

Searches for Charged Lepton Flavor Violation in tau and hadron decays at Belle and Belle II

NuFact 2024

Lemont, Illinois, United States

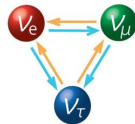
Paolo Leo

on behalf of the Belle and Belle II Collaboration

September 17, 2024

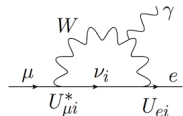


Observation of neutrino oscillations provided clear evidence that neutrinos are massive and **lepton flavour conservation** is violated.



What about the charged leptons?

- Charged LFV can occur through oscillations in **loops**
- The predicted rates are **GIM suppressed** $\propto \left(\frac{m_{\nu}}{M_W}\right)^4$ ($10^{-54} \sim 10^{-49}$) for all the LFV μ and τ decays.

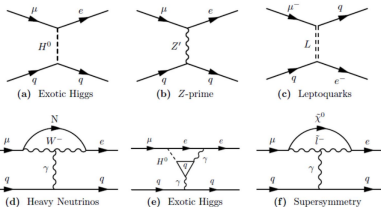


$$\text{BR}(\mu \rightarrow e\gamma) = \frac{3\alpha}{32\pi} \left| \sum_{i=2,3} U_{\mu i}^* U_{ei} \frac{\Delta m_{ii}^2}{M_W^2} \right|^2 < 10^{-54}$$

Observation of LFV will be a **signature of NP!**

Many scenarios of physics beyond the Standard Model (SM) introduce new sources of CLFV ($10^{-10} \sim 10^{-7}$).

Baryon Number Violation (BNV), crucial ingredient to explain matter-antimatter asymmetry, allowed in many models.



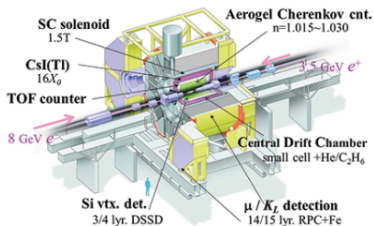
These models also holds for τ and hadron decays

- **Belle** (1999 - 2010) and **Belle II** (2018 -) operate at B-factories.
 - Asymmetric e^+e^- colliders optimized for the production of **B meson** pairs, but also **D mesons**, **τ leptons**, ... **dark sector**
 - Collisions mainly at $\Upsilon(4S)$: $\sqrt{s} = 10.58$ GeV (60 MeV below $\Upsilon(4S)$, $\Upsilon(5S)$ and others)
- **Advantages** of experiments at **B-factories**
 - **Well known** initial-state condition and **clean environment** (low particle multiplicity)
 - Hermetic detectors with excellent **particle identification** (PID) and **tracking performance**

Belle @KEKB, recorded

$$\int L dt = 1 \text{ ab}^{-1}$$

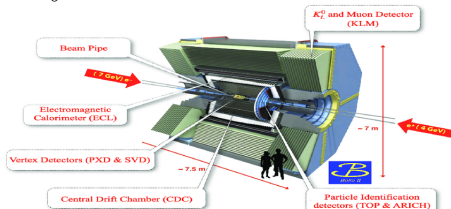
Belle Detector



Belle II @SuperKEKB, recorded

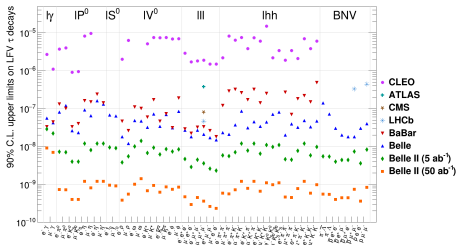
$$\int L dt = 427 \text{ fb}^{-1} \text{ (Run 1) [2018 - 2022]}$$

$$\int L dt = 103 \text{ fb}^{-1} \text{ (Run 2) [2024 -]}$$



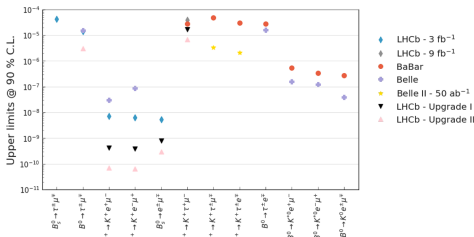
LFV at Belle and Belle II

Existing and expected limits on LFV τ decays [1]



- Neutrinoless 2-body or 3-body decays to **52 final states**.
- In some SM extensions, cLFV decays are expected at rates only one order of magnitude **below present bounds**.

