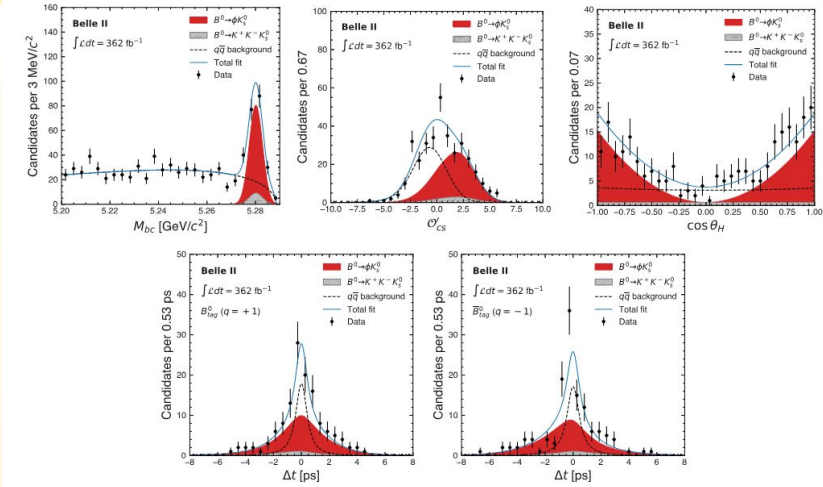


- Two tracks from φ , clean signature
- Major challenge : non resonant background with opposite-CP
- Helicity for longitudinal polarization
- Found ~ 160 signal in total, performed time dependent fit in ΔE , M_{BC} , ContSupp and ΔT variables

$$S = 0.54 \pm 0.26 \begin{matrix} +0.06 \\ -0.08 \end{matrix}$$

$$C = -0.31 \pm 0.20 \pm 0.05$$

- Results competitive with best measurements
 - HFLAV $C_{CP} = 0.01 \pm 0.14$, $S_{CP} = 0.74 \begin{matrix} +0.11 \\ -0.13 \end{matrix}$

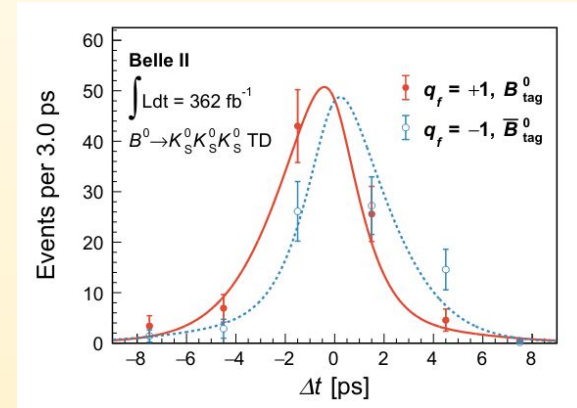
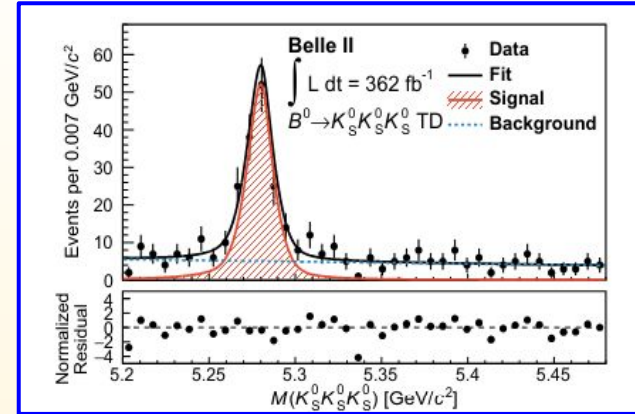


Time dependent $B \rightarrow K_S K_S K_S$

- $b \rightarrow s$ decay mediated by penguin loop, potentially sensitive to new physics
 - Very reliable theoretically
- B vertex challenging: no *prompt* tracks from B, but only reconstructed $K_S \rightarrow \pi^+ \pi^-$ extrapolated back;
 - For TD analysis (S_{CP}), using only candidates with enough hits on inner silicon vertex detector;
- Signal from 3-dimensional fit: M_{BC} , $M_{K_S K_S K_S}$, $BDT_{Cont.Supp.}$
- Signal yield = 158 ± 14 events

$$S = -1.37^{+0.35}_{-0.45} \pm 0.03$$

$$C = -0.07 \pm 0.20 \pm 0.05$$



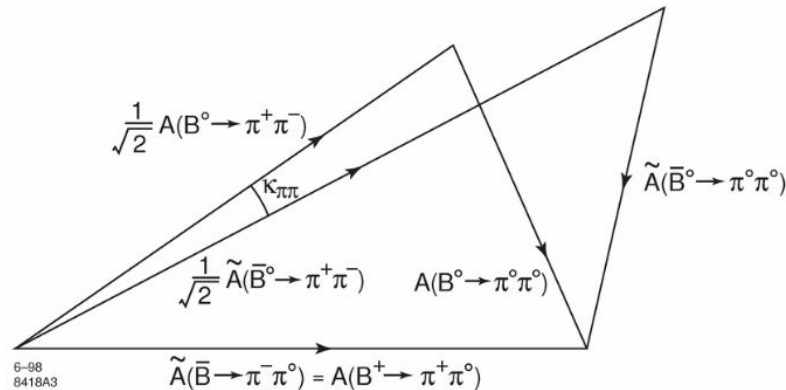
- The measurement of ϕ_2 from $B \rightarrow \pi\pi$ (or $B \rightarrow \rho\rho$) final states comes from an isospin analysis:

The following equalities hold:

$$\frac{1}{\sqrt{2}}A^{+-} + A^{00} = A^{+0}$$

$$\frac{1}{\sqrt{2}}\tilde{A}^{+-} + \tilde{A}^{00} = \tilde{A}^{+0}$$

$$A^{+0} = \tilde{A}^{+0}$$

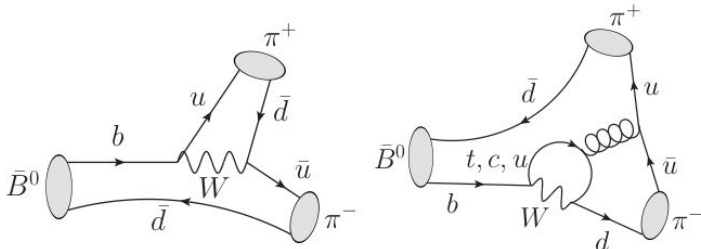


- Observables (for e.g. $B \rightarrow \pi\pi$):
 - branching fractions of: $B^0 \rightarrow \pi^+\pi^0, \pi^+\pi^-, \pi^0\pi^0$;
 - direct (time-independent) CP asymmetries: C^{+-}, C^{00} ;
 - time-dependent CP asymmetries: S^{+-}, S^{00} .
- Belle II will be able to measure all these observables;
- We expect to push the sensitivity to α to $\sim 1^\circ$.

M. Gronau and D. London,
PRL 65 (1990), 3381

Measurement of ϕ_2/α

Two amplitudes of comparable size with different weak phase:



Penguin in $B^0 \rightarrow \pi^+ \pi^-, \pi^0 \pi^0$, but not in $B^\pm \rightarrow \pi^\pm \pi^0$

$$\phi_2 = (\overline{A}^{+0}, A^{+0}), \phi_2^{eff} = (\overline{A}^{+-}, A^{+-})$$

Isospin analysis ^[Gronau-London PRL, 64 3381 (1990)]: constraints

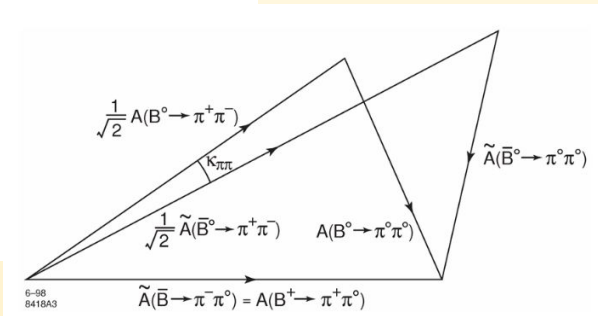
B^0 and B^\pm amplitudes:

$$A^{+0} = A^{+-} / \sqrt{2} + A^{00}$$

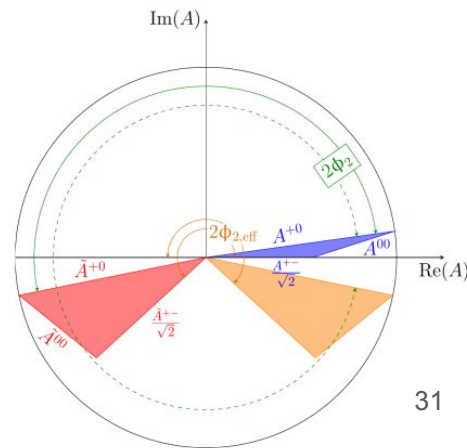
$$\overline{A}^{+0} = \overline{A}^{+-} / \sqrt{2} + \overline{A}^{00}$$

$$|A^{+0}| = |\overline{A}^{+0}|$$

Similar for $B \rightarrow \rho\rho$



- Need all branching fractions;
- Direct CP asymmetries: C^{+-}, C^{00} ;
- TD CP asymmetries: S^{+-}, S^{00} ;
 - S^{00} reduces folding ambiguities
- Belle II will be able to measure all these observables
 - Final sensitivity $\sim 1^\circ$