Existing and expected limits on LFV B decays [2]



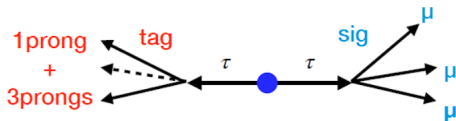
- Final state involving τ makes **harder the reconstruction** due to the presence of **missing energy**.
- **Hadronic B tag** used to infer the momentum of the signal side
- Belle II will improve limits by **1-2 orders**.

[1] Snowmass 2021: cLFV in τ sector - arXiv:2203.14919

[2] G. De Marino, Anomalies and Precision in the Belle II era (2021)

τ LFV channels

- Main analysis approach:
 - Inclusive of 3×1 and 3×3 topologies
 - Selection and background rejection using BDT



- Belle II with 424 fb^{-1}

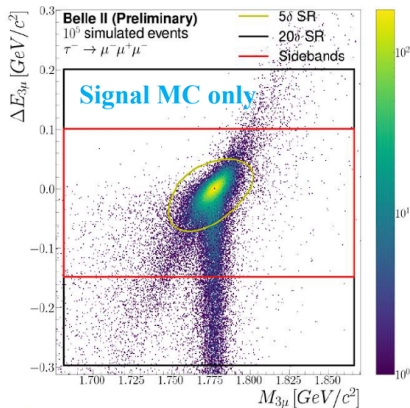
[arXiv:2405.07386](https://arxiv.org/abs/2405.07386)

- Extract signal yield from 2D plane ($M_{3\mu}$, $\Delta E_{3\mu}$):

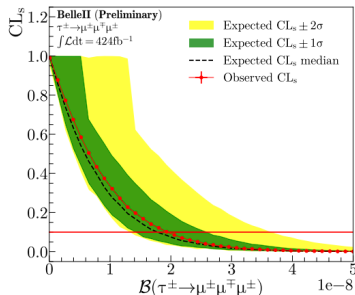
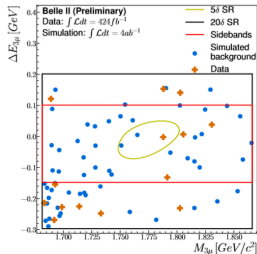
$$M_{3\mu} = \sqrt{E_{3\mu}^2 - P_{3\mu}^2}$$

$$\Delta E_{3\mu} = E_{3\mu}^{CM} - E_{\text{beam}}^{CM}$$

- For signal:
 - $\Delta E_{3\mu}$ close to 0 and $M_{3\mu}$ close to τ mass
 - Tails due to initial and final state radiation



- Signal: efficiency: 20.4% ($2.7 \times$ Belle efficiency)
- Number of expected BG: 0.5
- 1 event observed inside the SR
- $\mathcal{B}(\tau \rightarrow 3\mu) < 1.9 \times 10^{-8}$ at 90% C.L.