Toward ϕ_2/α : $B^0 \rightarrow \pi^0 \pi^0$

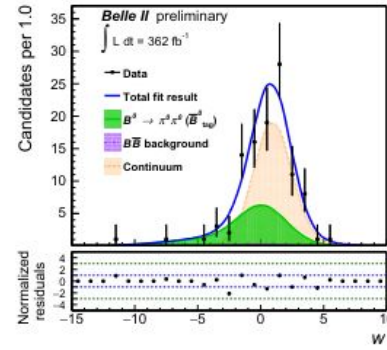
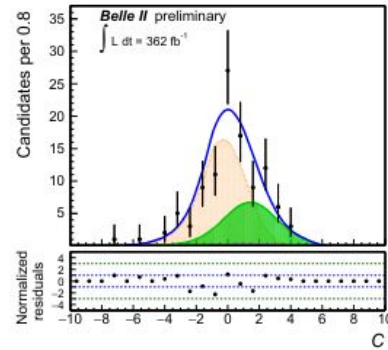
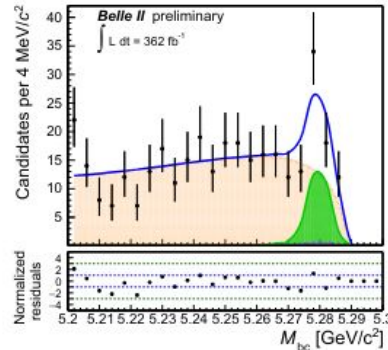
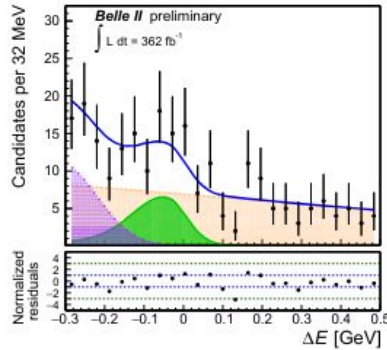
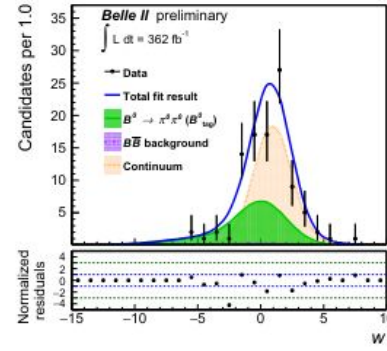
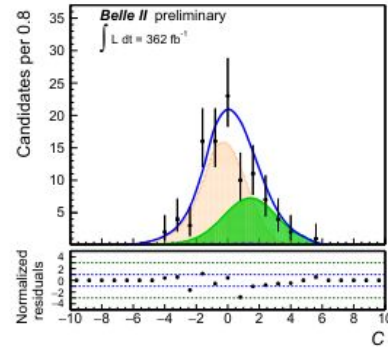
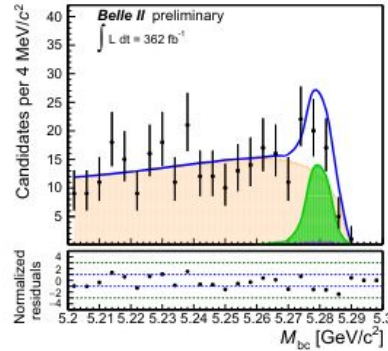
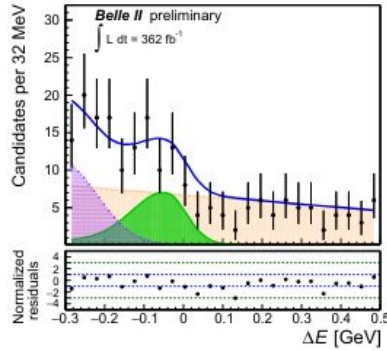
New for FCPC 2024



Previous results
[\[PRD107 \(2023\) 112009\]](#)

$B^0 \rightarrow \pi^0 \pi^0$

$\overline{B}^0 \rightarrow \pi^0 \pi^0$



signal enhanced region

Toward $\phi_2/\alpha: B^0 \rightarrow \pi^0 \pi^0$

New for FCPC 2024



Previous results
[\[PRD107 \(2023\) 112009\]](#)

Source	\mathcal{B}	\mathcal{A}_{CP}
π^0 efficiency	8.6 %	n/a
$\Upsilon(4S)$ branching fractions ($1 + f^{+-}/f^{00}$)	2.5 %	n/a
Continuum-suppression efficiency	1.9 %	n/a
$B\bar{B}$ -background model	1.7 %	0.034
Sample size $N_{B\bar{B}}$	1.5 %	n/a
Signal model	1.2 %	0.021
Continuum-background model	0.9 %	0.025
Wrong-tag probability calibration	n/a	0.008
Total systematic uncertainty	9.6 %	0.048
Statistical uncertainty	15.9 %	0.303

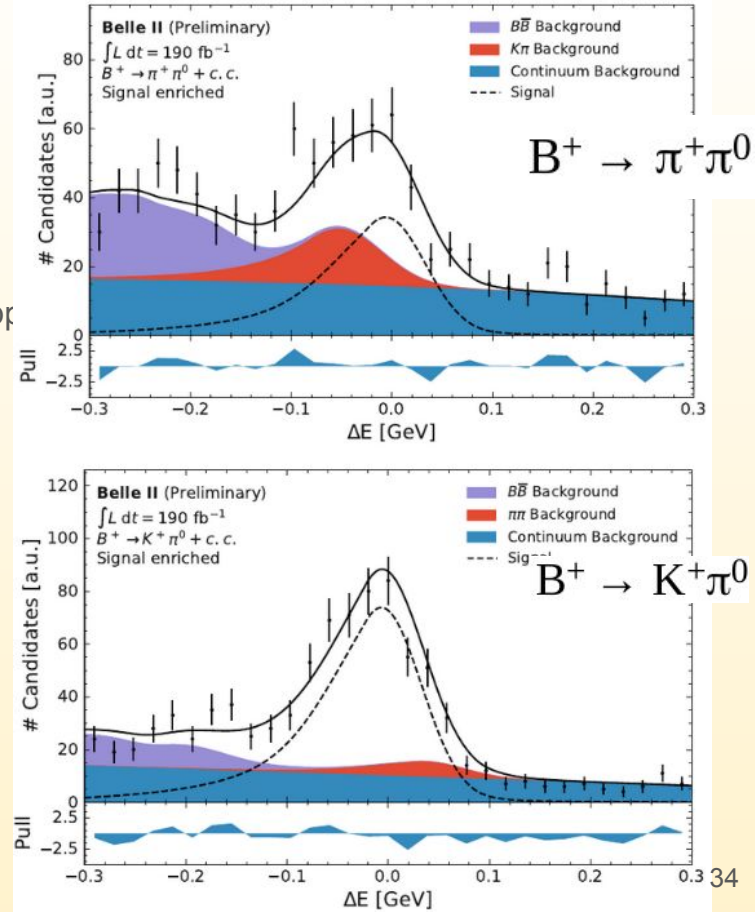
TABLE I. Fractional systematic uncertainties on the branching fraction and absolute systematic uncertainties on the CP asymmetry. Total systematic uncertainties, resulting from their sums in quadrature, are also given, and compared with statistical uncertainties.

$B^+ \rightarrow K^+ \pi^0 / \pi^+ \pi^0$

- $B^+ \rightarrow K^+ \pi^0$ enters in “ $K\pi$ ” puzzle
- Using common selection for both channels
 - Enhance pion and kaon final state
 - Background from continuum $q\bar{q}$ reduced with MVA
- BR and A^{CP} from 3D fit on M_{bc} , ΔE , $BDT_{Cont.Supp}$
 - Simultaneous fit to both samples
 - $D^+ \rightarrow K_s \pi^+$ and $D^0 \rightarrow K^- \pi^+$ for detector asymmetries
- Results:

$$\begin{aligned} \mathcal{B}(\pi^+ \pi^0) &= (6.1 \pm 0.5 \pm 0.5) \times 10^{-6} \\ \mathcal{B}(K^+ \pi^0) &= (14.3 \pm 0.7 \pm 0.8) \times 10^{-6} \\ \mathcal{A}^{CP}(\pi^+ \pi^0) &= -0.09 \pm 0.09 \pm 0.02 \\ \mathcal{A}^{CP}(K^+ \pi^0) &= 0.01 \pm 0.05 \pm 0.01 \end{aligned}$$

$$\text{WA: } \mathcal{A}_{K^+ \pi^0}^{CP} = 0.030 \pm 0.013, \mathcal{A}_{\pi^+ \pi^0}^{CP} = 0.03 \pm 0.04$$

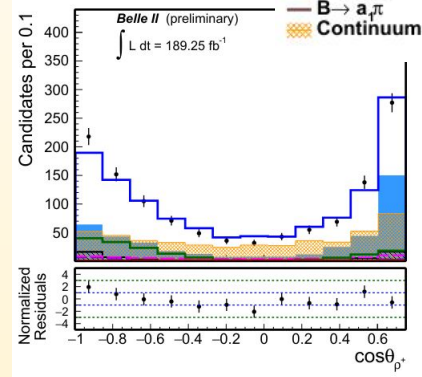
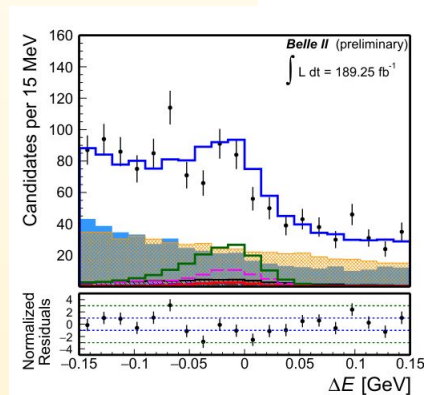
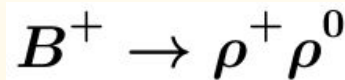
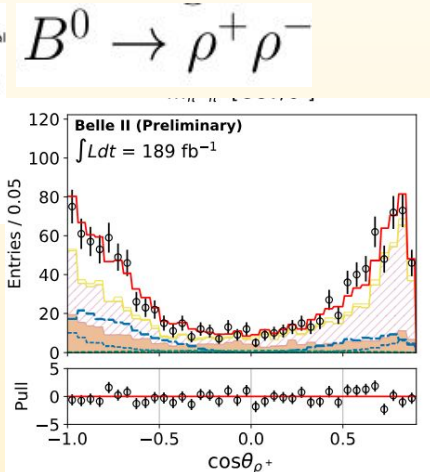
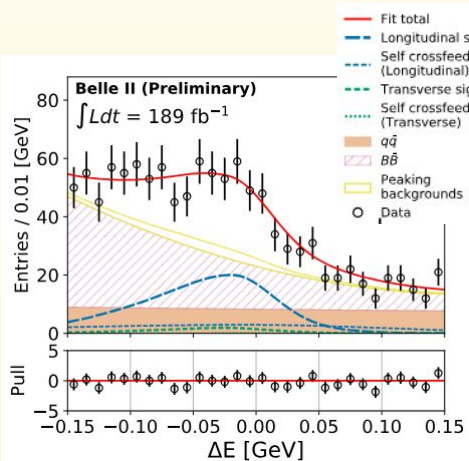