Most stringent limit to date

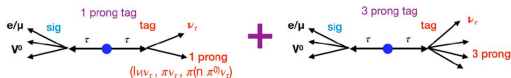
	UL at 90% C.L. on $\mathcal{B}(\tau \rightarrow 3\mu)$
ATLAS	3.8×10^{-7} ($\mathcal{L} = 20.3 \text{ fb}^{-1}$)
LHCb	4.6×10^{-8} ($\mathcal{L} = 3.0 \text{ fb}^{-1}$)
CMS	2.9×10^{-8} ($\mathcal{L} = 131 \text{ fb}^{-1}$)
Belle	2.1×10^{-8} ($\mathcal{L} = 782 \text{ fb}^{-1}$)
BaBar	3.3×10^{-8} ($\mathcal{L} = 486 \text{ fb}^{-1}$)
Belle II	1.9×10^{-8} ($\mathcal{L} = 424 \text{ fb}^{-1}$)

Search for $\tau \rightarrow lV^0 (V^0 = \rho, \omega, \phi, K^*)$ decays @ Belle

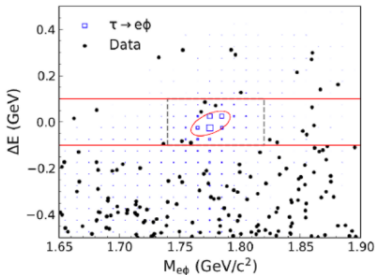
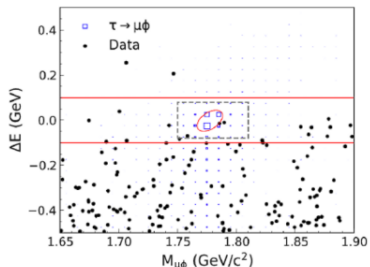
Previous search at Belle on 854 fb^{-1} exploiting
1-prong tag [1]

New results from Belle [2]:

- Increase the efficiency using
 - full data set of 980 fb^{-1} [2]
 - more decay modes in the tag side
 - background suppression with BDT



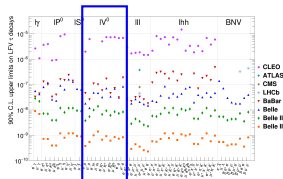
- Exploit topology and event/tag kinematics of the backgrounds
- Further suppress $\tau \rightarrow 3\pi\nu$ and $ee \rightarrow q\bar{q}$ with BDT
- Estimate expected background in SR from **sideband interpolation**



[1] Y. Miyazaki, *et. al.*, (Belle Collaboration) *Phys. Lett. B* 699, 251 (2011)

[2] N. Tsuzuki, *et. al.*, (Belle Collaboration) *JHEP* 2023, 118, (2023)

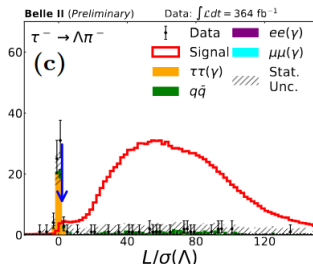
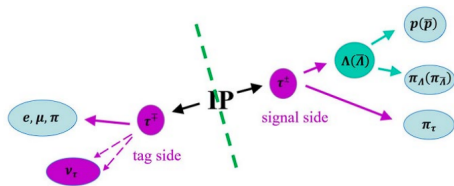
- No significant excess in all modes \rightarrow set ULs at 90% C.L.
- 30% improvement over previous measurements:
 - increased statistics (124 fb⁻¹)
 - higher signal efficiency (9%)