Toward ϕ_2/α : $B \rightarrow \rho\rho$

arxiv:2208.03554
arxiv:2206.12362



- Broad resonances of vector mesons, π^0 in final state
 - multiple non-negligible peaking background contributions
- CP analysis requires measurement of longitudinal polarization:
 - angular analysis using helicity angles of ρ 's



$$\mathcal{B}(B^0 \rightarrow \rho^+ \rho^-) = [2.67 \pm 0.28 (\text{stat}) \pm 0.28 (\text{syst})] \times 10^{-5},$$

$$f_L = 0.956 \pm 0.035 (\text{stat}) \pm 0.033 (\text{syst}),$$

$$\mathcal{B}(B^+ \rightarrow \rho^+ \rho^0) = [23.2_{-2.1}^{+2.2} (\text{stat}) \pm 2.7 (\text{syst})] \times 10^{-6},$$

$$f_L = 0.943_{-0.033}^{+0.035} (\text{stat}) \pm 0.027 (\text{syst}),$$

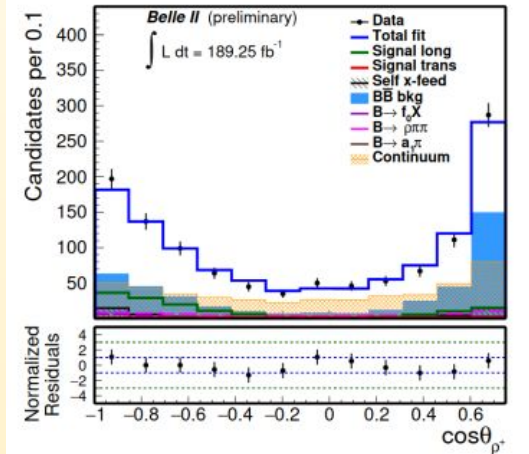
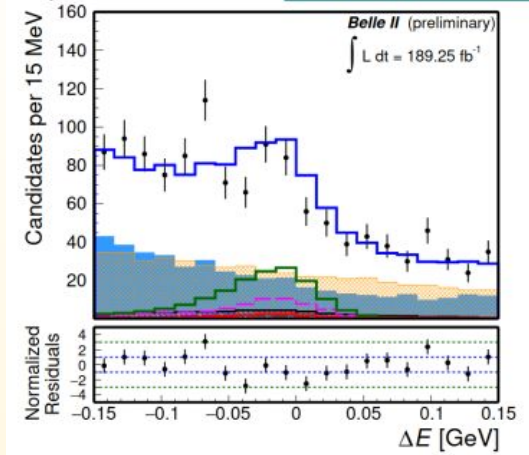
$$\mathcal{A}_{CP} = -0.069 \pm 0.068 (\text{stat}) \pm 0.060 (\text{syst}).$$

Toward ϕ_2/α : $B^+ \rightarrow \rho^+ \rho^0$

arXiv:2206.12362



- Similar to $B^0 \rightarrow \rho^+ \rho^-$
- 6D fit: ΔE , BDT, $2 * M(\pi\pi)$, $2 * \text{helicity angles}$
 - Template fit w/ correlation
- Results:
 - $N(\text{sig}) = 345 \pm 31$



$$\mathcal{A}^{\text{CP}} = -0.069 \pm 0.068 \text{ (stat)} \pm 0.060 \text{ (syst)}$$

$$\mathcal{B} = (23.2^{+2.2}_{-2.1} \text{ (stat)} \pm 2.7 \text{ (syst)}) \cdot 10^{-6}$$

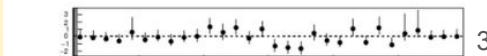
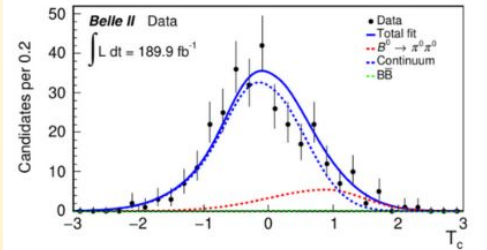
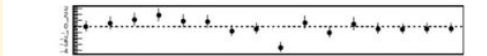
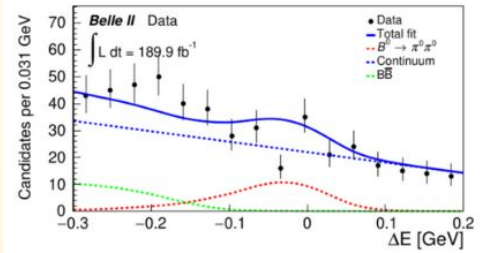
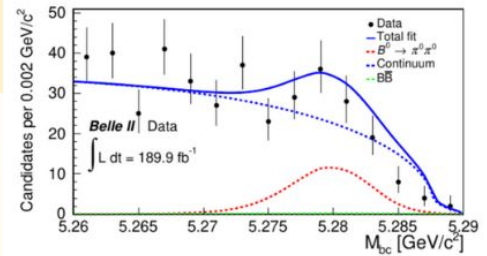
$$f_L = 0.943^{+0.035}_{-0.033} \text{ (stat)} \pm 0.027 \text{ (syst)}$$

WA: $\mathcal{A}^{\text{CP}} = -0.05 \pm 0.05, \mathcal{B} = (24.0 \pm 1.9) \cdot 10^{-6}$

Toward ϕ_2/α : $B^0 \rightarrow \pi^0 \pi^0$

[PRD107 (2023) 112009]
Superseded result

- ϕ_2/α from isospin analysis of $B \rightarrow \pi\pi/\rho\rho$ modes
 - BelleII will measure all modes
- $B^0 \rightarrow \pi^0 \pi^0$ most challenging mode, very hard for LHCb
- Fake photons background reduced with multivariate algorithm for $\pi^0 \rightarrow \gamma\gamma$ purity
 - Control channel: $B^0 \rightarrow D^0(K^+ \pi^- \pi^0) \pi^0$
- Using Flavour Tagger to get direct CP asymmetry
- Results:
 - N Yield: 93 ± 18
 - $B = (1.38 \pm 0.27 \pm 0.22) \times 10^{-6}$
 - $A_{CP} = 0.14 \pm 0.46 \pm 0.07$
- Competitive with Belle with $\frac{1}{3}$ of dataset

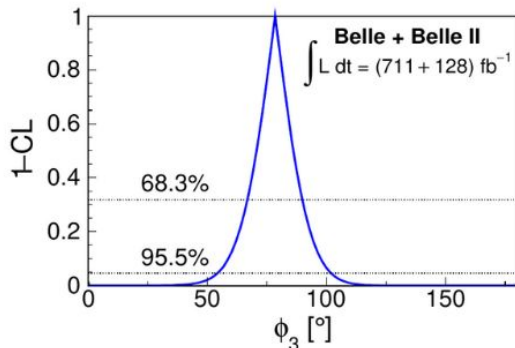
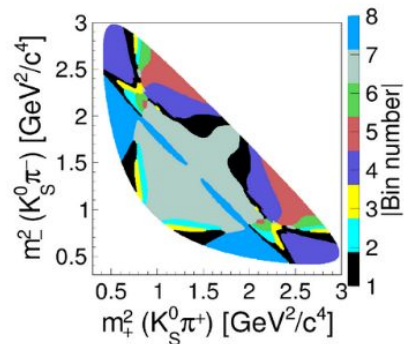


N

37

- Best sensitivity from the BPGGSZ method, exploiting the interference in the $D^0 \rightarrow K_S \pi^+ \pi^-$ Dalitz plot:

[J. High Energ. Phys. 2022, 63 \(2022\)](#)



$$\begin{aligned} \phi_3 &= (78.4 \pm 11.4 \pm 0.5 \pm 1.0)^\circ, \\ r_B^{DK} &= 0.129 \pm 0.024 \pm 0.001 \pm 0.002, \\ \delta_B^{DK} &= (124.8 \pm 12.9 \pm 0.5 \pm 1.7)^\circ, \\ r_B^{D\pi} &= 0.017 \pm 0.006 \pm 0.001 \pm 0.001, \\ \delta_B^{D\pi} &= (341.0 \pm 17.0 \pm 1.2 \pm 2.6)^\circ. \end{aligned}$$

- GLW method [[Phys.Lett.B 253 \(1991\) 483-488](#), [Phys.Lett.B 265 \(1991\) 172-176](#)]: consider decays of the D^0 to odd (-) and even (+) CP eigenstates and measure the observables:

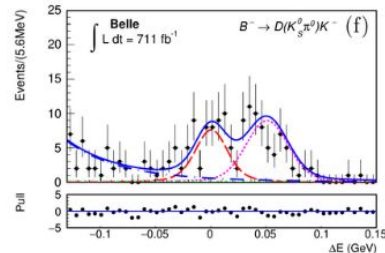
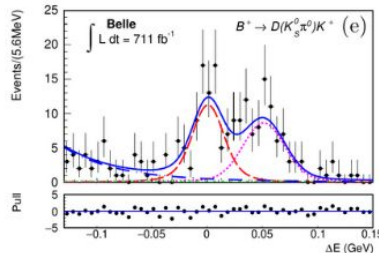
$$A_{CP\pm} \equiv \frac{\mathcal{B}(B^- \rightarrow D_{CP\pm} K^-) - \mathcal{B}(B^+ \rightarrow D_{CP\pm} K^+)}{\mathcal{B}(B^- \rightarrow D_{CP\pm} K^-) + \mathcal{B}(B^+ \rightarrow D_{CP\pm} K^+)} \quad \mathcal{R}_{CP\pm} \equiv \frac{\mathcal{B}(B^- \rightarrow D_{CP\pm} K^-) + \mathcal{B}(B^+ \rightarrow D_{CP\pm} K^+)}{\mathcal{B}(B^- \rightarrow D_{\text{flav}} K^-) + \mathcal{B}(B^+ \rightarrow D_{\text{flav}} K^+)}$$

which are related to ϕ_3 :

$$\begin{aligned} \mathcal{R}_{CP\pm} &= 1 + r_B^2 \pm 2r_B \cos \delta_B \cos \phi_3 \\ A_{CP\pm} &= \pm 2r_B \sin \delta_B \sin \phi_3 / \mathcal{R}_{CP\pm} \end{aligned}$$

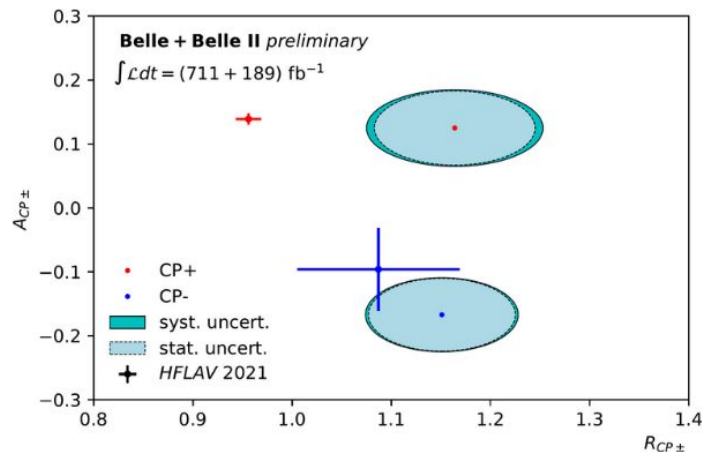
- Considering $D^0 \rightarrow K^+K^-$ as CP+, $D^0 \rightarrow K_S^0\pi^0$ as CP-, and $D^0 \rightarrow K^-\pi^+$ as flavor specific final state, we measure (on the Belle + Belle II data set):