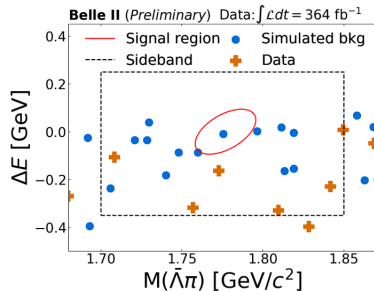
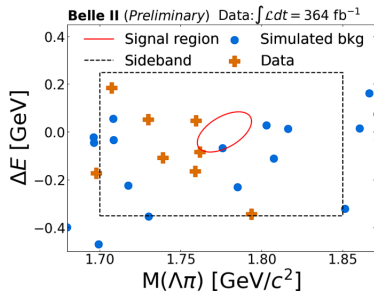
Mode	ε (%)	N_{BG}	σ_{sys} (%)	N_{obs}	$\mathcal{B}_{\text{obs}} (\times 10^{-8})$
$\tau^\pm \rightarrow \mu^\pm \rho^0$	7.78	$0.95 \pm 0.20(\text{stat.}) \pm 0.15(\text{syst.})$	4.6	0	< 1.7
$\tau^\pm \rightarrow e^\pm \rho^0$	8.49	$0.80 \pm 0.27(\text{stat.}) \pm 0.04(\text{syst.})$	4.4	1	< 2.2
$\tau^\pm \rightarrow \mu^\pm \phi$	5.59	$0.47 \pm 0.15(\text{stat.}) \pm 0.05(\text{syst.})$	4.8	0	< 2.3
$\tau^\pm \rightarrow e^\pm \phi$	6.45	$0.38 \pm 0.21(\text{stat.}) \pm 0.00(\text{syst.})$	4.5	0	< 2.0
$\tau^\pm \rightarrow \mu^\pm \omega$	3.27	$0.32 \pm 0.23(\text{stat.}) \pm 0.19(\text{syst.})$	4.8	0	< 3.9
$\tau^\pm \rightarrow e^\pm \omega$	5.41	$0.74 \pm 0.43(\text{stat.}) \pm 0.06(\text{syst.})$	4.5	0	< 2.4
$\tau^\pm \rightarrow \mu^\pm K^{*0}$	4.52	$0.84 \pm 0.25(\text{stat.}) \pm 0.31(\text{syst.})$	4.3	0	< 2.9
$\tau^\pm \rightarrow e^\pm K^{*0}$	6.94	$0.54 \pm 0.21(\text{stat.}) \pm 0.16(\text{syst.})$	4.1	0	< 1.9
$\tau^\pm \rightarrow \mu^\pm \bar{K}^{*0}$	4.58	$0.58 \pm 0.17(\text{stat.}) \pm 0.12(\text{syst.})$	4.3	1	< 4.3
$\tau^\pm \rightarrow e^\pm \bar{K}^{*0}$	7.45	$0.25 \pm 0.11(\text{stat.}) \pm 0.02(\text{syst.})$	4.1	0	< 1.7

- **Belle II:** [arXiv:2407.05117](https://arxiv.org/abs/2407.05117)

- Reconstruct exactly 4 charged tracks (total null charge) in one-prong tag approach
- $\Lambda(\bar{\Lambda})$ is reconstructed from proton (anti-proton) and pion
- Signal selection and background suppression using loose pre-selection, followed by Gradient-BDT
- The flight significance (L/σ) of Λ and $\bar{\Lambda}$ candidates is one of the most discriminating variables.

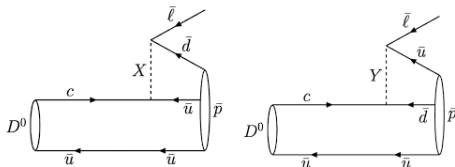


- Signal efficiencies are 9.5% and 9.9% for $\tau \rightarrow \Lambda\pi$ and $\tau \rightarrow \bar{\Lambda}\pi$ respectively
- Poisson counting experiment technique in signal region in the $M(\Lambda\pi) = \sqrt{E_{\Lambda\pi}^2 - P_{\Lambda\pi}^2}$ and $\Delta E = E_{\Lambda\pi}^{CM} - \sqrt{s}/2$ plane
- Expected events are 1 and 0.5 for $\tau \rightarrow \Lambda\pi$ and $\tau \rightarrow \bar{\Lambda}\pi$ respectively
- No events observed
- **World's best upper limits** at 90% C.L. of 4.7×10^{-8} for $\mathcal{B}(\tau \rightarrow \Lambda\pi)$ and 4.3×10^{-8} for $\mathcal{B}(\tau \rightarrow \bar{\Lambda}\pi)$



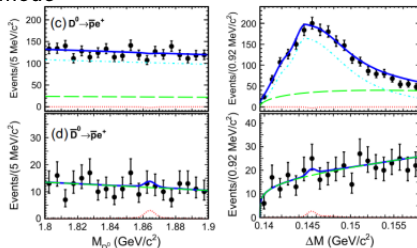
Hadron LFV channels

- Motivation:** BNV is one of the crucial ingredients to explain matter-antimatter asymmetry
 - In many models, BNV and LNV but their difference $\Delta(B - L) = 0$ is conserved
 - Valuable input to the search of leptoquarks



- Belle** performed a search for $D^0 \rightarrow pl^-$, $\bar{D}^0 \rightarrow pl^-$, $D^0 \rightarrow \bar{p}l^+$ and $\bar{D}^0 \rightarrow \bar{p}l^+$ ($l = e$ or μ) [PhysRevD.109.L031101](https://arxiv.org/abs/1003.1101)
 - 921 fb^{-1} integrated data luminosity at and 60 MeV below the $\Upsilon(4S)$ and at the $\Upsilon(5S)$ resonance
 - The well-known $D^0 \rightarrow K^- \pi^+$ is used for normalization to measure the branching fractions of signal modes.

- Signal yields are extracted with extended maximum likelihood fits to the unbinned M_{D^0} and ΔM distributions of each decay mode
- Separate PDFs are used for signal, peaking and combinatorial background
 - **Signal:** sum of 4 gaussian for ΔM , 2 Gaussian + 1 asymmetric Gaussian for M_{D^0}
 - **peaking background, combinatorial background** and the **sum of the fits** are shown in the plots.

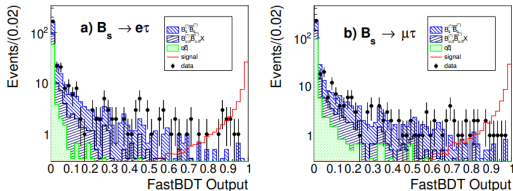
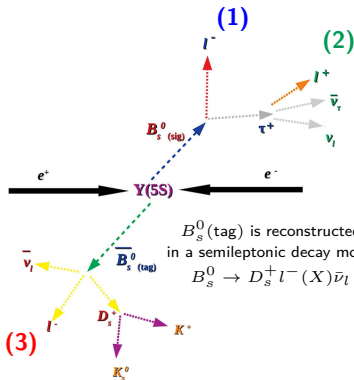


Decay mode	ϵ (%)	N_S	S (σ)	N_{pl}^{UL}	$\mathcal{B} \times 10^{-7}$
$D^0 \rightarrow pe^-$	10.2	-6.4 ± 8.5		17.5	< 5.5
$\bar{D}^0 \rightarrow pe^-$	10.2	-18.4 ± 23.0		22.0	< 6.9
$D^0 \rightarrow \bar{p}e^+$	09.7	-4.7 ± 23.0		22.0	< 7.2
$\bar{D}^0 \rightarrow \bar{p}e^+$	09.6	7.1 ± 9.0	0.6	23.0	< 7.6
$D^0 \rightarrow p\mu^-$	10.7	11.0 ± 23.0	0.9	17.1	< 5.1
$\bar{D}^0 \rightarrow p\mu^-$	10.7	-10.8 ± 27.0		21.8	< 6.5
$D^0 \rightarrow \bar{p}\mu^+$	10.5	-4.5 ± 14.0		21.1	< 6.3
$\bar{D}^0 \rightarrow \bar{p}\mu^+$	10.4	16.7 ± 8.8	1.6	21.4	< 6.5

- Most stringent upper limits to date
- First results for $D \rightarrow p\mu$

Belle: using 121 fb^{-1} collected at the $\Upsilon(5S)$ resonance mass. [JHEP08\(2023\)178](#)

- To suppress $J/\psi \rightarrow l^+ l^-$ background, $M_{l_1, l_2} \notin [3.01, 3.12]$ for electron and $M_{l_1, l_2} \notin [3.05, 3.12]$ for muon case
- To reduce **combinatorial background**, ensure l_1 and l_3 have the same charge
- FastBDT to remove $e^+ e^- \rightarrow q \bar{q}$ and $e^+ e^- \rightarrow B_s^{(*)0} \bar{B}_s^{(*)0}, B^{(*)} \bar{B}^{(*)} X$