$$\begin{aligned} \mathcal{R}_{CP+} &= 1.164 \pm 0.081 \pm 0.036, \\ \mathcal{R}_{CP-} &= 1.151 \pm 0.074 \pm 0.019, \\ \mathcal{A}_{CP+} &= (+12.5 \pm 5.8 \pm 1.4)\%, \\ \mathcal{A}_{CP-} &= (-16.7 \pm 5.7 \pm 0.6)\%. \end{aligned}$$

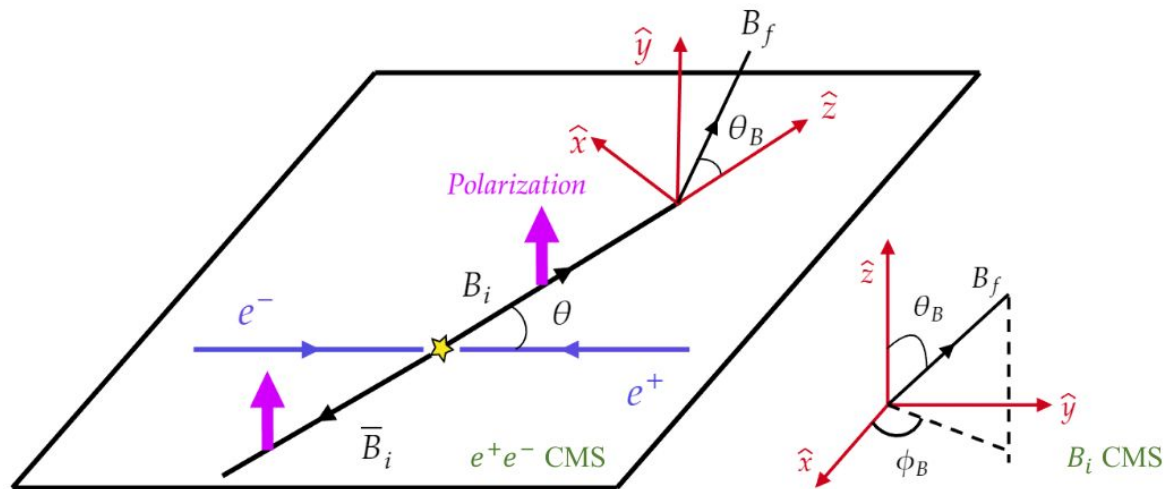


- The A_{CP} 's differ from each other at $\sim 3.5\sigma$;
- This translates into constraints on ϕ_3 :

	68.3% CL	95.4% CL
	[8.7, 20.5]	
ϕ_3 ($^\circ$)	[83.8, 96.1]	[4.7, 175.8]
	[163.4, 173.1]	
r_B	[0.282, 0.489]	[0.069, 0.560]



Polarized hyperon pairs in e^+e^- collisions



Polarization:

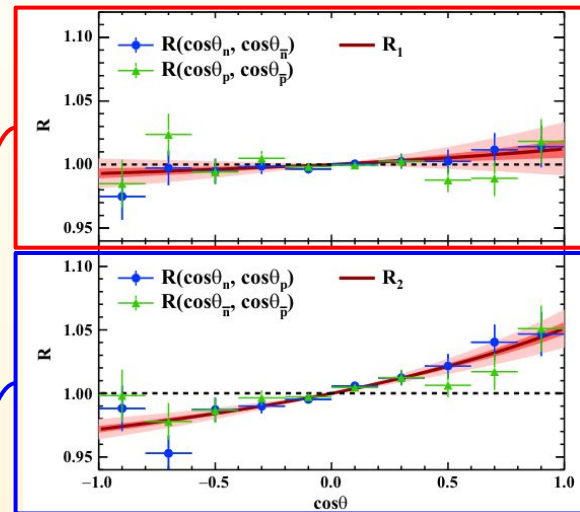
$$P_y(\cos\theta) = \frac{\sqrt{1-\alpha_\psi^2} \cos\theta \sin\theta}{1+\alpha_\psi \cos^2\theta} \sin(\Delta\Phi)$$

- Angular distribution of $\frac{d\Gamma}{d\Omega} \propto 1 + \alpha_\psi \cos^2\theta$, $\alpha_\psi \in [-1.0, 1.0]$
- Unpolarized e^+e^- beams \Rightarrow transverse polarized hyperon (if $\Delta\Phi \neq 0$):

$$e^+e^- \rightarrow J/\psi \rightarrow \Xi^+\Xi^- \rightarrow \Lambda(\rightarrow p\pi^-)\pi^- \bar{\Lambda}(\rightarrow \bar{n}\pi^0)\pi^+ + \text{cc}$$

- CPV in hyperons might arise from interference of S and P-wave
 - 10 billion J/ψ events: (144+123)k signal events (91% purity)
 - 9 helicity angles, 8 global parameters
- Several decay properties of Ξ^- and Λ are determined:

[PhysRevLett.132.101801](https://arxiv.org/abs/1302.1018)