	ϵ (%)	$N_{\text{bkg}}^{\text{exp}}$	N_{obs}	\mathcal{B} ($\times 10^{-4}$)
$B_s \rightarrow e^- \tau^+$	0.031 ± 0.007	0.68 ± 0.69	3	< 14
$B_s \rightarrow \mu^- \tau^+$	0.030 ± 0.007	0.77 ± 0.78	1	< 7.3

- Most stringent limit on $\mathcal{B}(B_s^0 \rightarrow \mu\tau) < 3.4 \times 10^{-5}$ reported by LHCb [1]
- **First such limit reported on the $B_s^0 \rightarrow e\tau$**
- Belle II could improve in the future
 - **More data** collected at the $\Upsilon(5S)$ resonance.
 - Enhanced analysis techniques such as **full reconstruction of the tag B_s^0**

[1] R. Aaij *et al.* (LHCb Collaboration), *Phys. Rev. Lett.* **123**, 211801 (2019).

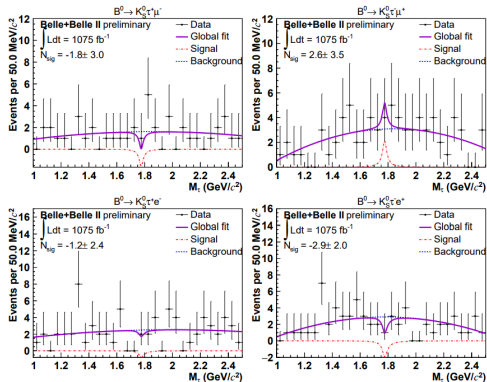
- **Motivation:** From the $\mathcal{B}(B^+ \rightarrow K^+ \nu \nu)$ excess [1] (2.7σ larger than SM) the predicted $\mathcal{B}(B \rightarrow K \tau \mu)$ is quite close to the current experimental sensitivities ($[2, 3] \times 10^{-6}$).
- **Belle and Belle II:** Search for LFV in $B^0 \rightarrow K_S^0 \tau l$ ($l = \mu, e$) from a combined analysis of **Belle (711 fb^{-1})** and **Belle II (364 fb^{-1})** dataset.
 - B_{tag} is fully reconstructed and kinematically constrained

$$M_{bc} \equiv \sqrt{E_{beam}^2/c^4 - |\vec{p}_{B_{tag}}|^2/c^2} > 5.27 \text{ GeV}/c^2$$
$$-0.15 < \Delta E < 0.1 \text{ GeV}$$

- **Full Event Interpretation (FEI) algorithm** score is used to select the best candidate
- τ lepton kinematics is obtained from kinematic constraints and the signal yields are extracted from τ mass (M_τ) as signal event peaks

[1] I. Adachi *et al.* (Belle II Collaboration), *Phys. Rev. D* 109, 112006 (2024).

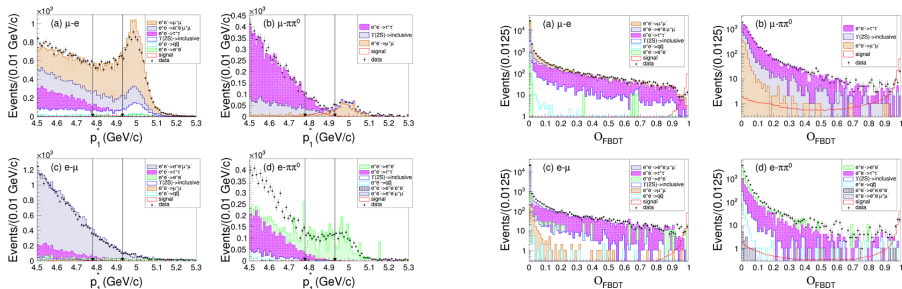
- BDT is used to remove **charm meson** semileptonic decays background.
- PDFs (Johnson's S_U function) are used to model M_{τ}



Channels	$\epsilon(10^{-4})$	N_{sig}	$\mathcal{B}(10^{-5})$	
			Central value	UL
$B^0 \rightarrow K_S^0 \tau^+ \mu^-$	1.7	-1.8 ± 3.0	$-1.0 \pm 1.6 \pm 0.2$	1.1
$B^0 \rightarrow K_S^0 \tau^- \mu^+$	2.1	2.6 ± 3.5	$1.1 \pm 1.6 \pm 0.3$	3.6
$B^0 \rightarrow K_S^0 \tau^+ e^-$	2.0	-1.2 ± 2.4	$-0.5 \pm 1.1 \pm 0.1$	1.5
$B^0 \rightarrow K_S^0 \tau^- e^+$	2.1	-2.9 ± 2.0	$-1.2 \pm 0.9 \pm 0.3$	0.8

These results are among the most stringent limits achieved of $b \rightarrow s \tau l$ transition to date.

- **Motivation:** Experimental limit on the two-body CLFV quarkonium decay provides complementary constraints on the Wilson coefficients of the effective Lagrangian of new physics models
- **Belle with 25 fb⁻¹:** [JHEP02\(2024\)187](#)
 - **Signal signature:** high-momentum lepton l_1
 - The τ lepton decays to $l_2\nu_2\nu_\tau$ or $\pi^+\pi^0\nu_\tau$
 - The l_2 is required to have different flavour respect to the non- τ lepton (l_1) coming from the Υ decay (to remove copious Bhabha background).
 - MVA (FastBDT) performed to further suppress the background (BhaBha)



- Signal efficiencies are **12.3% (8.1%)** for $\Upsilon(2S) \rightarrow \mu\tau$ ($\Upsilon(2S) \rightarrow e\tau$)
- Expected events are 3.9 ± 1.8 (5.9 ± 2.6) for $\Upsilon(2S) \rightarrow \mu\tau$ ($\Upsilon(2S) \rightarrow e\tau$)
- Observed events are 3 (12) for $\Upsilon(2S) \rightarrow \mu\tau$ ($\Upsilon(2S) \rightarrow e\tau$)
- Upper limits at 90% C.L. of

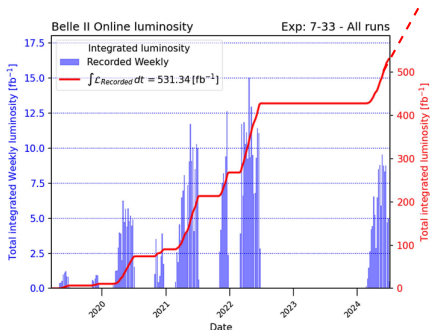
$$\mathcal{B}(\Upsilon(2S) \rightarrow \mu\tau) < 0.23 \times 10^{-6}$$

$$\mathcal{B}(\Upsilon(2S) \rightarrow e\tau) < 1.12 \times 10^{-6}$$

- Belle obtained 14 (3) times better upper limits for $\Upsilon(2S) \rightarrow \mu\tau$ ($\Upsilon(2S) \rightarrow e\tau$) as compared to previous results from BaBar [1].

[1] B. Aubert *et al.* (BaBar Collaboration), *Phys. Rev. Lett.* **104**, 151802 (2010).

- **Belle** is still providing **new LFV results in τ and hadron decays** and **Belle II** will contribute more in the future.
 - Some of them are **world leading results**: $\tau \rightarrow \mu\mu\mu$, $\tau \rightarrow lV^0$, $\tau \rightarrow \Lambda\pi$, $D \rightarrow pl$, $B^0 \rightarrow \tau e$, $\Upsilon(2S) \rightarrow l\tau$, and others...
- Within the next years of data taking Belle II will collect more data with expectations of significant improvements in current limits, spanning from a few parts in 10^{-10} to 10^{-9}



Coming soon

THANK YOU!