No CPV at $<10^{-2}$ precision level

- SM predictions $\sim 10^{-4}-10^{-5}$

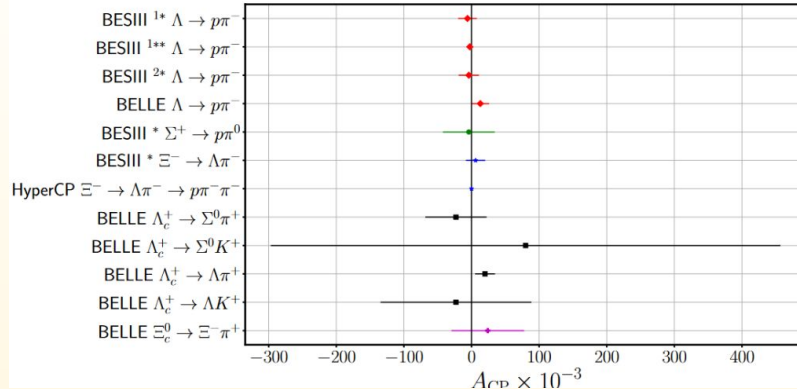
$\Delta I = 3/2$ transition in Λ decay

Parameters	This work	Previous result
$\alpha_{J/\psi}$	$0.611 \pm 0.007^{+0.013}_{-0.007}$	$0.586 \pm 0.012 \pm 0.010$ [18]
$\Delta\Phi_{J/\psi}$ (rad)	$1.30 \pm 0.03^{+0.02}_{-0.03}$	$1.213 \pm 0.046 \pm 0.016$ [18]
α_{Ξ}	$-0.367 \pm 0.004^{+0.003}_{-0.004}$	$-0.376 \pm 0.007 \pm 0.003$ [18]
ϕ_{Ξ} (rad)	$-0.016 \pm 0.012^{+0.004}_{-0.008}$	$0.011 \pm 0.019 \pm 0.009$ [18]
$\bar{\alpha}_{\Xi}$	$0.374 \pm 0.004^{+0.003}_{-0.004}$	$0.371 \pm 0.007 \pm 0.002$ [18]
$\bar{\phi}_{\Xi}$ (rad)	$0.010 \pm 0.012^{+0.003}_{-0.013}$	$-0.021 \pm 0.019 \pm 0.007$ [18]
α_{Λ^-}	$0.764 \pm 0.008^{+0.005}_{-0.006}$	$0.7519 \pm 0.0036 \pm 0.0024$ [37]
α_{Λ^+}	$-0.774 \pm 0.009^{+0.005}_{-0.005}$	$-0.7559 \pm 0.0036 \pm 0.0030$ [37]
$\alpha_{\Lambda 0}$	$0.670 \pm 0.009^{+0.009}_{-0.008}$	0.75 ± 0.05 [29]
$\bar{\alpha}_{\Lambda 0}$	$-0.668 \pm 0.008^{+0.006}_{-0.008}$	$-0.692 \pm 0.016 \pm 0.006$ [17]
$\delta_P - \delta_S$ (rad)	$0.033 \pm 0.020^{+0.008}_{-0.012}$	$-0.040 \pm 0.033 \pm 0.017$ [18]
$\xi_P - \xi_S$ (rad)	$0.007 \pm 0.020^{+0.018}_{-0.005}$	$0.012 \pm 0.034 \pm 0.008$ [18]
A_{CP}^{Ξ}	$-0.009 \pm 0.008^{+0.007}_{-0.002}$	$0.006 \pm 0.013 \pm 0.006$ [18]
$\Delta\phi_{CP}^{\Xi}$ (rad)	$-0.003 \pm 0.008^{+0.003}_{-0.007}$	$-0.005 \pm 0.014 \pm 0.003$ [18]
A_{CP}^{-}	$-0.007 \pm 0.008^{+0.002}_{-0.003}$	$-0.0025 \pm 0.0046 \pm 0.0012$ [37]
A_{CP}^0	$0.001 \pm 0.009^{+0.005}_{-0.007}$...
A_{CP}^{Λ}	$-0.004 \pm 0.007^{+0.003}_{-0.004}$...
$\alpha_{\Lambda 0}/\alpha_{\Lambda^-}$	$0.877 \pm 0.015^{+0.014}_{-0.010}$	1.01 ± 0.07 [29]
$\bar{\alpha}_{\Lambda 0}/\alpha_{\Lambda^+}$	$0.863 \pm 0.014^{+0.012}_{-0.008}$	$0.913 \pm 0.028 \pm 0.012$ [17]

Hyperon at Super Tau-Charm Facility (STCF)



- Many (null) results so far
 - BESIII and Belle
- BESIII: today
 - 10 billion J/ψ
- At super J/ψ factory
 - 10^{12} J/ψ per year
- CPV sensitivity in hyperon's decay
 - $10^{-4} - 10^{-5}$
 - challenging SM predictions



BESIII:
 Nature Phys. **15**, p 631-634 (2019)
 Phys. Rev. Lett. **125**, 052004 (2020)
 Nature **606**, 64-69 (2022)
 Phys. Rev. Lett. **129**, 131801 (2022)
 Phys. Rev. D **108**, L031106 (2023)

Belle:
 Sci. Bull. **68**, 583-592 (2023)

HyperCP:
 Phys. Rev. Lett. **93**, 262001, 2004.