BACKUP SLIDES

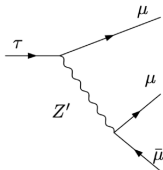
• Search for various decay models:

- $\tau \rightarrow lll$
- $\tau \rightarrow lK_S^0, \Lambda\pi$
- $\tau \rightarrow lV^0 (\rightarrow hh')$
- $\tau \rightarrow lP^0 (\rightarrow \gamma\gamma)$
- $\tau \rightarrow lhh'$
- $\tau \rightarrow l\gamma$

Simple: good determination of m_τ and E_τ
few SM background sources

Golden Channel: $\tau \rightarrow \mu\mu\mu$
Experimentally the most accessible

higher background



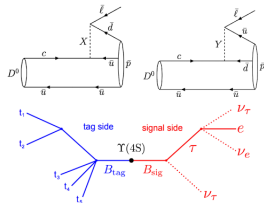
• **Motivation:** the decay channels forbidden in the SM but allowed in several new physics scenarios

- LFV decay $\tau \rightarrow lV^0$
 - The $\tau \rightarrow \mu\phi$ mode is a sensitive probe for leptoquark models
- BNV decay $\tau \rightarrow \Lambda(\bar{\Lambda})\pi$
 - BNV is one of the necessary conditions to explain the asymmetry of matter
 - Beyond SM scenarios allow for BNV and LNV
- LFV decay $\tau \rightarrow \mu\mu\mu$ (**Golden Channel**)

Physics Models	$\mathcal{B}(\tau \rightarrow \mu\mu\mu)$
SM	$10^{-53} \sim 10^{-55}$
SM + seesaw	10^{-10}
SUSY + Higgs	10^{-8}
SUSY + SO(10)	10^{-10}
Non-universal Z'	10^{-8}

- We present results for these other decay models:

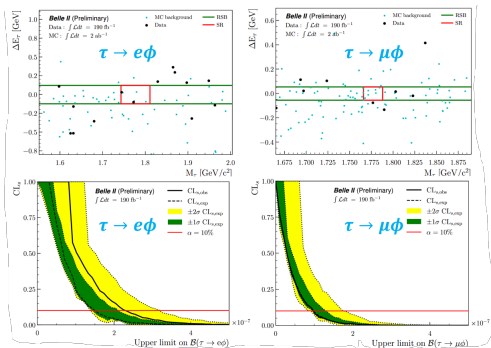
- $D \rightarrow pl$
- $B_s^0 \rightarrow \tau l$
- $B^0 \rightarrow K_S^0 \tau l$
- $\Upsilon(2S) \rightarrow l \tau$



- The decay channels are forbidden in the SM but allowed in **many BSM theories**.
- Some of them are searching also for **BNV**, and are optimal for **leptoquarks** searches.
- Final states involving τ generally require special techniques due to the presence of missing energy (neutrinos) and lack of a distinctive signature
 - Belle II offers **improved software/tools** (B-tagging with FEI)

- **Untagged inclusive reconstruction, reconstruct signal side as phi meson + lepton candidate, assign everything else (neutral clusters, tracks) to the rest of event (ROE):**
 - higher signal efficiency ($\sim 16\%$ improvement), more background
 - backgrounds reduced with pre selections and a BDT trained against $q\bar{q}$ events

[arXiv:2305.04759](https://arxiv.org/abs/2305.04759)



Experiment	Lum (fb $^{-1}$)	$\mathcal{B}_{UL}^{90}(e\phi) (\times 10^{-8})$ exp. / obs.	$\mathcal{B}_{UL}^{90}(\mu\phi) (\times 10^{-8})$ exp. / obs.
BaBar [1]	451	5.0 / 3.1	8.2 / 19
Belle	854	4.3 / 3.1	4.9 / 8.4
Belle II	190	15 / 23	9.9 / 9.7

- Results not competitive yet (Small data set)
- First, successfully untagged strategy approach for tau physics at Belle II
- exploited for other measurements